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# Evaluating the fairness of task-adaptive pretraining on unlabeled test data before text classification

# **Anonymous ACL submission**

#### **Abstract**

Few-shot learning benchmarks are critical for evaluating modern NLP techniques. But it's possible that benchmarks favor methods which easily make use of unlabeled text, because researchers can pretrain their models on unlabeled text from the test set. Given the dearth of research on this potential problem, we run experiments to quantify the bias caused by pretraining on unlabeled test set text instead of on unlabeled, independently drawn text. Controlled few-shot and zero-shot experiments on 25 classification tasks and 3 language models-BERT, GPT-2, and Mistral 7B—does not find evidence of overoptimism. Furthermore, we demonstrate the importance of repeated subsampling when studying fewshot text classification, and recommend that few-shot learning benchmarks include multiple training folds. Code and data are available here: https://github.com(currently omitted for anonymity).

#### 1 Introduction

For NLP benchmarks, it's standard to release text from the test set. This allows researchers to submit a file of predictions instead of submitting code. A potential concern is that researchers can use this text during training. Consider the Real-world Annotated Few-shot Tasks (RAFT) benchmark (Alex et al., 2021), which contains "few-shot" text classification tasks—tasks where the training set contains a relatively small number of labeled examples. Below is an excerpt from the RAFT paper (emphasis added):

For each task, we release a public training set with 50 examples and a larger unlabeled test set. We encourage unsupervised pre-training on the unlabelled examples and open-domain information retrieval.

In the RAFT competition, a model is evaluated by scoring its predictions on the same set of unlabeled text which the model may have been trained on (using an unsupervised training procedure). 040

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It's wrong to train a model on test set features with their labels and then evaluate on the test set when one needs to estimate performance on out-of-sample data. Test set performance would be overoptimistic (Hastie et al., 2009). This fact is widely known. But what if, as encouraged by Alex et al. (2021), a model is trained on test set features without test set labels? This paper studies this question for the domain of few-shot text classification.

#### 2 Motivation

NLP benchmarks for few-shot learning are prevalent, as having only a handful of labeled examples is more realistic. One consideration when designing these benchmarks is that some few-shot approaches can—at least theoretically—use unlabeled text from the test set. With Pattern-Exploiting Training (Schick and Schütze, 2021), for example, one can train the final classifier on test set text with soft labels predicted by an ensemble of supervised models. Or, with Pre-trained Prompt Tuning (Gu et al., 2022), one can pretrain the language model (LM) on unlabeled test set text before prompt-tuning on the labeled training set. A more classical approach would be to train a word2vec model (Mikolov et al., 2013) on unlabeled test set text, run this model on training text to get embeddings, and finally train a classifier on these embeddings with labels from the training set.

For other few-shot approaches, such as SetFit (Tunstall et al., 2022) and in-context learning with LLMs (as popularized by Brown et al., 2020), it's more common to only use labeled text.

While the ability to exploit unlabeled text is useful, doing so on test set text could be substantively different than applying it to text which is statisti-

cally independent of the test set. This difference in methodology may be more concerning in the few-shot setting than in the many-shot setting. It's conceivable that differences between few-shot methods are due just as much to how unlabeled text is used as they are to how the few, labeled examples are used. This raises the question: does pretraining a model on a benchmark's unlabeled test set text inflate the model's performance on that benchmark?

## 3 Related work

As indicated by the quote in §1, the RAFT benchmark implicitly assumes that the answer is no. The validity of using test set features is not a fringe opinion. The popular textbook by Hastie et al. (2009) contains the following passage without a reference or evidence (emphasis added):

There is one qualification: initial unsupervised screening steps can be done before samples are left out. For example, we could select the 1000 predictors with highest variance across all 50 samples, before starting cross-validation. Since this filtering does not involve the class labels, it does not give the predictors an unfair advantage.

The opposite opinion—that exploiting unlabeled test set features is unfair—may align more closely with best practices. For example, Gururangan et al. (2020) contains the following criticism of another study when comparing performances on a popular text classification benchmark:

Thongtan and Phienthrakul (2019) report a higher number (97.42) on IMDB, but they train their word vectors on the test set.

Jacovi et al. (2023) argue that benchmarks which release unlabeled test set text can be compromised in two ways. First, the text can be discretely labeled and trained on by model developers. Second, if test set texts were scraped from websites which also host their labels, e.g., movie reviews and ratings on IMDb, then an LLM may have already been pretrained on these labeled texts (Scenario 1 in Jacovi et al., 2023). They do not discuss potential problems with using unlabeled test set text by itself.

Moscovich and Rosset (2022) contains experiments and theory for unsupervised methods which are common to tasks involving tabular data. They

find that estimators of out-of-sample performance which were subject to these methods may be biased positively or negatively, depending on the parameters of the problem. They recommend further research on this bias in more domains, particularly when dealing with small sample sizes and high-dimensional data.

# 4 Experimental design

In the absence of theory or experiments on this question in NLP, we study whether pretraining on unlabeled test set text biases test set performance for 25 diverse text classification tasks and two types of LMs: BERT (Devlin et al., 2019), and GPT-2 (Radford et al., 2019). Appendix A describes each task

At a high level, the goal of the experiment is to first establish that pretraining is beneficial, in line with Gururangan et al. (2020). Second, given that pretraining has a detectable benefit, the experiment measures the accuracy difference between using test set text for the pretraining stage—an arguably unfair methodology—and using text which is independent of the test set—an inarguably fair methodology.

In more detail, the experiment starts by subsampling three separate sets of data from the full sample of data for a given text classification task:

- extra: n (either 50, 100, 200 or 500) unlabeled texts which are optionally used for pre-training
- train: m (either 50 or 100) labeled texts for classification training
- test: n labeled texts to report accuracy.

Next, three accuracy estimators are computed. The procedures used to obtain them are described below.

# 4.1 accextra

- 1. Train a freshly loaded, pretrained LM on the n unlabeled texts in extra using the LM's pretraining objective—masked language modeling loss for BERT, or autoregressive/causal language modeling loss for GPT-2.
- 2. Add a linear layer to this model, and finetune all of the LM's weights to minimize classification cross entropy loss on train.
- 3. Compute the classification accuracy of this model on test.

Step 1 is task-adaptive pretraining—a procedure broadly recommended by Gururangan et al. (2020). Step 2 is a canonical way to train a transformer-based LM for a classification task, according to Section 2 of Zhang et al. (2021).

acc<sub>extra</sub> is clearly an unbiased estimator of out-of-sample accuracy because it never trains on test.

## 4.2 $acc_{test}$

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acc<sub>test</sub> is identical to acc<sub>extra</sub>, except that pretraining is done on test instead of extra in step 1.

 $acc_{test}$  represents what one might see in a competition like RAFT, where pretraining on unlabeled text from test is encouraged. It's unclear whether this accuracy estimator is unbiased, because it was (pre)trained and evaluated on the same set of test set text. A reasonable hypothesis is that it's overoptimistic, i.e.,  $E[acc_{test}] > E[acc_{extra}]$ .

## 4.3 acc<sub>base</sub>

 $acc_{base}$  doesn't do pretraining; it doesn't make any use of unlabeled text. It simply trains a pretrained LM on train to do classification, and then computes this model's accuracy on test.

This score is a control. If there's no boost from  $acc_{base}$  to  $acc_{extra}$ , then it shouldn't be surprising that there's no difference between  $acc_{extra}$  and  $acc_{test}$ .

## 4.4 Repeated subsampling

The three accuracy estimators are paired, because their classification training and test sets are identical. The only difference is the source of unlabeled text for pretraining. For acc<sub>extra</sub>, the source is independent of test data. For acc<sub>test</sub>, the source is exactly the test set text. For acc<sub>base</sub>, no unlabeled text is used.

A potentially important source of variation in this experiment is the particular subsamples, i.e., the particular realizations of extra, train, and test for a given classification task. To expose this variation, the experiment procedure is repeated tens of times for each classification task. For example, for n=200, and for each of the 25 classification tasks, 50 (acc<sub>extra</sub>, acc<sub>test</sub>, acc<sub>base</sub>) triples are computed.

Appendix B explains more experiment choices.

# 5 Results

Figure 1 visualizes the distributions of  $acc_{extra}$  –  $acc_{base}$  and  $acc_{test}$  –  $acc_{extra}$  for m=50, n=200.  $acc_{extra}$  –  $acc_{base}$  is a control—it's the accuracy boost from pretraining on unlabeled independent text versus not pretraining at all.  $acc_{test}$  –  $acc_{extra}$  is the main quantity of interest: it's the evaluation bias from pretraining on unlabeled test set text instead of on unlabeled independent text.

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Table 1 contains means of these differences for each configuration of the experiment. It roughly suggests that while pretraining is consistently beneficial, pretraining on unlabeled test set text does not bias test set performance one way or the other.

A more complete analysis of this data is motivated and performed in the next section.

	BERT		GPT-2	
n = 50	4.1%		3.8%	
n = 50		0.19%		0.18%
n = 100	3.9%		4.1%	
		0.18%		0.11%
n = 200	3.9%		4.4%	
		-0.39%		-0.05%
n = 500	3.5%		4.6%	
		0.48%		-0.08%

(a) m = 50BERT GPT-2 6.2% 2.2% n = 50-0.08% -0.05% 6.1% 2.5% n = 100-0.37% 0.03% 4.1% 6.3% n = 2000.33% -0.01% 6.1% 3.9% n = 500-0.16% -0.21%

(b) m = 100

Table 1: Means of accuracy differences taken across all subsamples of the 25 classification tasks. For each cell, the upper-left of the diagonal corresponds to the sample mean of  $acc_{extra} - acc_{base}$ , and the lower-right corresponds to the sample mean of  $acc_{test} - acc_{extra}$ .

# 6 Analysis

Reporting means is not enough, especially when studying few-shot learning. Figure 1 demonstrates that there's considerable variance, despite pairing the accuracy estimators.<sup>2</sup> While these visualiza-

 $<sup>^{1}</sup>$ For n=50 and n=100, the experiment is repeated 100 times. For n=200, the experiment is repeated 50 times. For n=500, the experiment is repeated 20 times. In total, 81,000 finetuned BERT and GPT-2 models were evaluated in this experiment.

<sup>&</sup>lt;sup>2</sup>One source of variance is intentionally introduced: the subsamples/splits, as explained in §4.4. The other source of variance is inherent: the added linear layer to perform classification is initialized with random weights.

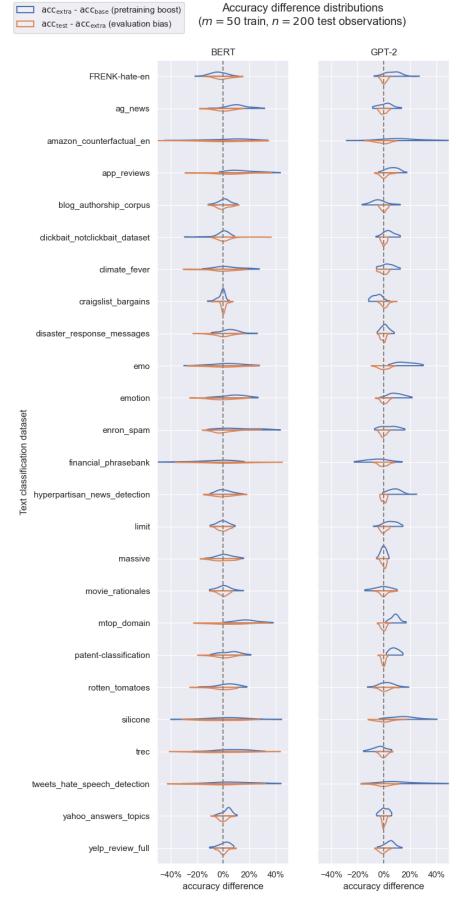


Figure 1

tions tell us about how raw accuracy differences vary, they do not tell us how the mean accuracy difference varies. We seek a neat answer to the core questions: on this benchmark of 25 classification tasks, how much does the overall accuracy differ between two modeling techniques, and how much does this difference vary?

One way to communicate the variance is to estimate the standard error of the mean difference across classification tasks. But the standard error statistic can be difficult to interpret (Morey et al., 2016). Furthermore, its computation is not completely trivial due to the data's hierarchical dependency structure: each triple, (acc<sub>extra</sub>, acc<sub>test</sub>, acc<sub>base</sub>), is drawn from (train, test), which is itself drawn from the given classification dataset.

#### 6.1 Model

This analysis does not aim to estimate standard errors. Instead, a hierarchical model is fit:

$$Y_{ijkl} \sim \text{Binomial}(n, \lambda_{ijkl}) \quad (1)$$

$$\log \text{it}(\lambda_{ijkl}) = \mu + \alpha z_i + U_j + V_{jk} + \beta x_{ijkl} \quad (2)$$

$$\mu \sim \text{Normal}(0, 1) \quad (3)$$

$$\alpha \sim \text{Normal}(0, 5) \quad (4)$$

$$U_j \sim \text{Normal}(0, \sigma_U) \quad (5)$$

$$V_{jk} \sim \text{Normal}(0, \sigma_V)$$
 (6)

$$\beta \sim \text{Normal}(0,1)$$
 (7)

$$\sigma_U, \sigma_V \sim \text{HalfNormal}(0, 1)$$
 (8)

- (1) number of correct predictions
- (2) logit link for accuracy rate, additive effects
- (3) prior for the global intercept
- (4) prior for the effect of the type of LM (BERT or GPT-2)—a control variable
- (5) prior for the effect of the classification task (partial-pooled to reduce overfitting)
- (6) prior for the nested effect of the task's subsampled dataset
- (7) prior for the effect of interest ( $x_{ijk1} = 1$  indicates the modeling intervention)
- (8) prior for standard deviations.

The model is fit using Markov Chain Monte Carlo, using the interface provided by the bambi package (Capretto et al., 2022). Appendix E.1 includes a simulation demonstrating the model's ability to correctly recover null and non-null effects.

# 6.2 Posterior predictions

In NLP benchmarks, methods are assessed by taking their average performance across tasks. To place the analysis results in this context, samples from the posterior predictive distribution of  $Y_{ijk1} - Y_{ijk0}$  (6.1) are taken, then averaged across i (the 2 LM types—BERT and GPT-2), j (the 25 classification tasks), and k (their subsamples), and divided by n to obtain the distribution of the average accuracy difference.

These distributions are plotted in Figure 2. Each distribution is that of the marginal effect of the modeling intervention: pretraining versus not pretraining before classification training (the pretraining boost), or pretraining on unlabeled test set text instead of on unlabeled independent text before classification training (the evaluation bias).

# 7 Discussion

Figure 2 demonstrates that the average pretraining boost is significant in every configuration of the experiment, ranging from 2% to 6%. This finding replicates that from Gururangan et al. (2020). After averaging across settings for m, n, and the 2 LM types, only two of the 25 classification tasks had a pretraining boost less than 0, and both were greater than -1%. Overall, pretraining is beneficial, so there may be a detectable evaluation bias.

As shown in Figure 2, the evaluation bias bounces inconsistently and insignificantly around 0. After averaging, 12 of the 25 classification tasks had a positive evaluation bias, and all tasks had an average evaluation bias less than 1% in absolute value. Given the lack of evidence for an evaluation bias in either direction, it's unlikely that a benchmark which releases unlabeled test set text can systematically promote models pretrained on it over equally performant models which pretrained on unlabeled independent text.

Moscovich and Rosset (2022) found that the evaluation bias caused by certain unsupervised methods for tabular data gets closer to 0 as n increases. This finding is not confirmed by this experiment. Figure 2 shows that for m=50 and m=100, distributions of the evaluation bias consistently hover around 0 across settings for n. But far more experiments varying n are needed to thoroughly assess this insensitivity.

<sup>&</sup>lt;sup>3</sup>The tasks were blog\_authorship\_corpus and movie rationales.

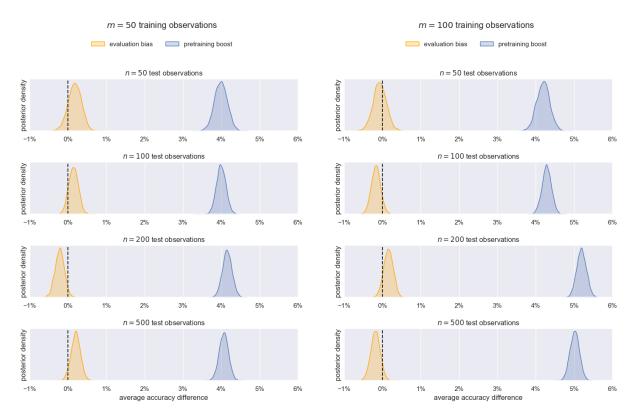


Figure 2: Distributions of average accuracy differences for m = 50 (left) and m = 100 (right). The evaluation bias is akin to  $\frac{\text{acc}_{\text{test}} - \text{acc}_{\text{extra}}}{\text{acc}_{\text{test}}}$ . The pretraining boost is akin to  $\frac{\text{acc}_{\text{extra}}}{\text{acc}_{\text{base}}}$ .

# 8 Overtraining

§4.3 posited that if there's no boost going from acc<sub>base</sub> to acc<sub>extra</sub>, then it shouldn't be surprising that there's no change going from acc<sub>extra</sub> to acc<sub>test</sub>. This check is meant to rule out undertraining as the cause of a null evaluation bias. But what if a model is *overtrained* on unlabeled text? Perhaps there's an evaluation bias when pretraining is unhelpful, because pretraining can only exploit noise in the unlabeled text which the model is then rewarded for when it's evaluated on that same text.

For example, in a brief experiment with PCA for a synthetic linear regression task (Appendix G), the evaluation bias increases with the effective rank of the features. In other words, fitting a PCA on test set features artificially improves test set performance particularly when fitting a PCA on independent features is unhelpful.

To test this hypothesis for text classification, GPT-2 is intentionally overtrained on unlabeled text for 2 epochs instead of 1.

For each of the 25 classification tasks and their subsamples, pretraining for 2 epochs instead of 1 resulted in a lower pretraining loss. The average pretraining loss is 20% lower, and the pretraining boost is negative, which indicates overfitting, as

intended. Figure 3 shows that, despite overtraining, the evaluation bias hovers around 0. Overtraining on unlabeled test set text causes test set performance to degrade to the same degree that overfitting on unlabeled independent text does.

#### 9 Zero-shot text classification

Prompting an LLM is a popular choice for solving NLP problems. Nothing prevents these prompts from being included as part of an LLM's pretraining data. For example, Gemma 2 (Gemma Team, 2024) is intentionally pretrained on prompts from the LMSYS benchmark (Zheng et al., 2023).

To study a modern prompting approach, the experiment in §4 is repeated with two modifications. First, task-adaptive pretraining is done on prompts—unlabeled texts with instructions for solving the task. Second, classification training is not performed. The further-pretrained LLM is prompted to do the task on text from the test set.

More specifically, pretraining is performed by adding a QLoRA adapter layer (Dettmers et al., 2024) to every linear layer in Mistral 7B<sup>4</sup> (Jiang et al., 2023). Perhaps notably, instructions mention the set of possible answers—the class names. Here

<sup>&</sup>lt;sup>4</sup>Mistral-7B-v0.3, the non-instruction-trained model.

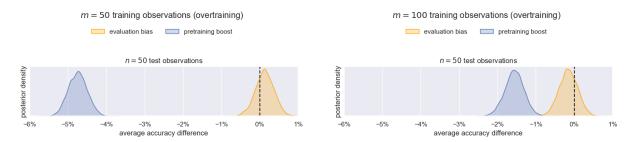


Figure 3: Distributions of average accuracy differences for m = 50 (left) and m = 100 (right) after pretraining GPT-2 for 2 epochs instead of 1 (§8).

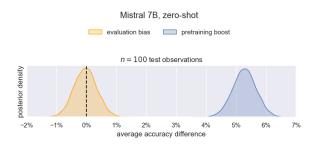


Figure 4: Distributions of average accuracy differences for zero-shot classification (§9). For each of the 25 classification tasks, 20 subsamples were taken.

is an example of a prompt for the ag\_news (Zhang et al., 2015) task:

Your task is to classify a given text as one of these categories:  $\label{eq:categories} \mbox{World}$ 

Sports Business Sci/Tech

The text is a news article. Answer with its topic.

### Text: Bombardier CEO Quits, Shares
Dive Paul Tellier stepped down on Monday
as president and chief executive of
Bombardier Inc. (BBDsvb.TO: Quote,
Profile, Research) (BBDb.
### Answer:

Figure 4 shows that while pretraining on prompts improves accuracy, pretraining on prompts directly from the test set does not increase test set accuracy compared to pretraining on independently drawn prompts.

12 of the 25 tasks had a positive evaluation bias and 13 had a negative evaluation bias. To analyze accuracies from each task (instead of averaging them as a benchmark would), a *p*-value for the following hypothesis test is computed for each task:

$$H_0: E[acc_{test} - acc_{extra}] = 0$$
  
 $H_1: E[acc_{test} - acc_{extra}] > 0.$ 

The p-value is estimated via permutation testing. It's then adjusted to control the false discovery rate (Benjamini and Hochberg, 1995). All p-values were greater than  $0.5.^5$  In other words, at the task level, there is still no evidence of evaluation bias.

A limitation of this experiment is that it doesn't account for data contamination. If Mistral 7B's pretraining data included labeled or unlabeled parts of the classification datasets used here, the pretraining boost and evaluation bias may be diluted.

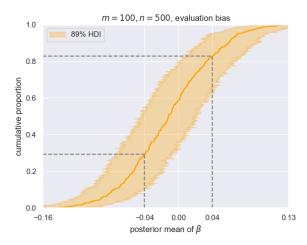
# 10 Meta-analysis

§4.4 briefly argues for subsampling multiple datasets from the full classification dataset. To assess this argument, the analysis was repeated on 500 random slices of the m=100, n=500 dataset of accuracies such that exactly 1 (acc<sub>extra</sub>, acc<sub>test</sub>, acc<sub>base</sub>) triple per classification task (instead of 20 triples) is included. This unreplicated data is often all you get from benchmarks.

Figure 5 (left) displays the cumulative distribution of the posterior mean of the evaluation bias for m=100, n=500 under this unreplicated experimental design. The distribution is quite variant. There's a 47% chance that the posterior mean of  $\beta$ —the average increase in the log-odds of a correct prediction by pretraining on unlabeled test set text instead of on unlabeled independent text—is outside the interval (-0.04, 0.04), which would indicate a significant negative or positive bias. For the zero-shot experiment in §9, there's a 49% chance that that the posterior mean of  $\beta$  is outside the interval (-0.07, 0.07). In other words, without

 $<sup>^5</sup>$ For the test that E[acc<sub>extra</sub> - acc<sub>base</sub>] > 0, 14 of the 25 p-values were less than 0.005, which demonstrates that the testing procedure may have some statistical power.

<sup>&</sup>lt;sup>6</sup>For 0.04, the odds ratio is  $e^{0.04} \approx 1.04$ . For context, the average odds ratio between adjacent submissions in the RAFT leaderboard is 1.03. For posterior means outside (-0.04, 0.04), all of their 89% credible intervals exclude 0, which evidences a non-null effect.



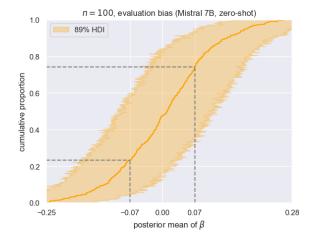


Figure 5: Distributions of this paper's conclusions for m = 100, n = 500 (left) and zero-shot n = 100 (right) had there been no technical replication (§10).

subsampling, one may as well flip a coin to decide whether pretraining on unlabeled test set text is fair.

# 11 Conclusion

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Across combinations for the number of classification training examples (m=50,100), the number of pretraining or evaluation examples (n=50,100,200,500), and for zero-shot prompting with an LLM, task-adaptive pretraining on unlabeled test set text—instead of on unlabeled independent text—did not result in a consistent or significant evaluation bias. This appears to be the case when pretraining helps ( $\S7$ ) and when it hurts ( $\S8$ ).

For benchmarks which release text from the test set, this finding doesn't completely absolve LLM evaluations from scrutiny. The reason is that the boost from pretraining on unlabeled text—which is often significant—could be viewed as a type of evaluation bias, depending on how LLMs generalize. More concretely, say there's a benchmark and two LLMs, A and B. A was not pretrained on unlabeled text from the test set of the benchmark, while B was. With the perspective that LLM benchmarks supply scores which are correlates of performance on real-world tasks—instead of indicators of performance solely on the benchmark's tasks—then B scoring higher on the benchmark than A may be a misleading signal. Because if pretraining on the benchmark's unlabeled text causes B to generalize better only within the distribution of the benchmark, then B's edge on this benchmark does not signal an edge in real-world tasks. This argument implies that knowing whether or not an LLM was pretrained on unlabeled text from the test set is still important.

One recommendation for designing few-shot benchmarks, which expands on the principle about robustness from Bragg et al. (2021) and recommendations from Madaan et al. (2024), is based on the meta-analysis in §10: empirical studies of fewshot learning should consider including multiple, independent subsamples of training data. While a single training set combined with a large test set is sufficient for precise, unbiased estimation of out-of-sample performance, this estimator is conditional on the training set. In few-shot learning, the training set is, by definition, minimal. The estimator hides two sources of variance—that from the randomly drawn training set, and that from randomness inherent in the training procedure. Figure 5 shows that this variance is large-enough to turn a methodology into a coin flip for two different training procedures. In-context learning with LLMs is also sensitive to the selection of few-shot examples (Lu et al., 2022, Alzahrani et al., 2024). Benchmarks which require training on multiple, independent subsamples would expose training variance.

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A limitation of this paper is that it does not analyze semi-supervised methods like Pattern-Exploiting Training. This paper also doesn't study hand-inspecting the test set text and targeting interventions accordingly. This paper's conclusions are limited to task-adaptive pretraining of LMs.

A direction for future research is to explore the role of causality. Jin et al. (2021) argue and demonstrate that the benefit of task-adaptive pretraining depends on the learning task's causal direction. Perhaps the principle of independent causal mechanisms is also relevant in assessing the fairness of pretraining on test set features.

# Acknowledgements

Currently omitted for anonymity.

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Hugging Face dataset	Author(s)	Number of classes	Text length (25, 75) percentiles
ag_news	Zhang et al. (2015)	4	(196, 266)
SetFit/amazon_counterfactual_en	O'Neill et al. (2021)	2	(60, 125)
app_reviews	Grano et al. (2017)	5	(10, 77)
blog_authorship_corpus	Schler et al. (2006)	2	(92, 556)
<pre>christinacdl/clickbait_notclickbait_dataset</pre>		2	(46, 69)
climate_fever	Diggelmann et al. (2020)	4	(80, 156)
aladar/craigslist_bargains	He et al. (2018)	6	(346, 713)
disaster_response_messages		3	(74, 178)
emo	Chatterjee et al. (2019)	4	(44, 83)
dair-ai/emotion	Saravia et al. (2018)	6	(53, 129)
SetFit/enron_spam	Metsis et al. (2006)	2	(342, 1553)
financial_phrasebank	Malo et al. (2014)	3	(79, 157)
classla/FRENK-hate-en	Ljubešić et al. (2019)	2	(34, 160)
hyperpartisan_news_detection	Kiesel et al. (2019)	2	(39, 63)
limit	Manotas et al. (2020)	2	(53, 123)
AmazonScience/massive	FitzGerald et al. (2023)	18	(24, 44)
movie_rationales	DeYoung et al. (2020)	2	(2721, 4659)
mteb/mtop_domain	Muennighoff et al. (2023)	11	(26, 44)
ccdv/patent-classification	Sharma et al. (2019)	9	(441, 775)
rotten_tomatoes	Pang and Lee (2005)	2	(76, 149)
silicone	Chapuis et al. (2020)	4	(29, 75)
trec	Wang et al. (2007)	6	(36, 61)
tweets_hate_speech_detection	Sharma (2019)	2	(62, 107)
yahoo_answers_topics	Huangzhao (2018)	10	(58, 213)
yelp_review_full	Zhang et al. (2015)	5	(287, 957)

Table 2: Brief descriptions of the 25 classification tasks used in this experiment. Click the link in the cell to be taken to the dataset homepage in https://huggingface.co/datasets. The dataset subset (or config) and the chosen prediction task are specified in code in src/pretrain\_on\_test/data.py.

# **B** Other experiment choices

This section expands on §4.

First, we clarify how classification training is performed. For BERT, the linear layer transforms the [CLS] token embedding. For GPT-2, the linear layer transforms the last token's embedding. The output dimension of the linear layer is the number of classes in the classification task. This layer, along with the rest of the weights in the LM, are finetuned to minimize classification cross entropy loss on train.

The BERT model used here is bert-base-uncased. The GPT-2 model used here is gpt2 (small), with 124M parameters.

train is stratify-sampled by the class to ensure every class is represented, and to reduce the variance of accuracy estimators. test is not stratify-sampled. We're only interested in the *difference* between accuracies, which is a function of the difference between model likelihoods because the priors are uniform. So even if accuracies are worse than the majority vote, differences are still meaningful for the purposes of this experiment.

train text is not included during pretraining to eliminate the overlap of pretraining data between acc<sub>extra</sub> and acc<sub>test</sub>. This choice was made in an effort to widen any gap between them. The experiment tries to go out of its way to provide evidence of a bias.

train contains m=50 or m=100 observations. m=50 is inspired by the RAFT benchmark. m=100 stretches the intention of "few" in few-shot learning, but was tested in an attempt to make lower-variance comparisons. BERT is quite sensitive—see Appendix D.2.

The discussion focuses on the BERT and GPT-2 results because their pretraining data is (likely) not already contaminated with text from the 25 text classification tasks. While modern NLP solutions usually involve LLMs, these models' pretraining data are opaque and more likely to include text from the 25 classification tasks (for example, from web-crawling the Dataset Viewer in Hugging-Face's datasets web pages, which hosts the experiment's data) (Jacovi et al., 2023). As a result, the comparisons—acc<sub>extra</sub> versus acc<sub>base</sub> and acc<sub>test</sub> versus acc<sub>extra</sub>—would be less valid.

## C Hyperparameters and reproducibility

This paper's experiment and analysis code, and data, is available here: https://github.com.

experiment. sh lists hyperparameters used for each classification task and experiment configuration. Hyperparameters were pre-specified based on Zhang et al. (2021), and to obey memory limits. Run the script on a GPU with at least 15 GB VRAM to reproduce results in §5. It takes about 5 days on a T4 GPU. Training is performed using the transformers package (Wolf et al., 2020).

## **D** Results

## **D.1** Individual analysis

The Jupyter notebook analysis/dataset.ipynb can be run to (1) produce visualizations of the distributions of  $acc_{extra}$ ,  $acc_{test}$ , and  $acc_{base}$  (for each classification task and experiment configuration), and (2) compute p-values for the hypothesis test specified in §9. For all settings of m and n, no p-values were statistically significant at the 0.05 level. Moreover, among the 25 classification tasks studied in this paper, and across settings for m and n, there weren't tasks that repeatedly popped up as having a positive evaluation bias.

Care has to be taken when attempting to analyze or interpret  $acc_{extra} - acc_{base}$  and  $acc_{test} - acc_{extra}$  together. That's because these differences are not independent: if  $acc_{extra}$  is high, then  $acc_{extra} - acc_{base}$  increases and  $acc_{test} - acc_{extra}$  decreases. This paper does not analyze the scores together, per se. We care about  $acc_{test} - acc_{extra}$ .  $acc_{extra} - acc_{base}$  only exists to sanity check that the pretraining code works; there may be an effect to detect.

#### **D.2** Difference distributions

Figure 1 and Figures 9 - 15 visualize the distributions of the paired differences— $acc_{extra} - acc_{base}$  and  $acc_{test} - acc_{extra}$ —for each configuration of the experiment.

# E Analysis

The analysis in §6 can be reproduced by running all of the Jupyter notebooks in analysis/fit\_posteriors/. Figure 2 can be reproduced by running the Jupyter notebook analysis/results/posterior\_pred.ipynb.

Posterior samples of  $\beta$  (which were used to draw posterior predictive samples) were taken from four chains with 1,000 draws each, after 500 steps of tuning.

#### E.1 Hierarchical model checks

Hierarchical models require some basic checks to have faith in their results (McElreath, 2018).

For each of the 22 hierarchical models (16 in §6, 4 in §8, and 2 in §9), no divergences were observed during the fitting procedure. All trace plots were healthy.

Figure 7 contains prior predictive distributions for m=100, n=200, demonstrating that priors are not unreasonable. Using default priors from the bambi package (Capretto et al., 2022), while scientifically unreasonable (because they result in wide, basin-like accuracy distributions), did not change the conclusions of this paper.

Figure 8 contains posterior distributions of  $\beta$  for m=100, n=200, demonstrating the hierarchical model's ability to recover both null and non-null effects. This test can be reproduced by running the Jupyter notebook analysis/test.ipynb.

# F Meta-analysis

The meta-analysis in §10 can be reproduced by running the script, analysis/meta/meta.py, and then the Jupyter notebook analysis/meta/meta.ipynb. No divergences were observed.

# **G** Experiment with PCA

This experiment's design is akin to \$4 except that the unsupervised pretraining procedure is PCA, the supervised training procedure is linear regression on synthetic data, and 2,000 subsamples are taken instead of 20-100. 20 features are generated with known effective ranks. The dependent variable is a linear transformation of these features plus independent, normally distributed noise with a standard deviation of 1. Performance is measured using  $R^2$ .

Figure 6 can be reproduced by running the note-book analysis/pca.ipynb

## H Zero-shot text classification

The zero-shot experiment files are in cloud\_scripts/gcp/experiments/zero\_shot/. Figure 4 can be reproduced by running the notebook in analysis/fit\_posteriors/zero\_shot and then the notebook, analysis/results/posterior\_pred.ipynb.

We only study n=100 in an initial effort to provide evidence of an evaluation bias (due to the relatively small test set), and take 20 repeated subsamples instead of 50. While n=100 is quite

small, benchmarks such as LegalBench (Guha et al., 2024) have test data in this range. And the analysis transparently exposes variance.

QLoRA hyperparameters were pre-specified: every adapter has rank 16 with  $\alpha=32$  (LoRA scaling factor), a 0.05 dropout rate, and no bias parameters. The adapter layers introduce 41,943,040 new, trainable parameters to Mistral 7B, whose parameters are frozen.

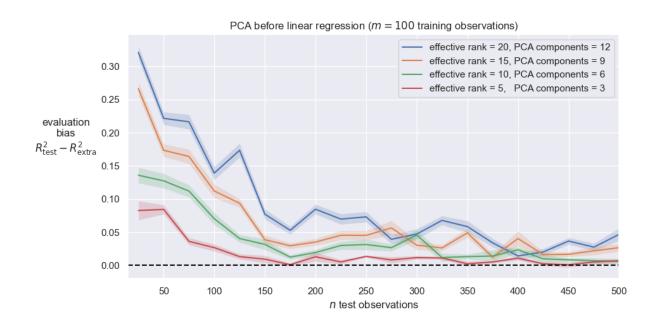


Figure 6: The shaded regions are 95% confidence intervals.

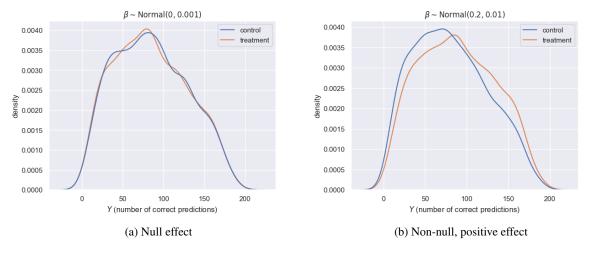


Figure 7: Prior predictive distributions for m=100, n=200 from two different priors for  $\beta$ —the expected increase in the log-odds of a correct prediction resulting from an intervention/treatment.

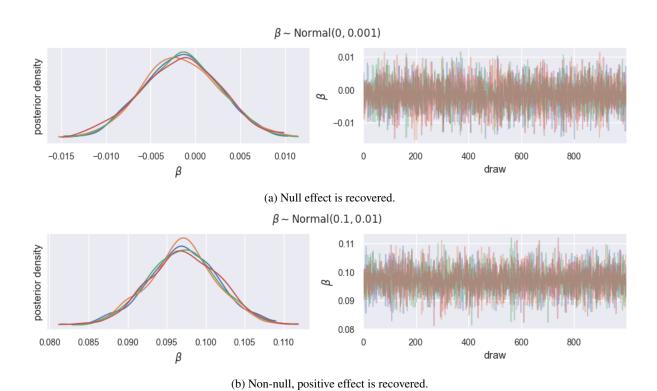


Figure 8: Posterior distributions and trace plots for null and non-null effects **from simulated data** where m=100, n=200, approximated by four chains with 1,000 draws each, after 500 steps of tuning. For each model, no divergences were observed during the fitting procedure. Visualizations were produced by the arviz package (Kumar et al., 2019).

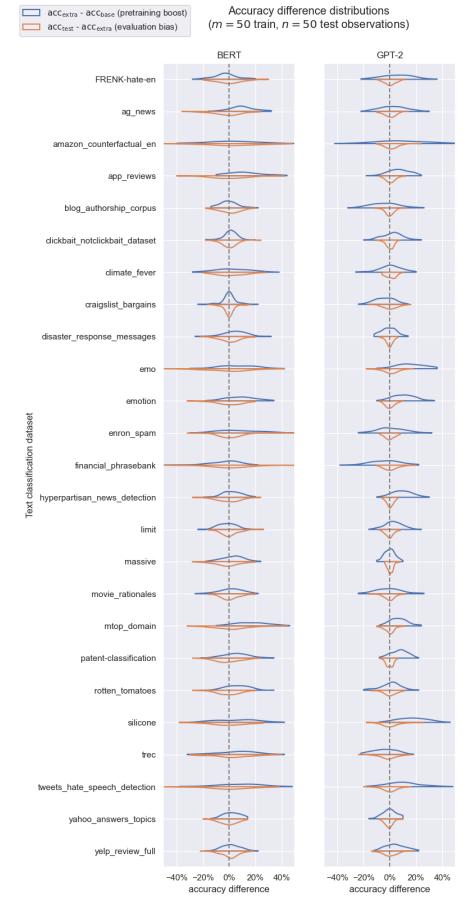


Figure 9

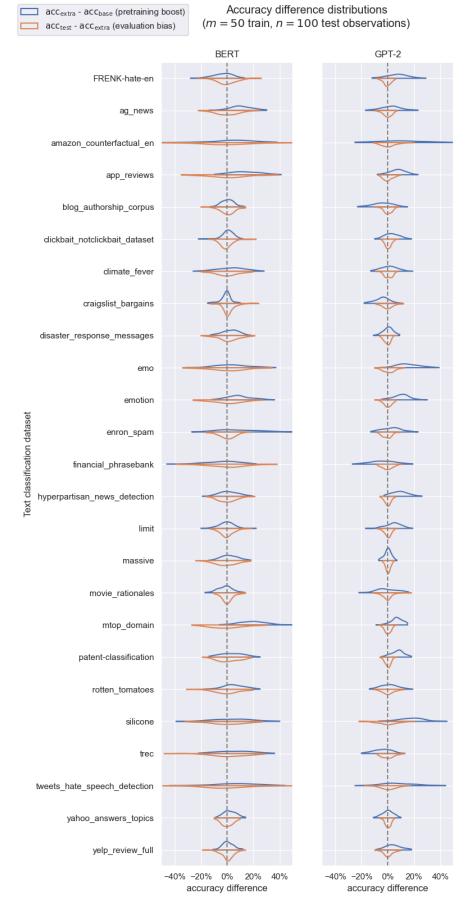


Figure 10

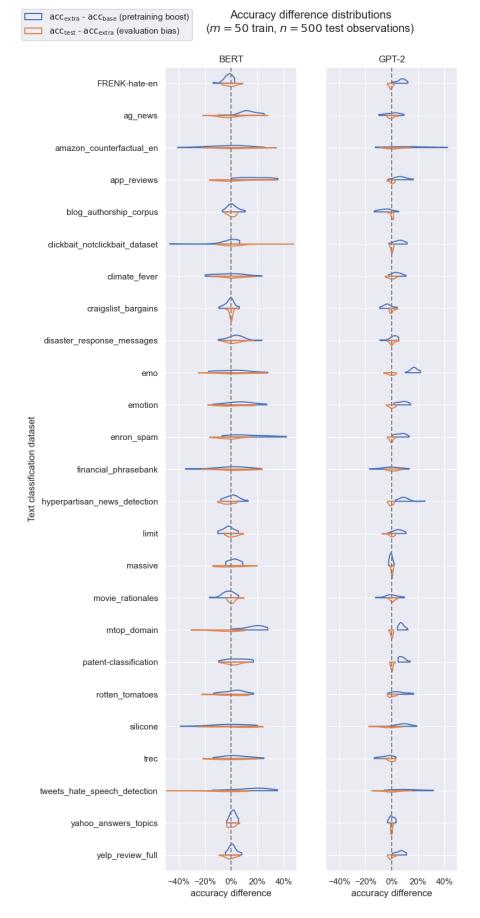


Figure 11



Figure 12

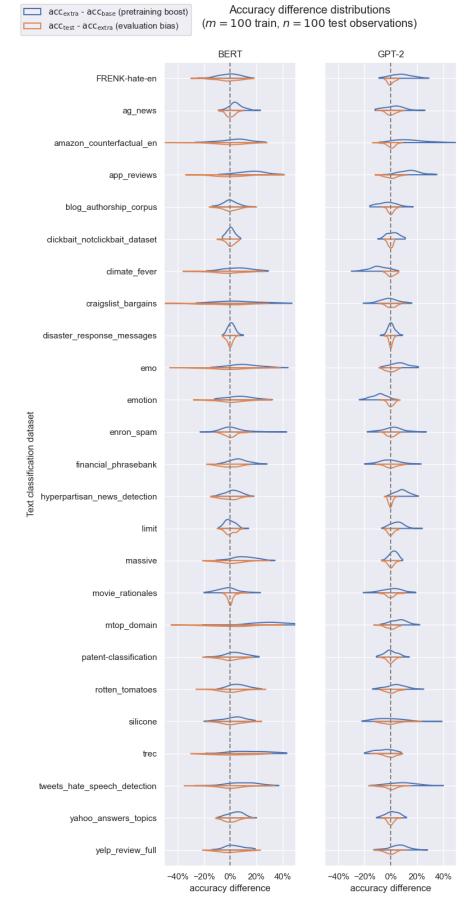


Figure 13



Figure 14

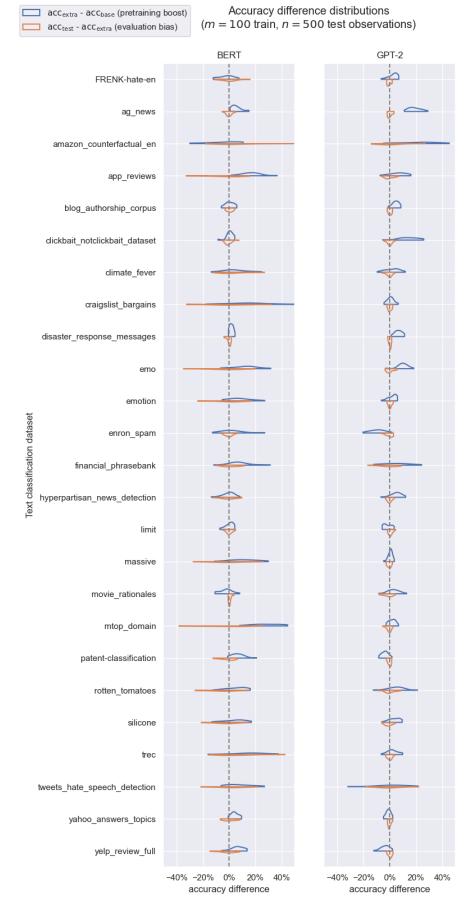


Figure 15