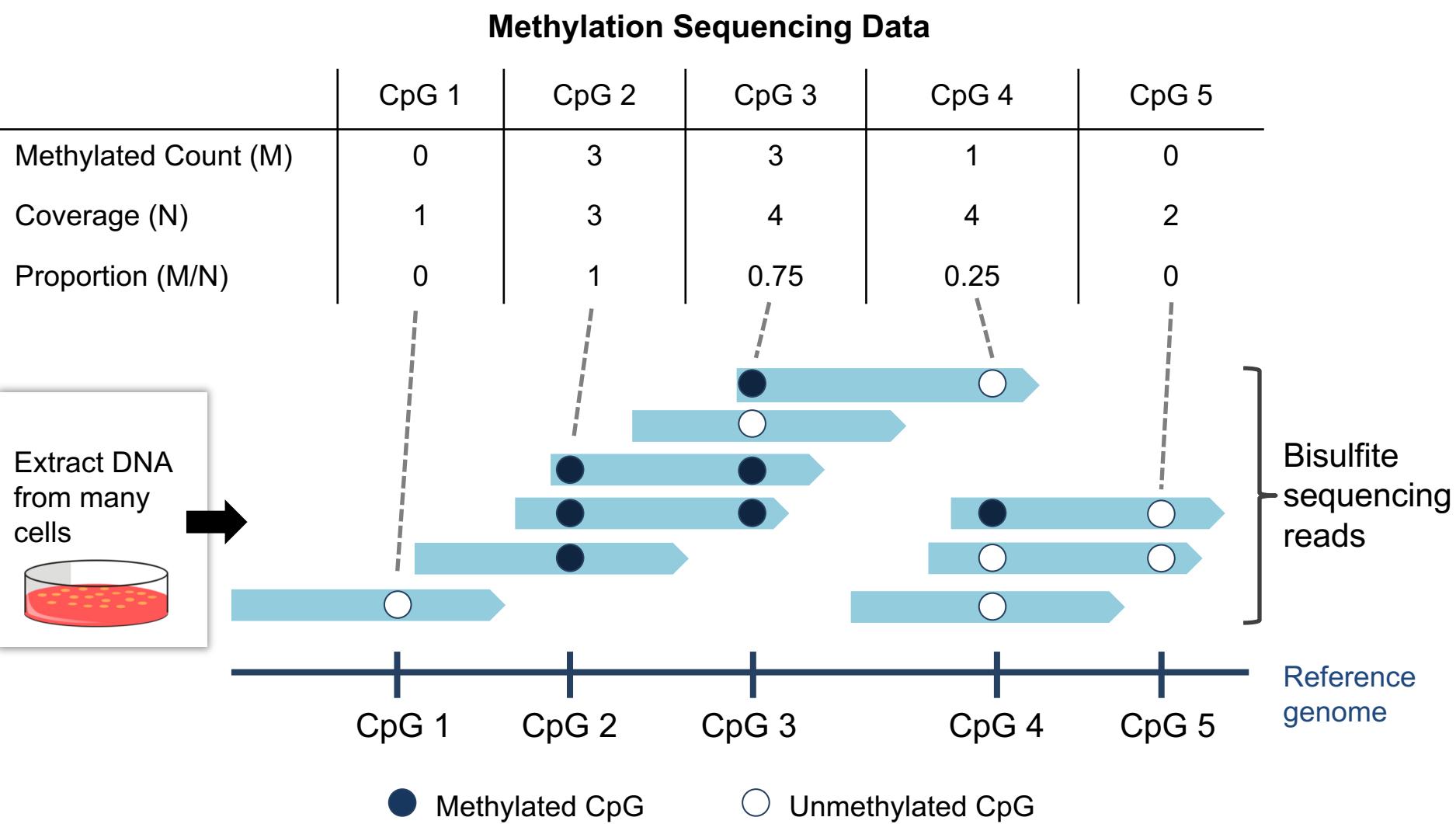


# *De novo* detection and accurate inference of differentially methylated regions

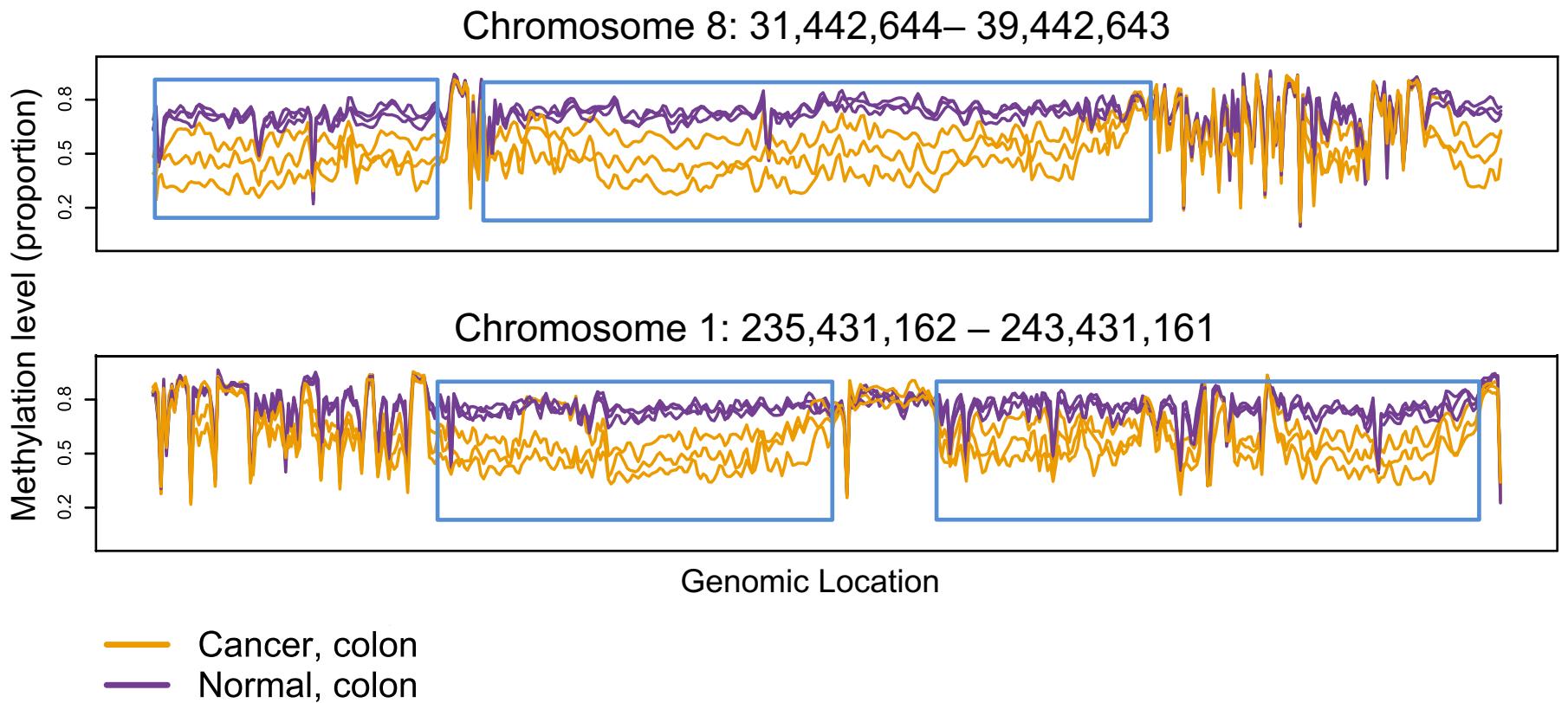
Keegan Korthauer, PhD

Joint Statistical Meetings, Vancouver, CA  
29 July 2018

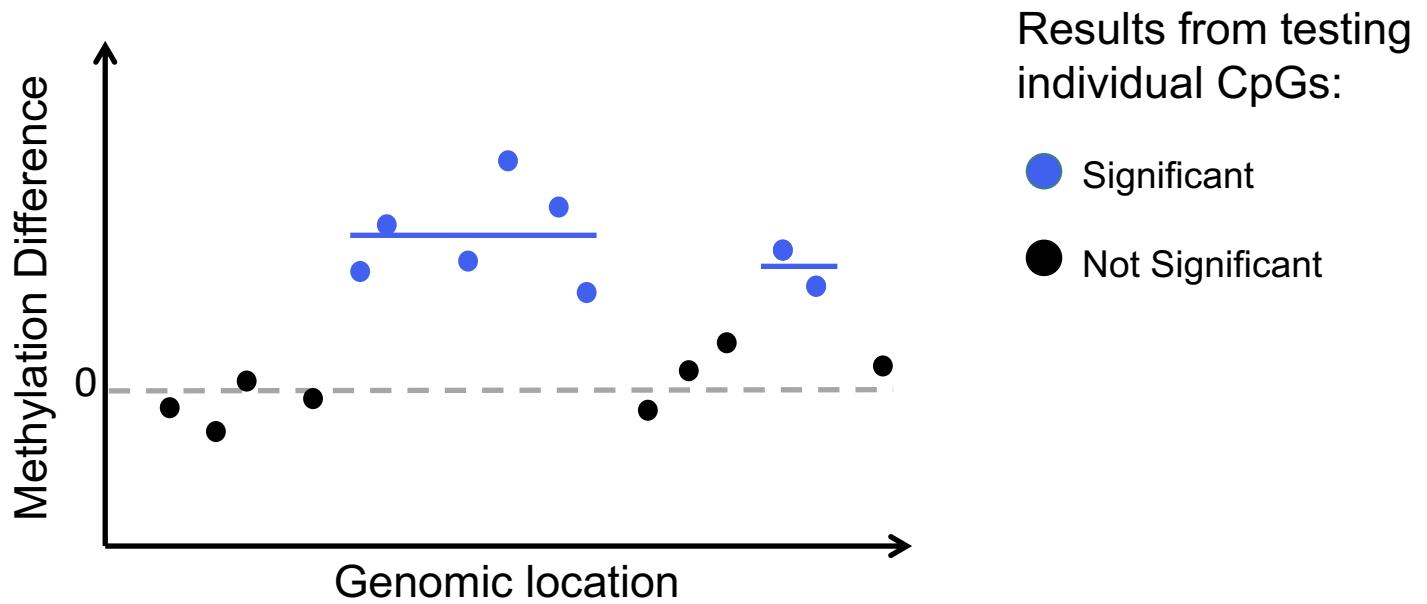
# Whole Genome Bisulfite Sequencing (WGBS)



# Differentially Methylated Regions (DMRs)



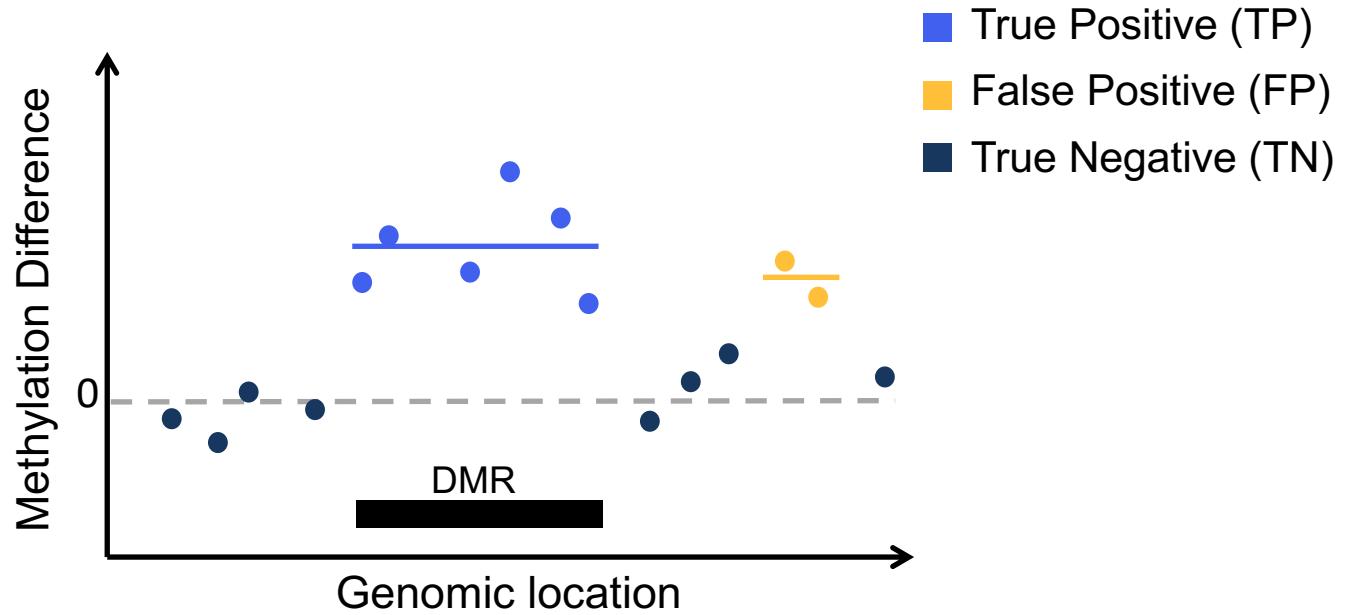
## Previous methods: Grouping significant CpGs



Examples:

- Bsmooth (Hansen et al., 2012)
- DSS (Feng et al., 2014; Wu et al., 2015)

# Error rate not controlled at the region level

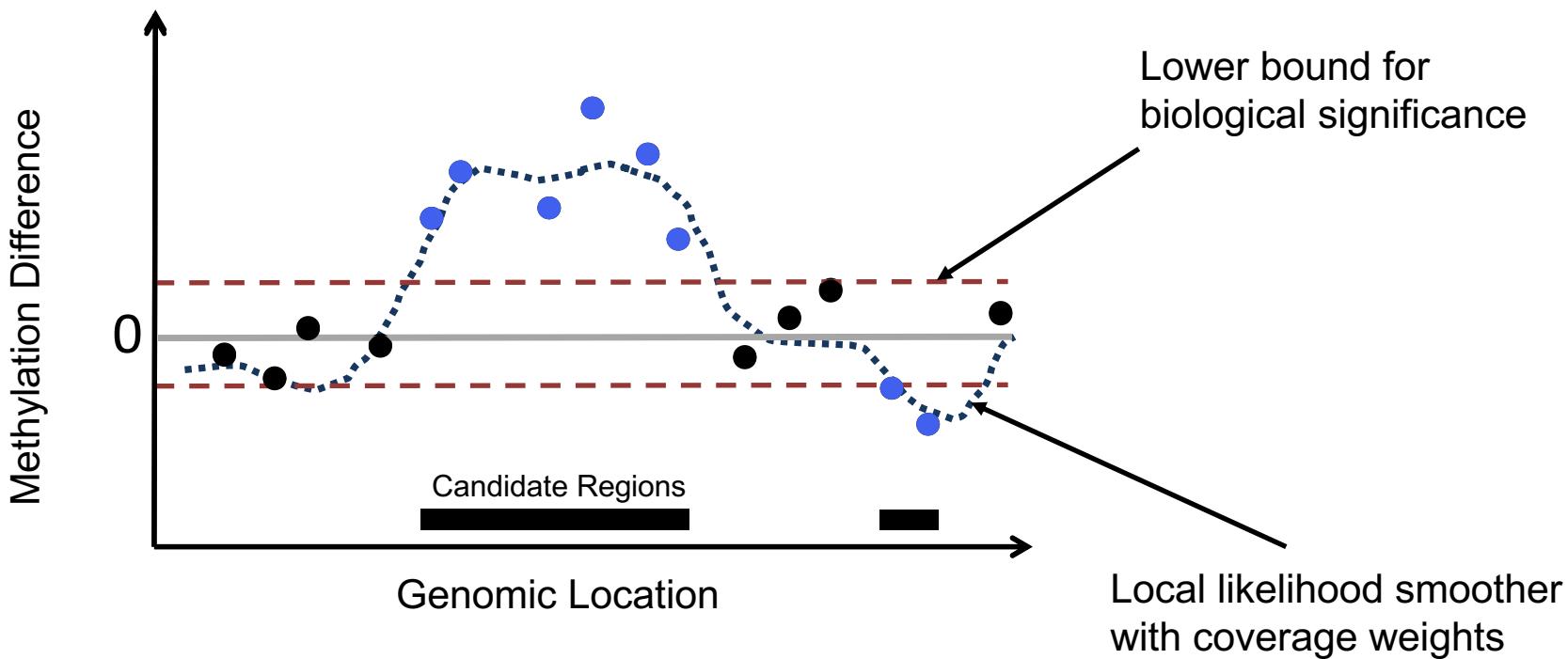


$$\text{False Discovery Rate (FDR)} = E \left[ \frac{FP}{TP + FP} \right]$$

$$\widehat{FDR}_{CpG} = \frac{2}{8} = 0.25 \quad vs \quad \widehat{FDR}_{DMR} = \frac{1}{2} = 0.50 \quad !$$

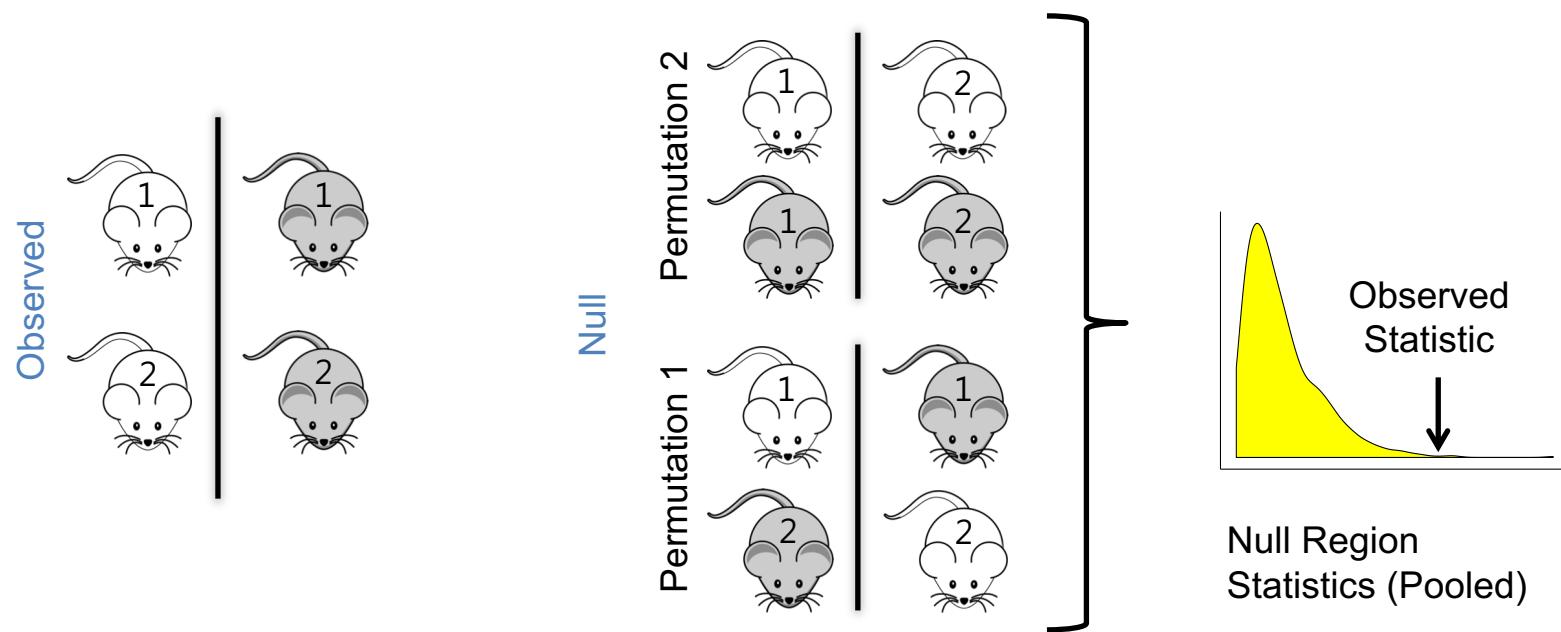
# dmrseq: (1) Detect *de novo* candidate regions

Genome-wide scan of CpG methylation difference



## dmrseq: (2) Assess region-level signal

- Formulate region-level summary statistic
- Compare region statistics against null permutation distribution to evaluate significance



# Region-level modeling

**CpG level:**

$$\begin{aligned} M_{ijr} | N_{ijr}, p_{ijr} &\sim \text{Bin}(N_{ijr}, p_{ijr}) \\ p_{ijr} &\sim \text{Beta}(a_{irs}, b_{irs}) \\ \pi_{irs} &= \frac{a_{irs}}{(a_{irs} + b_{irs})} \end{aligned}$$

$M_{ijr}$  = methylated read count

$i$  indexes CpGs

$N_{ijr}$  = total coverage

$j$  indexes samples, where  $j \in C_s$

$p_{ijr}$  = methylation proportion

$s$  indicates biological condition

$\pi_{irs}$  = methylation proportion for condition  $s$

**Region level:**

$$\begin{aligned} g(\boldsymbol{\pi}_r) &= \mathbf{X}\boldsymbol{\beta}_r \\ &= \underbrace{\sum_{l=1}^{L_r} \beta_{0lr} 1_{[i=l]} + X_j \beta_{1r}}_{\text{loci-specific intercept}} + \underbrace{\beta_{1r}}_{\text{condition effect}} \end{aligned}$$

$$H_0: \beta_{1r} = 0$$

# Region-level model fitting

Generalized Least Squares (GLS) with variance stabilizing transformation:

arcsine link transformation (Park & Wu 2016)

$$Z_{ijr} = \arcsin(2M_{ijr}/N_{ijr} - 1)$$

$$Var(M_{ijr}/N_{ijr}) \propto \pi_{ijr}(1 - \pi_{ijr}) \quad \text{but} \quad Var(Z_{ijr}) \approx \frac{1 + (N_{ijr} - 1)\gamma_{irs}}{N_{ijr}}$$



Variance depends on mean      Variance independent of mean

$$\mathbf{Z}_r = \mathbf{X}\boldsymbol{\beta}_r + \boldsymbol{\epsilon}_r$$

where  $E[\boldsymbol{\epsilon}_r] = \mathbf{0}$  and  $Var[\boldsymbol{\epsilon}_r] = \mathbf{V}_r$

$$\hat{\boldsymbol{\beta}}_r = (\mathbf{X}^t \mathbf{V}_r^{-1} \mathbf{X})^{-1} \mathbf{V}_r^{-1} \mathbf{X}^t \mathbf{V}_r^{-1} \mathbf{Z}_r$$

# Account for variability across samples and locations

(1) Correlation: Continuous Autoregressive (CAR) model

$$\rho(Z_{ijr}, Z_{kjr}) = e^{-\phi_r |t_{ir} - t_{kr}|}$$

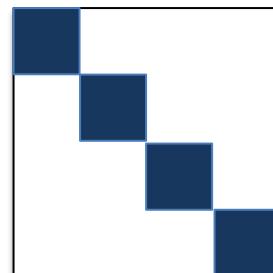
$t_{ir}$  = genomic location of CpG  $i$

(2) Variability dependent on coverage

$$Var(Z_{ijr}) \propto \frac{1}{N_{i \cdot r}}$$

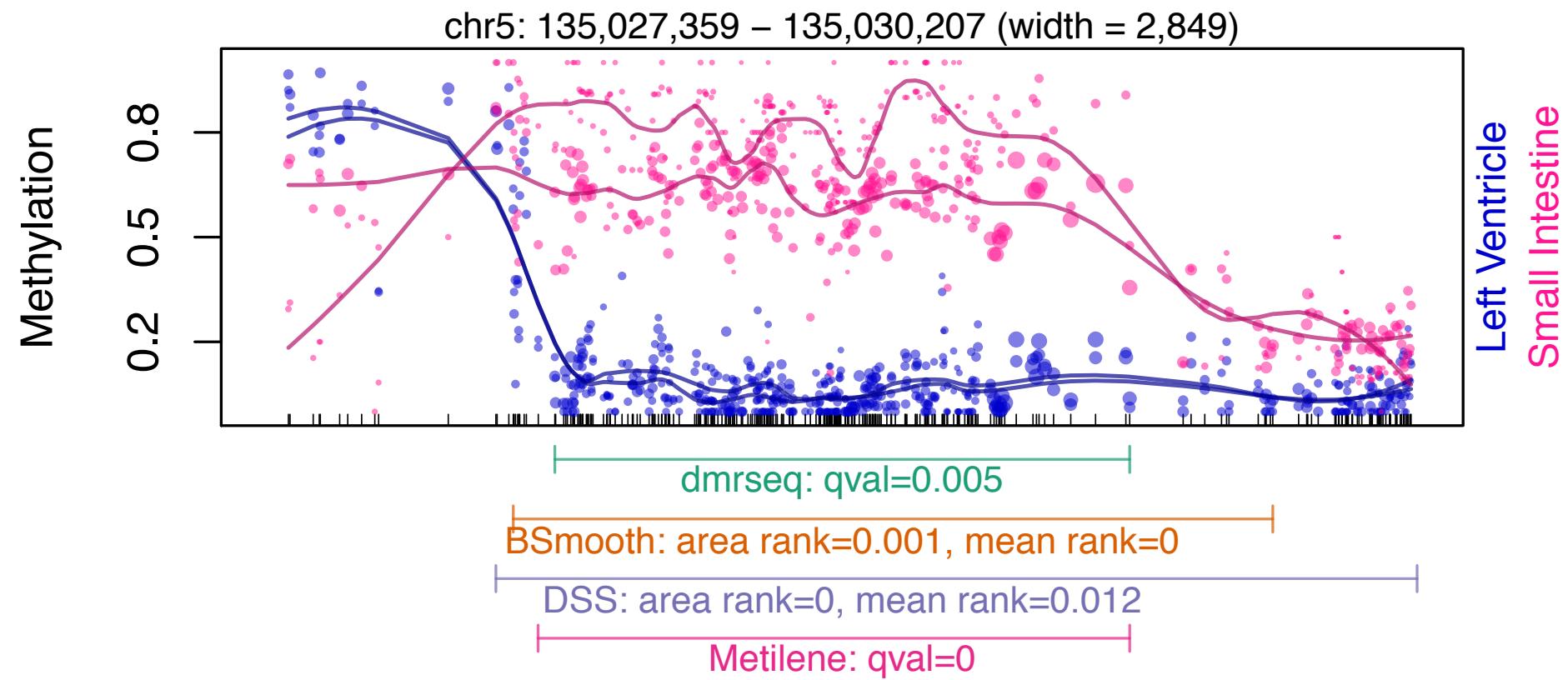
(3) Within sample correlation

Independent  
samples

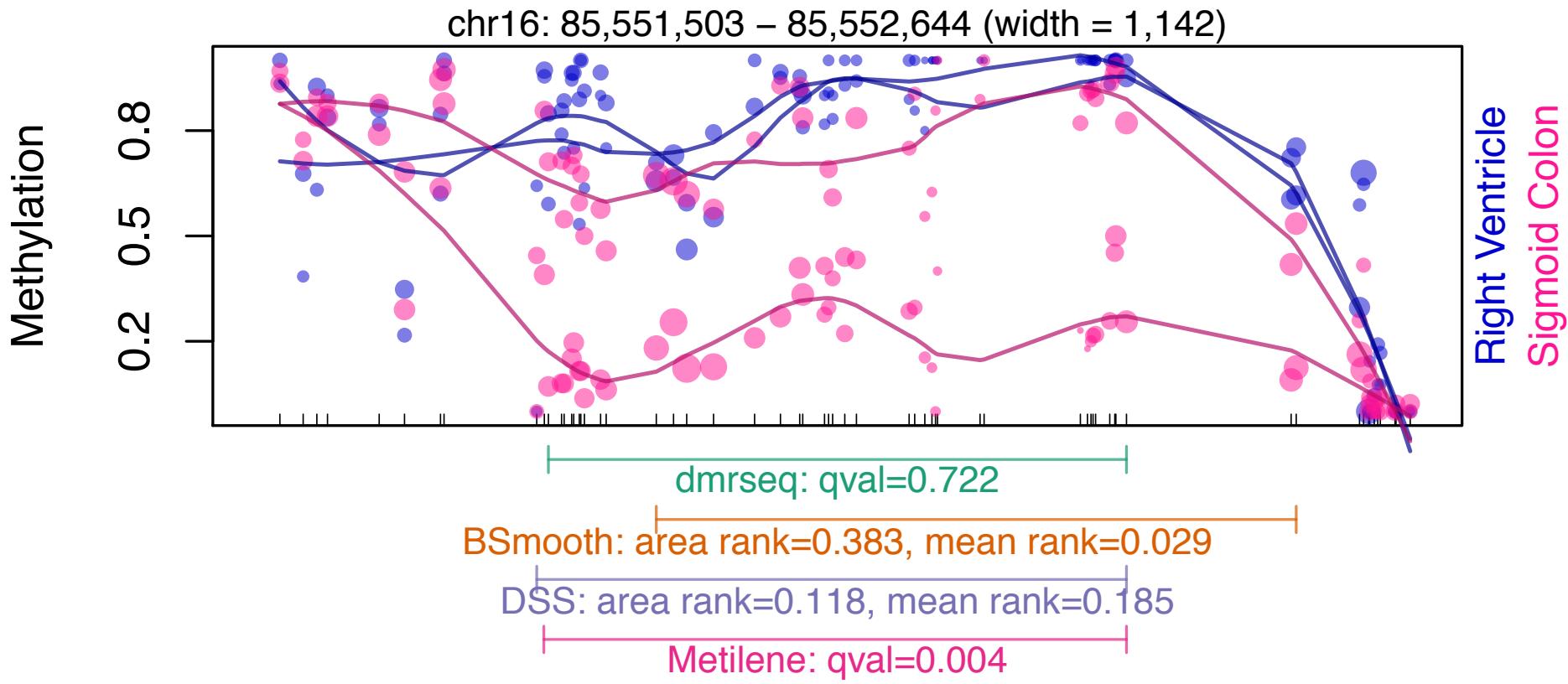


$$Cov(Z_{ijr}, Z_{ij^*r}) = 0$$

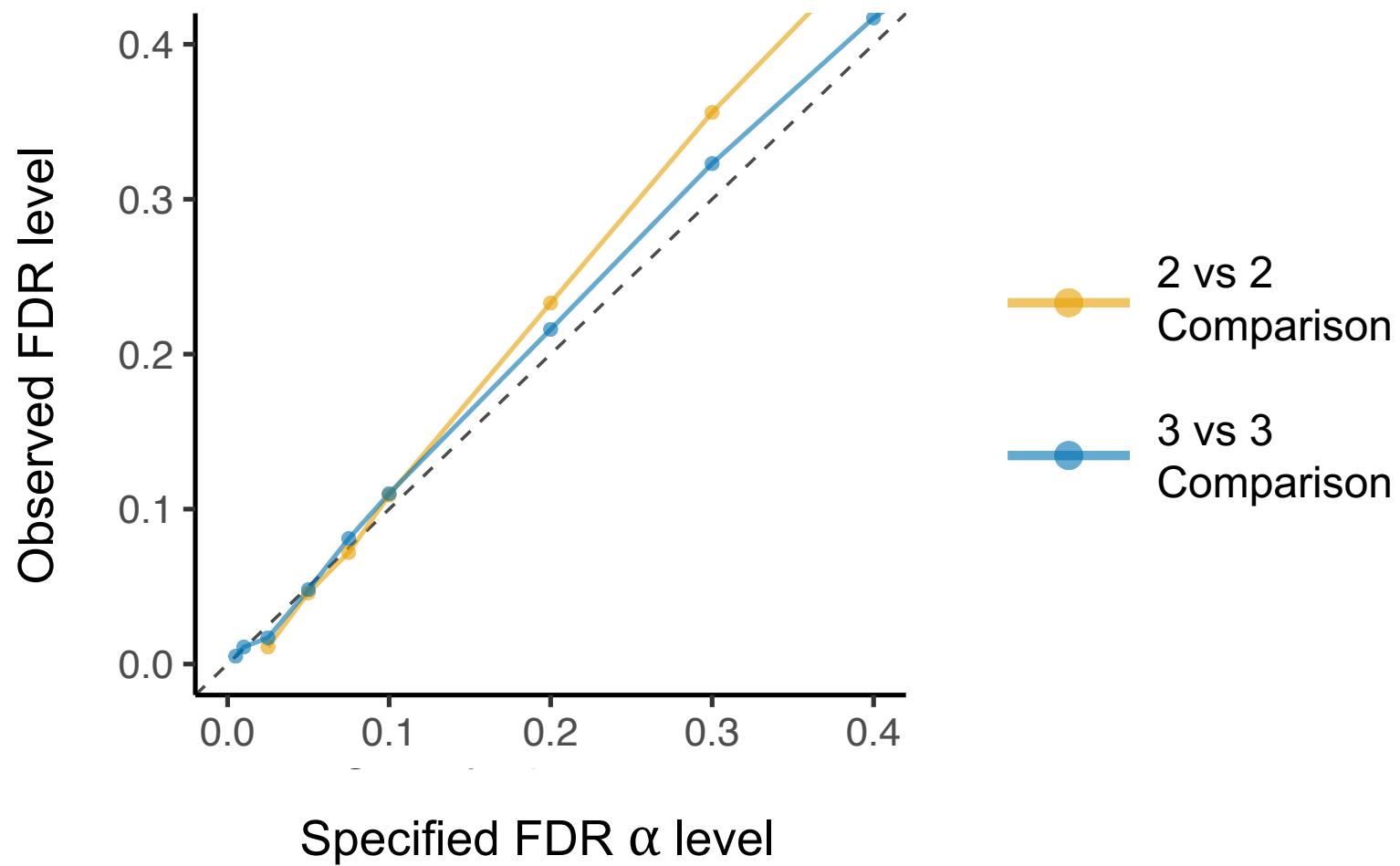
# Example: highly ranked DMR across all methods



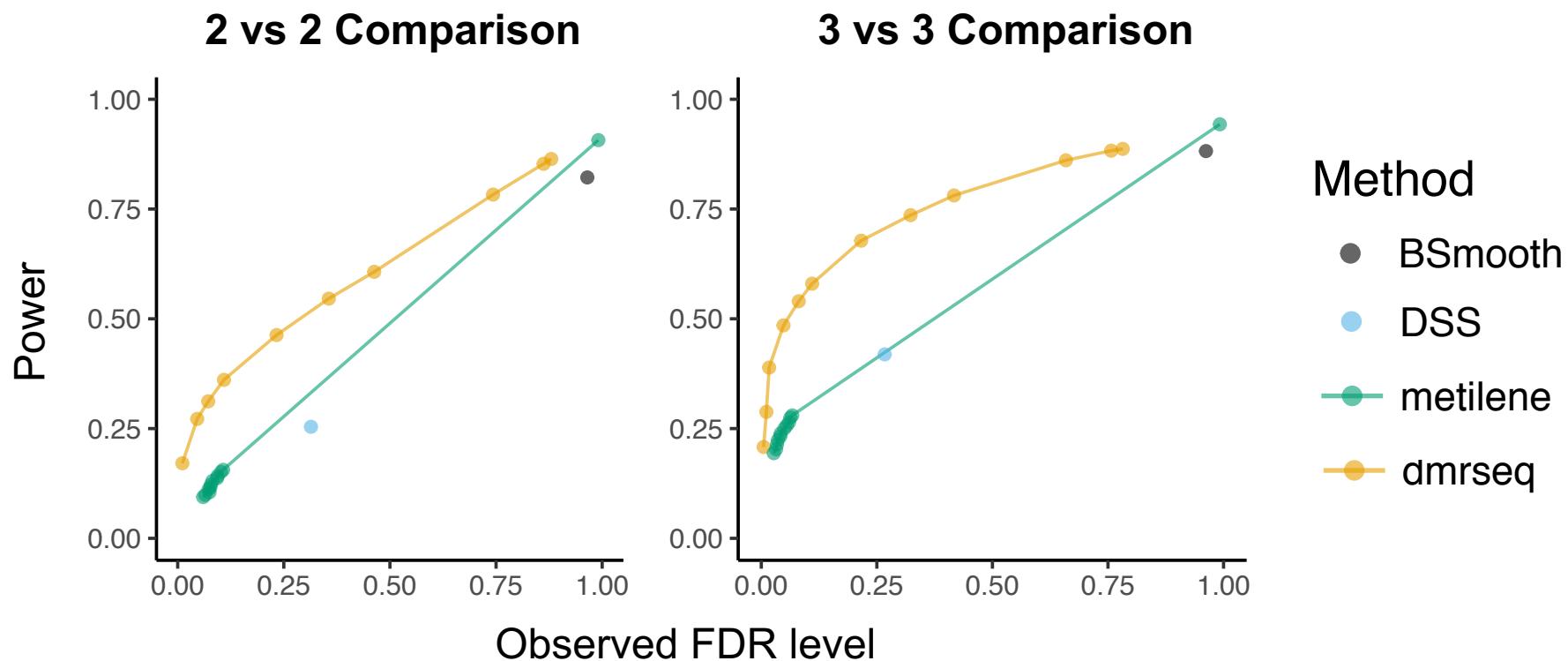
# Example: dmrseq accounts for sample variability



# Accurate FDR control in simulation

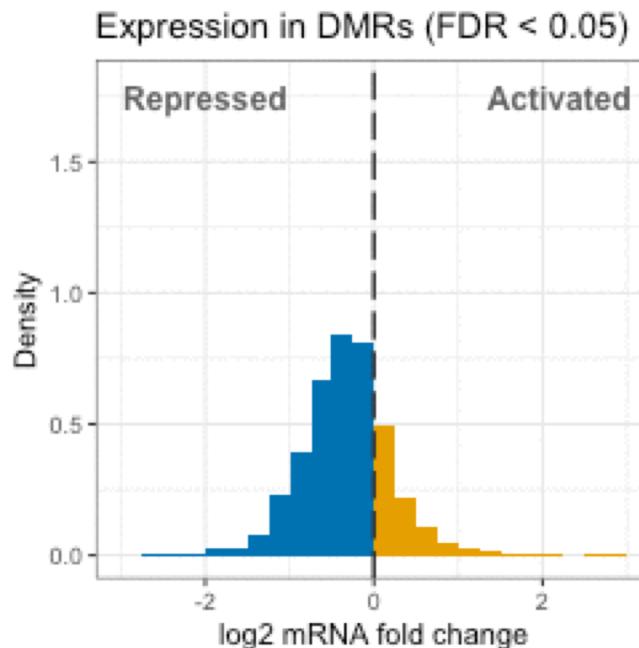
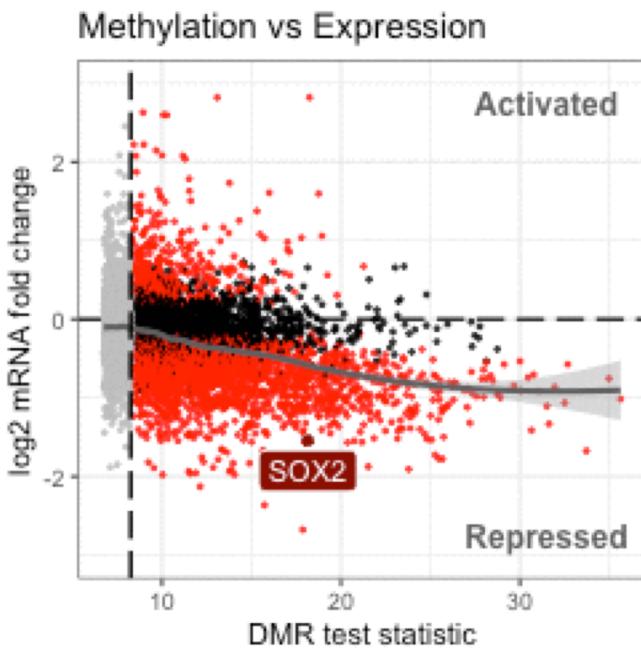


# High sensitivity and specificity in simulation



# Significant DMRs enriched for biological signal

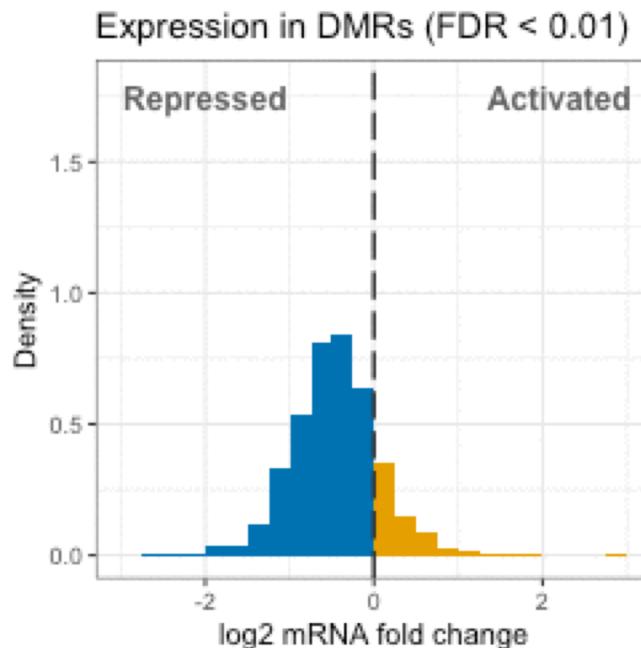
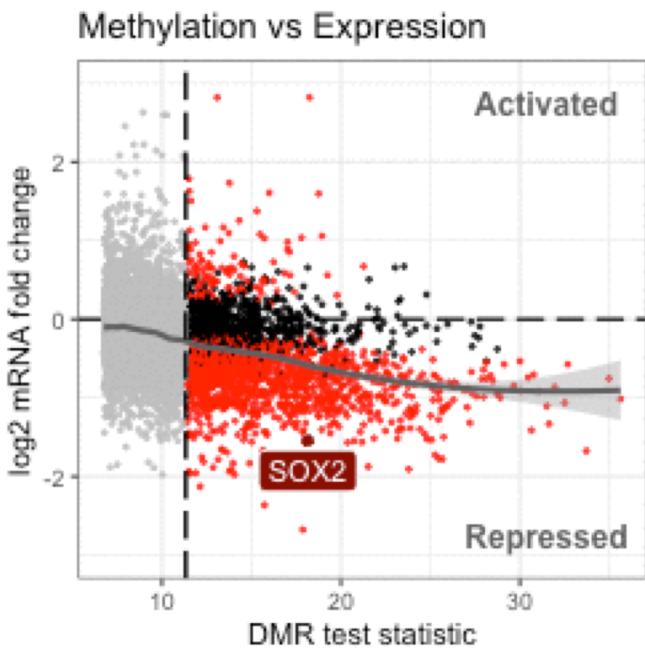
← Expression Decrease



Methylation Increase →

# Significant DMRs enriched for biological signal

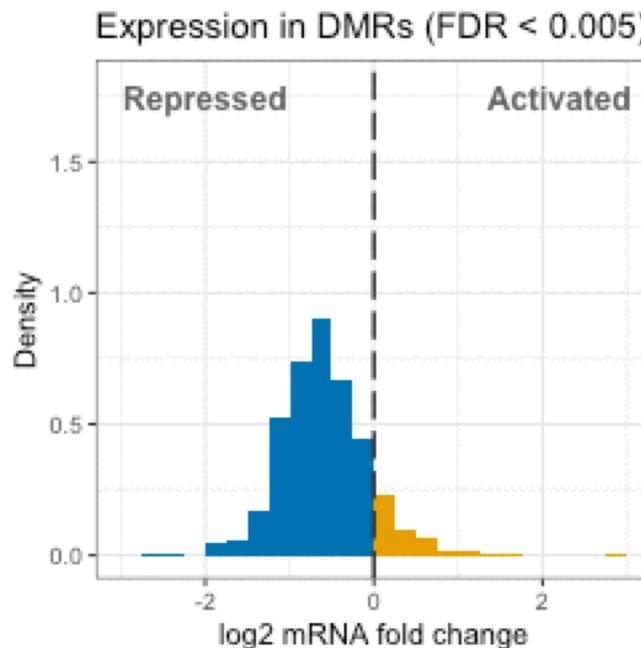
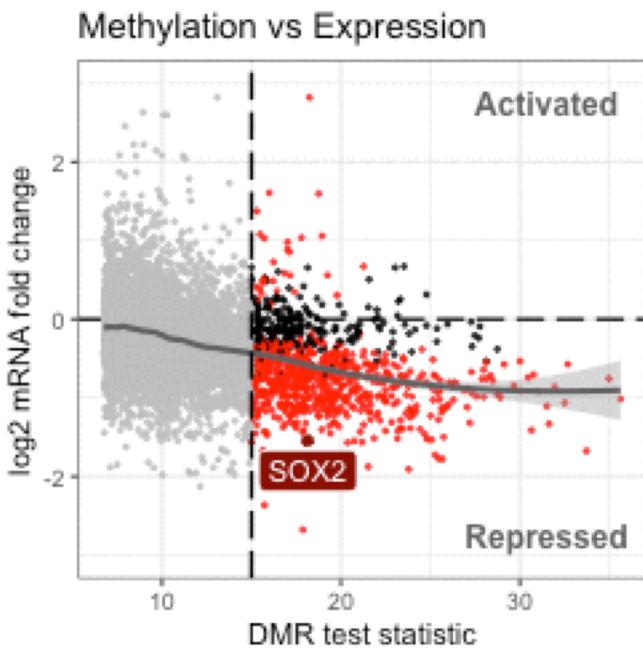
← Expression Decrease



Methylation Increase →

# Significant DMRs enriched for biological signal

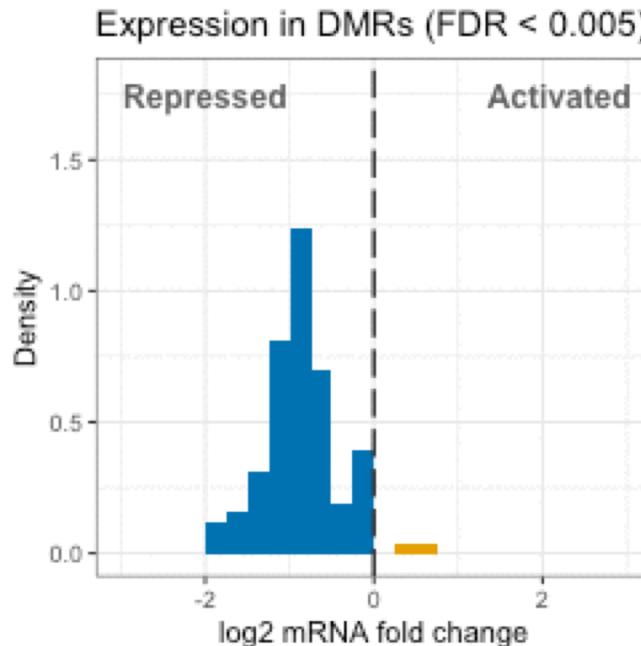
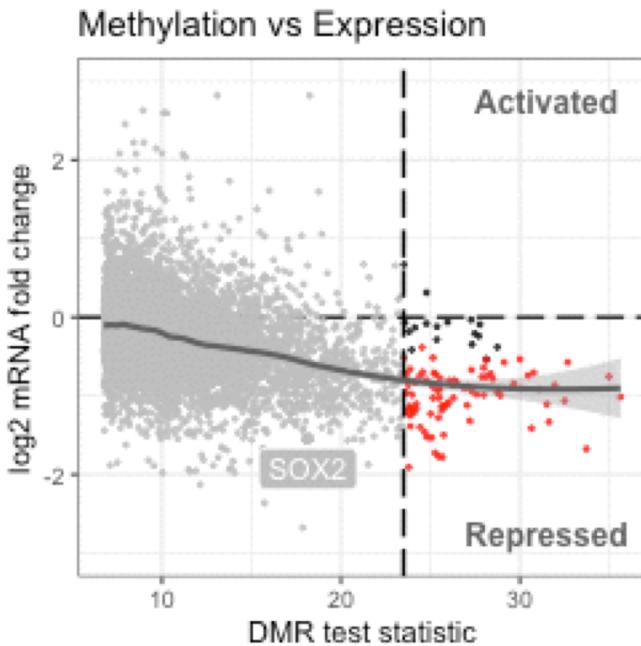
← Expression Decrease



Methylation Increase →

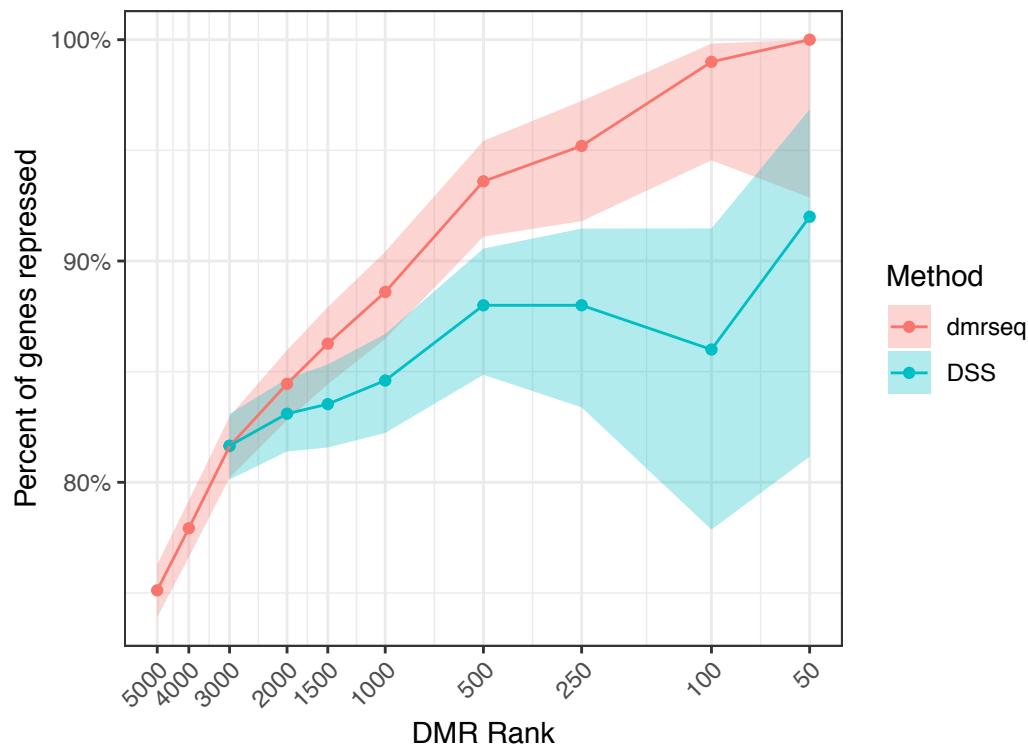
# Significant DMRs enriched for biological signal

← Expression Decrease



Methylation Increase →

# Increased biological signal in dmrseq DMRs



# Summary

- dmrseq **identifies and prioritizes DMRs** from bisulfite sequencing experiments
- **Models signal at the region level** in order to account for sample and spatial variability
- Achieves **accurate False Discovery Rate control** by generating a null distribution that pools information across the genome
- Detailed in “Detection and accurate False Discovery Rate control of differentially methylated regions from Whole Genome Bisulfite Sequencing” (*Biostatistics*, 2018)
- dmrseq R package available on Bioconductor



# Acknowledgements



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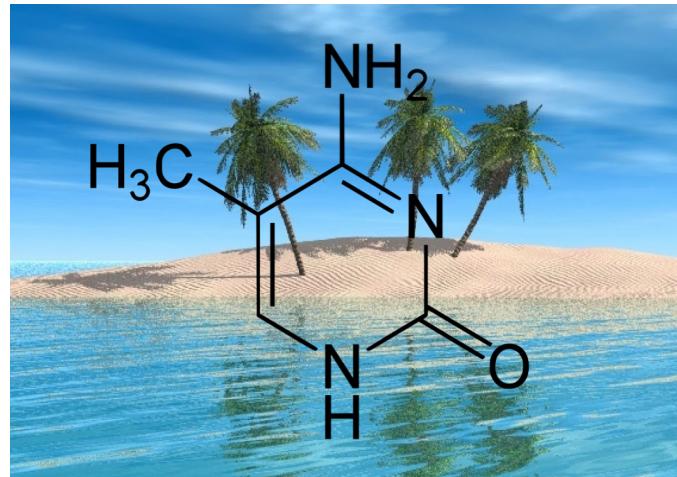
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