Phys 2920, Spring 2009 Problem Set #1

- 1. (a) Express the complex number 3+4i in polar form $(\rho e^{i\phi})$. (b) Express the complex number $(5.0)e^{4.5i}$ in a+bi form.
- 2. Find the unit vector in the direction of the vector $4\mathbf{i} 3\mathbf{j} + \mathbf{k}$.
- 3. In each case, determine whether vectors are linearly independent or linearly dependent:
- a) a = 2i + j 3k, b = i 4k, c = 4i + 3j k.
- b) a = 2i 3j + 2k, b = 2i 4j k, c = 3i + 2j k.
- **4.** (a) Prove that the vectors $\mathbf{a} = 3\mathbf{i} + \mathbf{j} 2\mathbf{k}$, $\mathbf{b} = -\mathbf{i} + 3\mathbf{j} + 4\mathbf{k}$ and $\mathbf{c} = 4\mathbf{i} 2\mathbf{j} 6\mathbf{k}$ can form the sides of a triangle. (b) Find the lengths of the medians of the triangle.
- **5.** For a set of N point charges q_i , the dipole moment is defined as

$$\mathbf{p} = \sum_{i=1}^{N} q_i \mathbf{r}_i$$

Suppose we change to a new coordinate system (with an origin shifted with respect to the old one by \mathbf{R}) such that the new position vectors are

$$\mathbf{r}_i' = \mathbf{r}_i - \mathbf{R}$$

What is the condition on the charges such that **p** has the same value in the new coordinates?

- **6.** Find the angle between $\mathbf{c} = 4\mathbf{i} 2\mathbf{j} + 4\mathbf{k}$ and $\mathbf{d} = 3\mathbf{i} 6\mathbf{j} 2\mathbf{k}$.
- 7. For what values of a are $\mathbf{A} = a\mathbf{i} 2\mathbf{j} + \mathbf{k}$ and $\mathbf{B} = 2a\mathbf{i} + a\mathbf{j} 4\mathbf{k}$ perpendicular?
- 8. Find the work done in moving an object along a straight line from (3, 2, -1) to (2, -1, 4) in a force field given by $\mathbf{F} = 4\mathbf{i} 3\mathbf{j} + 2\mathbf{k}$.
- **9.** If $\mathbf{a} = 2\mathbf{i} + \mathbf{j} 3\mathbf{k}$ and $\mathbf{b} = \mathbf{i} 2\mathbf{j} + \mathbf{k}$, find a vector of magnitude 5 perpendicular to both \mathbf{a} and \mathbf{b}
- 10. Simplify $(\mathbf{a} + \mathbf{b}) \cdot [(\mathbf{b} + \mathbf{c}) \times (\mathbf{c} + \mathbf{a})]$.
- 11. Use the "trick" with δ_{ij} and ϵ_{ijk} to show

$$\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c}) = \mathbf{c} \cdot (\mathbf{a} \times \mathbf{b})$$