

$$f' = f \left(\frac{1}{1 + \frac{u}{v}} \right)$$

Toward
Away

u = speed of source

Effectively, wavelength has been shortened
 $T = \frac{1}{f}$



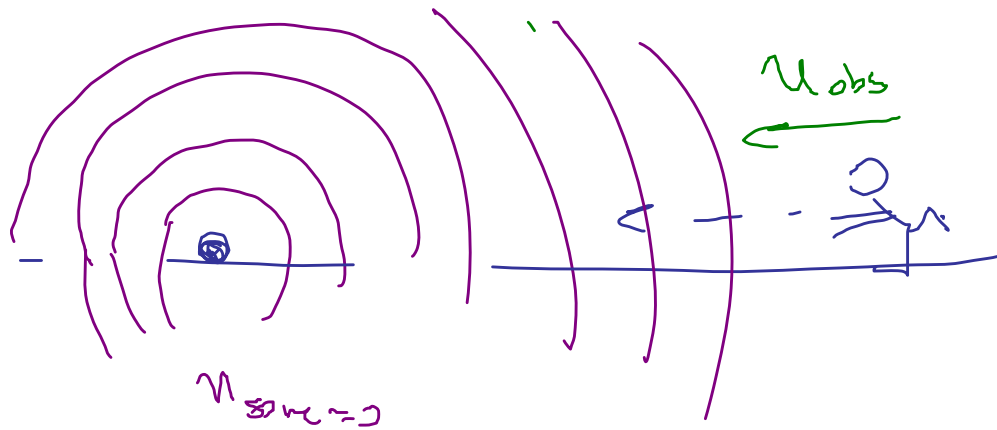
$$\lambda' = \lambda - uT$$

Stick figure

$$\lambda' f' = v$$

$$f' = \frac{v}{\lambda - uT} = \frac{v}{\frac{v}{f} - \frac{u}{f}} = f \left(\frac{v}{v - u} \right)$$

$$= f \left(\frac{1}{1 - \frac{u}{v}} \right)$$



You hear higher freq
because effectively
speed of waves
is greater
 λ same. (f')

Man

$$\lambda f' = v'$$

$$\frac{v}{f} f' = v + u_{\text{obs}}$$

$$v f' = f(v + u_{\text{obs}})$$

v = speed of sound

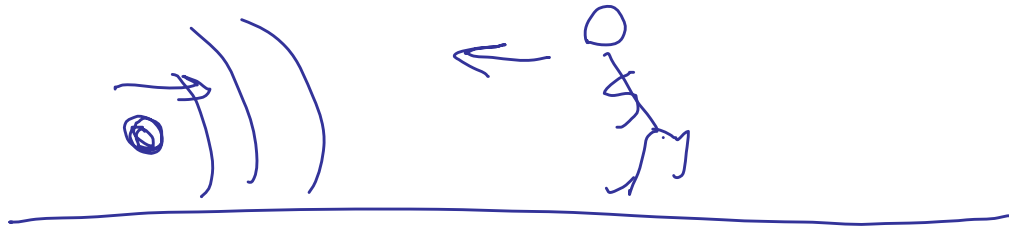
$$f' = \frac{f}{v} (v + u_{\text{obs}})$$

$$f' = f \left(1 + \frac{u_{\text{obs}}}{v} \right)$$

Moving observer

$$f' = f \left(1 \pm \frac{u_{\text{obs}}}{v} \right)$$

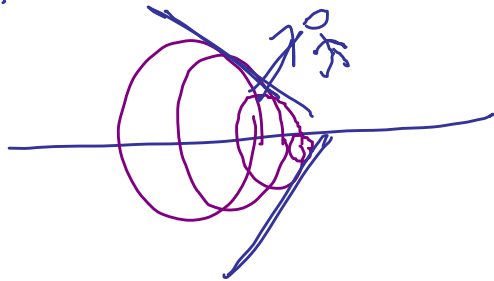
Toward
 Away



$$f' = f \left(\frac{1 \pm \frac{u_{\text{obs}}}{v}}{1 \mp \frac{u_{\text{source}}}{v}} \right)$$

General case

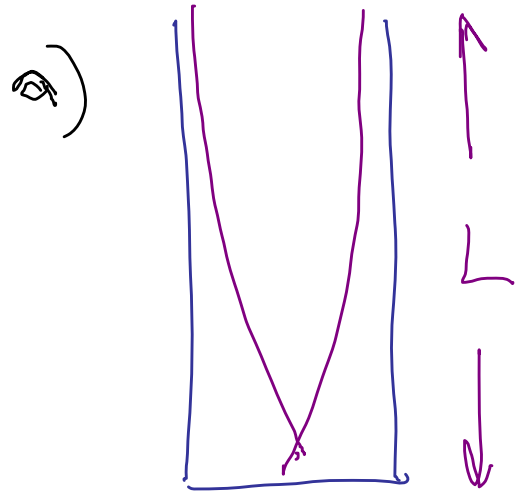
For these $u_{\text{source}} < v$



shock
p.241

Doppler effect for light Requires a diff formula.

14.70 Lowest note of organ is 22 Hz
Length of pipe necessary if a) Closed one
b) Open both



$$L = \frac{\lambda}{4} = \frac{1}{4} \frac{v}{f}$$

$$= \frac{1}{4} \frac{340 \text{ m/s}}{22 \text{ Hz}} = 3.9 \text{ m}$$



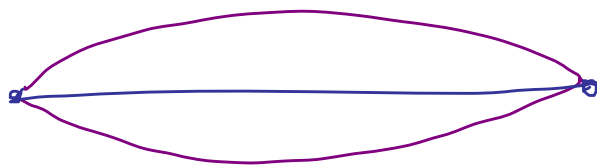
$$L = \frac{\lambda}{2} = \frac{1}{2} \frac{v}{f} = \frac{1}{2} \frac{340 \frac{\text{m}}{\text{s}}}{22 \frac{1}{\text{s}}} = 7.8 \text{ m}$$

14.68 A-string in piano is 440 Hz



is 38.9 cm long. Clamped on both ends.

$F = 667 \text{ N}$. Find mass of string.



$$L = \frac{\lambda}{2} = \frac{1}{2} \frac{v}{f}$$

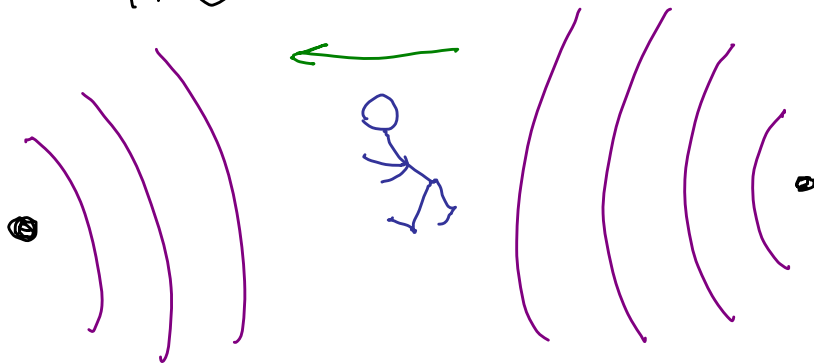
$$v = 342 \frac{\text{m}}{\text{s}}$$

$$v = \sqrt{\frac{F}{\mu}}$$

$$\mu = \frac{F}{\left(342 \frac{\text{m}}{\text{s}}\right)^2} = 5.69 \times 10^{-3} \frac{\text{kg}}{\text{m}}$$

$$\begin{aligned} \text{Mass of string} &= \mu L = 2.2 \times 10^{-3} \text{ kg} \\ &= 2.2 \text{ g} \end{aligned}$$

14.74 You're between two loudspeakers emitting 180-Hz tones. How fast would you have to move to perceive a beat frequency of 1.5 Hz between the two?



Moving observer

$$f' = f \left(1 \pm \frac{u_{\text{obs}}}{v} \right)$$

Given $\Delta f = f_{\text{ton}} - f_{\text{obs}} = 1.5 \text{ Hz}$

$$= f \left(1 + \frac{u_{\text{obs}}}{v} \right) - f \left(1 - \frac{u_{\text{obs}}}{v} \right) = 1.5 \text{ Hz}$$

$$2f \frac{u_{obs}}{v} = 1.5 \text{ Hz}$$

$$u_{obs} = \frac{1.5 \text{ Hz}}{180 \text{ Hz}} \frac{v}{2}$$

$$u_{obs} = 1.43 \frac{\text{m}}{\text{s}}$$

$$f = 180 \text{ Hz}$$

$$v = \text{speed of sound}$$

Examples



car goes down
road playing
concert A
to people
standing front.

What freq do they hear?

$$f' = f \left(\frac{1}{1 - \frac{v_{\text{source}}}{v}} \right) = (440 \text{ Hz}) \left(\frac{1}{1 - \frac{31.1 \frac{\text{m}}{\text{s}}}{343.5}} \right) = 484 \text{ Hz}$$

12.78

