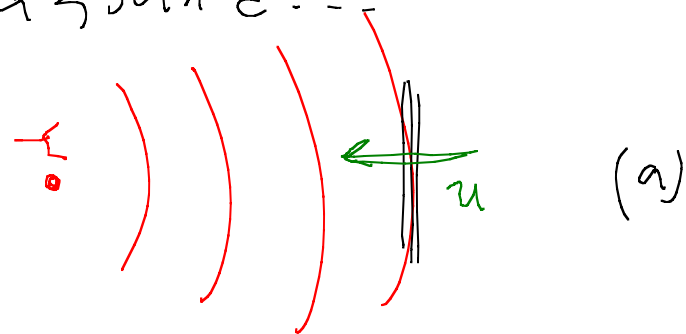


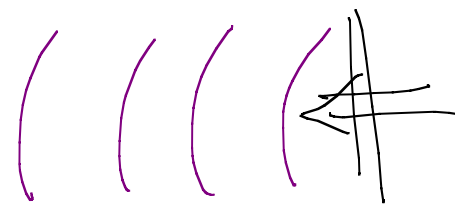
14.74 Obstetricians, ultrasound...
measure speed of the thing
bouncing sound waves

$$f' = f \frac{1 \pm \frac{u_{\text{obs}}}{v}}{1 \mp \frac{u_{\text{sound}}}{v}}$$

$$f = 5.0 \text{ MHz}$$



(a)



(b)

(a) Moving wall "hears"

(b) Moving wall re-emits

$$f \left(1 + \frac{u}{v} \right) = f'$$

$$\frac{f'}{1 - \frac{u}{v}} = f \frac{1 + \frac{u}{v}}{1 - \frac{u}{v}}$$

$$u = u_{\text{wall}} = u_{\text{obs}} = u_{\text{source}}$$

Shift in freq

$$f'' - f = 100 \text{ Hz} = f \left(\frac{1+x}{1-x} - 1 \right)$$

$$= f \left(\frac{1+x - 1+x}{1-x} \right)$$

$$x = \frac{u}{v}$$

$$100 \text{ Hz} = f \left(\frac{2x}{1-x} \right)$$

$$f = 5 \text{ MHz}$$

x is small

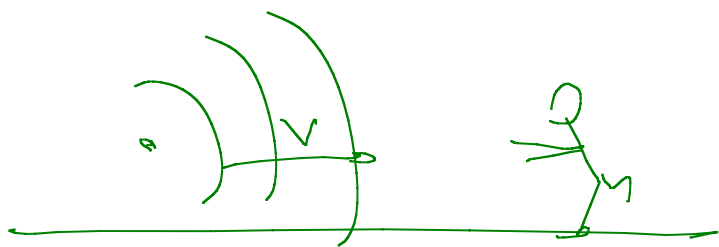
$$2x = \frac{100 \text{ Hz}}{5 \text{ MHz}}$$

$$x = 1 \times 10^{-5}$$

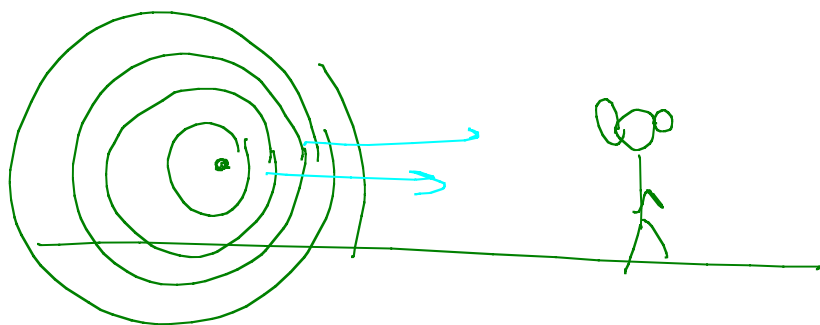
$$u = 1.5 \frac{\text{m}}{\text{s}}$$

$$v \approx 1440 \frac{\text{m}}{\text{s}}$$

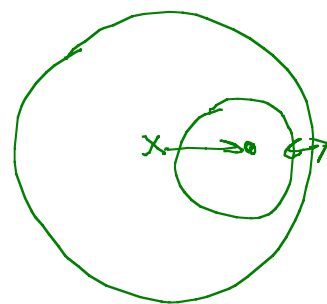
water



$$v_{\text{eff}} = v + u$$



Wavelength is eff shorter



New wavelength

$\lambda - \text{dist mve in } T$

$$\lambda - uT$$

$$= \lambda - u \frac{\lambda}{v}$$

$$= \lambda \left(1 - \frac{u}{v} \right)$$

$$T = \frac{1}{f}$$

$$f = \frac{v}{\lambda}$$

Standing Waves

14.66 A string on piano
is 38.9 cm long (440 Hz)

Tension is 667 N.

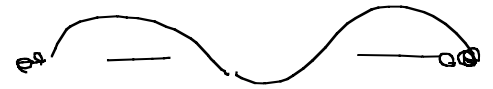
What is mass?

$$n=1 \quad L = \frac{\lambda}{2}$$

$$\lambda = 0.778 \text{ m}$$

$$\textcircled{v} = \lambda f = 342 \frac{\text{m}}{\text{s}}$$

$$= \frac{\textcircled{F}}{\mu}$$



$$L = n \frac{\lambda}{2} \quad n=1,2,3$$

$$\lambda = \frac{2L}{n}$$

$$f = \frac{v}{\lambda} = \frac{n v}{2L}$$

$$f = \frac{n}{2L} \sqrt{\frac{F}{\mu}}$$

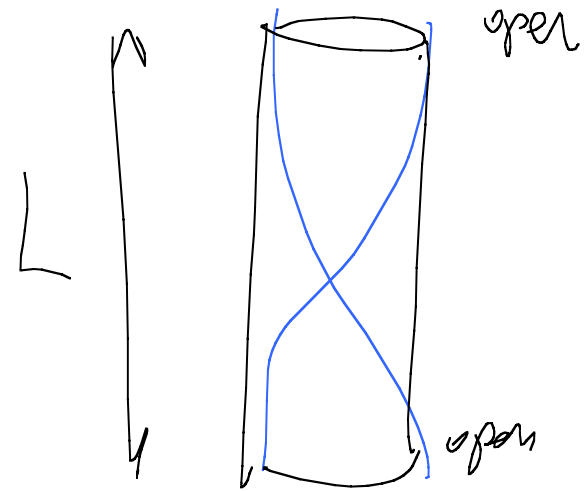
$$\mu = \frac{F}{v^2} = \frac{667 \text{ N}}{(342 \frac{\text{m}}{\text{s}})^2} = 5.69 \times 10^{-3} \frac{\text{kg}}{\text{m}}$$

$$m = \mu L = 2.21 \text{ g}$$

$$L = \frac{\lambda}{2}$$

$$n \frac{\lambda}{2}$$

$$f_n = \frac{nv}{2L}$$

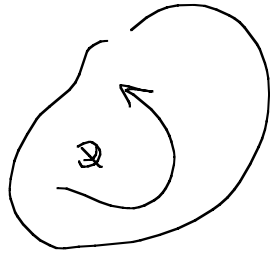


Closed on one end

$$f_n = \frac{nv}{4L}$$

$$n = 3, 5, 7, \dots$$

Rotns



θ, ω, α

$1 \text{ rev} = 2\pi \text{ rad}$

$$\tau = \sum r F \sin \theta$$

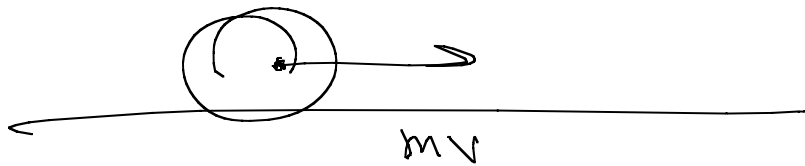
$$I = \sum m_i r_i^2$$

$$I_{\text{disk}} = \frac{1}{2} M R^2 \quad \text{etc}$$

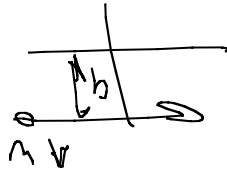
$$\tau_{\text{net}} = I \alpha$$

$$K_{\text{rot}} = \frac{1}{2} I \omega^2$$

$$v_{\text{cm}} = \omega R \quad \begin{array}{l} \text{rolling} \\ \text{w/ slipping} \end{array}$$



$$L = I \omega$$



$$K_{\text{tot}} = K_{\text{cm}} + K_{\text{rot}} \quad \text{etc.}$$

$$v = \omega R$$

Oscillations

$$\rightarrow \frac{d^2x}{dt^2} = - \cancel{A} x = -\omega^2 x$$

$$x = A \cos(\omega t + \phi)$$

$$\omega = \sqrt{\frac{k}{m}}$$

$$\omega = \sqrt{\frac{g}{L}}$$

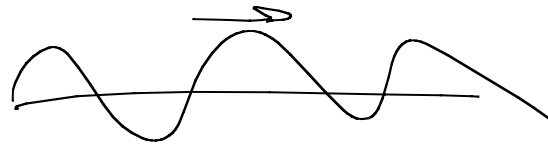
$$\omega = \sqrt{\frac{MgI}{L}}$$

etc.

Waves

$$\lambda, f, v$$

$$\lambda f = v$$



$$y = A \cos(kx \mp \omega t)$$

$$k = \frac{2\pi}{\lambda}, \text{ etc.}$$

Beats, Standing waves

Doppler Effect.
Intensity.

Thermal Physics

Gravity,

Fluid forces
dynamics.

Electricity & Magnetism & Light