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Lecture 1: August 24

Lecturer: Swapan Chatterji

Scribe: Keshav Deoskar

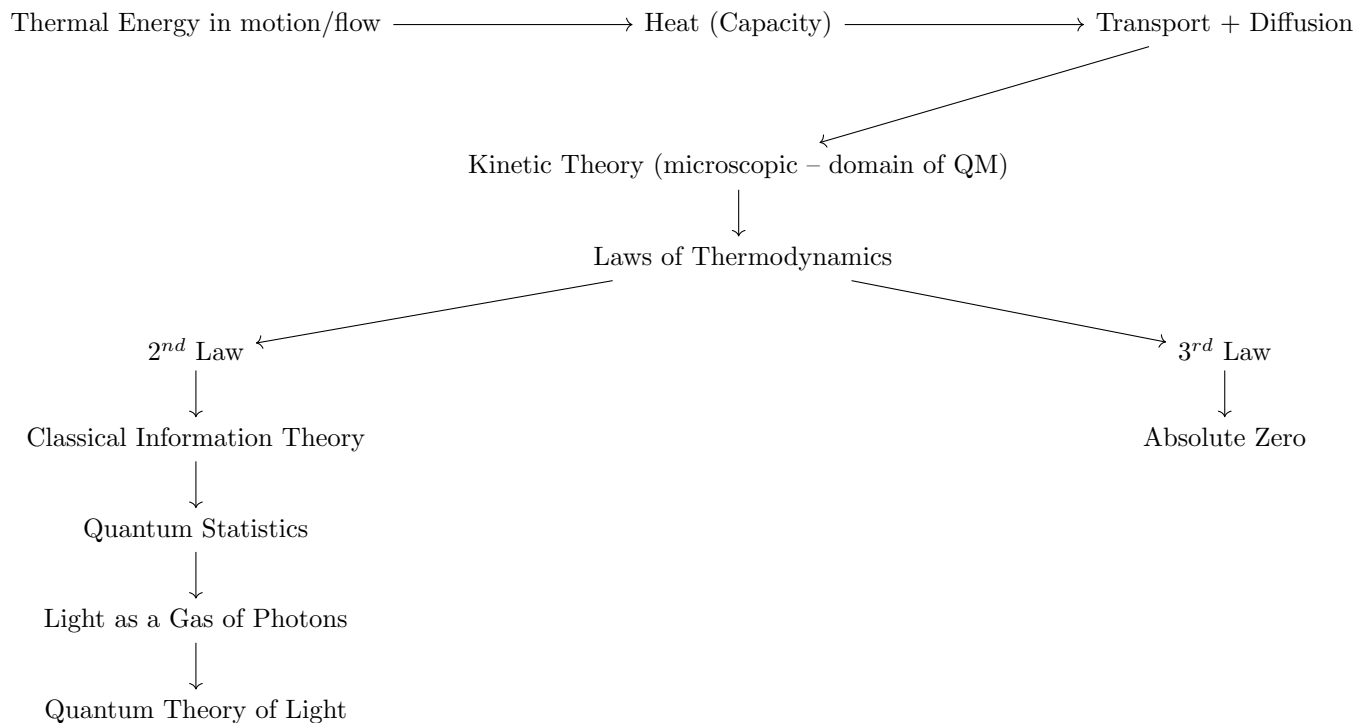
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1.1 Topics of study

In this class, we study Thermodynamics and Statistical Mechanics, as well as Quantum Mechanics. But why these two branches of physics together?

1.1.1 How are they related?

It turns out that the two are intimately connected, with both using probabilistic and statistical methods and with Quantum Mechanics being motivated by some phenomena in Stat Mech.



Physics 5C: Introductory Thermodynamics and Quantum Mechanics

Fall 2023

Lecture 2: August 28

Lecturer: Swapan Chatterji

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2.2 Preliminaries: Moles, Avogadro's Number

Mole: write definition from Blundell – good defn

Carbon was preferred in the definition of a mole because it is a solid, and so is easy to weigh.

Avogadro's Number, N_A : The number of objects in a mole.

$$N_A = 6.023 \times 10^{23}$$

Molar mass: Mass of one mole of an object.

$$M_{\text{olarnass}} = m \cdot N_A$$

where m is the weight of one object.

2.3 Thermodynamics vs. Kinetic Theory of Gasses vs. Statistical Mechanics

Write about each one from the slides:

The historical development looks something like:

Classical Thermodynamics \longrightarrow Kinetic Theory of Gases \longrightarrow Statistical Mechanics

2.4 Ideal Gas Laws

Write from slides

We can combine these three laws to derive the ***Ideal Gas Law***.

Why is it called the Ideal gas? Because

- First Assumption. WWrite from slides
- We assume there are no intermolectular forces.

2.5 Concepts of Heat and Heat Capacity

Write about heat and heat capacity

Note: Materials whose heat capacity is nonlinear are a big field of research.

2.6 Microstates and Macrostates

Consider 100 identical coins in a box, with each coin being in one of 2 states – "Heads" or "Tails". There are 2^{100} different possibilities that an arbitrary coin "shake" can produce. Each one of these states is a **microstate**.

On the other hand, suppose we're not interested in the exact configuration of each coin, but rather in the gross number of coins which land on Heads. Then, many microstates have the overall property that for ex. 30 coins are heads. Then, this is a **Macrostate**.

Note that microstates are all equally likely, whereas Macrostates are NOT equally likely. The system is completely described the set of all microstates, but what we usually measure is the macrostate of the system.

Write combinatorics review.

Write about the law of large numbers, logarithms, and Stirling's approximation.

2.7 Ergodicity: The "Erdogic" Hypothesis

"Ergo" → Indicates that this hypothesis has to do with the system doing work

Write from slides and see picture in gallery describing $6N$ dimensional space (in which each point is a configuration of the system)

2.8 Statistical Definition of Temperature

Write from slides, and include picture in gallery on Density of States.

Digression on Entropy: Changing bits in a computer changes the information and entropy, thus generating heat – write this better later.

2.9 Concept of "Ensembles"

Write about Microcanonical Ensemble, Canonical Ensemble. Grand Canonical Ensemble.

Physics 5C: Introductory Thermodynamics and Quantum Mechanics**Fall 2023****Lecture 0: September 19***Lecturer: Juan**Scribe: Keshav Deoskar***Disclaimer:** *LaTeX template courtesy of the UC Berkeley EECS Department.*

(Fill missed stuff later)

Q4 from homework: ∇^2 in spherical coordinates

In Cylindrical Coordinates, the Laplacian is

$$\nabla^2(v) = \sum_i \partial_i^2 v = \partial_x^2 v + \partial_y^2 v + \partial_z^2 v$$

The conversion from cylindrical to spherical coordinates is

$$x = r \sin \theta \cos \phi$$

$$y = r \sin \theta \sin \phi$$

$$z = r \cos \theta$$

So, $r = \sqrt{x^2 + y^2 + z^2}$ Thus,

$$\frac{\partial r}{\partial x} = \frac{x}{r} = \sin \theta \cos \phi$$

etc. etc. complete the question later.

Q5 from homework: Heat flow

We have the following system : (insert image) where the brick wall and insulated layer have two different thermal conductivities κ_1, κ_2 . The system is in steady state. Find the Heat Loss Rate per unit area of the wall.

Sol:

Our end goal is to find the Heat Flux \vec{J} , or rather $\vec{J} \cdot \vec{A}$. We have a temperature function $T(x)$ which satisfies the diffusion equation:

$$\vec{J} = \kappa \nabla T$$

Note: One of our boundary conditions is $J_1(p) = J_2(p)$ where p is the interface between the Brick Wall and Insulated Layer.

From the diffusion equation

$$J_{x_i} = -\kappa_i \nabla T_i$$

where the subscript i denotes which surface we're in.

Let T_1 and T_2 be the temperature functions in the brick and insulated layers respectively. We know that in the steady state, $\frac{\partial T}{\partial t} = 0$.

Newton's Law of Cooling:

Empirical law which states that a body's temperature cools off exponentially. So, for example, if we have hot cup of Tea placed in room temperature air, then $T_{cup} \propto e^{-\lambda T}$

(insert figure)

So, the differential equation describing this system is

Lecture 000: September 26

*Lecturer: Swapan Chatterji**Scribe: Keshav Deoskar*

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Entropy:

Recall from Claussius' Theorem that for a *reversible* process, we have

$$\oint \frac{dQ_{rev}}{T} dt = 0$$

This implies, from vector calculus, that

$$\int_A^B \frac{dQ_{rev}}{T} dt$$

is path-independent for some arbitrary points A and B .

This means that $\frac{dQ}{T}$ is an *exact differential* and so we *define* the **entropy** to be

$$dS = \frac{dQ_{rev}}{T}$$

Complete lecture notes later.

Physics 137A: Principles of Quantum Mechanics

Fall 2023

Discussion Section 7: September 26

GSI: Samuel Weiss

Scribe: Keshav Deoskar

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In the study of thermodynamics, we forget about all the microscopic states of the atoms we are studying and instead focus on the experimentally measurable macroscopic values.

There are some *Laws of Thermodynamics* – of which some were derived experimentally and some theoretically.

Laws of Thermodynamics:

First Law: $\Delta E = Q + W$ where Q and W are the Heat added and Work done to/on a system.

We can write this in differential form as

$$dE = dQ + dW$$

where the line through the d means that it is an *inexact* differential. So, Heat and Work done are inexact differentials while Energy is an exact differential. That is, there is some function $E(V, P)$ such that

$$dE = \frac{\partial E}{\partial V} dV + \frac{\partial E}{\partial P} dP$$

but no such functions exist for the heat and work.

As a consequence, the integral of dW i.e. $W_{AB} = \int_A^B dW$ depends on the path.

Reversible and Irreversible Processes:

Write from picture.

Closer look at reversible processes:

For a reversible process, we have

$$dW = -PdV$$

So, for a *finite* reversible process, we have

$$W = \int dW = - \int PdV$$

Plugging this relation back into the first law, we get

$$dE = dQ - PdV$$

So, considering some ideal gas – which follows the Ideal Gas Law $PV = Nk_B T$ and has Total Energy $\frac{d}{2}Nk_B T$ where d is the number of degrees of freedom, we have that

$$dQ = \frac{d}{2}Nk_B dT + PdV$$

Let's examine some cases:

- At constant volume i.e. $dV = 0$:

We have

$$dQ = \frac{d}{2}Nk_B dT = C_V dT$$

write out

- At constant pressure i.e. $dP = 0$: write out

Notice that $C_P = C_V + Nk_B$ – the heat capacity with pressure fixed is greater than the heat capacity with volume fixed!

One more case is $dQ = 0$.

write more from picture taken of board.

Second Law and Heat Engines:

Heat Engines Write about this stuff later.

Some exercise problems:

Q1. Some Quick Questions:

1. When an ideal gas undergoes adiabatic expansion, how does its temperature change?
Ans: During an adiabatic expansion, there is no flow of heat. So,

$$dQ = 0 \implies dU = dW$$

However, the gas is expanding which means work is done by the gas.