Assignment 5

Code ▼

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- 1. The data set asthma comes from a study of the relationship between childhood asthma and exposure to air pollution from concentrated animal feeding operations (CAFOs). For this problem, treat asthma (Yes/No) as following a binomial distribution given exposure, and use a smooth version of logistic regression for (a)-(c) below.
- a. Choose a criterion by which to select the smoothing parameter. Plot this criterion versus the smoothing parameter and choose the optimal value for use in (b) and (c).

```
df1 = data.frame(asthma)
library(stringr)
df1$Asthma = str replace(df1$Asthma,"Yes",'1')
df1$Asthma = str replace(df1$Asthma,"No",'0')
df1<-df1[order(df1$Exposure),]
attach(df1)
A<-as.numeric(as.character(df1$Asthma))
E<-df1$Exposure
fitl$deviance
[1] 388.4937
                                                                                                                             Hide
library(locfit)
locfit 1.5-9.4 2020-03-24
                                                                                                                             Hide
n \le -length(A)
k \le seq(10,n,by=10) #h = k/n
cv \le mcr \le gcv \le rep(0, length(k))
for (i in 1:length(k)){
 fit <- locfit(A \sim lp(E, nn = k[i]/n, deg = 1), family = "binomial", ev = dat(ev = TRUE))
 pihat <- fitted(fit)
 yhat <- (pihat > .5)*1
 mcr[i] <- mean(abs(A-yhat))
 cv[i] <- (-2*(sum(log(pihat[A==1]))+sum(log(1-pihat[A==0])))/n)
 # gcv[i] <- gcv(fit)["gcv"]
```

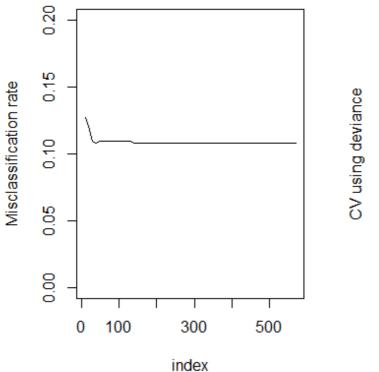
procv: no points with non-zero weight

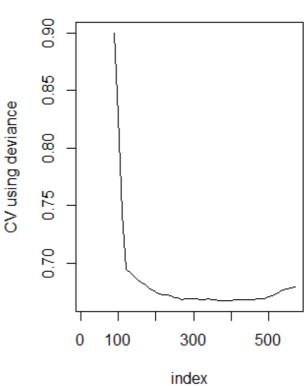
 $gev[i] < -(-2*n*fit$dp["lk"]/(n-fit$dp["df2"])^2)$

```
par(mfrow=c(1,2))
plot(k,mcr,type="l",xlab = 'index',ylab="Misclassification rate", ylim=c(.0,.2))
plot(k,cv,type="l",xlab = 'index',ylab="CV using deviance")
```

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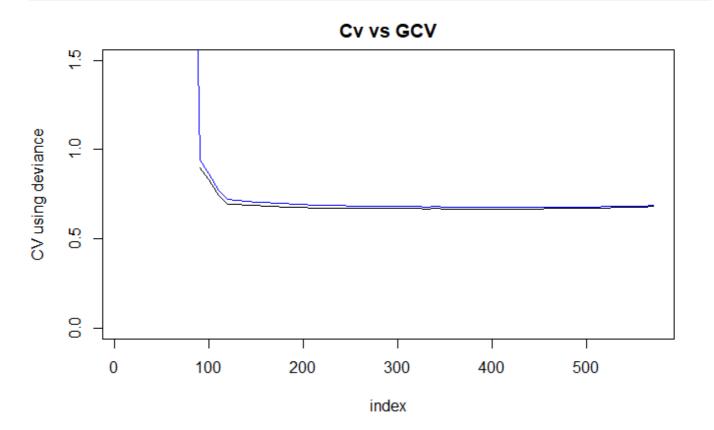
par(mfrow=c(1,1))





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 $plot(k,cv,type="l",xlab='index',ylab="CV using deviance",main="Cv vs GCV",ylim=c(0.0,1.5))\\ lines(k,gcv,type="l",xlab='index',ylab="GCV",col='blue')$



b. Plot a smooth curve estimating the relationship between exposure and the log-odds of developing asthma.

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h_cv<-k[which.min(cv)]

which.min(cv)

[1] 38

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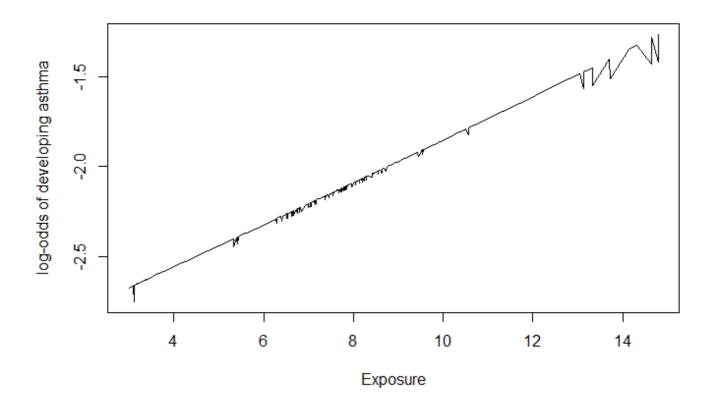
h_gcv<-k[which.min(gcv)]

which.min(gev)

[1] 45

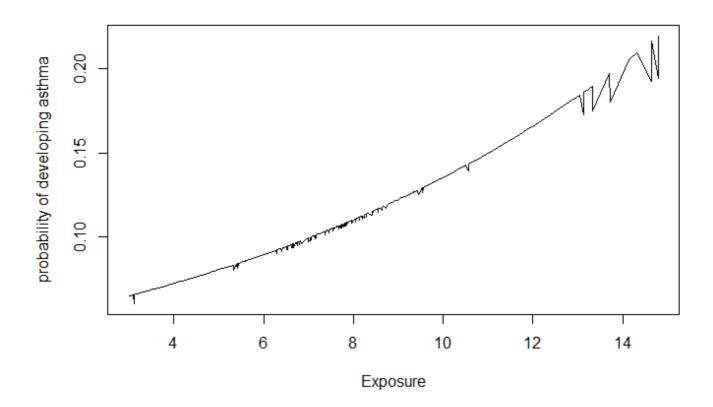
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fit <-locfit(A~lp(E,nn=h_gcv/n,deg = 1),family="binomial",ev=dat(cv=TRUE))
pihat <- fitted(fit)
plot(E,log(pihat/(1-pihat)),type = "l",xlab = 'Exposure',ylab = 'log-odds of developing asthma')
```



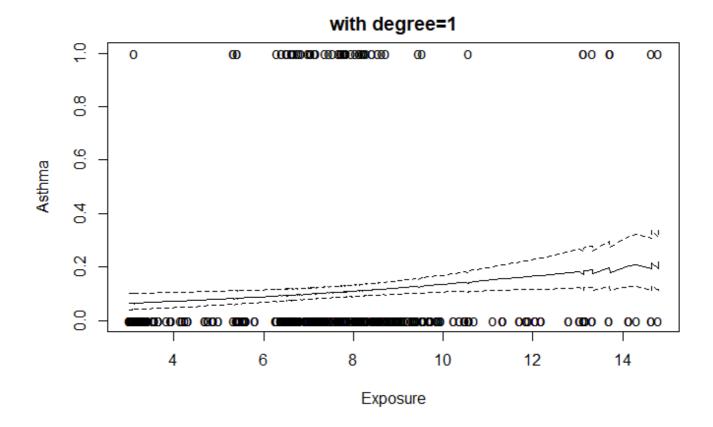
c. Plot a smooth curve estimating the relationship between exposure and the probability of developing asthma, with confidence bands.

plot(E,fitted(fit),type="l",xlab='Exposure',ylab='probability of developing asthma')



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plot(fit,band='local',get.data = T,main='with degree=1',xlab = 'Exposure',ylab='Asthma')



```
fit1 <-lm(A \sim 1, family = "binomial")
In lm.fit(x, y, offset = offset, singular.ok = singular.ok, ...):
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fit2<-lm(A~E,family="binomial")
In lm.fit(x, y, offset = offset, singular.ok = singular.ok, ...):
extra argument 恸拖family恸炸 will be disregarded
                                                                                                              Hide
fit3 <- ksmooth(A,E,kernel="normal",bandwidth=30)
anova(lm(fit3$y~fit3$x))
ANOVA F-tests on an essentially perfect fit are unreliable
Analysis of Variance Table
Response: fit3$y
      Df Sum Sq Mean Sq F value Pr(>F)
        1 1.5087e-05 1.5087e-05 851385799 < 2.2e-16 ***
Residuals 573 0.0000e+00 0.0000e+00
Signif. codes: 0 "*** 0.001 "** 0.01 " 0.05 ". 0.1 " 1
                                                                                                              Hide
anova(fit1,fit2)
Analysis of Variance Table
Model 1: A \sim 1
Model 2: A \sim E
 Res.Df RSS Df Sum of Sq
                             F Pr(>F)
1 574 55.315
2 573 54.845 1 0.46997 4.9101 0.02709 *
Signif. codes: 0 "*** 0.001 "** 0.01 " 0.05 " 0.1 " 1
  3. The library ISLR contains a dataset called Wage with information about wages and demographic factors
```

3. The library ISLR contains a dataset called Wage with information about wages and demographic factors (age, gender, health, education, etc). Fit three splines to estimate the relationship between age and wage: natural base, B-spline and smooth-splines.

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library(ISLR)

Attaching package: 拗拖ISLR坳炸

Wage

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names(Wage)

```
[1] "year" "age" "maritl" "race" "education" "region" "jobclass"
```

[8] "health" "health_ins" "logwage" "wage"

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str(Wage)

'data.frame': 3000 obs. of 11 variables:

\$ year : int 2006 2003 2004 2009 2004 2004 2008 2006 2004 2006 ...

\$ age : int 18 18 18 18 18 18 18 18 18 18 ...

\$ maritl : Factor w/ 5 levels "1. Never Married",..: 1 1 1 1 1 1 1 1 1 1 ...

\$ race : Factor w/ 4 levels "1. White", "2. Black",..: 1 2 1 1 1 1 1 1 1 1 ...

\$ education : Factor w/ 5 levels "1. < HS Grad",..: 1 2 1 1 1 2 2 1 2 3 ...

\$ region : Factor w/ 9 levels "1. New England",..: 2 2 2 2 2 2 2 2 2 2 ...

\$ jobclass : Factor w/ 2 levels "1. Industrial",..: 1 1 1 1 1 1 1 1 1 2 ...

\$ health : Factor w/ 2 levels "1. <=Good", "2. >=Very Good": 1 2 2 1 1 2 2 2 2 2 ...

 $\$ health_ins: Factor w/ 2 levels "1. Yes", "2. No": 2 1 2 2 1 2 2 1 2 ...

\$ logwage : num 4.32 4.26 3.73 3.9 4.24 ... \$ wage : num 75 70.5 41.7 49.6 69.6 ...

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Wage<-Wage[order(Wage\$age),] head(Wage)

	y <int> <in< th=""><th></th><th>race <fctr></fctr></th><th>education <fctr></fctr></th><th>region <fctr></fctr></th><th>jobclass <fctr></fctr></th></in<></int>		race <fctr></fctr>	education <fctr></fctr>	region <fctr></fctr>	jobclass <fctr></fctr>
231655	2006 18	1. Never Married	1. White	1. < HS Grad	2. Middle Atlantic	1. Industria
157244	2003 18	1. Never Married	2. Black	2. HS Grad	2. Middle Atlantic	1. Industria
83515	2004 18	1. Never Married	1. White	1. < HS Grad	2. Middle Atlantic	1. Industria
453584	2009 18	1. Never Married	1. White	1. < HS Grad	2. Middle Atlantic	1. Industria
85657	2004 18	1. Never Married	1. White	1. < HS Grad	2. Middle Atlantic	1. Industria
87661	2004 18	1. Never Married	1. White	2. HS Grad	2. Middle Atlantic	1. Industria
6 rows 1-8 of 11 columns						
						

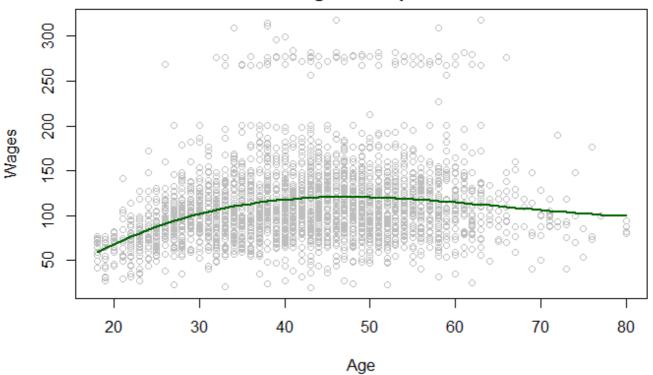
```
attach(Wage)
```

a. State the criterion by which to select the smoothing parameter and use it to select. Plot this criterion versus the smoothing parameter and choose the optimal value for use in (b) and (c).

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```
#Plotting the Regression Line to the scatterplot
library(splines)
fit<-lm(Wage$wage~bs(Wage$age))
plot(Wage$age,Wage$wage,col="grey",xlab="Age",ylab="Wages",main = "Regression plot")
lines(Wage$age,predict(fit),col="darkgreen",lwd=2,type="l")
```

Regression plot



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```
lm.fit=lm(wage~age,data=Wage) coef(lm.fit)
```

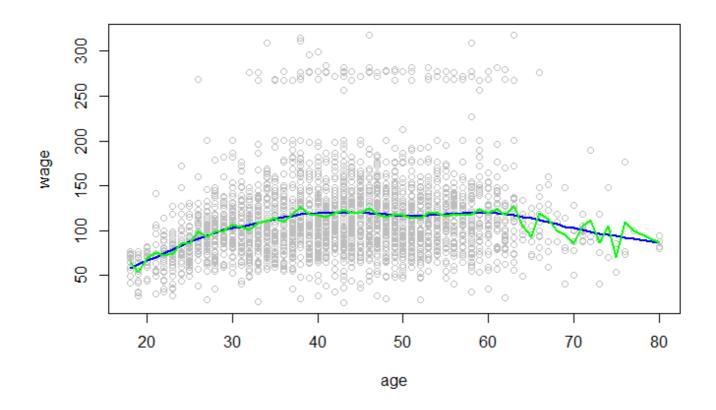
```
(Intercept) age
81.7047354 0.7072759
```

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```
plot(age,wage,col = 'grey')
lines(smooth.spline(age,wage,df=10),lwd=2,col="blue")
```

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lines(smooth.spline(age,wage,df=61),lwd=2,col="green")



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NA NA

b. Plot a smooth curve estimating the relationship between age and the wages.

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```
plot(age,wage,col='grey')
spline_fit_10=smooth.spline(Wage$age,Wage$wage,df=10)
spline_fit_CV=smooth.spline(Wage$age,Wage$wage,cv=TRUE)
```

cross-validation with non-unique 'x' values seems doubtful

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spline_fit_CV\$df

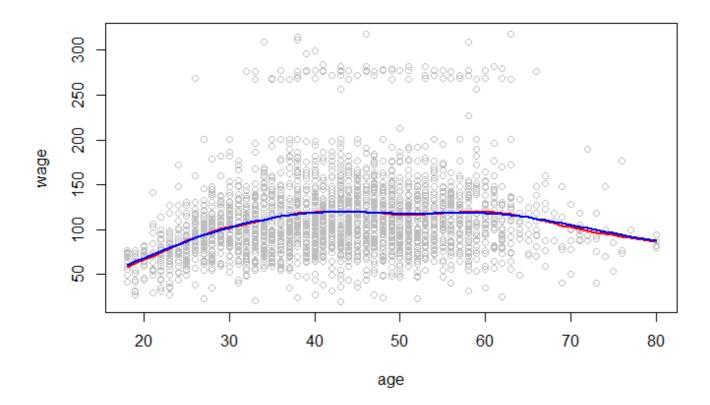
[1] 6.794596

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lines(spline_fit_10\$x,spline_fit_10\$y,lwd=2,col='red')

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lines(spline_fit_CV\\$x,spline_fit_CV\\$y,lwd=2,col='blue')



c. Compare the three models.

```
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```

plot(age,wage,col='gray')
#Natural spline model
fit1<-lm(wage~ns(age,df=10))
lines(age,predict(fit1),lwd =2,col='yellow')

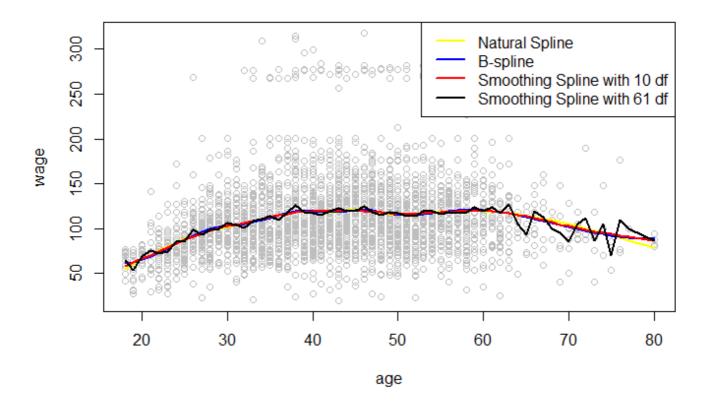
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#B-spline model
fit2<-lm(wage~bs(age,df=10))
lines(age,predict(fit2),lwd =2,col='blue')
#Smoothing spline model
#plot(age,wage,col='gray')
lines(smooth.spline(age,wage,df=10),lwd =2,col='Red')

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lines (smooth.spline (age, wage, df=61), lwd=2, col='black')

legend ("topright", c ("Natural Spline", "B-spline", "Smoothing Spline with 10 df", "Smoothing Spline with 61 df"), col=c ("yellow", "blue", "red", "black"), lwd=2)

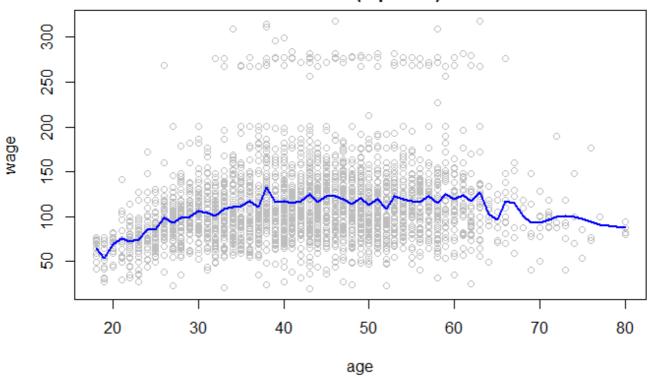


d. Use B-splines to create 4 plots corresponding to splines with degrees of freedom = $p \times number of points$, for the following p's: p = 0.05, 0.5, 0.75, 0.98.

```
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```

```
n=length(age)
dfl=floor(.05*n)
#plot(age,wage,col="grey")
fit3<-lm(wage~bs(age,df=df1))
plot(age,wage,col="grey",main=paste('df=',df1,' (n points)'))
lines(age,predict(fit3),lwd =2,col='blue')
```

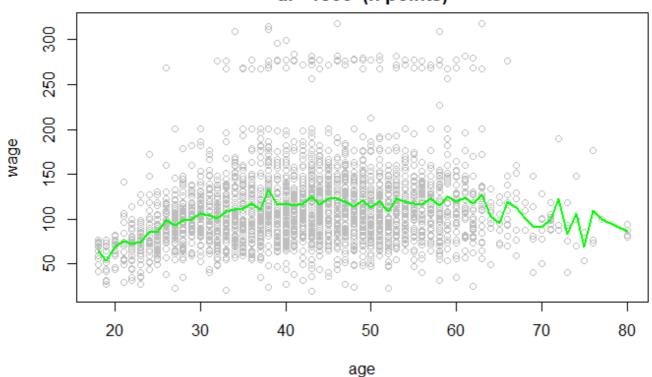
df= 150 (n points)



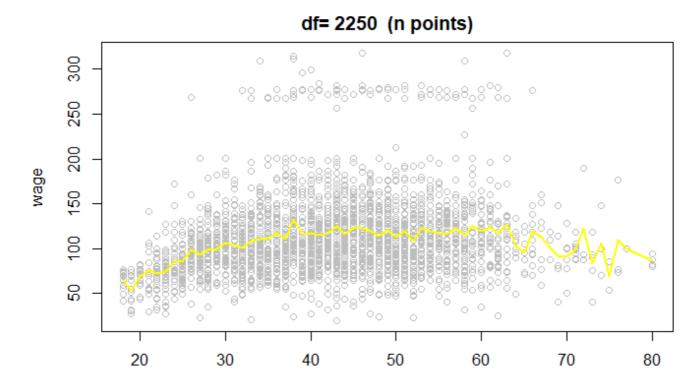
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df2 = floor(.5*n) fit4<-lm(wage~bs(age,df=df2)) plot(age,wage,col="grey",main=paste('df=',df2,' (n points)')) lines(age,predict(fit4),lwd =2,col='green')

df= 1500 (n points)



```
df3 = floor(.75*n)
fit5<-lm(wage~bs(age,df=df3))
plot(age,wage,col="grey",main=paste('df=',df3,' (n points)'))
lines(age,predict(fit5),lwd =2,col='yellow')
```

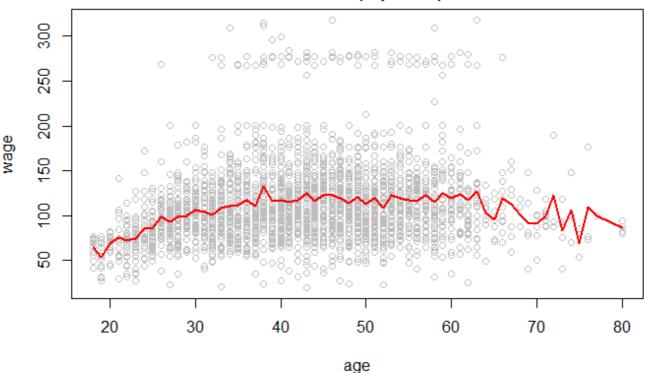


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```
df4=floor(.98*n)
fit6<-lm(wage~bs(age,df=df4))
plot(age,wage,col="grey",main=paste('df=',df4,' (n points)'))
lines(age,predict(fit6),lwd =2,col='red')
```

age

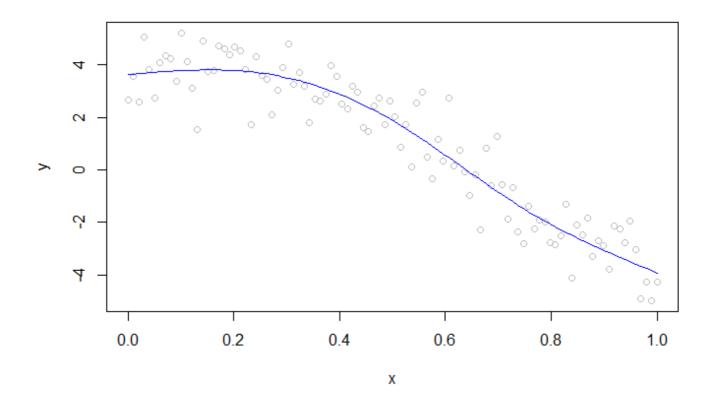
df= 2940 (n points)



4 (a) Write the set of truncated spline basis functions for representing a cubic spline function with three knots inside [0, 1].

```
##
library(splines)
X <- seq(0, 1, length=100)
knots <- c(0.25, 0.50, 0.75)
n=length(x)
set.seed(1); err=1
y<- (2.3*cos(3.0*x) + 1.2*sin(4.5*x) + cos(1.92*x) + rnorm(n, 0, err))
```

b. For $x \in [0, 1]$ and equally spaced knots, plot the above basis functions (exclude the intercept term).



c. For the same range and knots as in (b), plot the B–spline basis functions, again excluding the intercept term. You may use the splines package to construct them for you.

```
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```

