

Standing Waves

2 waves moving in opp. directions

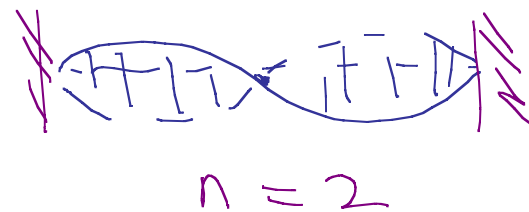
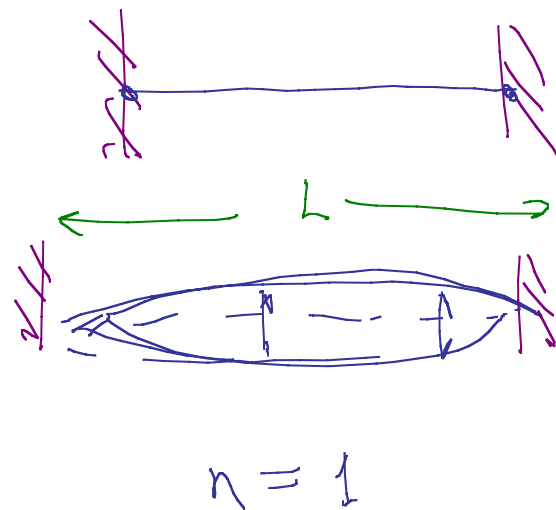
Example:

Lowest mode:

$$L = \frac{\lambda}{2} \quad f = \frac{v}{\lambda} = \frac{2v}{L}$$

Next mode

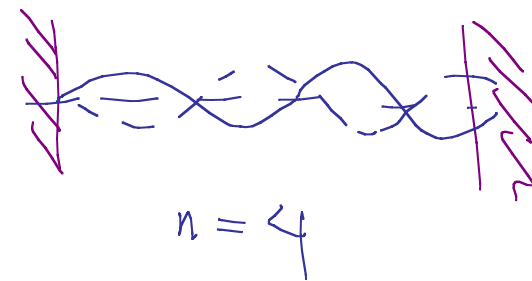
$$L = \lambda \quad f = \frac{v}{\lambda} = \frac{v}{L}$$



$$L = n \frac{\lambda}{2} \quad \lambda = \frac{2L}{n}$$

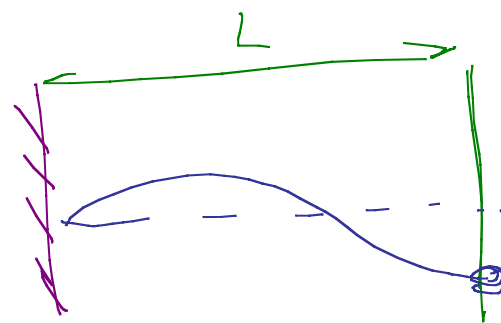
$$f = \frac{v}{\lambda} = \frac{nv}{2L} = n \frac{v}{2L}$$

$$v = \sqrt{\frac{F}{\mu}}$$



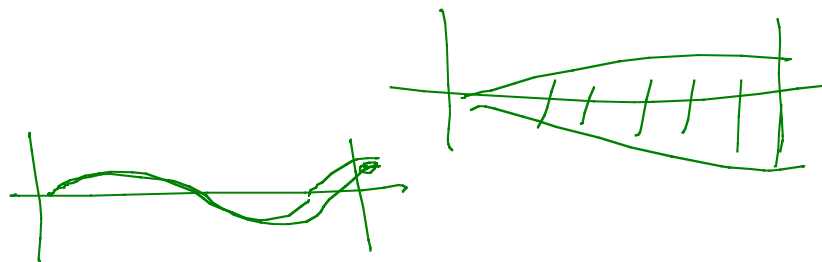
1:2:3:4

If string fixed one end
free on other



$$L = \frac{1}{4}\lambda, \frac{3}{4}\lambda, \frac{5}{4}\lambda$$

$$= \frac{n\lambda}{4} \quad n \text{ odd}$$



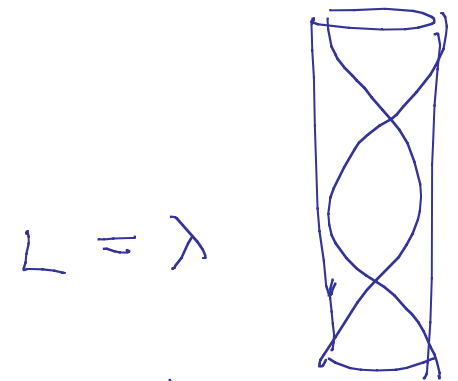
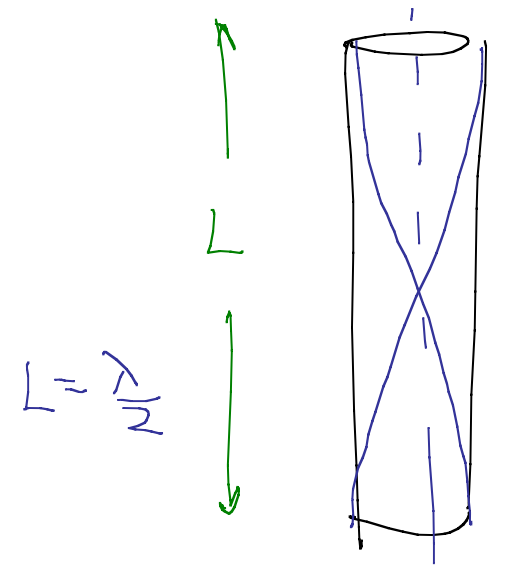
Standing Sound Waves, Pipe

Open both ends

$$L = n \frac{\lambda_n}{2} \quad \lambda_n = \frac{2L}{n}$$

$$f_n = \frac{v}{\lambda_n} = \frac{n v}{2L}$$

$$f_n: 1:2:3:4:5$$



n^{th} mode

$$\underline{v = 343 \frac{m}{s}}$$

$$331 \frac{m}{s} \quad 0^\circ C$$

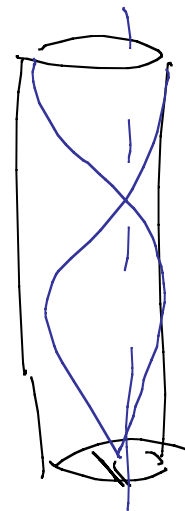
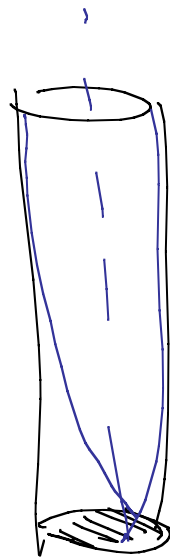
$$L = \frac{n}{4} \lambda \quad n = 1, 3, 5, 7 \quad L = \frac{1}{4} \lambda$$

$$\lambda = \frac{4L}{n}$$

$$f_n = \frac{v}{\lambda_n} = \frac{nv}{4L} \quad n \text{ odd}$$

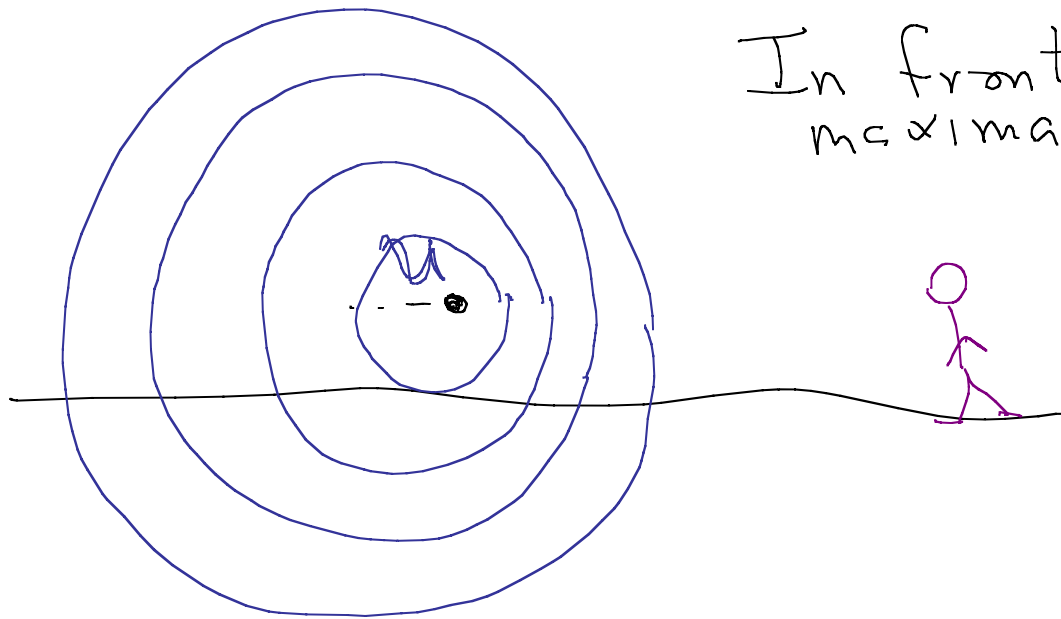
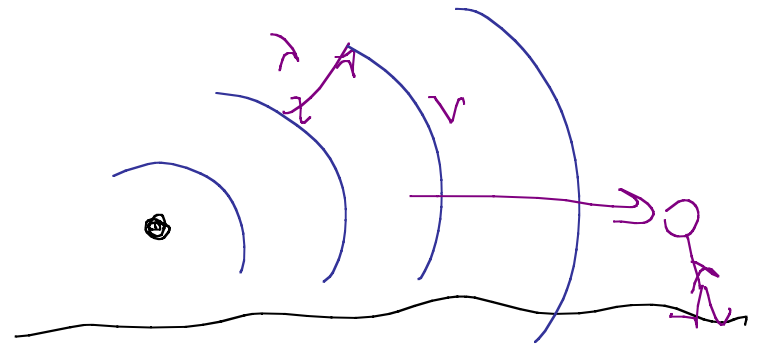
$$1 : 3 : 5 : 7 : \dots$$

$$L = \frac{3}{4} \lambda$$



Doppler Effect

Source is moving



In front, dist between maxima is shorter

λ got smaller

$$f\lambda = v$$

$$f_{\text{observed}} = f' \quad \begin{matrix} \uparrow \\ \text{is} \\ \text{bigger} \end{matrix}$$

Moving
source

$$f' = \frac{f}{\left(1 \pm \frac{u}{v}\right)}$$

- toward
+ away

Moving observer

$$f' = f \left(1 \pm \frac{u}{v}\right)$$

+ toward
- away

