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Sept. 19, 2007

1. The moon is receding from the Earth at a rate of about $3.0 \frac{\text{cm}}{\text{vear}}$. Convert this value to units of $\frac{m}{s}$.

You can use the relation 1 year = 3.16×10^7 s.

We find:

$$3.0 \frac{\text{cm}}{\text{year}} = (3.0 \frac{\text{cm}}{\text{year}}) \left(\frac{1.0 \text{ m}}{100 \text{ cm}} \right) \left(\frac{1 \text{ year}}{3.16 \times 10^7 \text{ s}} \right) = 9.49 \times 10^{-10} \frac{\text{m}}{\text{s}}$$

- 2. Vector A has a magnitude of 7.2 and is directed at 50° above the x axis. Vector **B** has a magnitude of 12.8 and points in the -y direction.

a) Find the x and y components of A and B.

With $\theta = 50^{\circ}$,

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$$\theta=50^\circ$$
,
$$A_x=A\cos\theta=7.2\cos50^\circ=4.63 \qquad A_y=A\sin\theta=7.2\sin50^\circ=5.52$$
 Since P points in the condition and has magnitude 12.8 if

Since ${\bf B}$ points in the -y direction and has magnitude 12.8 it is clear that

$$B_x = 0 B_y = -12.8$$

b) Find the magnitude and direction of A + B

If C = A + B then

$$C_x = A_x + B_x = 4.63$$
 $C_y = A_y + B_y = -7.28$

Then

$$C = \sqrt{C_x^2 + C_y^2} = 8.63$$

and the direction of C is given by

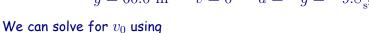
$$\tan \theta = \frac{C_y}{C_x} = -1.57 \implies \theta = \tan^{-1}(-1.57) = -57.5^{\circ}.$$

This result for the angle is correct because C clearly has to be in the 4th quadrant.

- **3.** A rock is thrown vertically upward from ground level so that it reaches a maximum height of 60.0 m.
- a) What was the initial speed of the rock?

From the time that the rock is thrown to the time it reaches max height, we know:

$$y = 60.0 \text{ m}$$
 $v = 0$ $a = -g = -9.8 \frac{\text{m}}{\text{s}^2}$



$$v^2 = v_0^2 + 2ay$$
 \implies $v_0^2 = v^2 - 2ax = 0 - 2(-9.8 \frac{\text{m}}{\text{s}^2})(60.0 \text{ m}) = 1176 \frac{\text{m}^2}{\text{s}^2}$

60.0 m

Then:

$$v_0 = 34.3 \frac{\text{m}}{\text{s}}$$

b) How long did it take the rock to reach maximum height?

At what time does v=0? Use

$$v = v_0 + at$$
 \Longrightarrow $t = \frac{(v - v_0)}{a} = \frac{(0 - 34.3\frac{\text{m}}{\text{s}})}{-9.8\frac{\text{m}}{\text{s}^2}} = 3.50 \text{ s}$

You must show all your work and include the right units with your answers!

$$A_x = A\cos\theta \qquad A_y = A\sin\theta \qquad A = \sqrt{A_x^2 + A_y^2} \qquad \tan\theta = A_y/A_x$$

$$v_x = v_{0x} + a_x t \qquad x = v_{0x}t + \frac{1}{2}a_x t^2 \qquad v_x^2 = v_{0x}^2 + 2a_x x \qquad x = \frac{1}{2}(v_{0x} + v_x)t$$

$$v_y = v_{0y} + a_y t \qquad y = v_{0y}t + \frac{1}{2}a_y t^2 \qquad v_y^2 = v_{0y}^2 + 2a_y y \qquad y = \frac{1}{2}(v_{0y} + v_y)t$$

$$g = 9.80 \frac{m}{s^2} \qquad \mathbf{F}_{\text{net}} = m\mathbf{a}$$