This is a power conversion element that interfaces a nonlinear time domain model, in the Hammerstein-Wiener (HW) framework, to the OpenDSS dynamics mode. The model senses terminal voltage and updates the injected current at each OpenDSS time step. Figure 1 shows the relationship between HW and OpenDSS domains, and it defines the key signal locations to reference when reading the Delphi code. In a snapshot mode, the model injected current will be constant, as determined by its ratings and initial power output level. The initial application is for photovoltaic (PV) inverter modeling, and the parameters are defined in those terms. The PV inverter models are based on a project sponsored by EPRI at the University of Pittsburgh [1], and they are intended to fill a gap between very detailed [2] and very simple [3] models.

## **Hammerstein-Wiener Model in Discrete Time Domain**

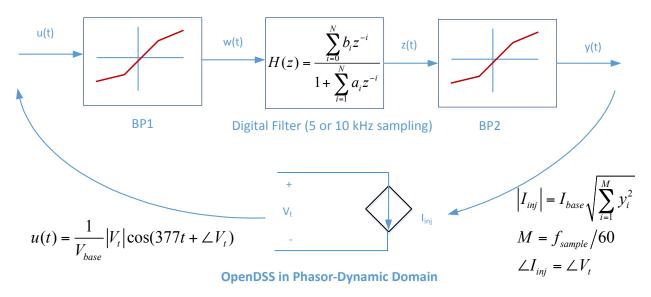


Figure 1: Interface between HW and OpenDSS solution variables

Input parameters are listed below. The HW components in Figure 1 work on per-unit variables, so the user will generally *adjust only the three bold-italics* parameters for specific applications.

- Basefreq: as other PC elements (assumed 60 in Figure 1)
- BP1: XYCurve defining the input piecewise linear block in Figure 1
- BP2: XYCurve defining the output piecewise linear block in Figure 1
- Bus1: as other PC elements
- Enabled: as other PC elements
- Filter: XYCurve defining the infinite impulse response (IIR) digital filter coefficients in Figure 1. X values are the numerator coefficients and Y values are the denominator coefficients, and note that  $a_0$ =1 must be input explicitly. This also enforces equal order in numerator and denominator.
- Fsample: sampling rate for H(z), either 5 kHz or 10 kHz in this project.
- Like: as other PC elements
- Phases: as other PC elements, but only 1-phase implemented now. 3-phase under development.
- Ppct: real power output in snapshot mode, based on Prated. Unity power factor assumed.
- **Prated**: inverter's rated power in Watts

- Spectrum: as other PC elements, but not implemented here.
- Vrated: rated line-to-line voltage (3-phase) or line-to-neutral voltage (1-phase) in volts

#### **HWTest.DSS**

This file illustrates two inverter models in a snapshot solution. The inverters are connected to a 360-volt source, which matches the lab tests done at 208 volts. The short circuit current supplied by the source is 7354 amps. When *phases*=3, the VCCS component works in snapshot mode, but not yet in dynamics mode. *BP1*, *BP2*, *Filter* and *Fsample* have no effect in snapshot mode. The initial currents will be

$$I_{\rm SMA1} = \frac{3000}{208} \frac{100}{100} = 14.42 \text{ and } I_{\rm SMA3} = \frac{3000}{360\sqrt{3}} \frac{50}{100} = 2.41$$

```
Clear
new circuit.HWTest
~ basekv=0.360 pu=1.0 angle=0 phases=3 bus1=SourceBus r1=0.02 r0=0.02 x1=0.02 x0=0.02

redirect HW_Inverters.txt

New VCCS.PV1 Phases=1 Bus1=SourceBus.1 Prated=3000 Vrated=208
~ Ppct=100 bp1='bp1_1phase' bp2='bp2_1phase' filter='z_1phase' fsample=10000

New VCCS.PV3 Phases=3 Bus1=SourceBus Prated=3000 Vrated=360
~ Ppct= 50 bp1='bp1_1phase' bp2='bp2_1phase' filter='z_1phase' fsample=10000

Set Voltagebases=[0.360]
set maxiterations=100
calcv
Solve
```

## HWDynTest.dss

The file that runs a dynamics test has been set up to run either the single-phase inverter or the microinverter, feeding a bolted fault with source impedance adjusted to match that of Pitt's electric power lab. The fault's *ontime* value will determine when the HW model departs from its initial condition. In this case, *Fsample* is 10 kHz, so the OpenDSS time step must be at least 0.1 ms, but it can be longer. The HW model can run at a faster time step within each OpenDSS time step.

```
Clear

// EPSL impedance is 10% on 75 kVA positive sequence, 5% zero sequence,
assume X/R = 2

new circuit.HWDynamic

~ basekv=0.360 pu=1.0 angle=0 phases=3 bus1=SourceBus r1=0.029 x1=0.058

r0=0.014 x0=0.029

redirect HW_Inverters.txt

New vccs.pv Phases=1 Bus1=SourceBus.1 Prated=3000 Vrated=208 Ppct=100

~ bp1='bp1_1phase' bp2='bp2_1phase' filter='z_1phase' fsample=10000

//New vccs.pv Phases=1 Bus1=SourceBus.1 Prated=190 Vrated=208 Ppct=89.5

//~ bp1='bp1_micro' bp2='bp2_micro' filter='z_micro' fsample=10000

new fault.flt bus1=Sourcebus.1 phases=1 r=0.001 temporary=yes ontime=0.1

new monitor.invvi element=vccs.pv terminal=1 mode=0
```

```
new monitor.invpq element=vccs.pv terminal=1 mode=1
new monitor.invst element=vccs.pv terminal=1 mode=3
new monitor.fltvi element=fault.flt terminal=1 mode=0

Set Voltagebases=[0.360]
set maxiterations=100
calcv

set mode=snap
solve

set mode=dynamic
set stepsize=0.01 // 0.0001 matches fsample
set number=25 // 2500 matches fsample
Solve
```

# HW Inverters.txt

This included file defines *BP1*, *BP2*, and a 14<sup>th</sup>-order filter for the microinverter, listed below. The single-phase inverter data is formatted the same way, but it has a 51-order filter, which means its transient response will last longer.

```
// library model for microinverter
New XYcurve.bp1 micro npts=3
~ xarray=[-0.882023 0.0 0.882023]
~ yarray=[-0.19 0.0 0.19]
New XYcurve.bp2 micro npts=5
~ xarray=[-0.085467 -0.0202 0.0 0.0202 0.085467]
~ yarray=[ 4.59572
                  1.0
                         0.0 -1.0 -4.595721
New XYcurve.z micro npts=14
~ xarray=[ 1.000000000000 -1.3802100241988 -0.9341004900495 1.1196620891546
0.1499829369937 1.2123723040884 -0.7654392492287 -0.9113338678997
0.3694835076144 \ 0.1034830928158 \ 0.1549604084080 \ -0.2209879303901
0.1373924816843 -0.0352249177928 | // denominator
~ yarray=[ 0.000000000000 -0.2328126380366 0.9436331671129 -0.5290906112039
0.5053547399078 \ -1.1387058093285 \ -0.0677012182563 \ 0.5067831545610
0.4003099336092 -0.3026288423351 ] // numerator
```

# Example BP1 and BP2

Sample non-linear blocks for the single-phase inverter are shown in Figure 2. They do not necessarily display appropriate symmetry and offset characteristics. Work is ongoing to improve the stability of the fitted model, some of which has been reflected in the non-linear blocks defined in HW\_Inverters.txt listed previously. Note that **BP2** decreases with X, which required a bug fix to the XYCurve object in OpenDSS for reverse lookup. It's possible that InvControl is also affected by this fix.

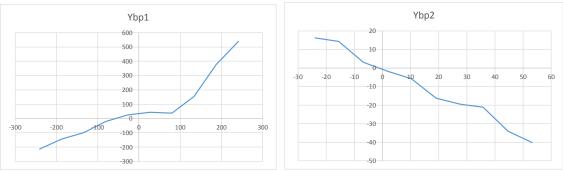


Figure 2: Sample 10-point nonlinear blocks BP1 and BP2

# Single-phase Inverter Sample Outputs

Figure 3 shows the single-phase inverter model running at OpenDSS time steps of 0.1 ms. On the left, internal HW model current waveform is in black, RMS in red and peak in blue. The model initialization is smooth, but steady state is not well established until about 0.1 seconds elapse. The red trace on the left is the per-unit RMS current injected into the feeder network. On the right, this is plotted in Amps.

In Figure 3, the OpenDSS time step matches the HW model time step. When OpenDSS runs at a slower time step, the HW model still runs internally at *Fsample*=10 kHz. However, the output is only sampled at the slower time step, and the current injections are only updated at the slower time step. Figure 4 shows this effect. Especially at 10 ms time step, the waveform is "choppy" but the RMS vs. time is not affected very much.

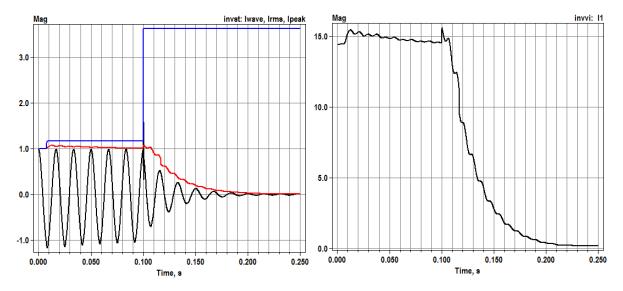


Figure 3: Current waveform, RMS and peak state variables [per-unit] for single-phase inverter. h=0.1 ms (left) and injected current into the feeder [Amps] (right)

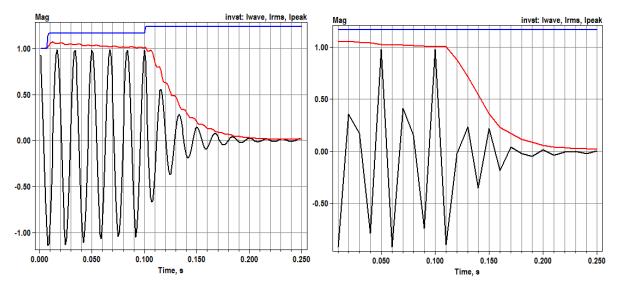
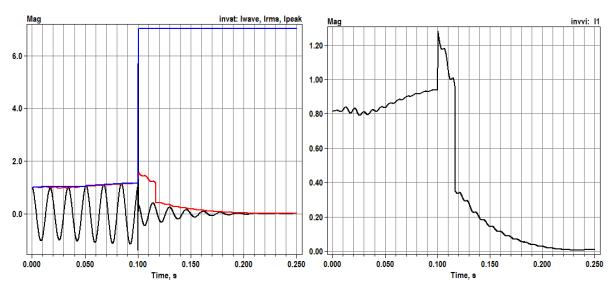


Figure 4: Current waveform, RMS and peak state variables [pu] for single-phase inverter. h=1 ms (left) and 10 ms (right)

# Microinverter Sample Outputs

Figure 5 shows a microinverter response to the same fault. With a 14<sup>th</sup>-order filter at 10 kHz sampling rate, the transient response is shorter in duration. Initialization is smooth, but the accuracy could be improved. The model captures a transient current peak that loads the inverter terminal voltage. When OpenDSS runs at a step longer than 0.1 ms, this loading effect is not captured because the RMS function smooths the current peak. Therefore, the peak current is reduced when the OpenDSS time step increases, shown in Figure 4 compared to Figure 3, or Figure 6 compared to Figure 5.



 $Figure \ 5: Microinverter \ current \ state \ variables \ [per-unit] \ (left) \ and \ injected \ current \ into \ the \ feeder \ [Amps] \ (right) \ at \ h=0.1 \ ms.$ 

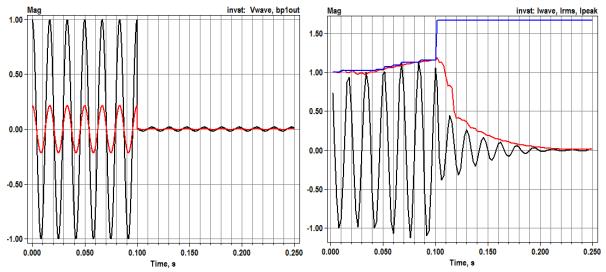


Figure 6: Microinverter voltage state variables (left) and current state variables (right) at h=2 ms.

# **Code Listings**

The most significant parts of the VCCS code define, initialize and integrate the state variables. Listings follow.

Evaluating H(z) in Figure 1 requires history storage for both input and output. A second copy of both history terms is required for the predictor and corrector steps. Otherwise, when the OpenDSS and HW steps are unequal, the last step's history could be corrupted by a partial update before the corrector step initiates. The history terms are *z*, *whist*, *zlast* and *wlast*, allocated to a size determined from the base and sampling frequencies. A ring buffer indexing scheme is used to manage this storage, with helper functions MapIdx and OffsetIdx.

The overloaded InitStateVars procedure extracts terminal voltage and current from the most recent snapshot solution. Then it steps back in time at the sampling frequency to initialize the history terms. The history of z is determined from the history of current, i, passed in reverse through BP2. The HW model current uses generator convention while the OpenDSS current uses passive convention, leading to a negative sign on the initial values of z.

The overloaded IntegrateStates procedure is called twice in each OpenDSS time step, first as predictor (Forward Euler) and then as corrector (Backward Trapezoidal). Each time, it extracts terminal voltage and ensures that *whist* and *z* begin afresh from the previous OpenDSS time step. Then, it runs through the *BP1*, *z*, and *BP2* evaluations defined in Figure 1 for the number of sampling steps contained in an OpenDSS time step. RMS current is calculated "brute force" at the end of the OpenDSS time step, for both predictor and corrector. This value, *slrms*, is later injected into the grid via the overloaded procedure GetInjCurrent (not listed below). Note that the current angle updates are not yet implemented. The peak current state variable is checked every HW step, in order to catch "fast" peaks that might not appear in monitor output. The other state variables, and the *wlast / zlast* history terms, are only updated at each OpenDSS <u>corrector</u> time step.

### private

```
Fbp1: TXYcurveObj;
Fbp1_name: String;
Fbp2: TXYcurveObj;
```

```
Fbp2 name: String;
        Ffilter: TXYcurveObj;
        Ffilter name: String;
        BaseCurr: double; // line current at Ppct
        FsampleFreq: double; // discretization frequency for Z filter
        Fwinlen: integer;
        Ffiltlen: integer;
        Irated: double; // line current at full output
        Fkv: double; // scale voltage to HW pu input
        Fki: double; // scale HW pu output to current
        // Support for Dynamics Mode - PU of Vrated and BaseCurr
        sVwave: double;
        sIwave: double;
        sIrms: double;
       sIpeak: double;
        sBP1out: double;
        sFilterout: double;
        vlast: complex;
       y2: pDoubleArray;
        z: pDoubleArray;
                             // current digital filter history terms
        whist: pDoubleArray;
        zlast: pDoubleArray; // update only after the corrector step
        wlast: pDoubleArray;
        sIdxU: integer; // ring buffer index for z and whist
        sIdxY: integer; // ring buffer index for y2 (rms current)
       y2sum: double;
// helper functions for ring buffer indexing, 1..len
function MapIdx(idx, len: integer):integer;
begin
 while idx <= 0 do idx := idx + len;
 Result := idx mod (len + 1);
 if Result = 0 then Result := 1;
end;
function OffsetIdx(idx, offset, len: integer):integer;
 Result := MapIdx(idx+offset, len);
end;
// support for DYNAMICMODE
// NB: The test data and HW model used source convention (I and V in phase)
      However, OpenDSS uses the load convention
procedure TVCCSObj.InitStateVars;
var
 d, wt, wd, val, iang, vang: double;
 i, k: integer;
 // initialize outputs from the terminal conditions
 ComputeIterminal;
 iang := cang(Iterminal^[1]);
 vang := cang(Vterminal^[1]);
 sVwave := cabs(Vterminal^[1]) / Vrated;
 sIrms := cabs(Iterminal^[1]) / BaseCurr;
 sIwave := sIrms;
 sIpeak := sIrms;
 sBP1out := 0;
```

```
sFilterout := 0;
  vlast := cdivreal (Vterminal^[1], Vrated);
  // initialize the history terms for HW model source convention
  d := 1 / FsampleFreq;
  wd := 2 * Pi * ActiveSolutionObj.Frequency * d;
  for i := 1 to Ffiltlen do begin
   wt := vang - wd * (Ffiltlen - i);
   whist[i] := 0;
   whist[i] := Fbp1.GetYValue(sVwave * cos(wt));
   wlast[i] := whist[i];
  end;
  for i := 1 to Fwinlen do begin
   wt := iang - wd * (Fwinlen - i);
   val := sIrms * cos(wt); // current by passive sign convention
   y2[i] := val * val;
    k := i - Fwinlen + Ffiltlen;
   if k > 0 then begin
     z[k] := -Fbp2.GetXvalue (val); // HW history with generator convention
      zlast[k] := z[k];
   end:
  end;
  // initialize the ring buffer indices; these increment by 1 before actual use
  sIdxU := 0;
 sIdxY := 0;
end;
// this is called twice per dynamic time step; predictor then corrector
procedure TVCCSObj.IntegrateStates;
var
 t, h, d, f, w, wt: double;
 vre, vim, vin, scale, y: double;
 nstep, i, k, corrector: integer;
 vnow: complex;
 iu, iy: integer; // local copies of sIdxU and sIdxY for predictor
begin
 ComputeIterminal;
  t := ActiveSolutionObj.DynaVars.t;
  h := ActiveSolutionObj.DynaVars.h;
  f := ActiveSolutionObj.Frequency;
  corrector := ActiveSolutionObj.DynaVars.IterationFlag;
  d := 1 / FSampleFreq;
  nstep := trunc (1e-6 + h/d);
  w := 2 * Pi * f;
 vnow := cdivreal (Vterminal^[1], Vrated);
  vin := 0;
  y := 0;
  iu := sIdxU;
  iy := sIdxY;
  for k := 1 to FFiltlen do begin
   z[k] := zlast[k];
   whist[k] := wlast[k];
  end:
  for i:=1 to nstep do begin
   iu := OffsetIdx (iu, 1, Ffiltlen);
```

```
// push input voltage waveform through the first PWL block
   scale := 1.0 * i / nstep;
   vre := vlast.re + (vnow.re - vlast.re) * scale;
   vim := vlast.im + (vnow.im - vlast.im) * scale;
   wt := w * (t - h + i * d);
   vin := (vre * cos(wt) + vim * sin(wt));
   whist[iu] := Fbp1.GetYValue(vin);
    // apply the filter and second PWL block
   z[iu] := 0;
    for k := 1 to Ffiltlen do begin
     z[iu] := z[iu] + Ffilter.Yvalue pt[k] * whist[MapIdx(iu-k+1,Ffiltlen)];
    for k := 2 to Ffiltlen do begin
     z[iu] := z[iu] - Ffilter.Xvalue_pt[k] * z[MapIdx(iu-k+1,Ffiltlen)];
    end;
   y := Fbp2.GetYValue(z[iu]);
    // updating outputs
   if (corrector = 1) and (abs(y) > sIpeak) then
     sIpeak := abs(y); // catching the fastest peaks
    // update the RMS
   iy := OffsetIdx (iy, 1, Fwinlen);
   y2[iy] := y * y; // brute-force RMS update
   if i = nstep then begin
     y2sum := 0.0;
     for k := 1 to Fwinlen do y2sum := y2sum + y2[k];
     sIrms := sqrt(2.0 * y2sum / Fwinlen); // TODO - this is the magnitude, what
about angle?
   end;
 end;
 if corrector = 1 then begin
   sIdxU := iu;
   sIdxY := iy;
   vlast := vnow;
   sVwave := vin;
   sBPlout := whist[sIdxU];
   sFilterout := z[sIdxU];
   sIwave := y;
   for k := 1 to FFiltlen do begin
     zlast[k] := z[k];
     wlast[k] := whist[k];
   end;
 end;
end:
```

## DG Prot Fdr.dss

Our last example illustrates use of the VCCS model in an IEEE test feeder for DG protection analysis. See Figure 7, with feeder data defined in [4]. The DG was originally assumed to contribute fault current as a rotating machine, but here the source is a PV inverter, represented with a VCCS. Note that the VCCS does not emulate solar panel efficiency, power fluctuations, or smart inverter control; for those features, please use other components of OpenDSS (e.g. PVSystem, InvControl, ExpControl). In Figure 7, we will apply single-line-to-ground faults (SLGF) at the feeder mid-point location, bus **Bm** or fault location **3**.

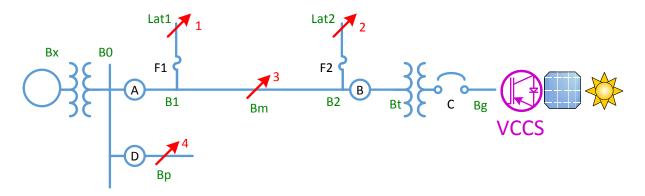


Figure 7: IEEE test feeder for DG protection analysis [4]

Here is a partial listing of the test file **DG\_Prot\_Fdr.dss**, showing the 1.7 MVA wind turbine generator commented out, and an equivalent 1.7 MW PV generator comprised of single-phase inverters. In either case, a 1700-kVA wye/wye interconnection transformer interfaces the DG to the primary feeder.

```
// DG interconnection transformer and a conventional machine
new Transformer.Tq phases=3 windings=2 buses=(Bt Bq) conns=(Wye Wye)
~ kvs='12.47 0.36' kvas='1700 1700' taps='1 1' XHL=5
//new Vsource.WindGen1 bus1=Bg basekv=0.36 pu=1.0 angle=-60.0
//\sim X1=0.0127 R1=0.0 X0=100.0 R0=0.0
redirect HW Inverters.txt
New vccs.pv1 Phases=1 Bus1=Bg.1 Prated=567e3 Vrated=208 Ppct=100
~ bp1='bp1 1phase' bp2='bp2 1phase' filter='z 1phase' fsample=10000
New vccs.pv2 Phases=1 Bus1=Bg.2 like=pv1
New vccs.pv3 Phases=1 Bus1=Bq.3 like=pv1
// Inverter Model Monitors
new monitor.invst1 element=vccs.pv1 terminal=1 mode=3
new monitor.invst2 element=vccs.pv2 terminal=1 mode=3
new monitor.invst3 element=vccs.pv3 terminal=1 mode=3
new monitor.invvi element=vccs.pv1 terminal=1 mode=0
new monitor.invpq element=vccs.pv1 terminal=1 mode=1
```

Figure 8 shows the current and voltage through recloser B, on the high side of the interconnection transformer, with a 1700-kW PV inverter source backfeeding the fault at Bm. The fault occurs at 0.2 seconds, just after steady-state DG output currents have stabilized. The faulted phase voltage (Figure 8 right) collapses almost immediately. Figure 9 shows the same fault response for a Thevenin equivalent source in place of the PV. The Thevenin impedance is sized to produce 6 pu short-circuit current at the source terminals based on 1700 kVA. As a result, the fault contribution is higher and the feeder primary voltage on the faulted phase, at recloser B, is maintained at a low level indefinitely.

In conclusion, the HW model response and initialization has improved since the last version of this Tech Note. Per-unit scaling has also been implemented. Work continues to improve stability and quality of the HW model fitting process.

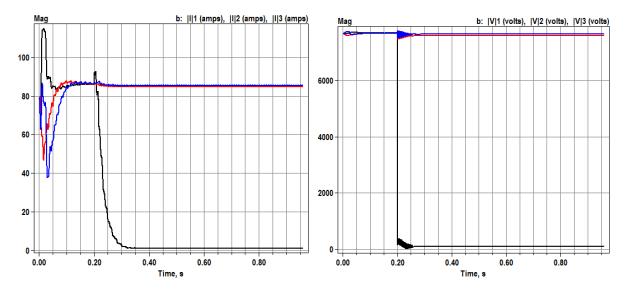


Figure 8: Currents (left) and voltages (right) at recloser B with 1.7 MW PV and single-phase inverter model

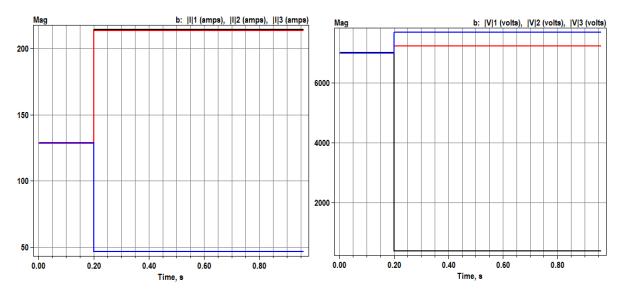


Figure 9: Currents (left) and voltages (right) at recloser B with 1.7 MW rotating machine (Thevenin equivalent)

### References

- [1] L. M. Wieserman, T. E. McDermott, and R. C. Dugan, "Open and Short Circuit Testing of Photovoltaic Inverters," *IEEE Transactions on Power Delivery,* submitted.
- [2] M. E. Ropp and S. Gonzalez, "Development of a MATLAB/Simulink Model of a Single-Phase Grid-Connected Photovoltaic System," *IEEE Transactions on Energy Conversion*, vol. 24, pp. 195-202, 2009.
- [3] L. Wieserman and T. E. McDermott, "Fault current and overvoltage calculations for inverter-based generation using symmetrical components," in *2014 IEEE Energy Conversion Congress and Exposition (ECCE)*, 2014, pp. 2619-2624.
- [4] T. E. McDermott, "A test feeder for DG protection analysis," in *Power Systems Conference and Exposition (PSCE), 2011 IEEE/PES,* 2011, pp. 1-7.