Worked Examples from Introductory Physics
Vol. II: Rotation, Vibrations and Waves

David Murdock
Tenn. Tech. Univ.

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To the Student. Yeah, *You.*

Hi. It's me again. Since you have obviously read all the stuffy pronouncements about the purpose of this problem–solving guide in Volume 1 (The Green Book), I won't make them again here.

I will point out that I've got *lots* more work to do on Volume 2, and I'm just making it available so that these chapters (such as they are) may be of some help to you. In fact, the whole set of books is a perpetual work in progress.

However....

Reactions, please!

Please help me with this project: Give me your reaction to this work: Tell me what you liked, what was particularly effective, what was particularly confusing, what you'd like to see more of or less of. I can be reached at `murdock@tntech.edu` or even at x–3044. If this effort is helping you to learn physics, I'll do more of it!

DPM