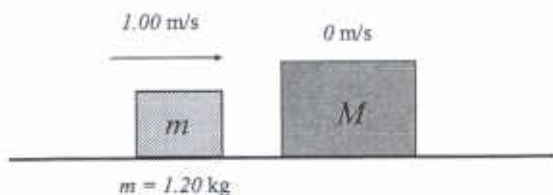


Phys 2010, Section 3  
Quiz #4 — Fall 2003

1. A 1.20 kg mass slides to the right with a speed of  $1.00 \frac{\text{m}}{\text{s}}$  on a frictionless track; it collides with a stationary mass  $M$  and sticks to it.

After the collision, the combined mass moves to the right with speed  $0.700 \frac{\text{m}}{\text{s}}$ .



a) Find the value of  $M$ . (Hint: Use the condition of conservation of momentum and solve for  $M$ !)

Total momentum conserved in collision. This gives:

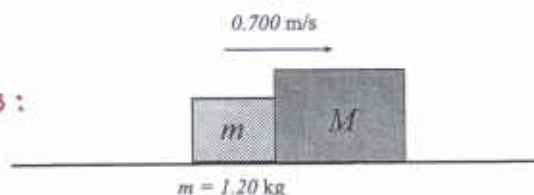
$$(1.20 \text{ kg})(1.00 \frac{\text{m}}{\text{s}}) = (1.20 \text{ kg} + M)(0.700 \frac{\text{m}}{\text{s}})$$

(Before the collision only the 1.20 kg mass is in motion; afterwards both masses move with same velocity)

Solve for  $M$ :

$$(1.20 \text{ kg} + M) = \frac{(1.20 \text{ kg})(1.00 \frac{\text{m}}{\text{s}})}{(0.700 \frac{\text{m}}{\text{s}})} = 1.71 \text{ kg}$$

$$\rightarrow M = \boxed{0.514 \text{ kg}}$$



b) How much kinetic energy is lost in this collision?

Total KE before collision is:

$$KE_{\text{init}} = \frac{1}{2} (1.20 \text{ kg}) (1.00 \frac{\text{m}}{\text{s}})^2 = 0.600 \text{ J}$$

Total KE after collision is

$$KE_{\text{final}} = \frac{1}{2} (1.20 \text{ kg} + 0.514 \text{ kg}) (0.700 \frac{\text{m}}{\text{s}})^2 = 0.420 \text{ J}$$

Then the amt of KE lost is

$$|\Delta KE| = 0.600 \text{ J} - 0.420 \text{ J} = \boxed{0.180 \text{ J}}$$

2. A disk of radius 6.00 cm is turning at a rate of  $188.0 \frac{\text{rad}}{\text{s}}$ .  
 a) Find its angular velocity in units of revolutions per second.

$$188.0 \frac{\text{rad}}{\text{s}} = (188.0 \frac{\text{rad}}{\text{s}}) \left( \frac{1 \text{ rev}}{2\pi \text{ rad}} \right) = \boxed{29.9 \frac{\text{rev}}{\text{s}}}$$

- b) Find the speed of a point of the rim of the disk.

At the rim (edge) of disk,  $r = 0.0600 \text{ m}$ , so

$$v = \omega r = (188 / \text{s})(0.0600 \text{ m}) = \boxed{11.3 \frac{\text{m}}{\text{s}}}$$

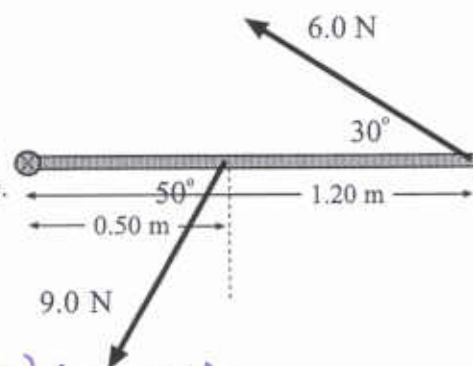
3. Two forces act on a bar of length 1.20 m which turns around a frictionless pivot, as shown. (You can ignore the mass of the bar.)

Find the total torque which acts on the bar. Be clear about the *direction* (clockwise or counter-clockwise) of the net torque.

Taking the counter-clockwise direction as positive we get:

$$\begin{aligned} \sum \tau &= -(9.0 \text{ N})(0.50 \text{ m}) \sin 50^\circ + (6.0 \text{ N})(1.20 \text{ m}) (\sin 30^\circ) \\ &= \boxed{0.153 \text{ N}\cdot\text{m}} \end{aligned}$$

Positive sign tells us net torque is counterclockwise



You must show all your work and include the right units with your answers!

$$F_{\text{net}} = ma \quad g = 9.80 \frac{\text{m}}{\text{s}^2} \quad \text{sohcahtoa...sohcahtoa...mmm-hmm-mm, sohcahtoa}$$

$$KE = \frac{1}{2}mv^2 \quad \mathbf{p} = m\mathbf{v} \quad \text{For isolated system } \mathbf{P} \text{ is conserved}$$

$$2\pi \text{ rad} = 360^\circ = 1 \text{ rev} \quad \omega = \omega_0 + \alpha t \quad \theta = \omega_0 t + \frac{1}{2}\alpha t^2 \quad \omega^2 = \omega_0^2 + 2\alpha\theta \quad |\tau| = Fr \sin \phi$$

$$v = \omega r \quad a_T = \alpha r \quad a_c = \frac{v^2}{r} = \omega^2 r$$