

Review 10-3

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1. Calculate the amortized cost of the i th TABLE-INSERT operation when $\alpha_{i-1} < 1/2$.

Case 1: $\alpha_{i-1} < 1/2$ and $\alpha_i < 1/2$.

$$\text{num}_i = \text{num}_{i-1} + 1$$

$$\text{size}_{i-1} = \text{size}_i$$

$$\hat{c}_i = c_i + \Phi_i - \Phi_{i-1}$$

$$= 1 + \text{size}_i/2 - \text{num}_i - \text{size}_{i-1}/2 + \text{num}_{i-1}$$

$$= 1 + \text{size}_i/2 - \text{num}_i - \text{size}_i/2 + \text{num}_{i-1}$$

$$= 0$$

Case 2: $\alpha_{i-1} < 1/2$ but $\alpha_i \geq 1/2$.

$$\text{num}_i = \text{num}_{i-1} + 1$$

$$\text{size}_{i-1} = \text{size}_i$$

$$\alpha_i = \frac{\text{num}_i}{\text{size}_i}$$

$$\hat{c}_i = c_i + \Phi_i - \Phi_{i-1}$$

$$= 1 + 2 * \text{num}_i - \text{size}_i - \text{size}_{i-1}/2 + \text{num}_{i-1}$$

$$= 1 + (2 * (\text{num}_{i-1} + 1) - \text{size}_i) - \text{size}_{i-1}/2 + \text{num}_{i-1}$$

$$= 3 * \text{num}_{i-1} - \frac{3}{2} \text{size}_{i-1} + 3$$

$$= 3 * \alpha_{i-1} * \text{size}_{i-1} - \frac{3}{2} \text{size}_{i-1} + 3$$

$$< \frac{3}{2} \text{size}_{i-1} - \frac{3}{2} \text{size}_{i-1} + 3$$

$$= 3$$