

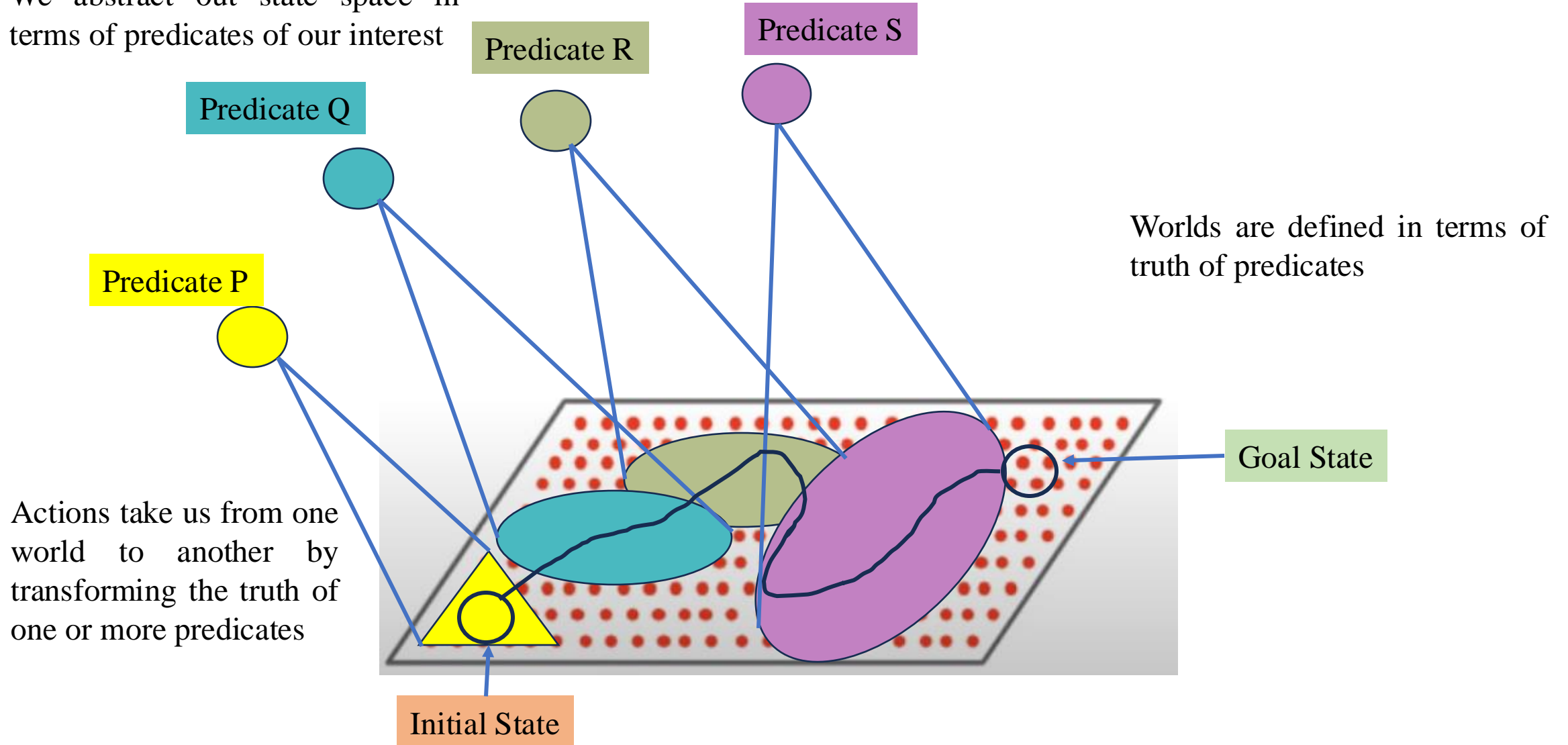
# AIFA: PLANNING

24/03/2025

**Koustav Rudra**

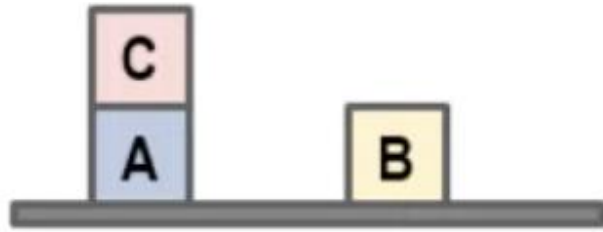
# State Spaces $\rightarrow$ Predicate Worlds

We abstract out state space in terms of predicates of our interest



# Blocks World

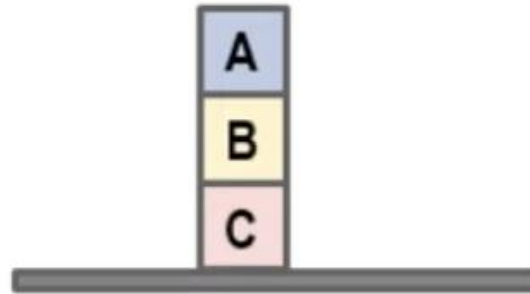
- Classical test bed for planning algorithms



**Initial State**

Predicates describing initial state:

- On(C,A)
- On(A, Table)
- On(B, Table)
- Clear(B)
- Clear(C)



**Target State**

Predicates describing initial state:

- On(A,B)
- On(B,C)
- On(C, Table)

**Actions:**

**Move(X,Y):** Move X on top of Y

**Precond:** Clear(X), Clear(Y)

**Effect:** On(X,Y)

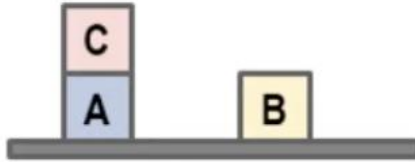
**Move(X,Table):** Move X to Table

**Precond:** Clear(X)

**Effect:** On(X,Table)

The planning task is to determine the actions for reaching the target state from the initial state

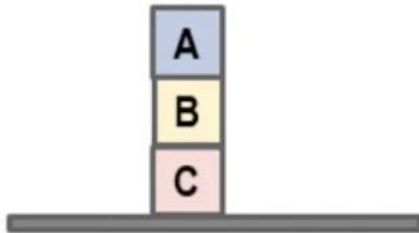
# Choosing Actions



$\text{On}(C, A), \text{On}(A, \text{Table}), \text{On}(B, \text{Table}), \text{Clear}(C), \text{Clear}(B)$



$\text{On}(A, B), \text{On}(B, C)$

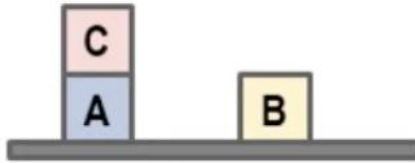


**Move(X,Y):** Move X on top of Y  
**Precond:**  $\text{Clear}(X), \text{Clear}(Y)$   
**Effect:**  $\text{On}(X, Y)$

**Move(X,Table):** Move X to Table  
**Precond:**  $\text{Clear}(X)$   
**Effect:**  $\text{On}(X, \text{Table})$

- We can move C to the Table
  - This achieves none of the goal predicates
- We can move C to the top of B
  - This achieves none of the goal predicates
- We can move B to the top of C
  - This achieves  $\text{On}(B, C)$

# Partial Solutions

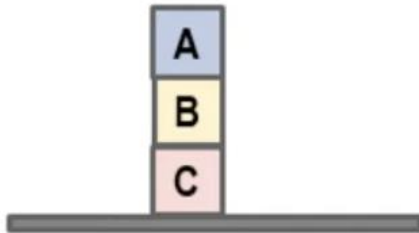


On(C, A), On(A, Table), On(B, Table), Clear(C), Clear(B)

Clear(C), Clear(B)

Move(B, C)

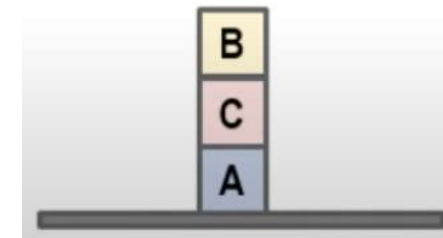
On(A, B), On(B, C)



**Move(X,Y):** Move X on top of Y  
**Precond:** Clear(X), Clear(Y)  
**Effect:** On(X,Y)

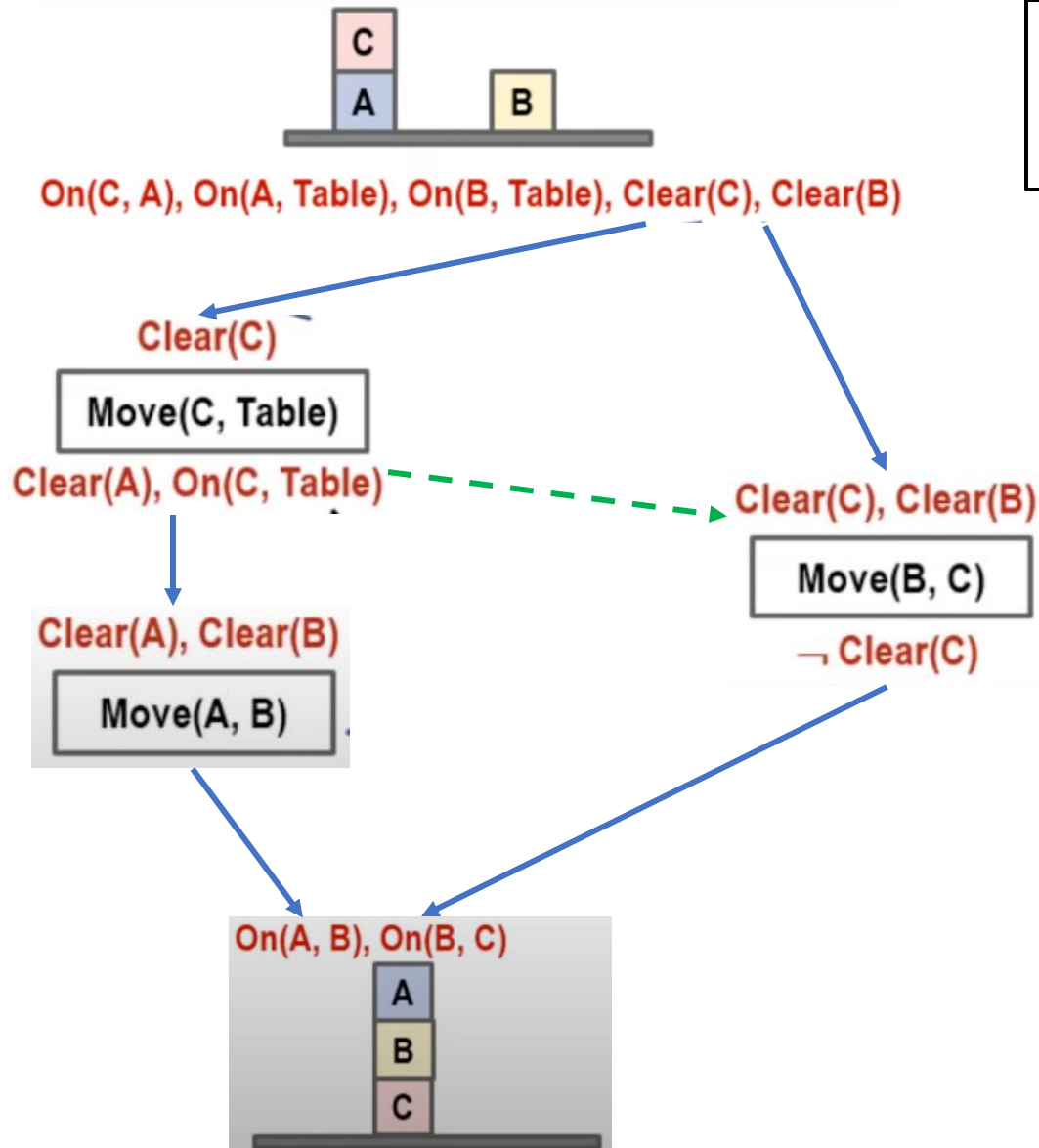
**Move(X,Table):** Move X to Table  
**Precond:** Clear(X)  
**Effect:** On(X,Table)

- We use Move(B,C) to achieve the subgoal On(B,C)
- But if we apply this move at the beginning, we get:



- We do not want

# Partial Solutions

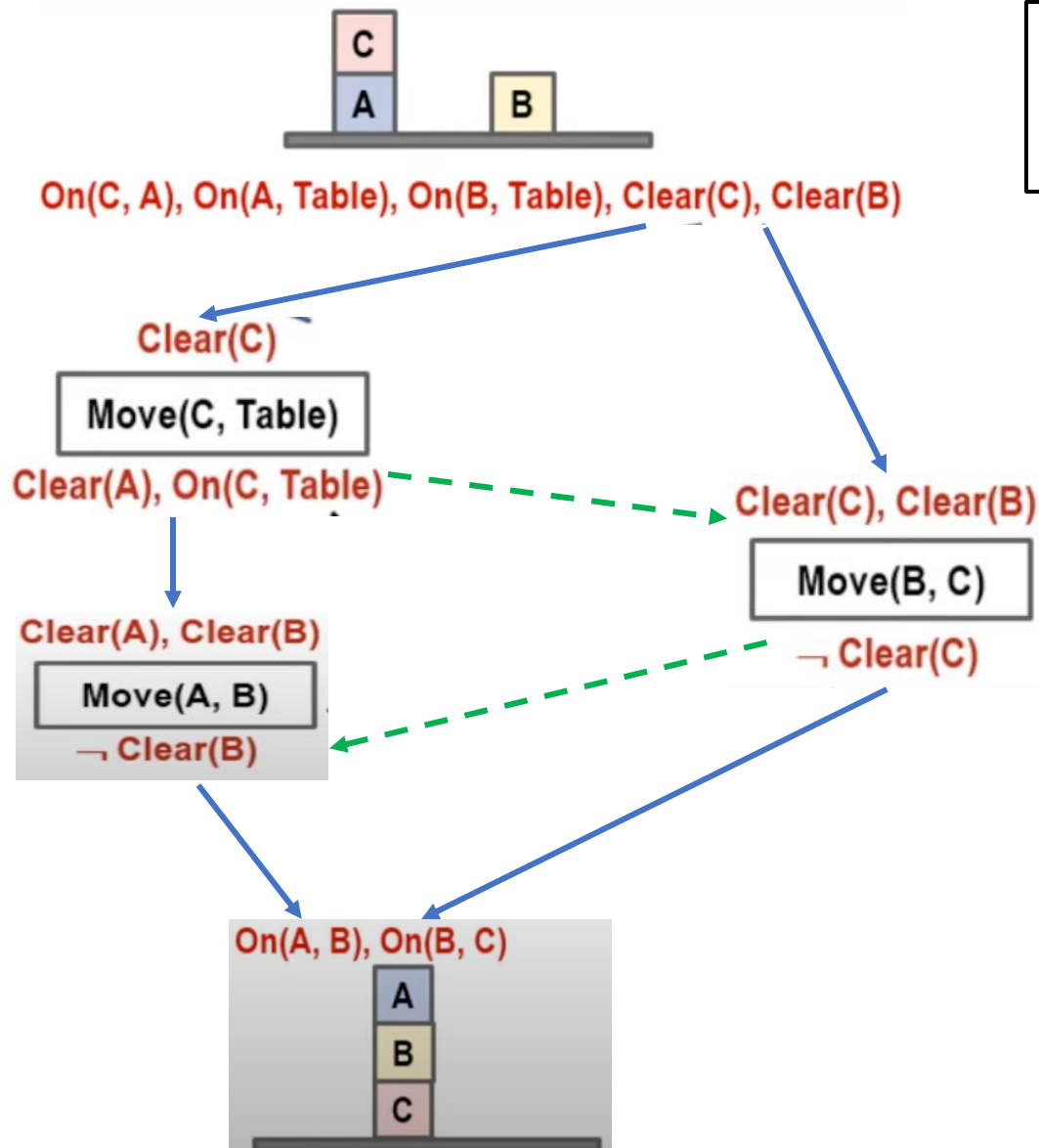


**Move(X,Y):** Move X on top of Y  
**Precond:** Clear(X), Clear(Y)  
**Effect:** On(X,Y)

**Move(X,Table):** Move X to Table  
**Precond:** Clear(X)  
**Effect:** On(X,Table)

- Move(B,C) removes the Clear(C) predicate which is essential for Move(C, Table)
- Hence Move(C, Table) must precede Move(B,C)
- Can Move(B,C) and Move(A,B) be executed in any order?

# Partial Solutions



**Move(X,Y):** Move X on top of Y  
 Precond: Clear(X), Clear(Y)  
 Effect: On(X,Y)

**Move(X,Table):** Move X to Table  
 Precond: Clear(X)  
 Effect: On(X,Table)

- Move(B,C) removes the Clear(C) predicate which is essential for Move(C, Table)
- Hence Move(C, Table) must precede Move(B,C)

How to achieve each sub-goals?

Which actions to choose?

How to serialize the actions so that precedence constraints get satisfied?

The only total order is:

- Move(C, Table)
- Move(B, C)
- Move(A, B)

Do we always need total ordering?

# Some partial orders may stay

- Actions

Which of these situations are allowed by these actions?

Op( **ACTION:** RightShoe,  
**PRECOND:** RightSockOn,  
**EFFECT:** RightShoeOn )

Op( **ACTION:** RightSock,  
**EFFECT:** RightSockOn )

Op( **ACTION:** LeftShoe,  
**PRECOND:** LeftSockOn,  
**EFFECT:** LeftShoeOn )

Op( **ACTION:** LeftSock,  
**EFFECT:** LeftSockOn )





# Some partial orders may stay

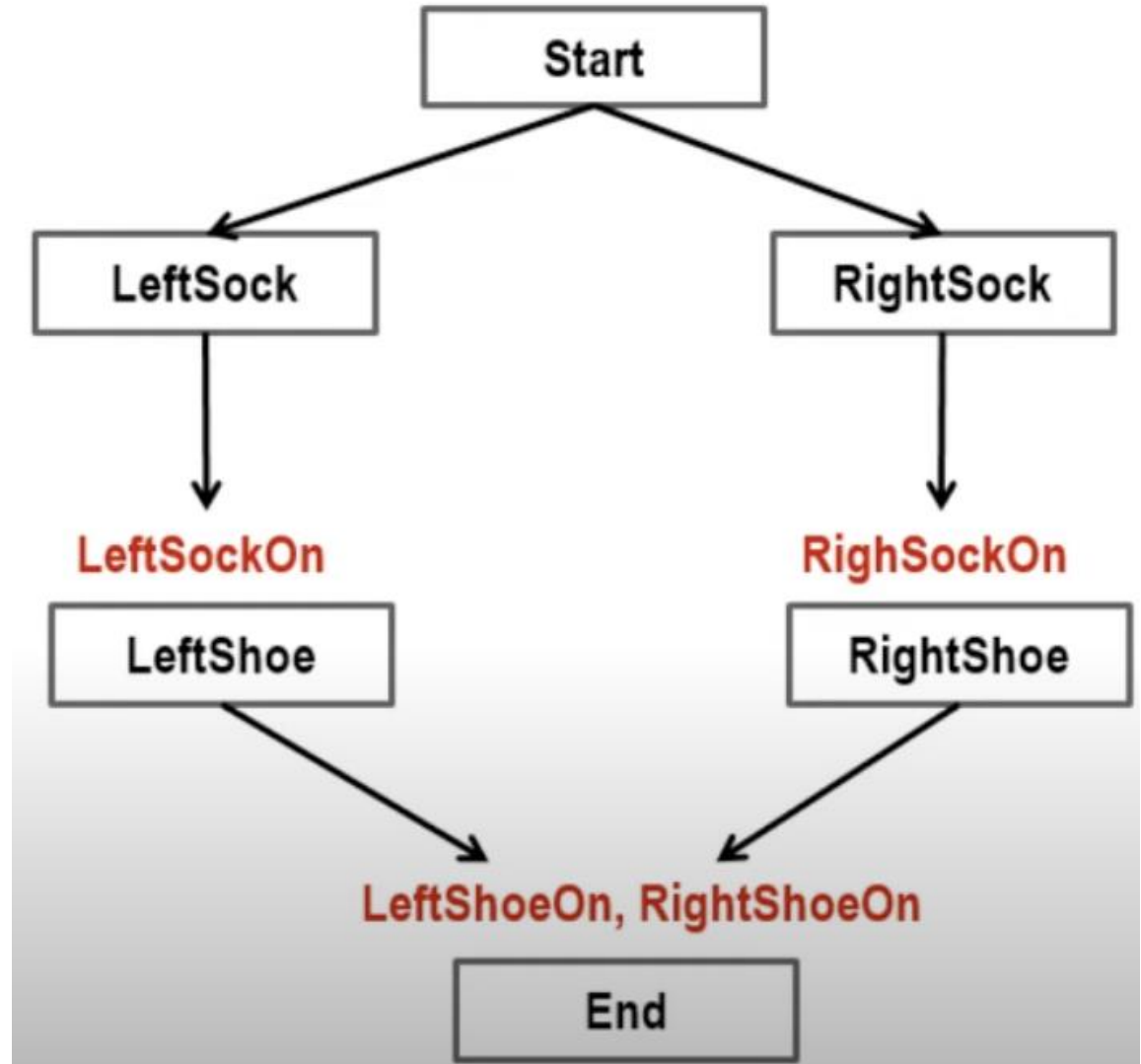
- Actions

Op( **ACTION:** RightShoe,  
**PRECOND:** RightSockOn,  
**EFFECT:** RightShoeOn )

Op( **ACTION:** RightSock,  
**EFFECT:** RightSockOn )

Op( **ACTION:** LeftShoe,  
**PRECOND:** LeftSockOn,  
**EFFECT:** LeftShoeOn )

Op( **ACTION:** LeftSock,  
**EFFECT:** LeftSockOn )



# Planning: Automation

- Partial order planning
- GraphPlan
- SATPlan
- Stochastic Planning

# Partial Order Planning

- **Basic Idea:** Make choices only that are relevant to solving the current part of the problem
- **Least Commitment Choices:**
  - **Orderings:** Leave actions unordered, unless they must be sequential
  - **Bindings:** Leave variables unbound, unless needed to unify with conditions being achieved
  - **Actions:** usually not subject to “least commitment”

# Terminology

- **Totally Ordered Plan**

- There exists sufficient orderings  $O$  such that all actions in  $A$  are ordered with respect to each other

- **Fully Instantiated Plan**

- There exist sufficient constraints in  $B$  such that all variables are constrained to be equal to some constant

- **Consistent Plan**

- There are no contradictions in  $O$  or  $B$

- **Complete Plan**

- Every precondition  $P$  of every action  $A_i$  in  $A$  is achieved:
  - There exists an effect of an action  $A_j$  that comes before  $A_i$  and unifies with  $P$ , and no action  $A_k$  that deletes  $P$  comes between  $A_j$  and  $A_i$

# STRIPS

- Stanford Research Institute Problem Solver
- Many planners today use specification languages that are variants of the one used in STRIPS
- Our running example:
  - Given:
    - **Initial State:** The agent is at home without tea, biscuits, book
    - **Goal State:** The agent is at home with tea, biscuits, book
    - A set of actions

# State Representation

- States are represented by conjunctions of function-free ground literals
  - $At(Home) \wedge \sim Have(Tea) \wedge \sim Have(Biscuits) \wedge \sim Have(Book)$
- Goals are also described by conjunction of literals
  - $At(Home) \wedge Have(Tea) \wedge Have(Biscuits) \wedge Have(Book)$
- Goals can also contain variables
  - $At(x) \wedge Sells(x, Tea)$
  - The above goal is **being at a shop that sells tea**

# Representing Actions

- **Action description:** serves as a name
- **Precondition:** a conjunction of positive literals
- **Effect:** a conjunction of literals (+ve or –ve)
- OP(
  - **ACTION:**  $Go(there)$
  - **PRECOND:**  $At(there) \wedge Path(there, there)$
  - **EFFECT:**  $At(there) \wedge \sim At(here)$
  - )

# Representing Plans

- A set of plan steps
  - Each step is one of the operators for the problem
- A set of step ordering constraints
  - Each ordering constraint is of the form  $S_i < S_j$
  - indicating  $S_i$  must occur sometime before  $S_j$
- A set of variable binding constraints of the form  $v=x$ 
  - $v$  is a variable in some step
  - $x$  is either a constant or another variable
- A set of causal links written as  $S \rightarrow c: S'$  indicating  $S$  satisfies the precondition  $c$  for  $S'$



# Example

- Initial Plan
- Plan(
  - STEPS: {
    - S1: Op( ACTION: start),
    - S2: Op( ACTION: finish, PRECOND: RightShoeOn  $\wedge$  LeftShoeOn)
    - },
  - ORDERINGS:  $\{S_1 < S_2\}$ ,
  - BINDINGS: {},
  - LINKS: {}
- )

# POP Example: Get Tea, Biscuits, Book

Initial State:

Op( **ACTION:** Start,  
    **EFFECT:**  $\text{At}(\text{Home}) \wedge \text{Sells}(\text{BS}, \text{Book})$   
                   $\wedge \text{Sells}(\text{TS}, \text{Tea})$   
                   $\wedge \text{Sells}(\text{TS}, \text{Biscuits})$  )

Goal State:

Op( **ACTION:** Finish,  
    **PRECOND:**  $\text{At}(\text{Home}) \wedge \text{Have}(\text{Tea})$   
                   $\wedge \text{Have}(\text{Biscuits})$   
                   $\wedge \text{Have}(\text{Book})$  )

Actions:

Op( **ACTION:** Go(y),  
    **PRECOND:**  $\text{At}(x)$ ,  
    **EFFECT:**  $\text{At}(y) \wedge \neg \text{At}(x)$ )

Op( **ACTION:** Buy(x),  
    **PRECOND:**  $\text{At}(y) \wedge \text{Sells}(y, x)$ ,  
    **EFFECT:**  $\text{Have}(x)$ )

START

$At(Home) \wedge Sells(BS, Book) \wedge Sells(TS, Tea) \wedge Sells(TS, Biscuits)$

Op( **ACTION:** Go(y),  
**PRECOND:** At(x),  
**EFFECT:** At(y)  $\wedge$   $\neg$ At(x))

Op( **ACTION:** Buy(x),  
**PRECOND:** At(y)  $\wedge$  Sells(y, x),  
**EFFECT:** Have(x))

$At(y1) \wedge Sells(y1, Book)$

Buy(Book)

$At(y2) \wedge Sells(y2, Tea)$

Buy(Tea)

$At(y3) \wedge Sells(y3, Biscuits)$

Buy(Biscuits)

$Have(Book) \wedge Have(Tea) \wedge Have(Biscuits) \wedge At(Home)$

FINISH

START

$At(Home) \wedge Sells(BS, Book) \wedge Sells(TS, Tea) \wedge Sells(TS, Biscuits)$

$\{y1 \setminus BS\}$

$\{y2 \setminus TS\}$

$\{y3 \setminus TS\}$

Op( **ACTION:** Go(y),  
**PRECOND:** At(x),  
**EFFECT:** At(y)  $\wedge$   $\neg$ At(x))

Op( **ACTION:** Buy(x),  
**PRECOND:** At(y)  $\wedge$  Sells(y, x),  
**EFFECT:** Have(x))

~~$At(y1) \wedge Sells(y1, Book)$~~

~~$At(y2) \wedge Sells(y2, Tea)$~~

~~$At(y3) \wedge Sells(y3, Biscuits)$~~

$At(BS) \wedge Sells(BS, Book)$

$At(TS) \wedge Sells(TS, Tea)$

$At(TS) \wedge Sells(TS, Biscuits)$

Buy(Book)

Buy(Tea)

Buy(Biscuits)

$Have(Book) \wedge Have(Tea) \wedge Have(Biscuits) \wedge At(Home)$

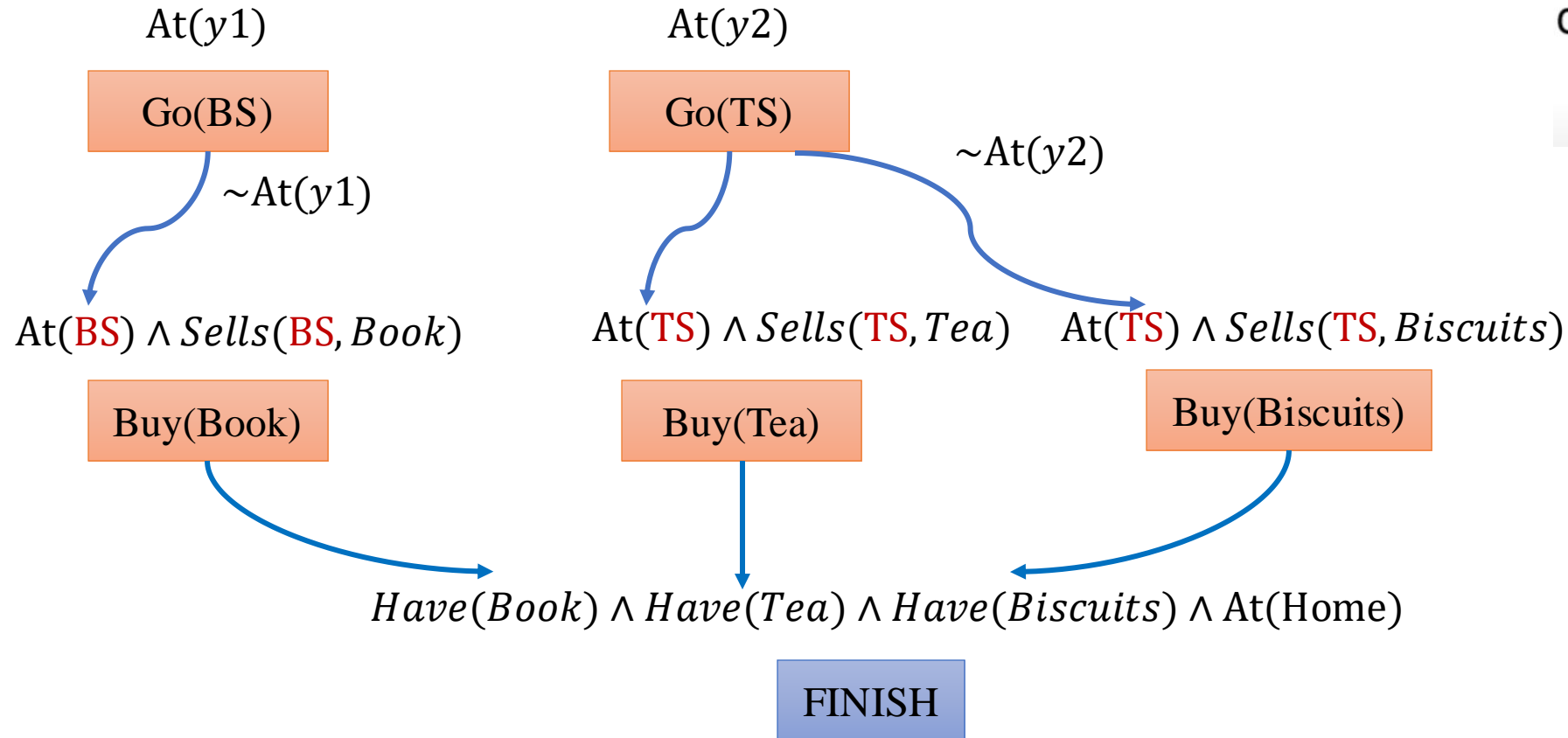
FINISH

START

$At(Home) \wedge Sells(BS, Book) \wedge Sells(TS, Tea) \wedge Sells(TS, Biscuits)$

Op( **ACTION:** Go(y),  
**PRECOND:** At(x),  
**EFFECT:** At(y)  $\wedge$   $\neg$ At(x))

Op( **ACTION:** Buy(x),  
**PRECOND:** At(y)  $\wedge$  Sells(y, x),  
**EFFECT:** Have(x))

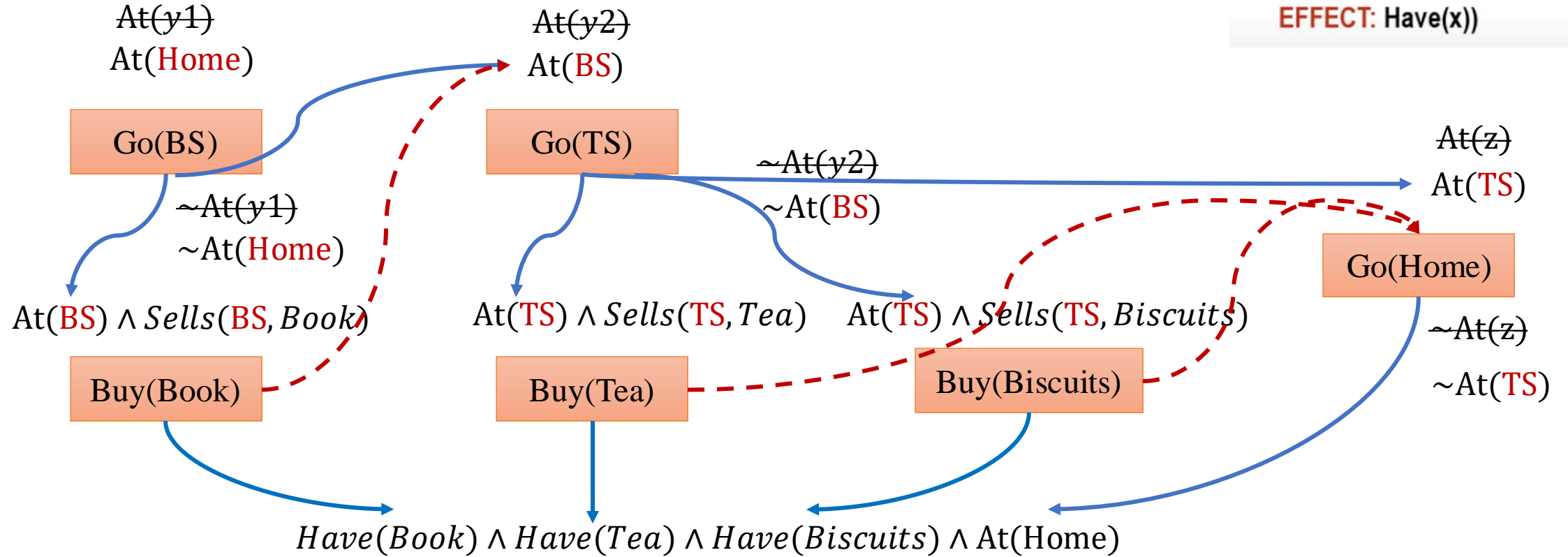


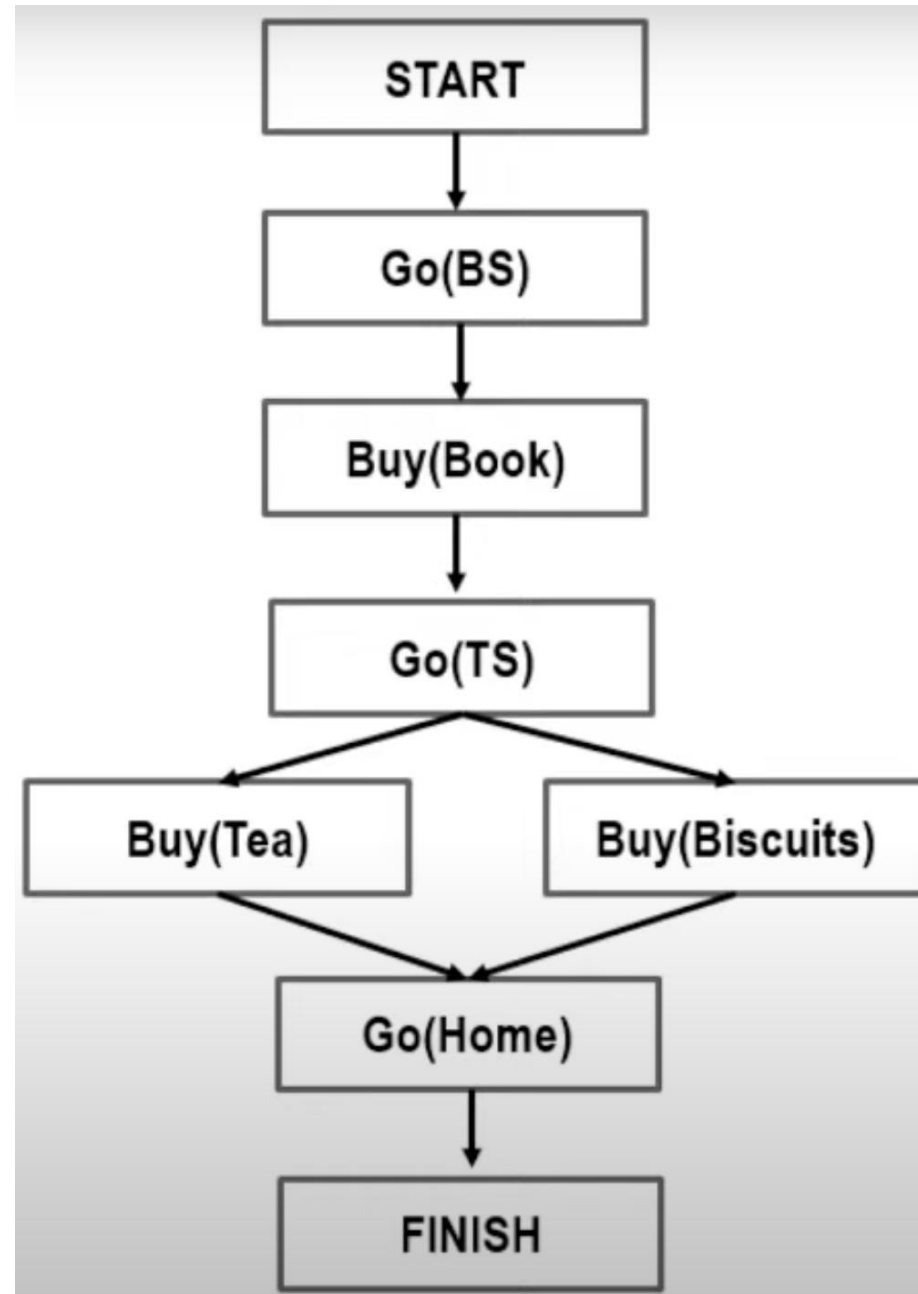
START

$At(Home) \wedge Sells(BS, Book) \wedge Sells(TS, Tea) \wedge Sells(TS, Biscuits)$

Op( **ACTION:** Go(y),  
**PRECOND:** At(x),  
**EFFECT:** At(y)  $\wedge$   $\neg$ At(x))

Op( **ACTION:** Buy(x),  
**PRECOND:** At(y)  $\wedge$  Sells(y, x),  
**EFFECT:** Have(x))





- Ordering
- Causal Constraints

Thank You