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Source Code:
# -*- coding: utf-8 -*-
Created on Sun Mar 19 21:36:40 2017
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from PIL import Image, ImageDraw
import random as rn
import numpy as np
import math as mt
import itertools as it
"To resize the image to replicate border pixels before convolution as per the filter size"
def resize_image(ip_im, filter_size):
  r, c = ip_im.shape
  filter_n = int((filter_size-1)/2)
  op_r = r + 2*(filter_n)
  op_c = c+2*(filter_n)
  op_im = np.zeros((op_r,op_c))
  for i in range(r):
    for j in range(c):
       op_im[i+filter_n][j+filter_n] = ip_im[i][j]
  for i in range(filter n):
    for j in range(filter n):
       op_im[i][j] = op_im[filter_n][filter_n]
  for i in range(filter_n):
    for j in range(op_c-filter_n, op_c):
       op im[i][j] = op im[filter n][op c-filter n-1]
  for i in range(op_r-filter_n, op_r):
    for j in range(filter_n):
       op_im[i][j] = op_im[op_r-filter_n-1][filter_n]
  for i in range(op_r-filter_n, op_r):
    for j in range(op c-filter n, op c):
       op_im[i][j] = op_im[op_r-filter_n-1][op_c-filter_n-1]
  for i in range(filter n):
    for j in range(filter_n, op_c-filter_n):
       op_im[i][j] = op_im[filter_n][j]
  for i in range(op_r-filter_n, op_r):
    for j in range(filter_n, op_c-filter_n):
       op_im[i][j] = op_im[op_r-filter_n-1][j]
  for i in range(filter_n, op_r-filter_n):
    for j in range(filter n):
       op im[i][j] = op im[i][filter n]
  for i in range(filter n, op r-filter n):
    for j in range(op c-filter n, op c):
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op im[i][j] = op im[i][op c-filter n-1]

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return op_im
"To perform convolution of ip with filter"
def convolution(ip,filter):
  filter size = int(mt.sqrt(filter.size))
  filter_n = int((filter_size-1)/2)
  ip_r, ip_c = ip.shape
  r = ip_r - 2*filter_n
  c = ip_c - 2*filter_n
  op im = np.zeros((r, c))
  for i in range(r):
    for j in range(c):
       for k in range(filter size):
         for I in range(filter size):
            op_{im[i][j]} = op_{im[i][j]} + (filter[k][l] * ip[i+k][j+l])
  return op_im
"To create the gaussian filter"
def gauss filter(im, size, sigma):
  size = int(size)
  sigma = float(sigma)
  og im = np.array(im)
  filter = np.zeros((size,size))
  filter n = int((size-1)/2)
  y, x = np.ogrid[float(-filter_n):float(filter_n+1),float(-filter_n):float(filter_n+1)]
  sum = 0
  for i in range(size):
    for j in range(size):
       e = mt.exp((-((x[0][j]**2)+(y[i][0]**2))/(2*(sigma**2))))
       filter[i][j] = e*(1/(2*mt.pi*(sigma**2)))
       sum = sum + filter[i][j]
  for i in range(size):
    for j in range(size):
       filter[i][j] = filter[i][j]/sum
  r, c = og im.shape
  m_im = resize_image(og_im, size)
  m r, m c = m im.shape
  op im = convolution(m im, filter)
  op_im = Image.fromarray(op_im)
  return op_im
"To obtain the X-derivative"
def grad_x(ip_im):
  filter_x = [[-1,0,+1], [-2,0,+2], [-1,0,+1]]
  filter x = np.array(filter x)
  m im = resize image(ip im, 3)
  op_im = convolution(m_im, filter_x)
  return op im
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"To obtain the Y-derivative"
def grad y(ip im):
  filter_y = [[+1,+2,+1], [0,0,0], [-1,-2,-1]]
  filter y = np.array(filter y)
  m_im = resize_image(ip_im, 3)
  op_im = convolution(m_im, filter_y)
  return op_im
"To obtain the output of the Hessian Detector"
def hessian detector(im):
  ip im = np.array(im)
  r, c = ip im.shape
  op im = np.zeros((r, c))
  f im = op im
  im_xx = grad_x(grad_x(ip_im))
  im_yy = grad_y(grad_y(ip_im))
  im_xy = grad_x(grad_y(ip_im))
  for i in range(r):
    for j in range(c):
       op_{im[i][j]} = (im_{xx[i][j]} * im_{yy[i][j]}) - (im_{xy[i][j]} ** 2)
  op im max = np.amax(op_im)
  op_im_min = np.amin(op_im)
  old_range = op_im_max - op_im_min
  for i in range(r):
    for j in range(c):
       op_im[i][j] = (op_im[i][j] - op_im_min) * (255/old_range)
  for i in range(r):
    for j in range(c):
       if(op_im[i][j] < 125):
         op_im[i][j] = 0
       else:
         op im[i][i] = 255
  op_im = resize_image(op_im, 3)
  r, c = op im.shape
  for i in range(1, r-1):
    for j in range(1, c-1):
       if(op_im[i][j] != max(op_im[i-1][j-1], op_im[i-1][j], op_im[i-1][j+1], op_im[i][j-1], op_im[i][j],
op_im[i][j+1], op_im[i+1][j-1], op_im[i+1][j], op_im[i+1][j+1])):
         f_{im}[i-1][j-1] = 0
       else:
         f_{im[i-1][j-1]} = op_{im[i][j]}
  f_im = f_im.astype(np.uint8)
  f im = Image.fromarray(f im)
  return f im
"To generate the sample space of potential point pairs for RANSAC operation"
def gen sample space(im):
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ip im = np.asarray(im)
  r, c = ip im.shape
  n points = 0
  sample_space = []
  for i in range(r):
    for j in range(c):
       if(ip_im[i][j] != 0):
         n_points = n_points + 1
  for i in range(r):
    for j in range(int(c/3),c):
       if(ip_im[i][j] != 0):
         sample space.append([j, i])
  sample space = list(it.combinations(sample space, 2))
  return sample space, n points
"To perform the RANSAC operation and obtain potential line models"
def ransac(im, sample_space, n_points):
  ip_im = np.asarray(im)
  r, c = ip im.shape
  r_iter = 500
  r dist = 3
  r no inlier = 70
  r ratio = 0.06
  fit pt mod = []
  while(r_iter != 0):
    sample_space, pt_mod = select_one(sample_space)
    l_mod = line_model(pt_mod)
    inliers = []
    no_inlier = 0
    put flag = 1
    for i in range(r):
       for j in range(c):
         if(ip im[i][i] != 0):
           x, y = find_inter_pt(l_mod, j, i)
           dist = mt.sqrt(((x - j)**2) + ((y - i)**2))
           if(dist < r dist):
              inliers.append([j, i])
              no inlier = no inlier + 1
    if(no_inlier/n_points > r_ratio and no_inlier > r_no_inlier):
       ratio = no_inlier/n_points
       inliers.sort()
       in len = len(inliers)
       if([ratio, [inliers[0], inliers[in_len - 1]]] not in fit_pt_mod):
         if(fit pt mod == []):
           fit_pt_mod.append([ratio, [inliers[0], inliers[in_len - 1]]])
         for k in fit pt mod:
           if(inliers[0] in k[1] or inliers[in len - 1] in k[1] or ratio == k[0]):
              put flag = 0
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break
        if(put flag == 1):
           fit pt mod.append([ratio, [inliers[0], inliers[in len - 1]]])
    r iter = r iter - 1
  fit pt mod.sort()
  return fit_pt_mod
"To plot the 4 line models with the strongest support obtained from RANSAC"
def plot_ransac(ip_im, ip_im2, fit_pt_mod):
  no plot = 4
  i = len(fit pt mod) - 1
  while(no plot != 0):
    pt mod = fit pt mod[i][1]
    x1 = pt \mod[0][0]
    y1 = pt_mod[0][1]
    x2 = pt_mod[1][0]
    y2 = pt_mod[1][1]
    ip_im_draw = ImageDraw.Draw(ip_im)
    ip_im_draw = endpt_draw(ip_im_draw, x1, y1, x2, y2)
    ip_im_draw.line((x1, y1, x2, y2), fill = 255)
    ip im2 draw = ImageDraw.Draw(ip im2)
    ip im2 draw = endpt draw(ip im2 draw, x1, y1, x2, y2)
    ip im2 draw.line((x1, y1, x2, y2), fill = 255)
    i = i - 1
    no_plot = no_plot-1
  return ip im, ip im2
"To create a line model(m and c) from two points"
def line_model(pt_list):
  x1 = pt list[0][0]
  y1 = pt_list[0][1]
  x2 = pt_list[1][0]
  y2 = pt list[1][1]
  if((x2 - x1) == 0):
    m = mt.inf
  else:
    m = (y2 - y1)/(x2 - x1)
  c = y2 - (m*x2)
  return [m, c]
"To find the intersection point of the normal from (x, y) to the line represented by line_model"
def find_inter_pt(line_model, x, y):
  m = line_model[0]
  c = line model[1]
  xi = (x + (m*y) - (m*c))/(1 + m**2)
  yi = ((m*x) + ((m**2)*y) - ((m**2)*c))/(1 + m**2) + c
  return xi, yi
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"To select a single pair of points from the sample space"
def select one(sample space):
  space len = len(sample space)
  pti = rn.randint(0, space len-1)
  l mod = sample space[pti]
  sample_space.remove(l_mod)
  return sample_space, I_mod
"To obtain the Hough transform, also with local maxima calculated"
def hough(ip im):
  ip im = np.asarray(ip_im)
  r, c = ip im.shape
  bin r = int(((r + (c/2)) * 2) + 1)
  offset = int((bin_r - 1) / 2)
  bin c = 181
  bin_space = np.zeros((bin_r, bin_c))
  for i in range(r):
    for j in range(c):
      if(ip im[i][j] != 0):
        for angle in range(bin_c):
           r = int(((i * mt.cos(mt.radians(angle))) + (i * mt.sin(mt.radians(angle)))) + offset)
           bin space[r][angle] = bin space[r][angle] + 5
  bin space = bin space.astype(np.uint8)
  bin space im = Image.fromarray(bin space)
  bin space = resize image(bin space, 3)
  op im = np.zeros((bin r, bin c))
  for i in range(1, bin r-1):
    for j in range(1, bin_c-1):
      if(bin_space[i][j] != max(bin_space[i-1][j-1], bin_space[i-1][j], bin_space[i-1][j+1], bin_space[i][j-1],
bin_space[i][j], bin_space[i][j+1], bin_space[i+1][j-1], bin_space[i+1][j], bin_space[i+1][j+1])):
         op_{im}[i-1][j-1] = 0
      else:
         op im[i-1][j-1] = bin space[i][j]
  op im = Image.fromarray(op im)
  return op im, bin space im
"To plot the 4 lines obtained from the Hough transform"
def hough map(ip im, ip im2, hough im):
  hough_im_c = np.asarray(hough_im)
  bin_r, bin_c = hough_im_c.shape
  r, col = np.asarray(ip_im).shape
  offset = int((bin r - 1) / 2)
  max_pt_list = []
  max pt = 0
  no of pts = 10
  ip im draw = ImageDraw.Draw(ip im)
  ip im2 draw = ImageDraw.Draw(ip im2)
  hough im c.setflags(write = 1)
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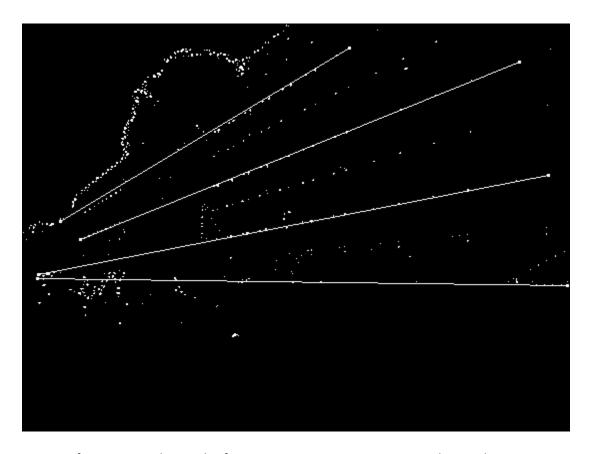
```
while(no of pts!=0):
    for i in range(bin r):
       for j in range(bin c):
         if(hough_im_c[i][j] > max_pt):
           max pt = hough im c[i][j]
           r = i - offset
           angle = j
           acc i = i
           acc_j = j
    hough im c[acc i][acc j] = 0
    a = mt.cos(mt.radians(angle))
    b = mt.sin(mt.radians(angle))
    x0 = int(r * a)
    y0 = int(r * b)
    m = (-mt.cos(mt.radians(angle)))/(mt.sin(mt.radians(angle)))
    c = r/(mt.sin(mt.radians(angle)))
    x1 = x0 + 400
    y1 = (x1 * m) + c
    x2 = x0 - 50
    y2 = (x2 * m) + c
    #ip im = ip im.convert('RGB')
    if(no of pts in [10, 9, 8, 2]):
       ip_im_draw = endpt_draw(ip_im_draw, x1, y1, x2, y2)
       ip im draw.line((x0, y0, x1, y1), fill = 255)
       ip_im_draw.line((x0, y0, x2, y2), fill = 255)
       ip im2 draw = endpt draw(ip im2 draw, x1, y1, x2, y2)
      ip_im2_draw.line((x0, y0, x1, y1), fill = 255)
       ip_im2_draw.line((x0, y0, x2, y2), fill = 255)
    hough_im_c[r+offset][angle] = 0
    max pt list.append([r+offset, angle])
    no_of_pts = no_of_pts - 1
    max_pt = 0
  return ip im, ip im2
"To draw the 3x3 square at the end-points"
def endpt draw(ip im draw, x0, y0, x1, y1):
  ip im draw.line((x0-1, y0+1, x0+1, y0+1), fill = 255)
  ip im draw.line((x0-1, y0+1, x0-1, y0-1), fill = 255)
  ip_im_draw.line((x0+1, y0+1, x0+1, y0-1), fill = 255)
  ip_im_draw.line((x0-1, y0-1, x0+1, y0-1), fill = 255)
  ip_im_draw.line((x1-1, y1+1, x1+1, y1+1), fill = 255)
  ip_im_draw.line((x1-1, y1+1, x1-1, y1-1), fill = 255)
  ip_im_draw.line((x1+1, y1+1, x1+1, y1-1), fill = 255)
  ip im draw.line((x1-1, y1-1, x1+1, y1-1), fill = 255)
  return ip im draw
"Main function"
def main():
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og_im = Image.open("road.png")
  og_im.show()
  sigma = 0.5
  size = 5
  g_im = gauss_filter(og_im, size, sigma)
  h_im = hessian_detector(g_im)
  h_im.show()
  r_{im} = h_{im.copy()}
  r_og_im = og_im.copy()
  sample_space, n_pts = gen_sample_space(r_im)
  draw_model = ransac(r_im, sample_space, n_pts)
  r_op_im, r_op_im_raw = plot_ransac(r_og_im, r_im, draw_model)
  r_op_im_raw.show()
  r_op_im.show()
  ho_im = h_im.copy()
  ho_og_im = og_im.copy()
  ho_int_im, ho_tr_im = hough(ho_im)
  ho_tr_im.show()
  ho_op_im, ho_op_im_raw = hough_map(ho_og_im, ho_im, ho_int_im)
  ho_op_im_raw.show()
  ho_op_im.show()
main()
```

Output Images:



Output of the Hessian Detector



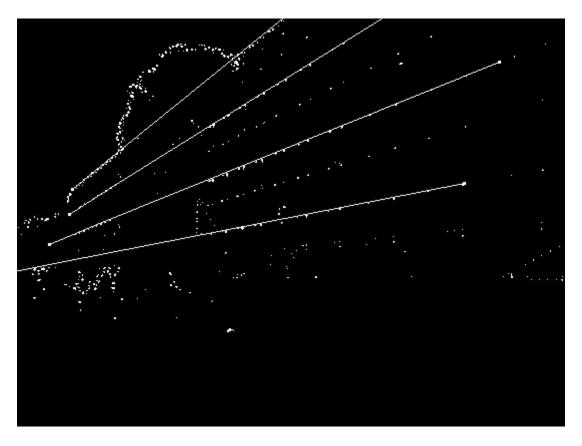
Output of RANSAC on the result of Hessian Detector. Repetitions are detected sometimes.



Lines found using RANSAC on the original image.



The Hough Transform obtained from the result of Hessian Detector



Lines found using Hough Transform drawn on the result of Hessian Detector



Lines found using Hough Transform drawn on the original image

Notes:

For the Hessian Detector, the threshold is the primary parameter. A good threshold results in well-defined points. The corners of the vegetation are also detected, which can errors in the process of line detection. It is crucial to normalize the intensities of the pixels after the process of calculating the Determinant of Hessian. If this step is not performed, then a chipped image form is obtained. Non-maximum suppression is performed to obtain the local maxima. The initial step is a Gaussian blur, performed with a sigma value of 0.5 and a filter size of 5.

For RANSAC operation, a sample space is necessary, which is generated using the output of the Hessian Detector. The ransac function has initial parameters, such as the number of iterations (set to 500), threshold distance (set to 3), the required number of inliers for a potential fit model (set to 70) and the inlier to total points ratio (set to 0.06). There may be repetitions in detection sometimes. Lowering the number of iterations will result in less detections for the same ratio and the same number of required inliers. Hence, the tweaking of parameters has to be done carefully. Lowering the number of iterations may require lowering the required number of inliers as well. Line models that seem like a potential fit are stored and the strongest 4 lines are then plotted.

For Hough Transform, the parameters of the bin space are important. The angle parameter goes from 0 to 180, while the parameter r may vary, and depends upon the angle, as bin space is generated using the parametric form. The local maxima from the Hough transform are obtained, and then converted back to lines. 4 of such lines that look like the best fit are drawn.