CAP6676 Knowledge Representation, Fall 2015

Instructor: Guo-Jun Qi. Due: November 3rd, 2015.

Machine Problem 2: Logistic Regression: Learning and Inference

In this machine problem, you will implement the (stochastic) gradient ascent algorithm to learn the parameters for logistic regression model.

Step 1: Use the same dataset in MP2 for the experiments. You will need to compare the results between LR model and decision tree model.

Step 2: Implement the learning algorithm for LR model with batch-mode gradient ascent algorithms. You should NOT use any off-the-shelf optimization library here. You need to derive the derivative of loglikelihood function to the model parameters over the entire training set, and update the model parameters iteratively. Choose a stop criterion to decide when to terminate the iteration.

For example, you can stop the algorithm when

- a. the increment of loglikelihood between two successive iterations is smaller than a threshold, OR
- b. the absolute value of the derivatives is smaller than a threshold, OR
- c. a maximum number of iterations has been reached.

You should monitor and <u>plot</u> the curve of the objective loglikelihood over iterations, and report your observation in your report. Also, <u>plot</u> how the training and test error evolve over iterations, and <u>report</u> if you observe any overfitting phenomenon (i.e., decreasing training error but increasing test error).

Step 3: Run stochastic gradient ascent algorithms. Choose a proper size of randomly chosen subset. Repeat the process in Step 4. In addition, <u>report</u> how the size of subset in each iteration affects the result.

Step 4: Add the L₂ regularizer $-\frac{1}{2\sigma^2}||w||^2$ to the likelihood function, and maximize this regularized loglikelihood function by gradient and stochastic gradient ascent methods. Repeat Step 2 and Step 3.

In addition, tune the parameter σ on a separate validation set or by a cross-validation process. Report if this regularization mechanism can reduce the overfitting effect.

Step 5: Write the report following the above steps. Submit your report to cap6676ucf@gmail.com by November 3rd. Remember to compare the LR result with that of decision tree, report see which is better on your dataset. Explain why?

<u>Note</u>: In case that your chosen dataset contains categorical values of attributes, you can convert them into a binary vector indicating the categorical values. For example, for an attribute with K possible categories, construct a K-dimensional binary vector with the entry corresponding to the category set to one, and the other entries set to zero.