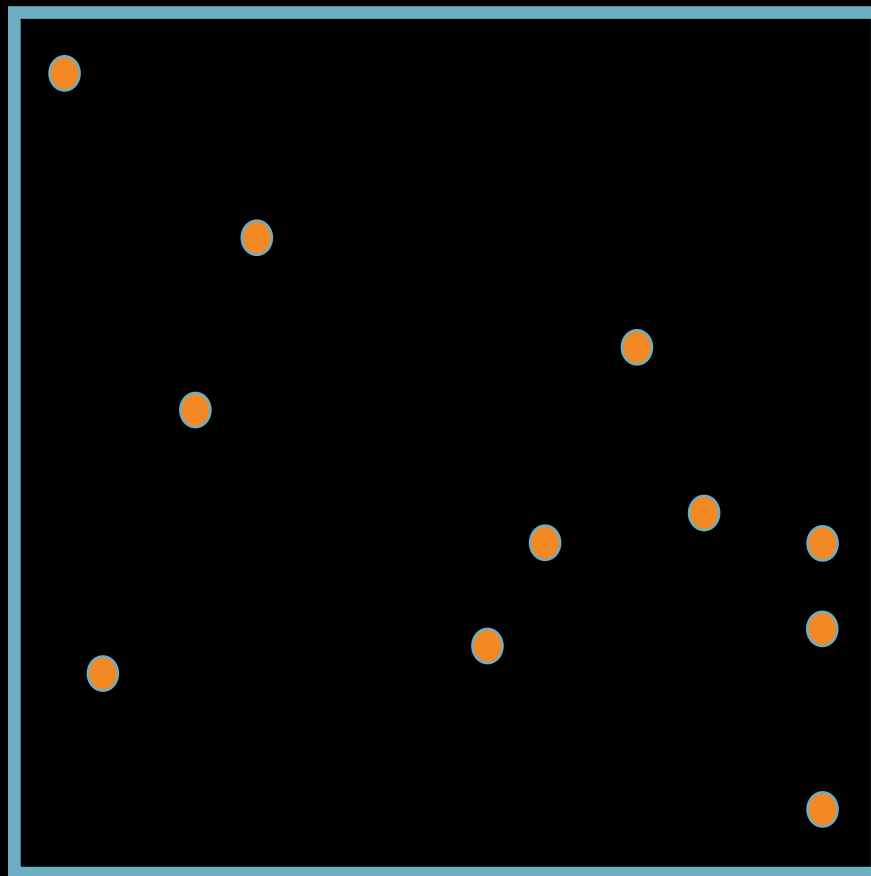


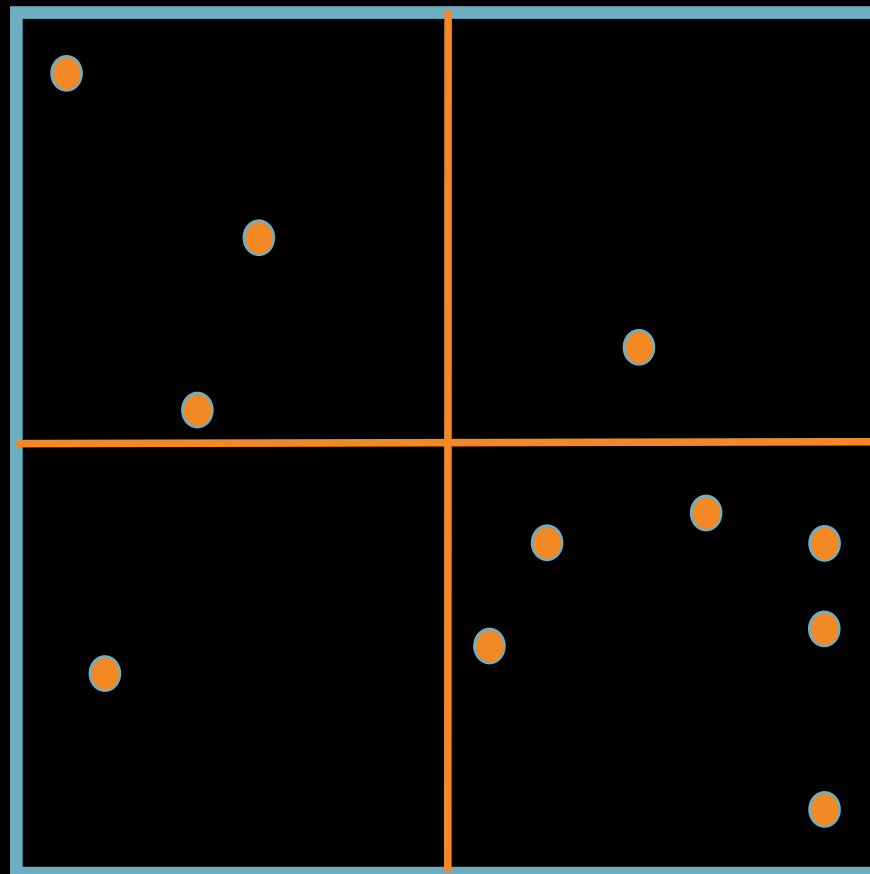
# Quadtrees

João Comba

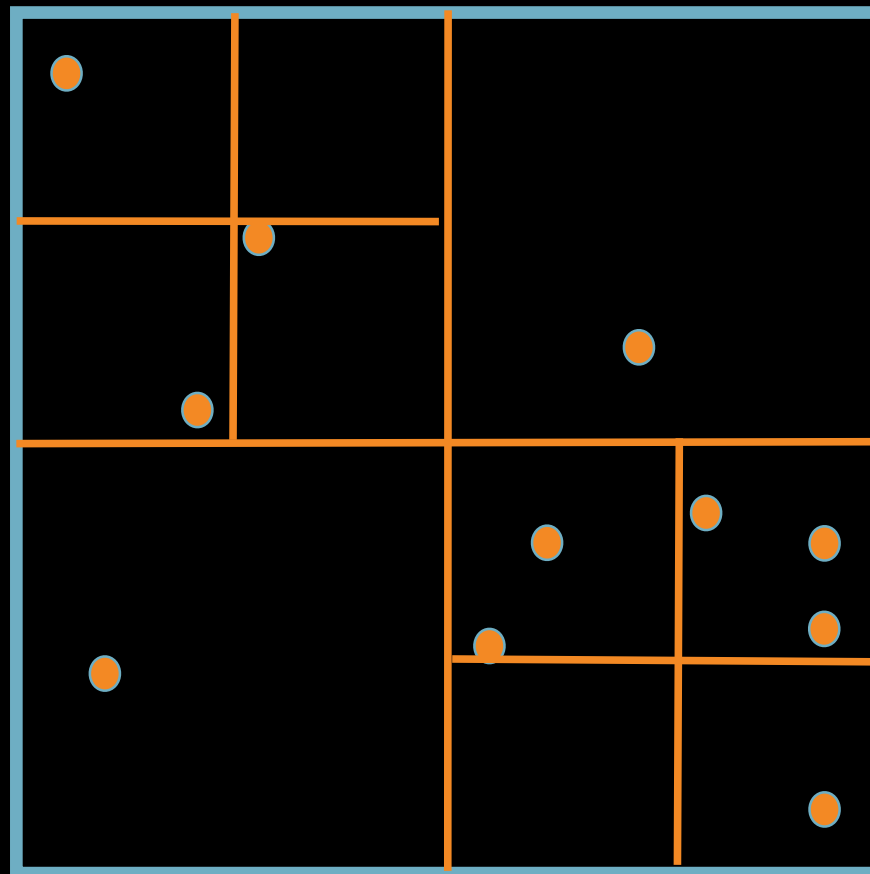
# Quadrees



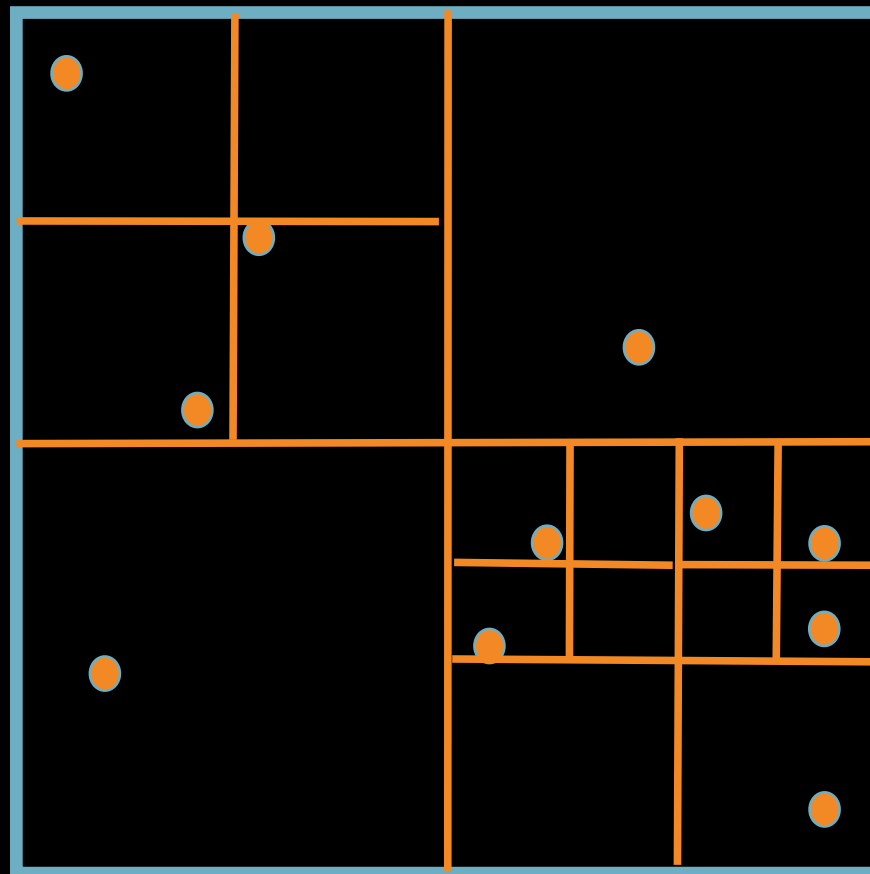
# Quadtrees



# Quadrees



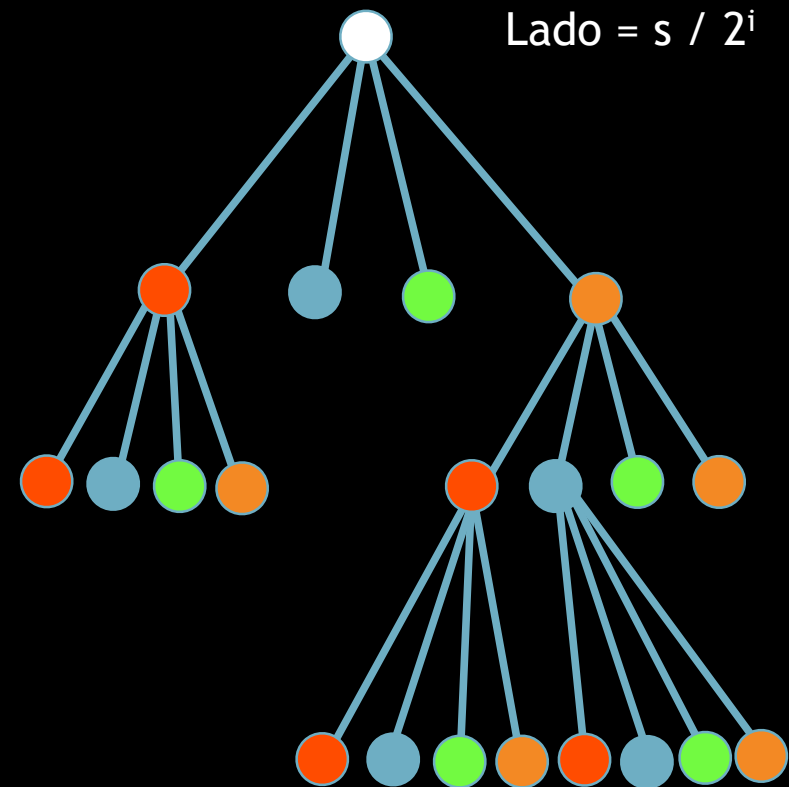
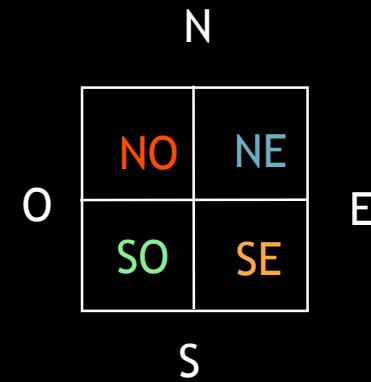
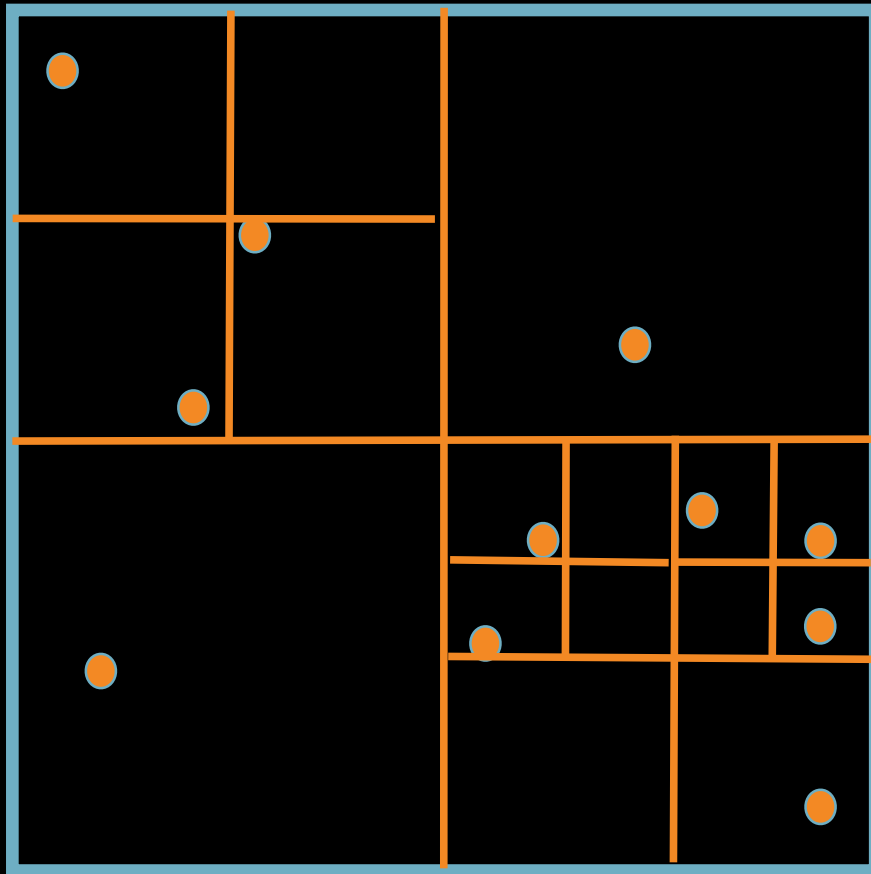
# Quadrees



# Quadrees

- Tipo de dados representados (pontos, linhas, regioes, volumes, outros)
- Principio guiando a subdivisao
- Resolucao (variavel ou nao)

# Quadrees Pontuais



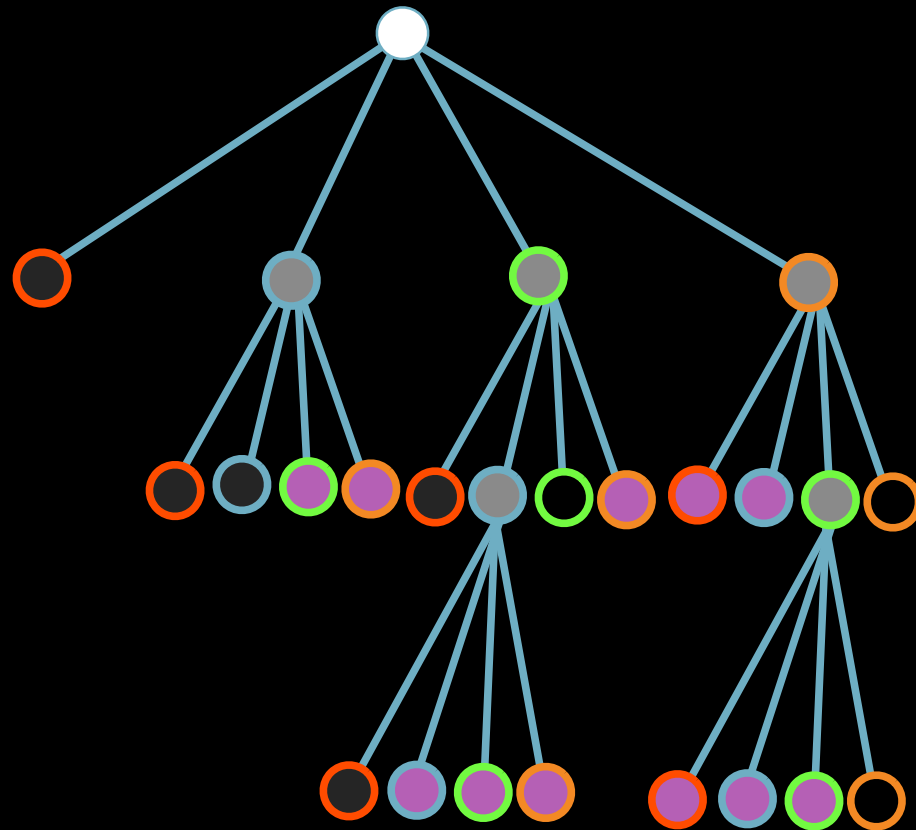
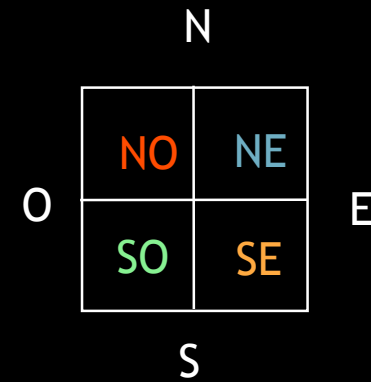
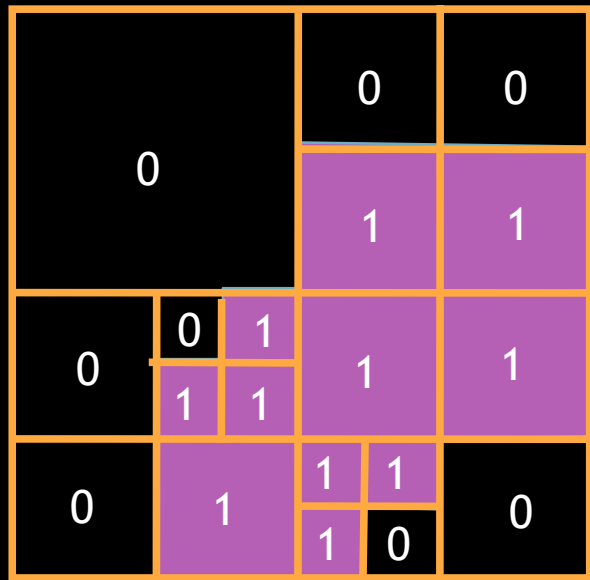
# Quadrees de Regioes

0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	1	1	1	1
0	0	0	0	1	1	1	1
0	0	0	1	1	1	1	1
0	0	1	1	1	1	1	1
0	0	1	1	1	1	0	0
0	0	1	1	1	0	0	0

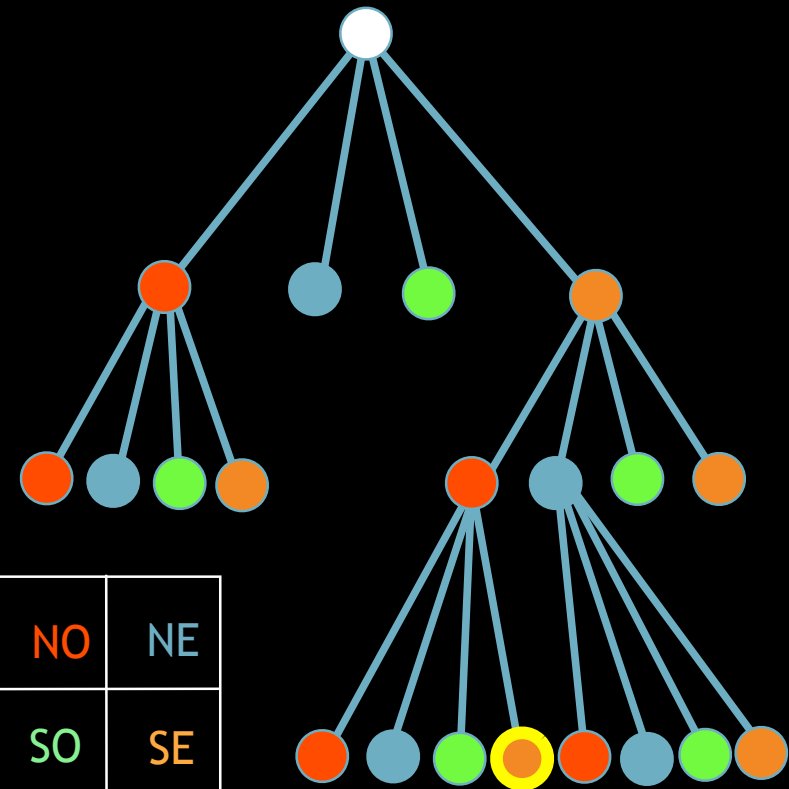
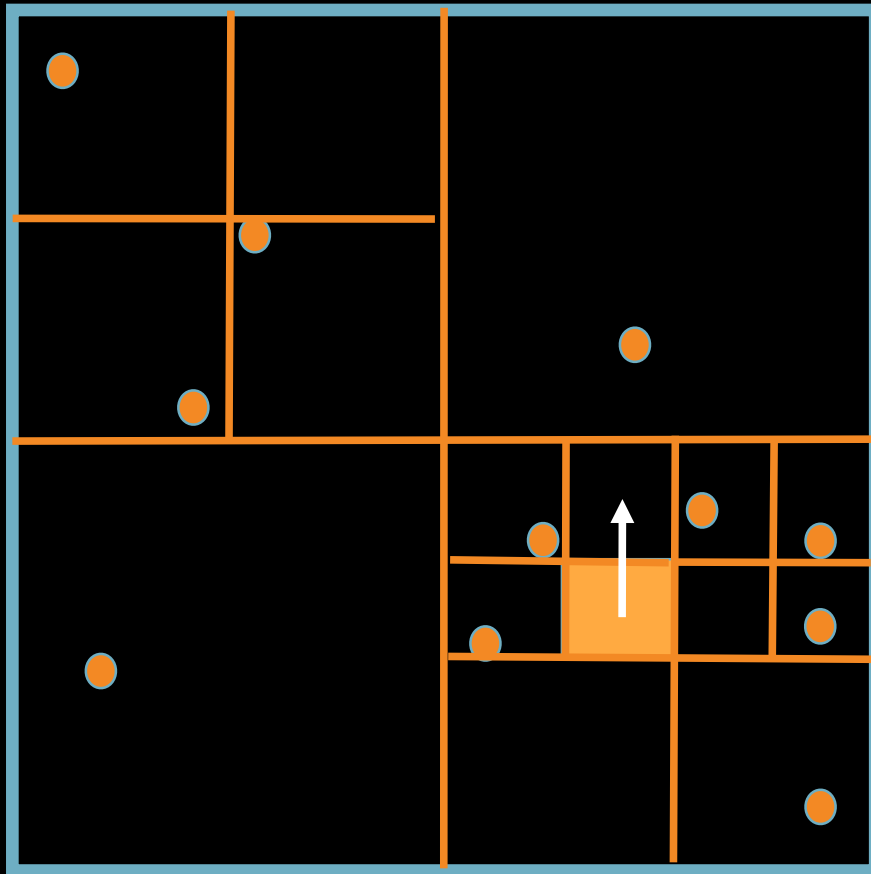
0			0	0
			1	1
0	0	1	1	1
	1	1		
0	1	1	1	0
		1	0	



# Quadtrees de Regioes

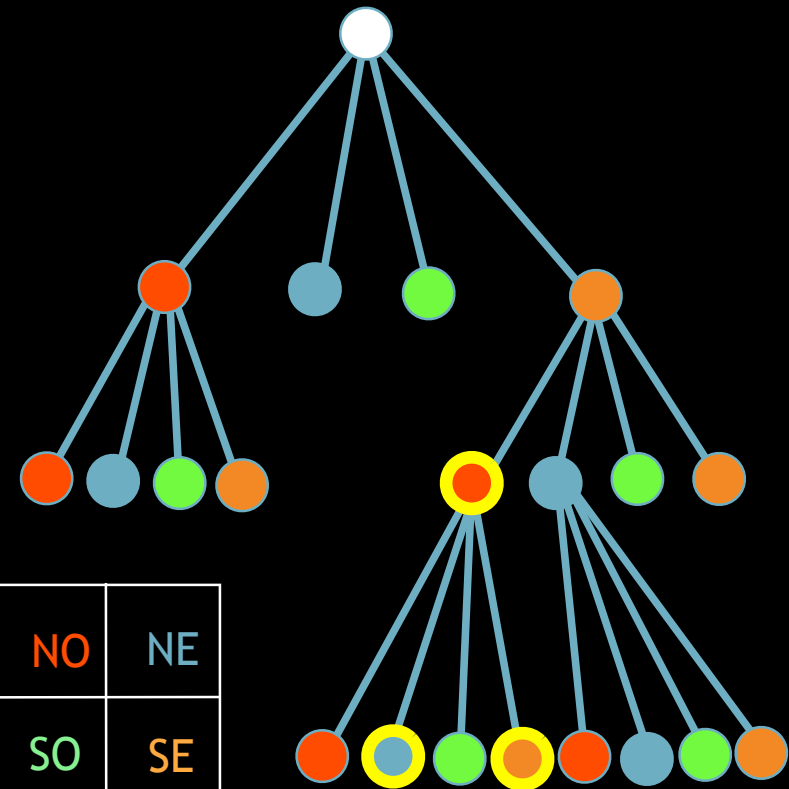
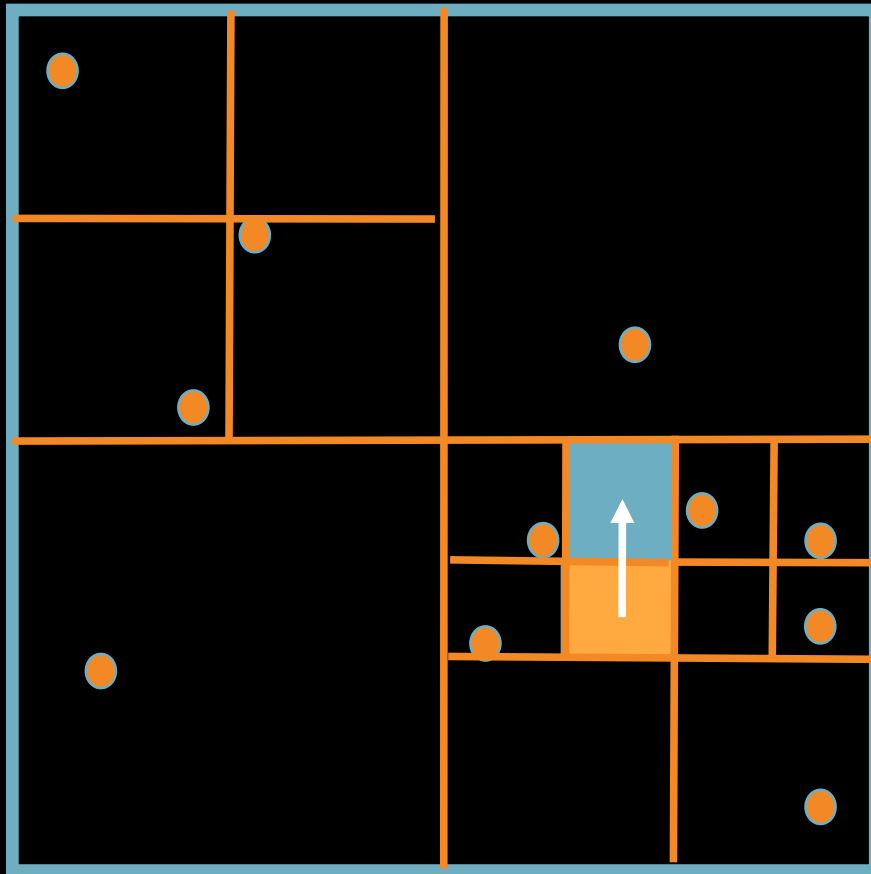


# Busca de Vizinhos

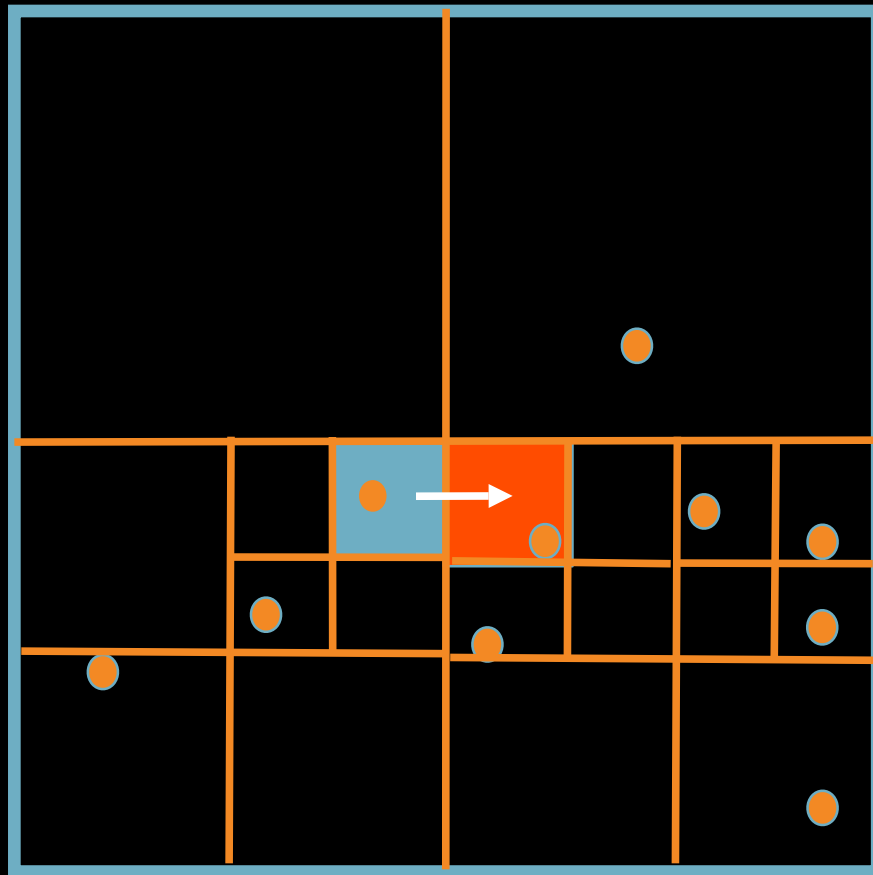


NO	NE
SO	SE

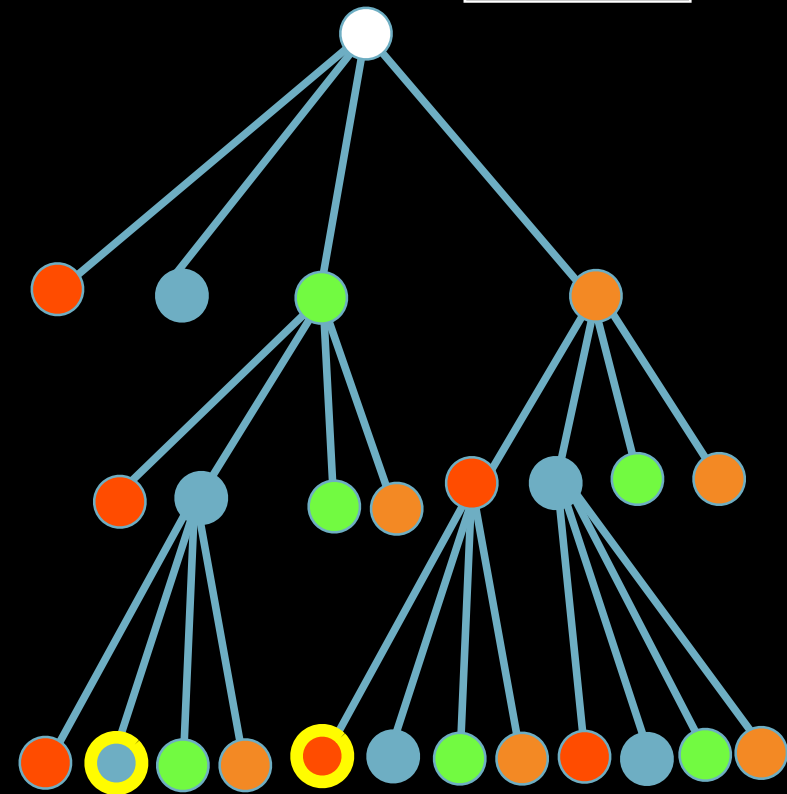
# Busca de Vizinhos



# Busca de Vizinhos (Por Aresta)

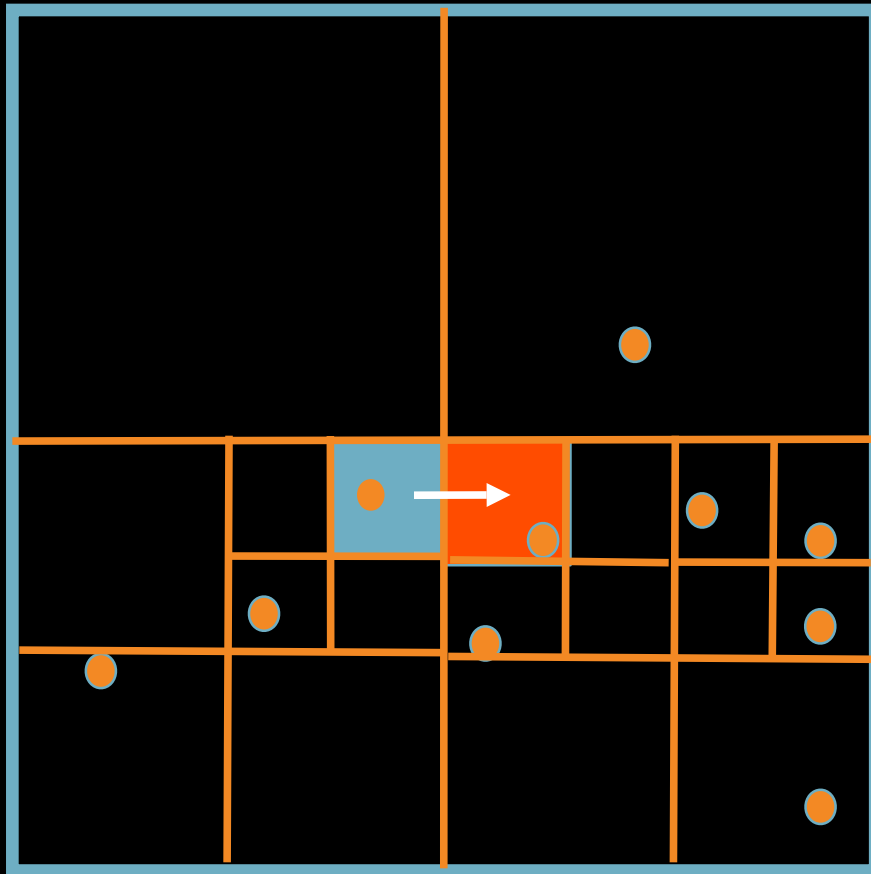


NO	NE
SO	SE

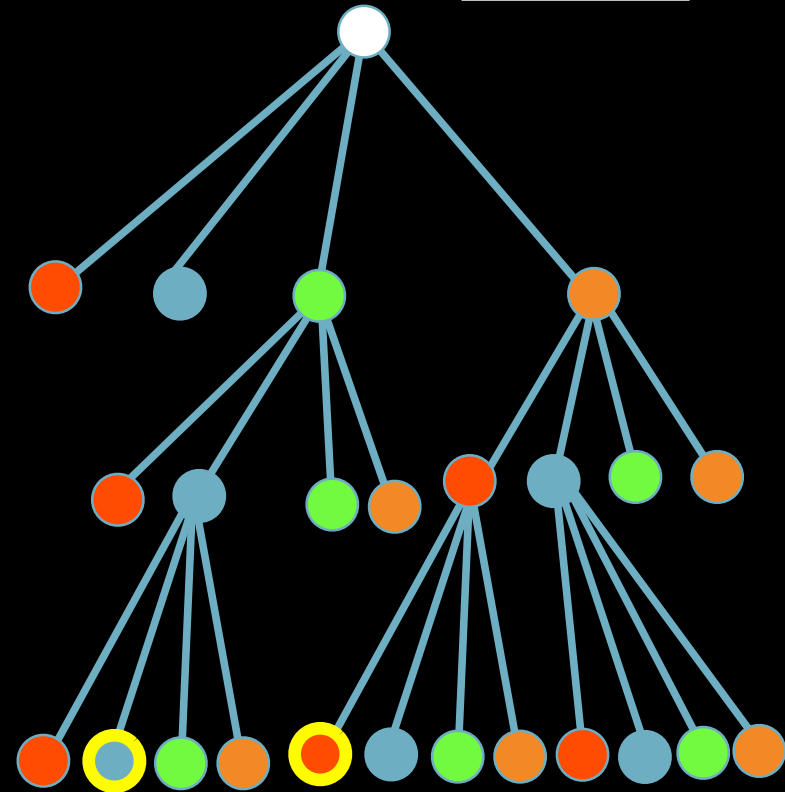


# Busca de Vizinhos (Por Aresta)

1. Achar o ancestral comum

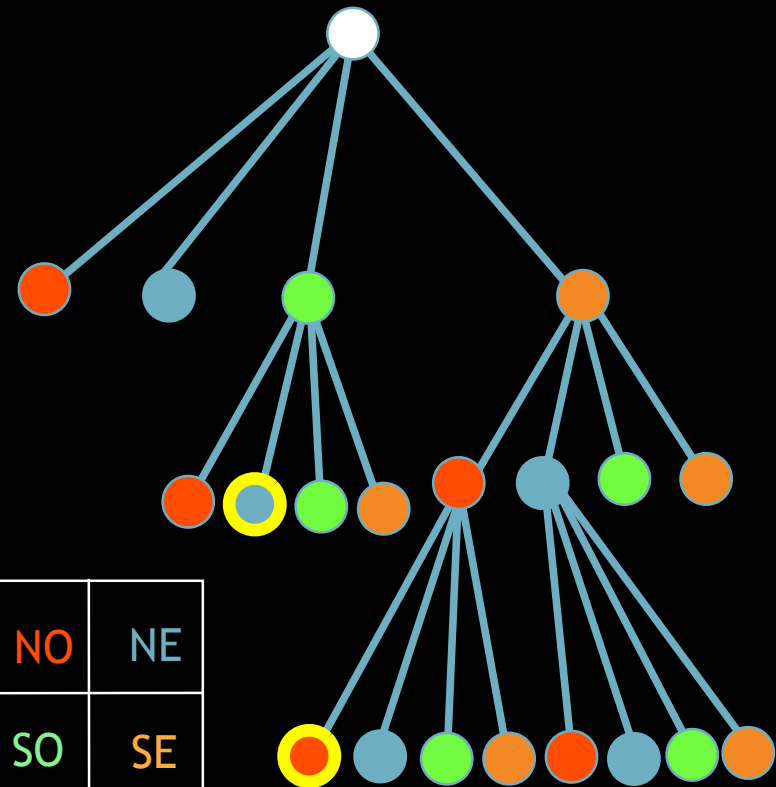
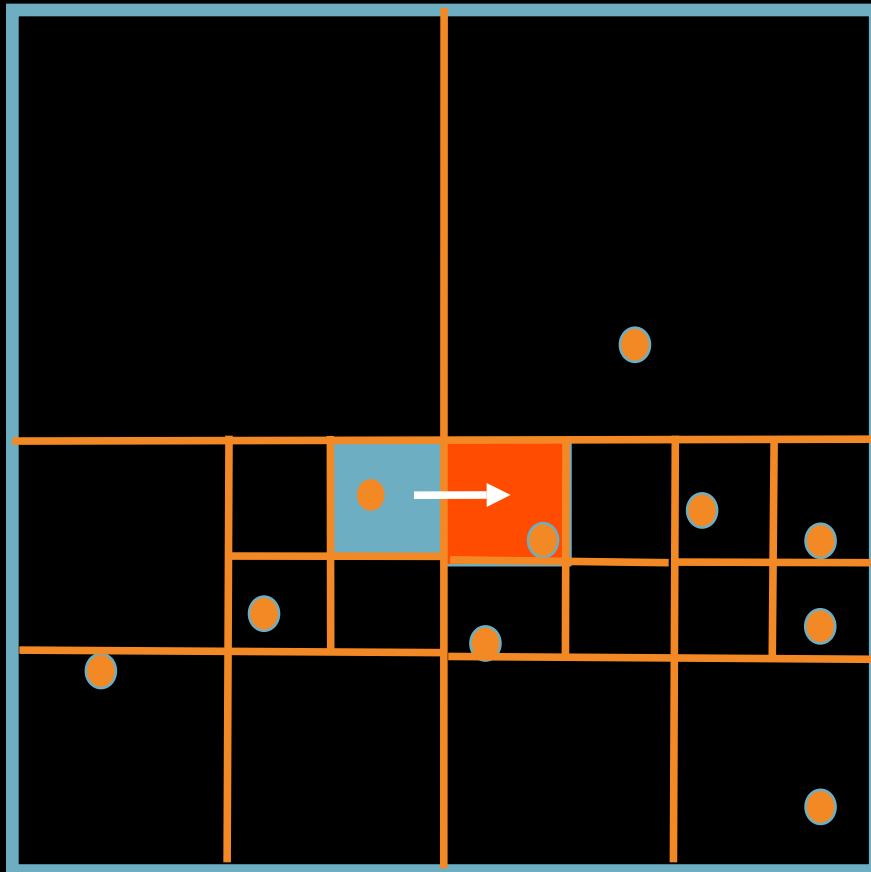


NO	NE
SO	SE



# Busca de Vizinhos

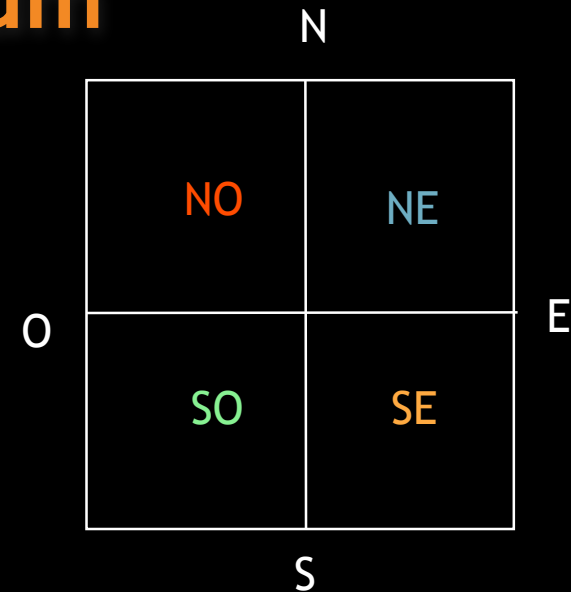
1. Achar o ancestral comum



NO	NE
SO	SE

# Achar o ancestral comum

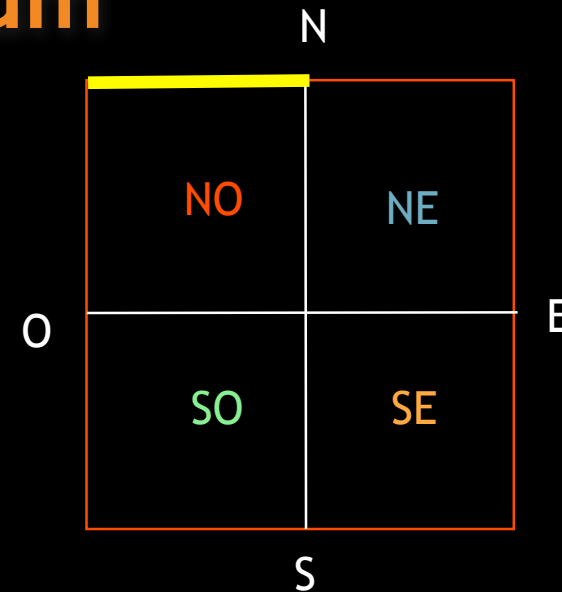
DIR(i) X QUAD(o)	NO	NE	SO	SE
N	T	T	F	F
E	F	T	F	T
S	F	F	T	T
O	T	F	T	F
NO	T	F	F	F
NE	F	T	F	F
SO	F	F	T	F
SE	F	F	F	T



$ADJ(I,O) = \text{TRUE}$ , se e somente se se o quadrante O e' adjacente a aresta ou vertice i do bloco contendo O

# Achar o ancestral comum

DIR(i) X QUAD(o)	NO	NE	SO	SE
N	T	T	F	F
E	F	T	F	T
S	F	F	T	T
O	T	F	T	F
NO	T	F	F	F
NE	F	T	F	F
SO	F	F	T	F
SE	F	F	F	T

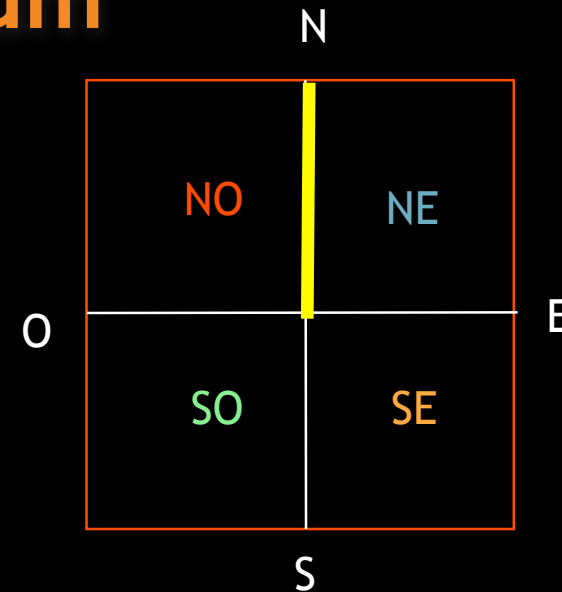


$ADJ(I,O) = \text{TRUE}$ , se e somente se se o quadrante O e' adjacente a aresta ou vertice i do bloco contendo O



# Achar o ancestral comum

DIR(i) X QUAD(o)	NO	NE	SO	SE
N	T	T	F	F
E	F	T	F	T
S	F	F	T	T
O	T	F	T	F
NO	T	F	F	F
NE	F	T	F	F
SO	F	F	T	F
SE	F	F	F	T



$ADJ(I,O) = \text{TRUE}$ , se e somente se se o quadrante O e' adjacente a aresta ou vertice i do bloco contendo O

# Achar o ancestral comum

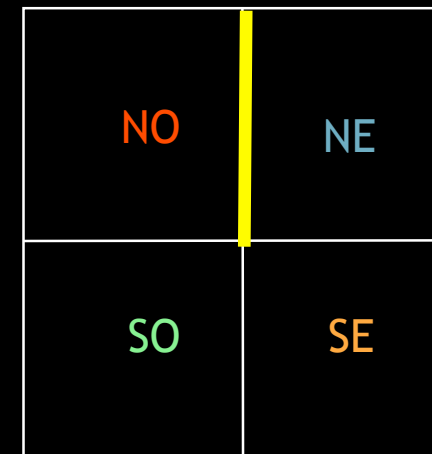
DIR(i) X QUAD(o)	NO	NE	SO	SE
N	SO	SE	NO	NE
E	NE	NO	SE	SO
S	SO	SE	NO	NE
O	NE	NO	SE	SO
NO	SE	SO	NE	NO
NE	SE	SO	NE	NO
SO	SE	SO	NE	NO
SE	SE	SO	NE	NO

NO	NE
SO	SE

**REFLECT(I,O)** = tipo do bloco de tamanho igual (nao necessariamente irmao) compartilhando a aresta

# Achar o ancestral comum

DIR(i) X QUAD(o)	NO	NE	SO	SE
N	SO	SE	NO	NE
E	NE	NO	SE	SO
S	SO	SE	NO	NE
O	NE	NO	SE	SO
NO	SE	SO	NE	NO
NE	SE	SO	NE	NO
SO	SE	SO	NE	NO
SE	SE	SO	NE	NO



**REFLECT(I,O)** = tipo do bloco de tamanho igual (nao necessariamente irmao) compartilhando a aresta

# Achar o ancestral comum

DIR(i) X QUAD(o)	NO	NE	SO	SE
NO	-	N	O	-
NE	N	-	-	E
SO	O	-	-	S
SE	-	E	S	-

NO	NE
SO	SE

**ARESTA\_COMUM(I,O)** = retorna o tipo da aresta comum ao bloco contendo o quadrante O e seu vizinho na direcao de I

# Busca de Vizinho por aresta

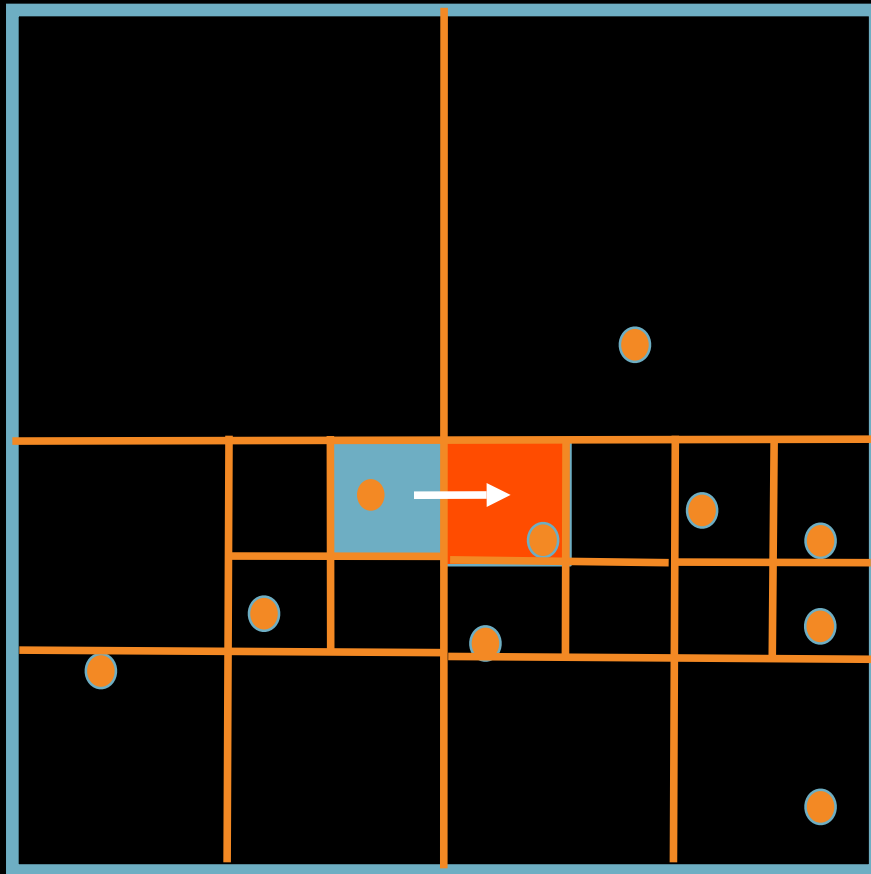
1. Localizar o mais proximo ancestral comum. Guardar o caminho
2. Refletir o caminho de subida para descer na arvore

PROCEDURE VizinhoPorAresta(P,I)

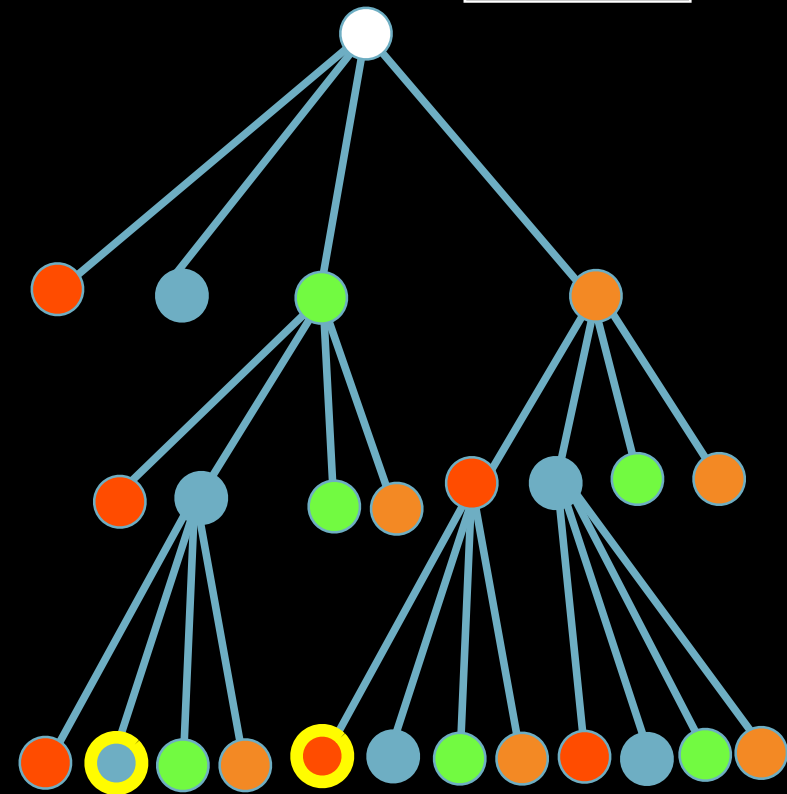
1. RETURN (SON(IF ADJ(I, TIPO(P))  
          THEN VizinhoPorAresta(PAI(P), I)  
          ELSE PAI(P),  
          REFLECT(I, TIPO(P))));

## Busca de Vizinhos (Por Aresta)

## 1. Achar o ancestral comum

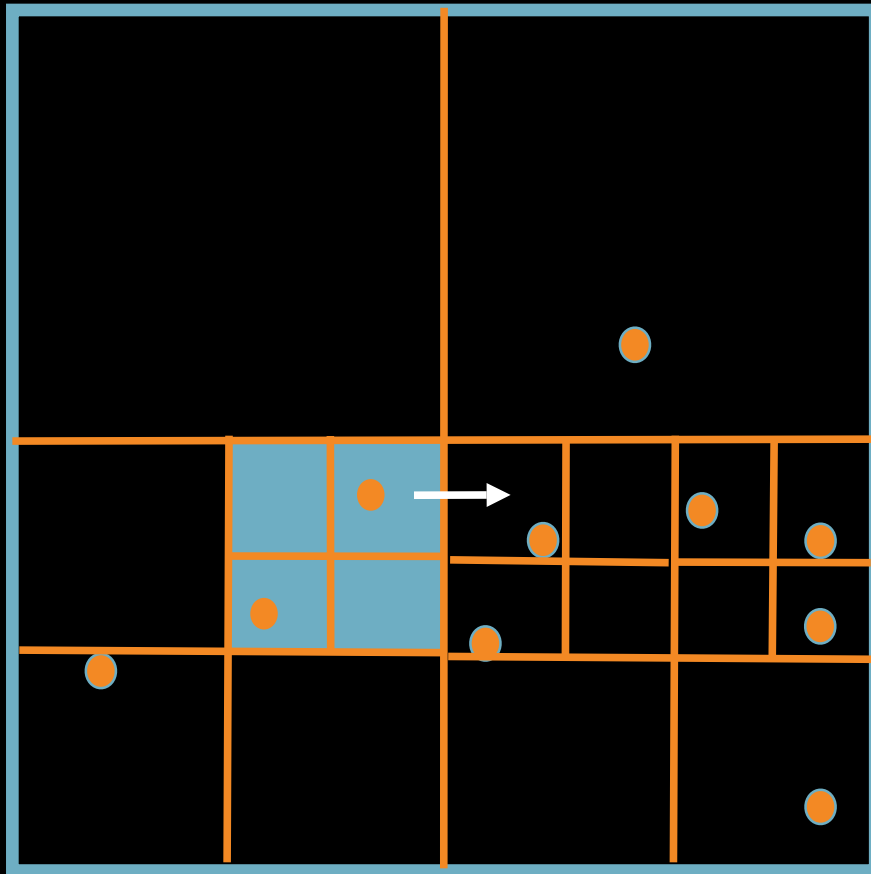


NO	NE
SO	SE

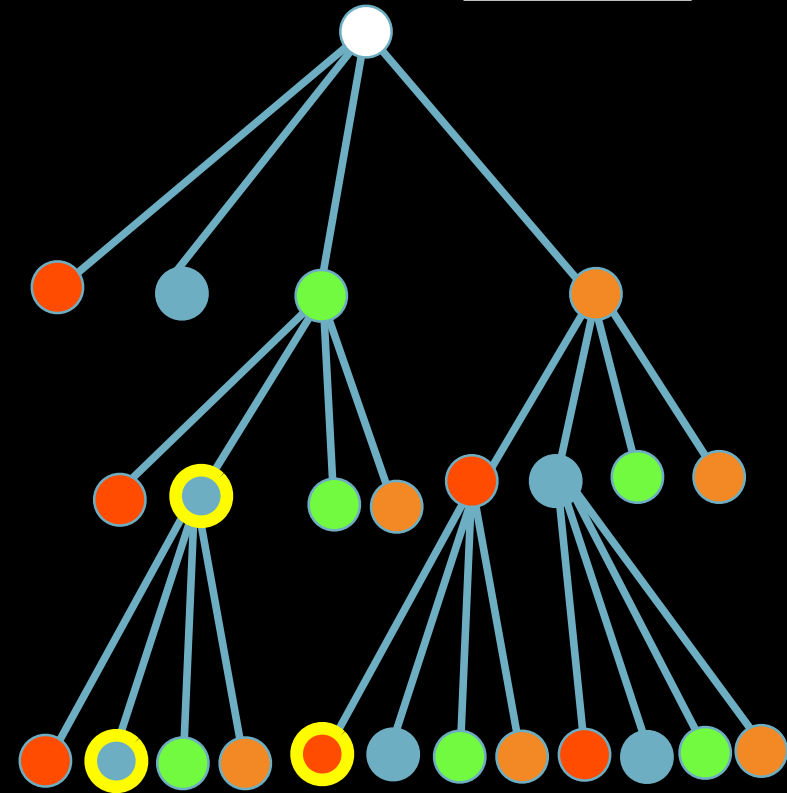


# Busca de Vizinhos (Por Aresta)

Caminho = NE

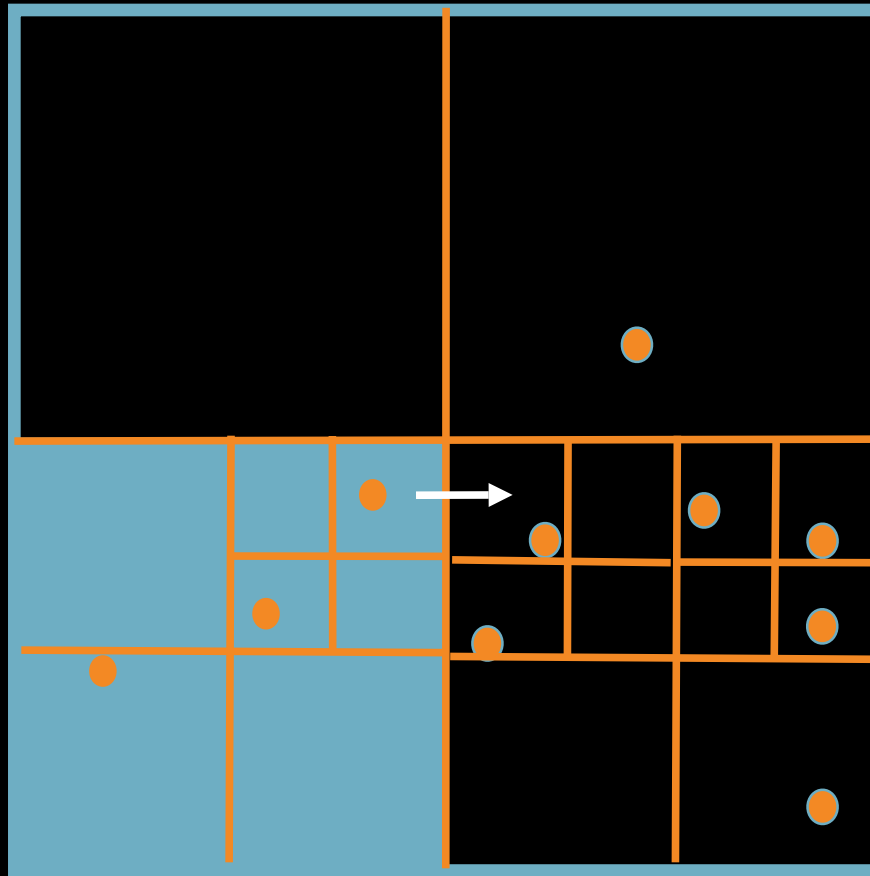


NO	NE
SO	SE

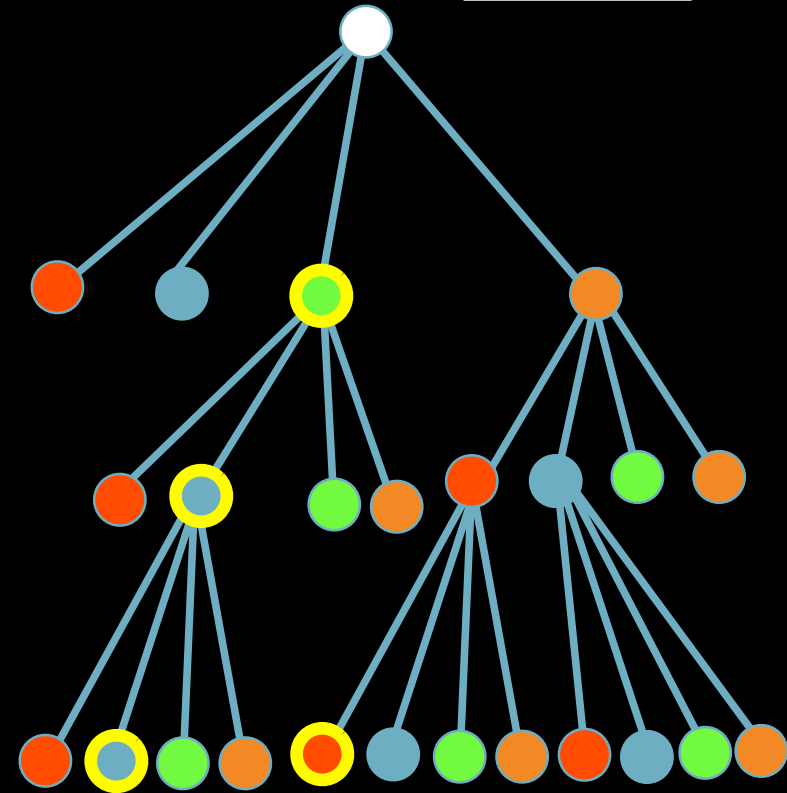


# Busca de Vizinhos (Por Aresta)

Caminho = NE, NE



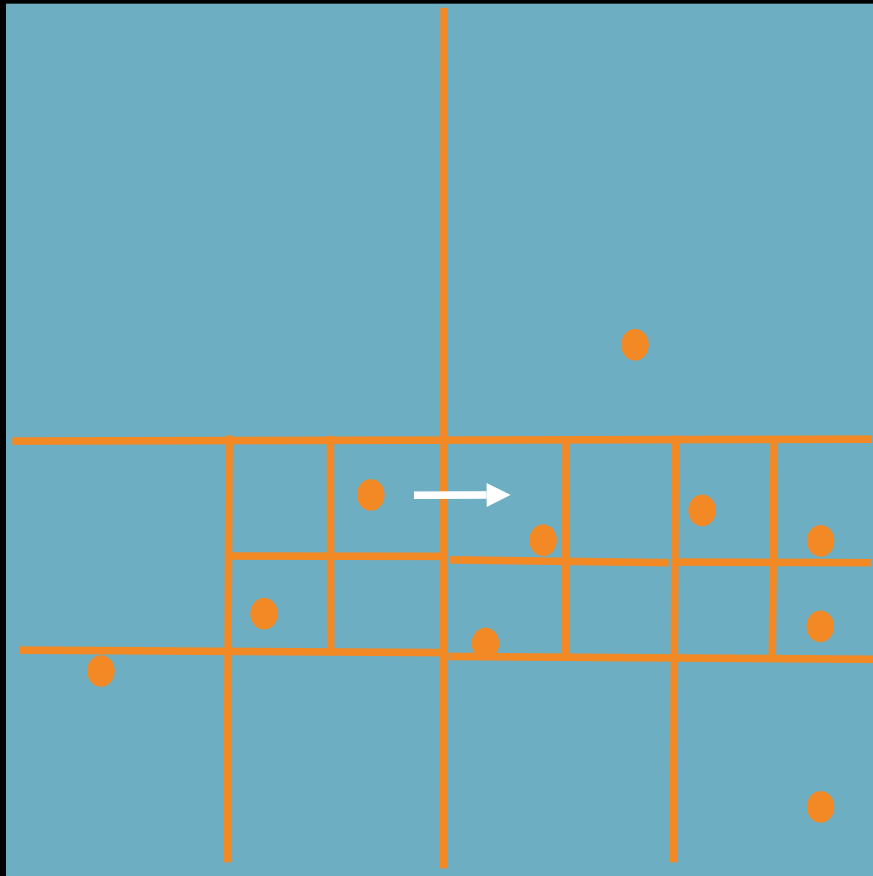
NO	NE
SO	SE



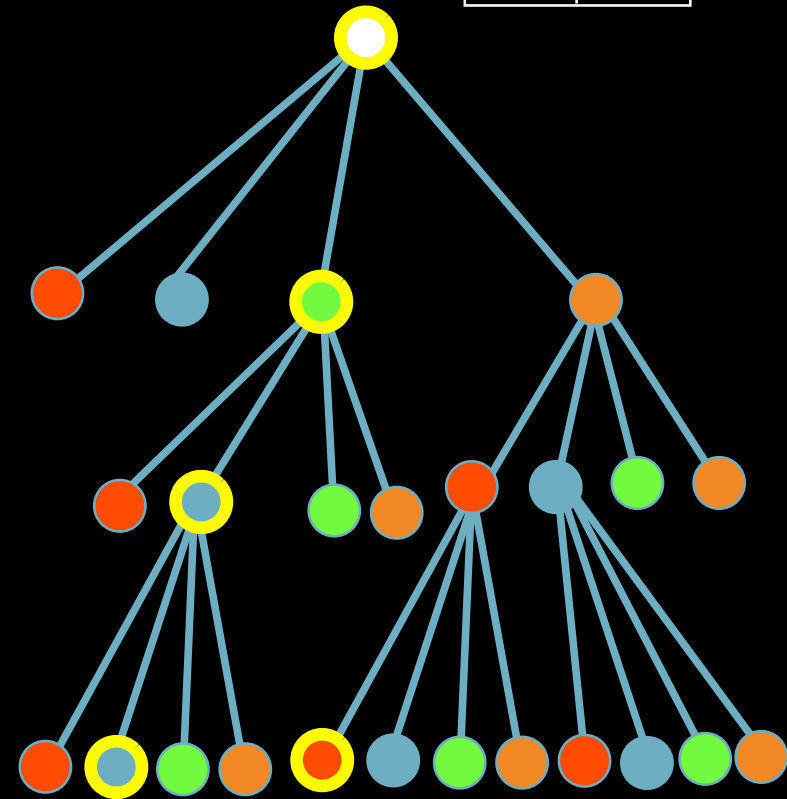


# Busca de Vizinhos (Por Aresta)

Caminho = NE, NE, SO

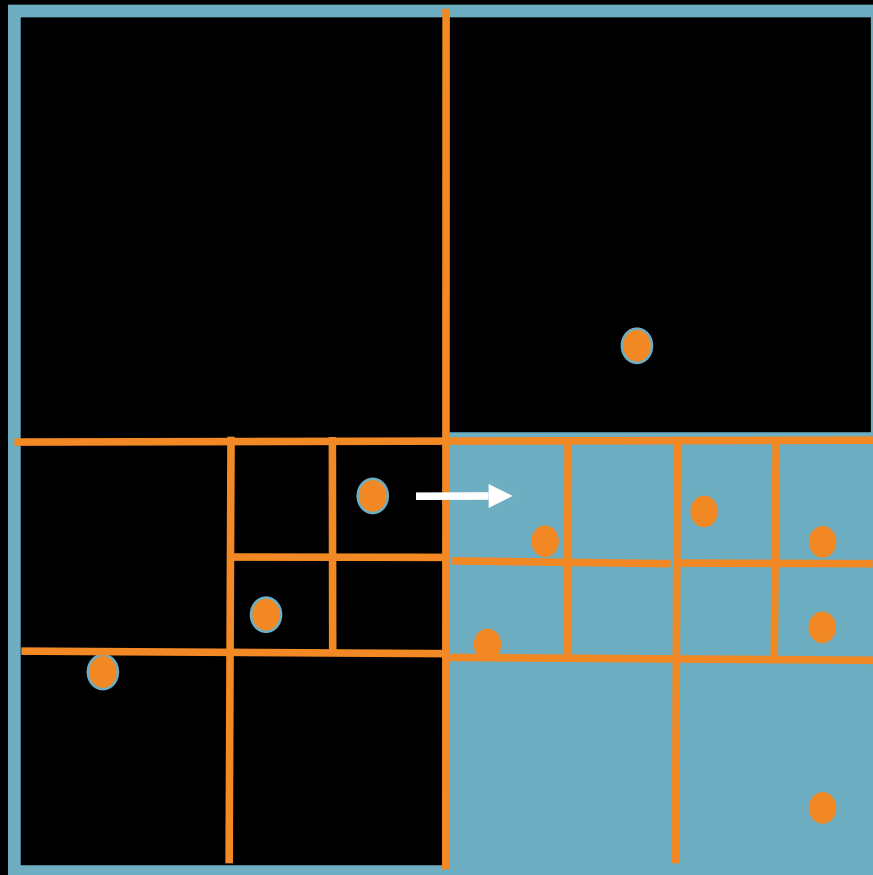


NO	NE
SO	SE



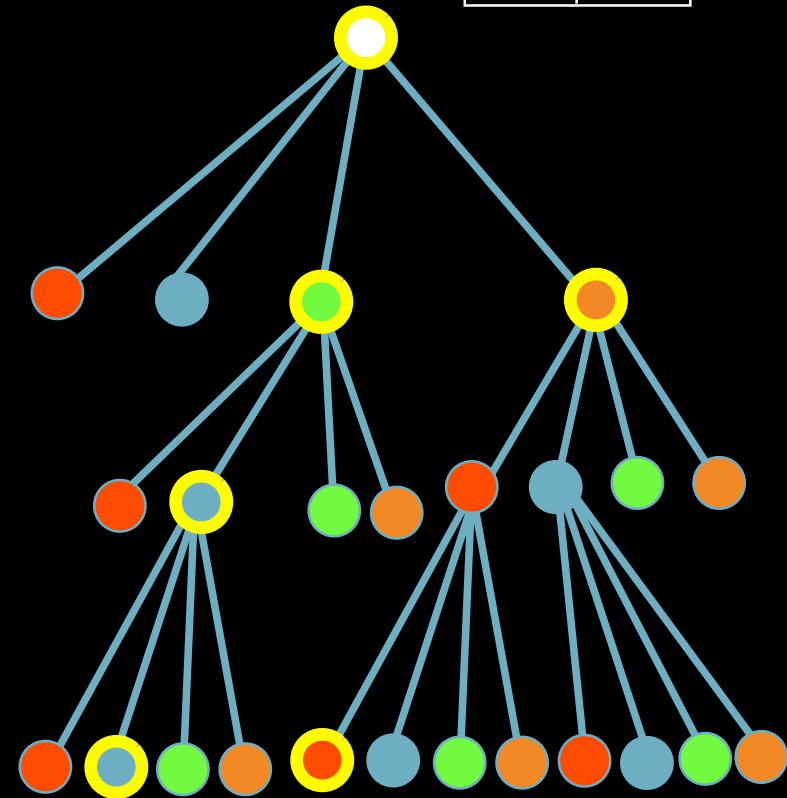
# Busca de Vizinhos (Por Aresta)

Caminho = NE, NE, SO



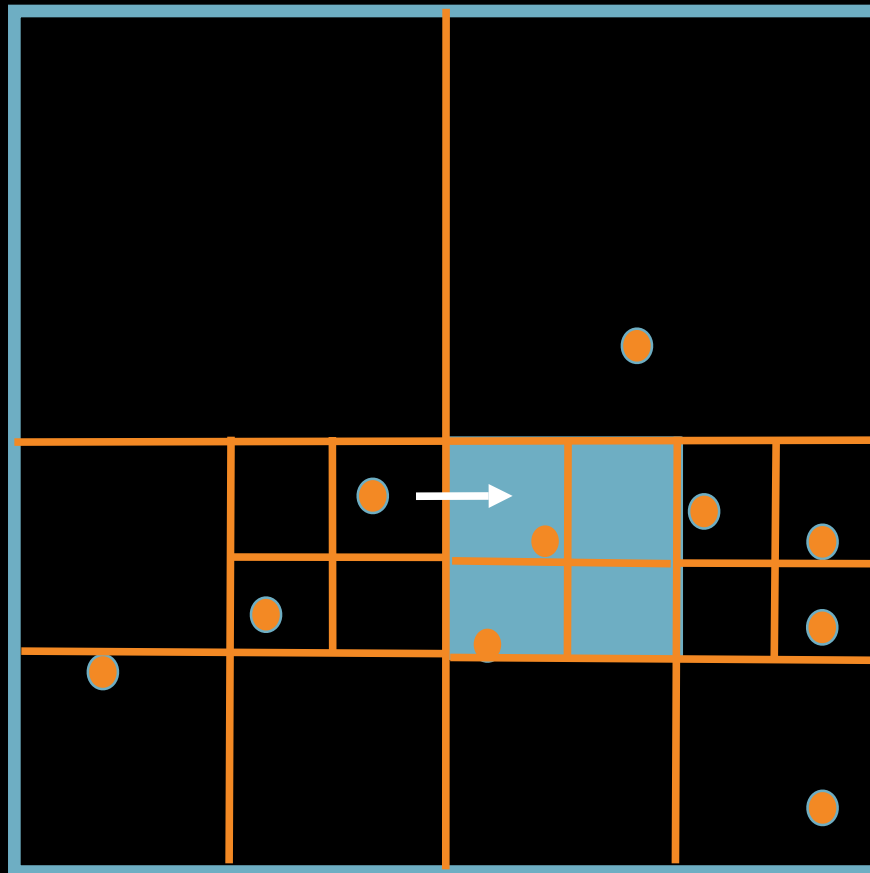
Caminho Reverso = SE

NO	NE
SO	SE



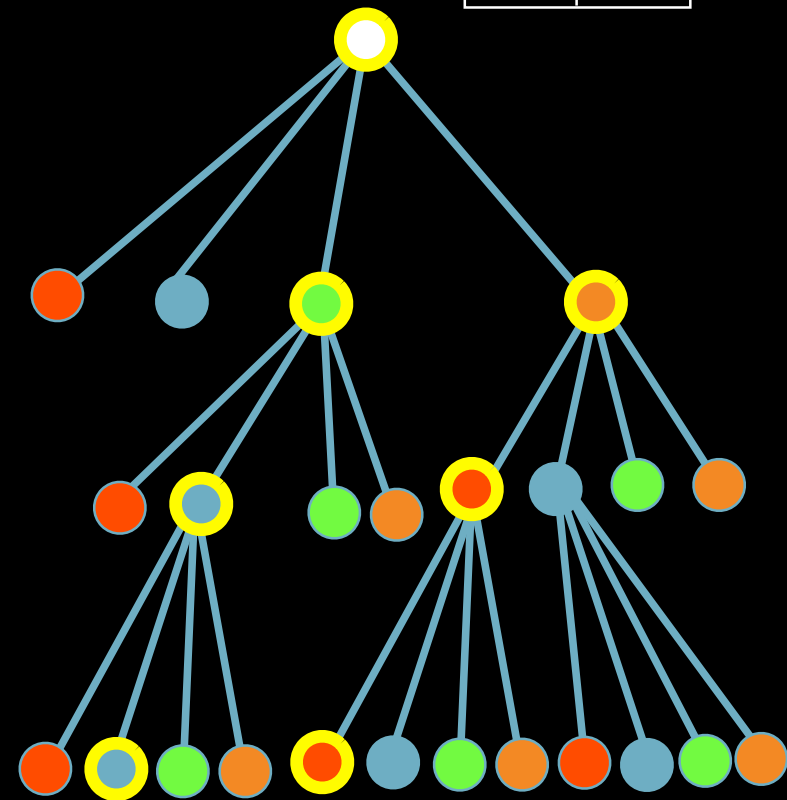
## Busca de Vizinhos (Por Aresta)

Caminho = NE, NE, SO



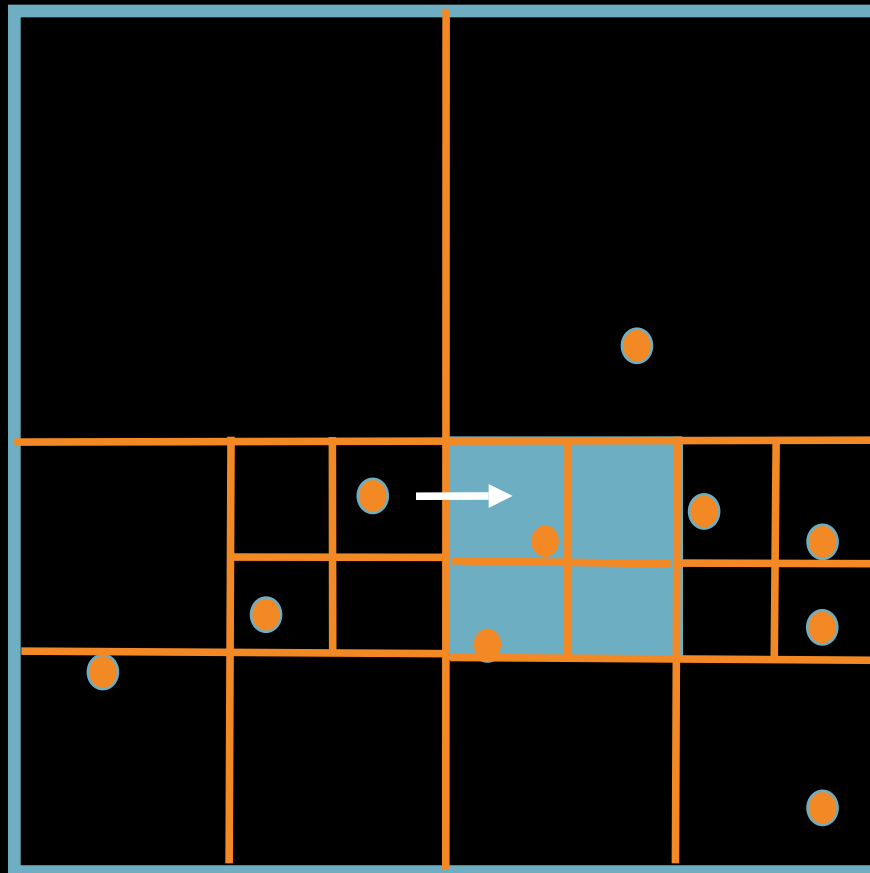
**Caminho Reverso = SE, NO**

NO	NE
SO	SE



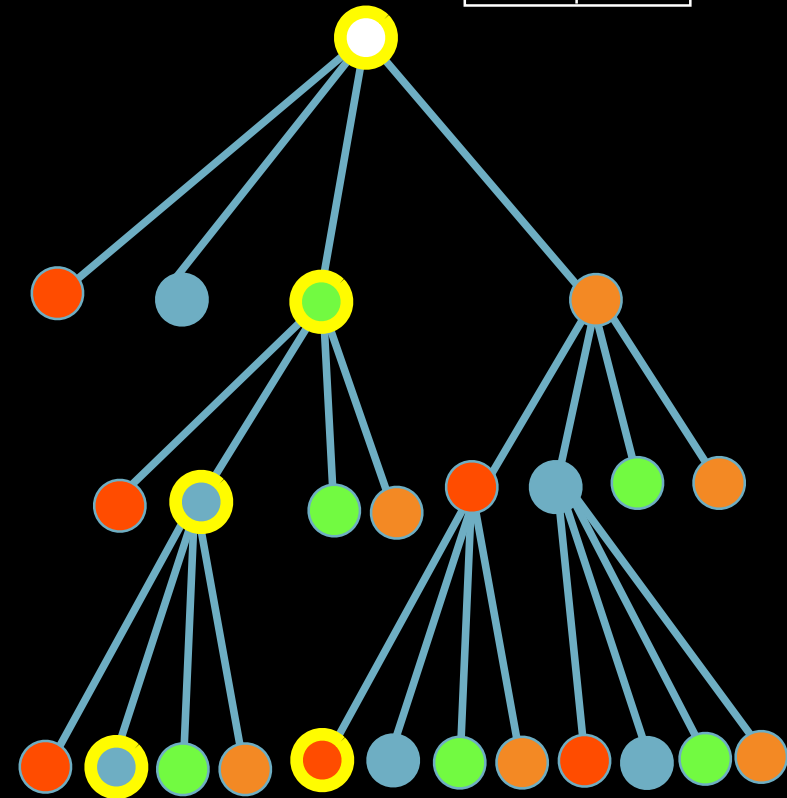
# Busca de Vizinhos (Por Aresta)

Caminho = NE, NE, SO



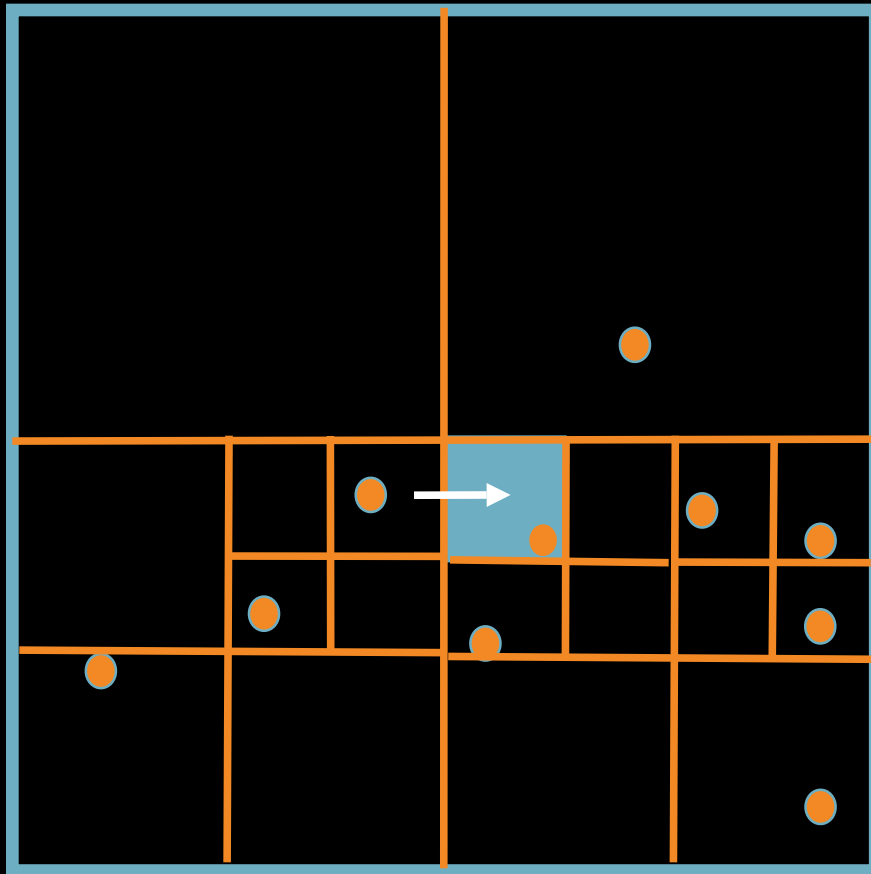
Caminho Reverso = SE, NO

NO	NE
SO	SE



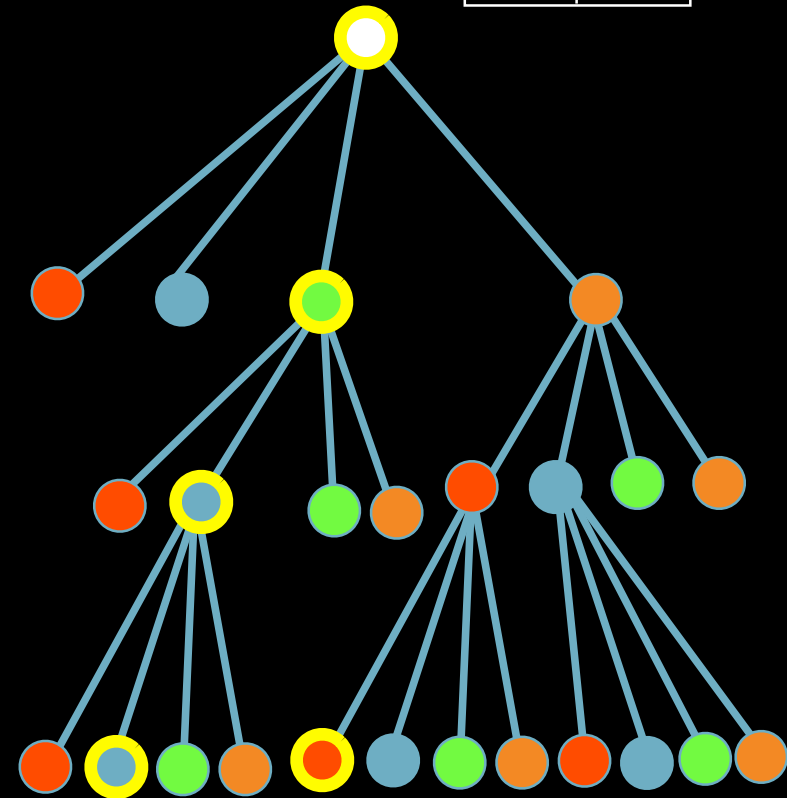
# Busca de Vizinhos (Por Aresta)

Caminho = NE, NE, SO



Caminho Reverso = SE, NO, NO

NO	NE
SO	SE



# Busca de Vizinho por vértice

**PROCEDURE** VizinhoPorVertice(P,I)

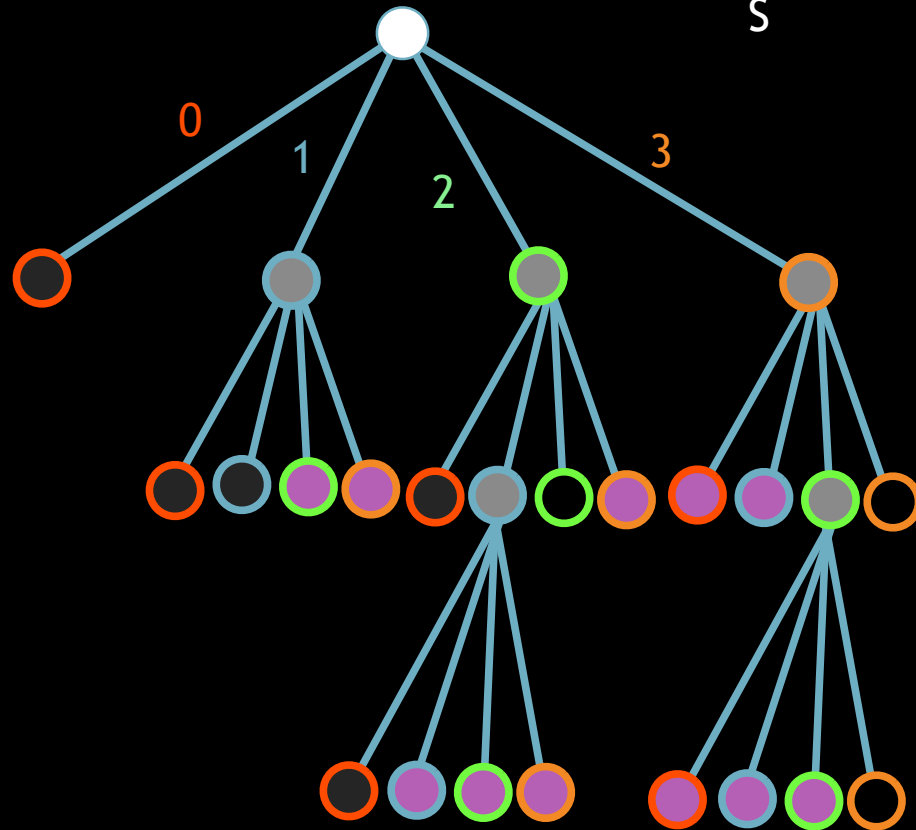
```
1.  RETURN (SON(IF ADJ(I, TIPO(P))  
        THEN VizinhoPorVertice(PAI(P), I)  
        ELSIF ARESTA_COMUM(I, TIPO(P)) != NULL  
        THEN VizinhoPorAresta(  
            PAI(P), ARESTA_COMUM(I, TIPO(P))  
        ELSE PAI(P),  
        REFLECT(I, TIPO(P))));
```

# Representacao Linearizada

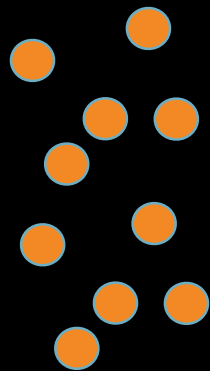
$Q = \{12, 13, 211, 212, 213, 23, 30, 31, 320, 321, 322\}$

0			0	0
			1	1
0	0	1	1	1
	1	1	1	1
0	1	1	1	0
		1	0	

	N		
	0	1	
O	2	3	E
	S		

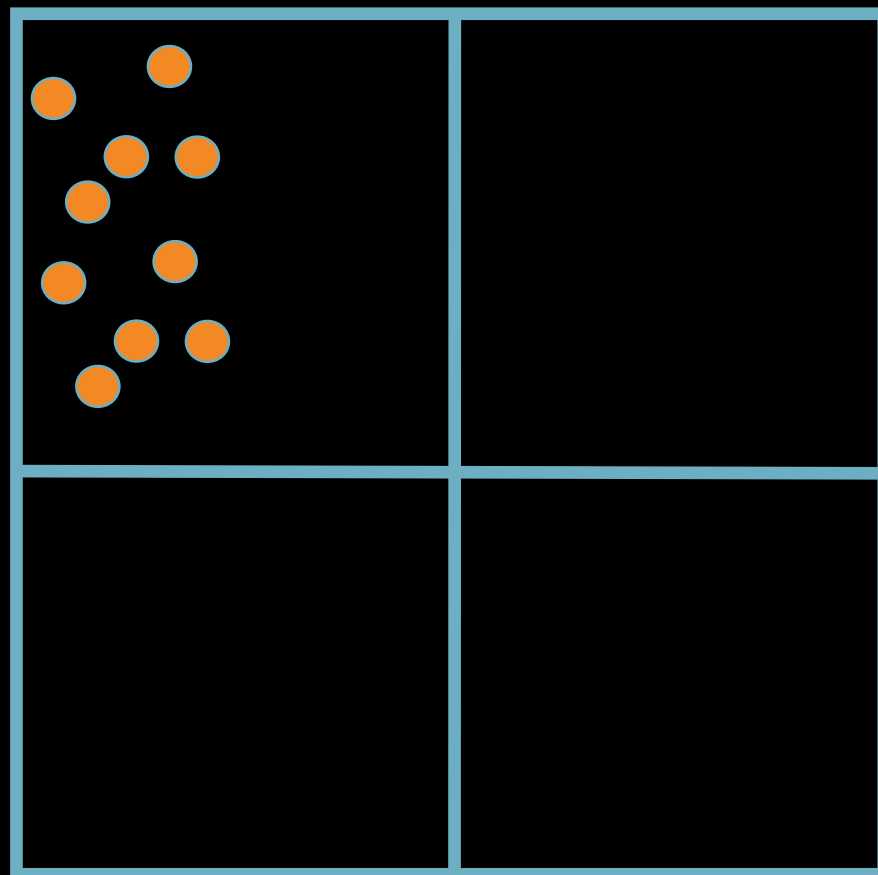


# Achar o dominio inicial

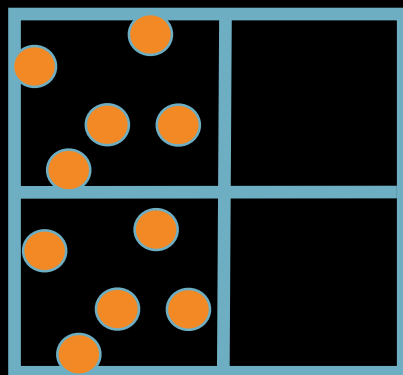




# Achar o dominio inicial

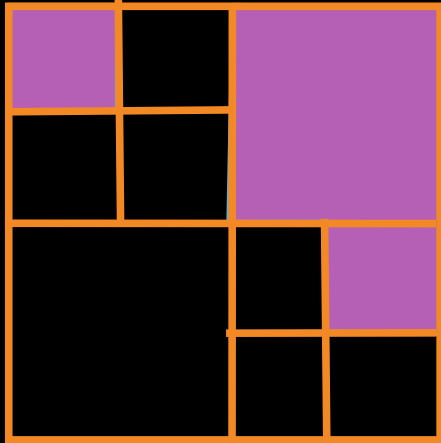


# Achar o dominio inicial

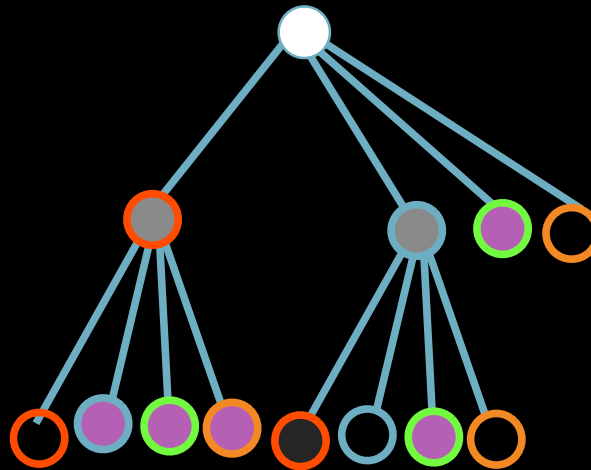
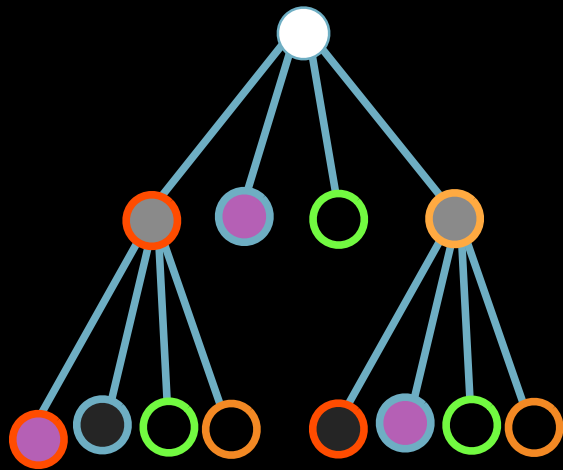
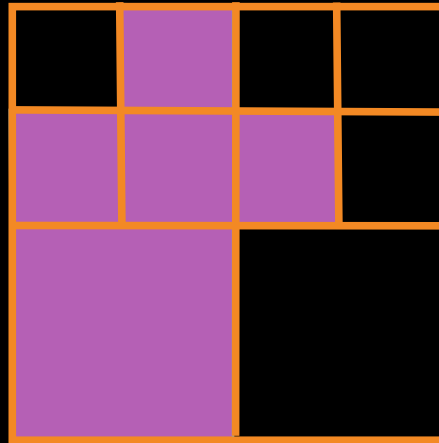


# Operacoes Booleanas

A

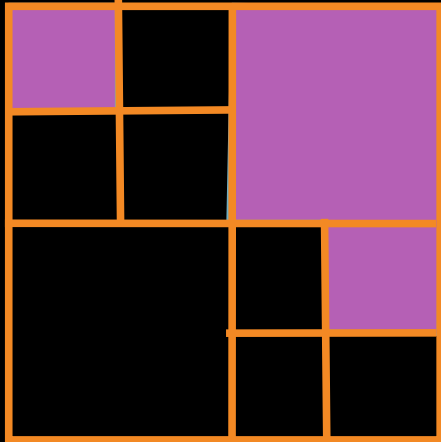


B

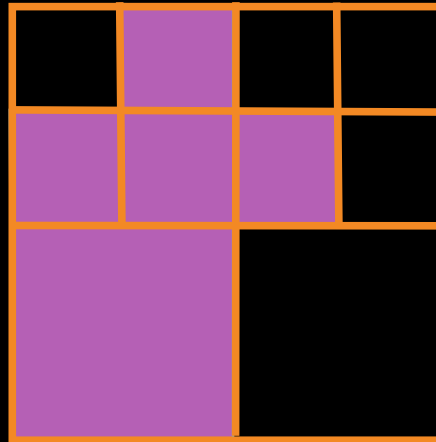


# Operacoes Booleanas

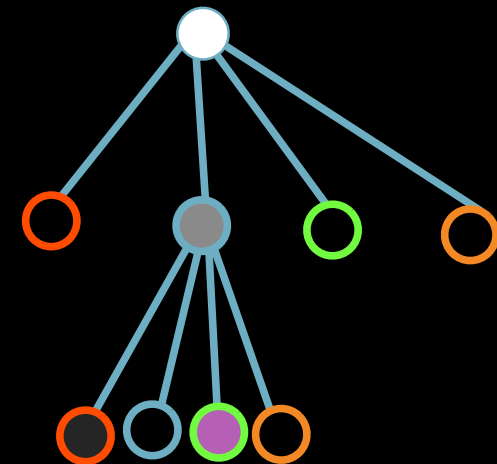
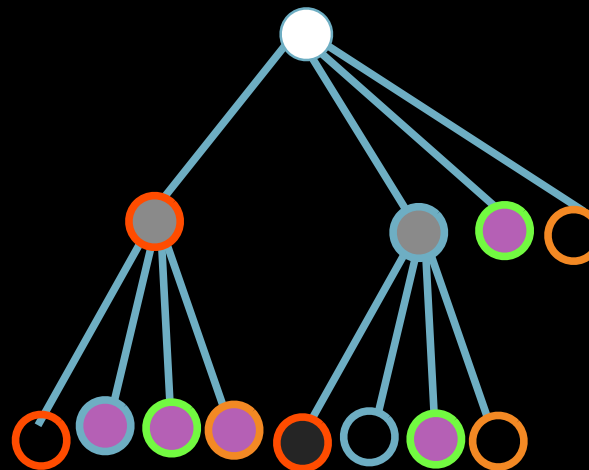
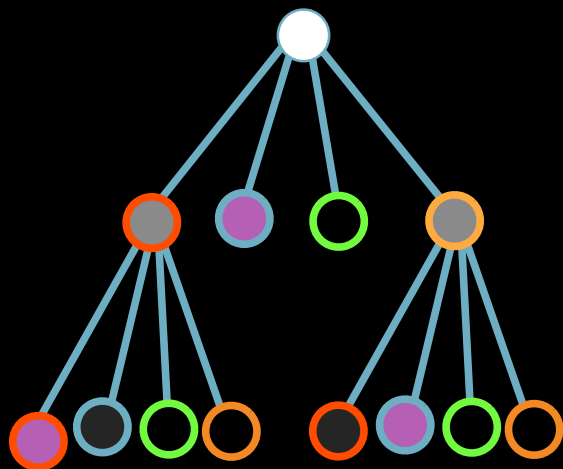
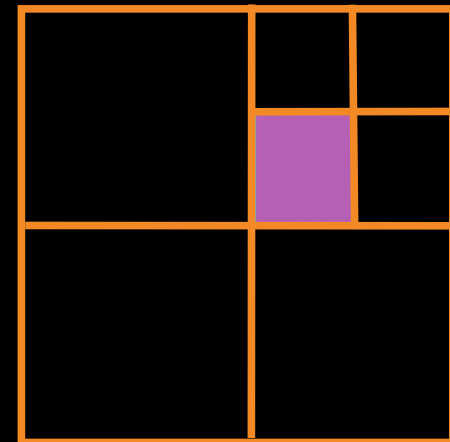
A



B

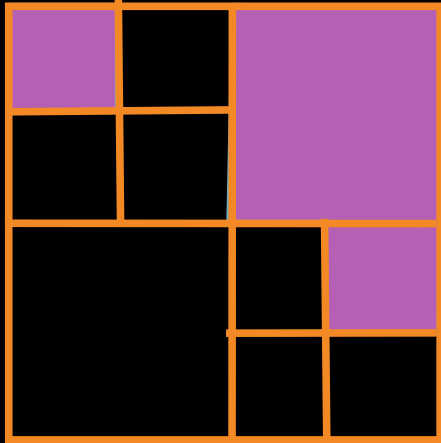


A inter B

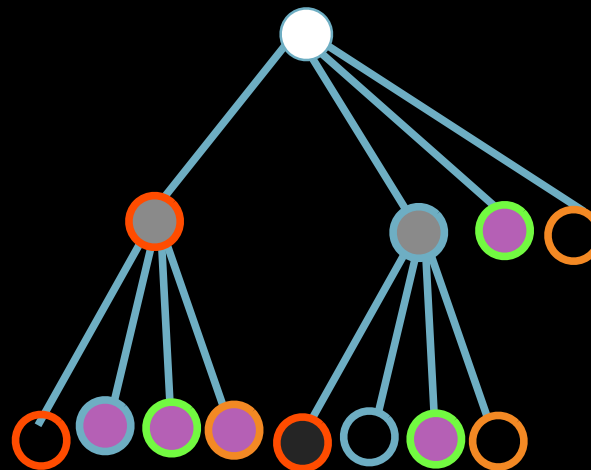
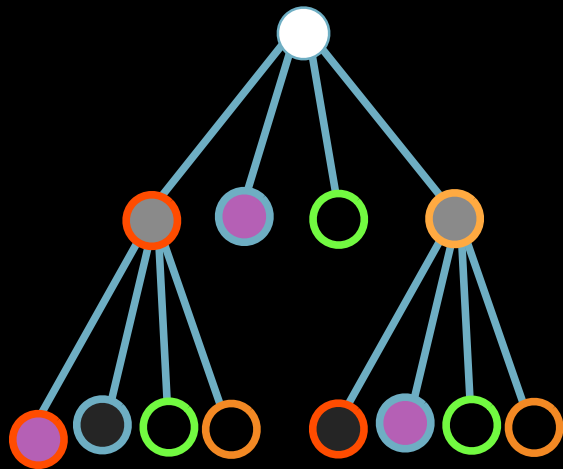
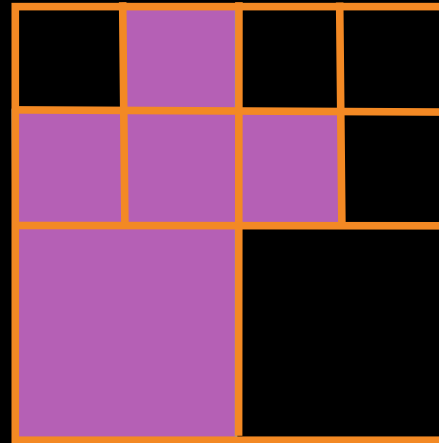


# Operacoes Booleanas

A

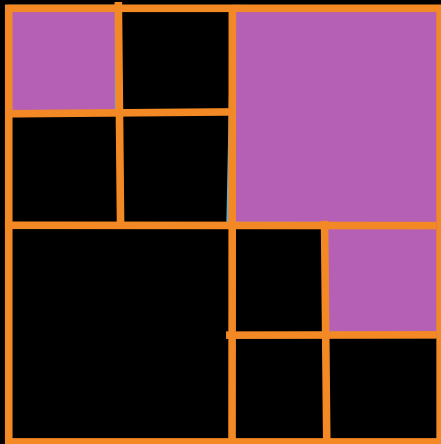


B

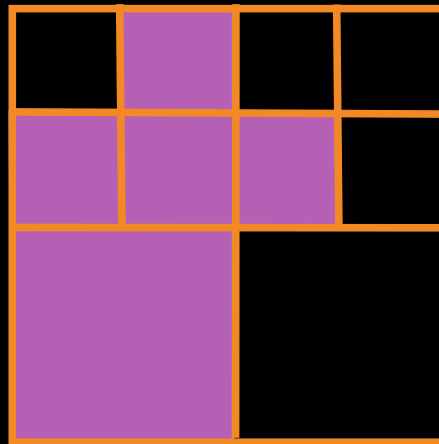


# Operacoes Booleanas

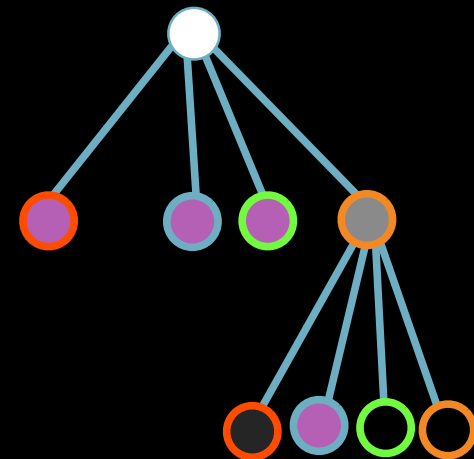
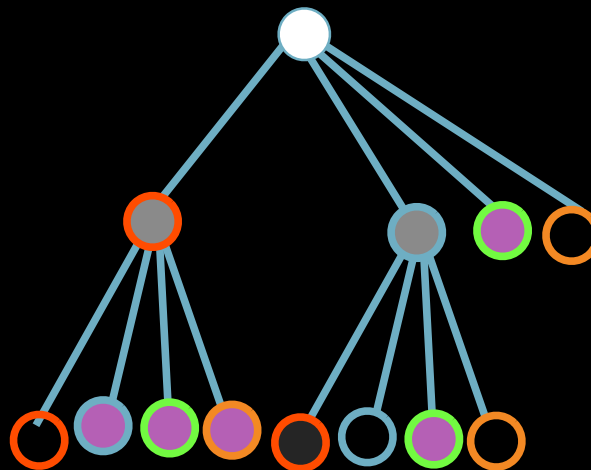
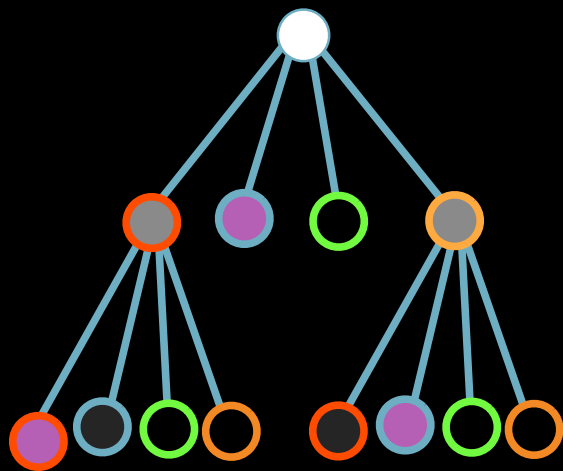
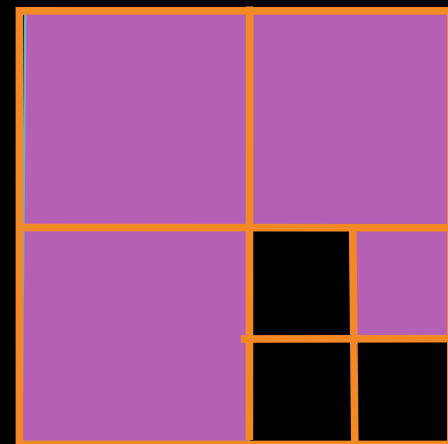
A



B



A uniao B

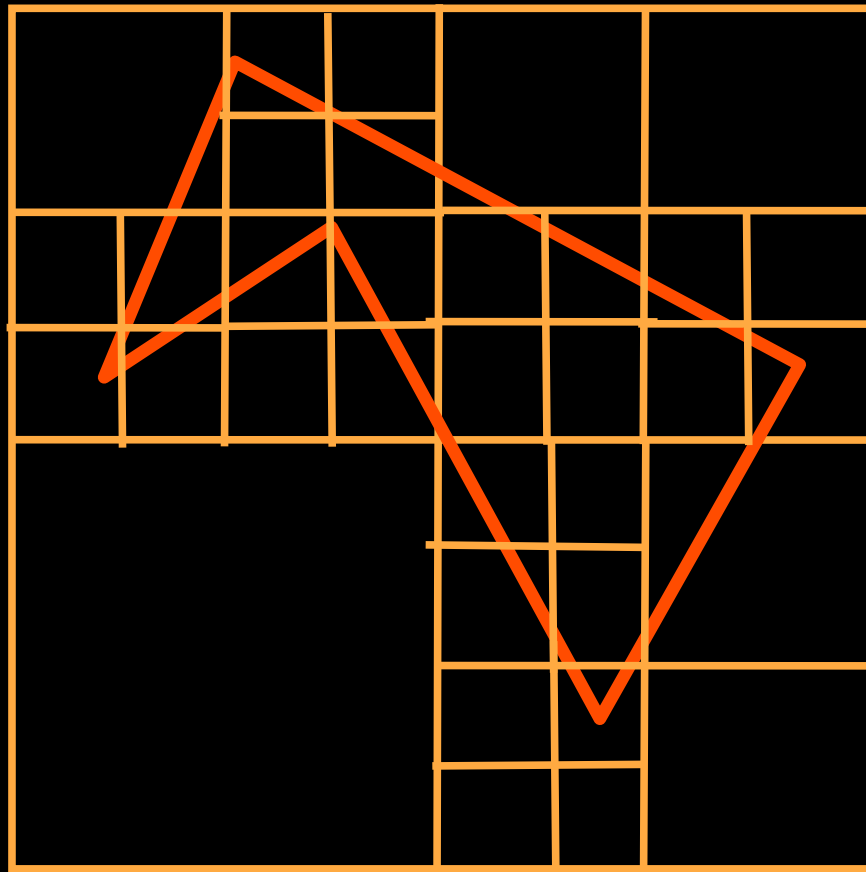


# Operacoes Booleanas

ALGORITMO Intersecao(s,t)

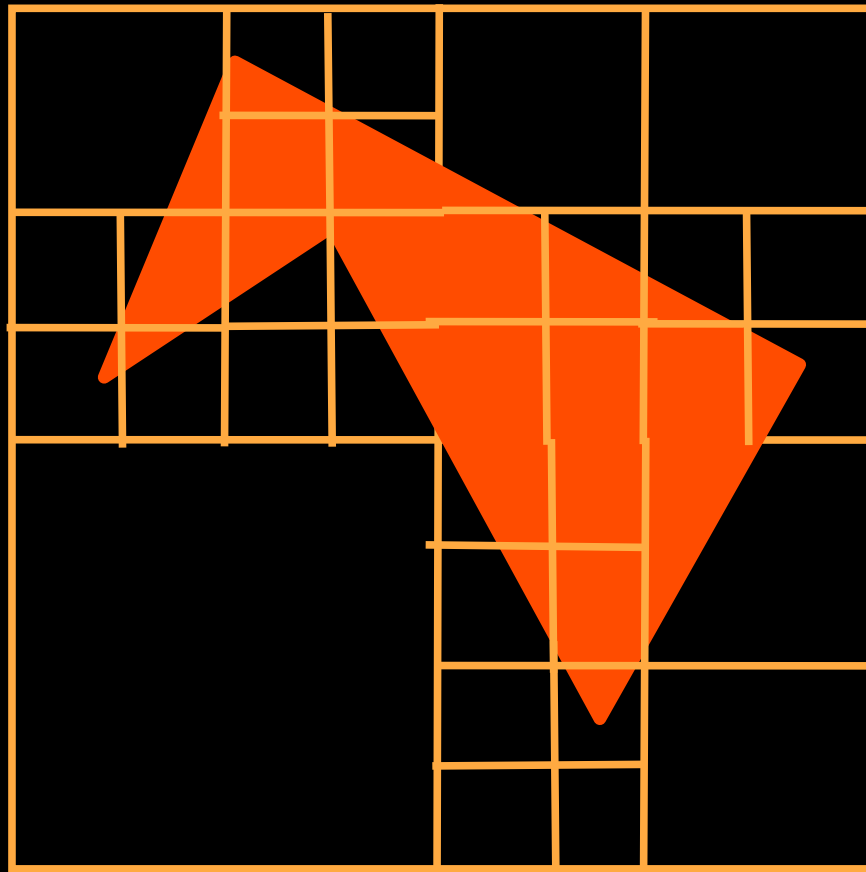
1. IF (VAZIO(S) ou VAZIO(T))
2. THEN RETURN NODO(NULL,NULL,VAZIO)
3. ELSE IF (CHEIO(S)) THEN RETURN COPY\_TREE(t)
4. ELSE IF (CHEIO(T)) THEN RETURN COPY\_TREE(s)
5. ELSE
6.   FOR i=0 TO 3
7.     p[i] = Intersecao(son(s,i),son(t,i));
8.   IF (VAZIO(P[0]) e VAZIO(P[1]) e VAZIO(P[2]) e VAZIO(P[2]))
9.     RETURN NODO(NULL,NULL, VAZIO)
10. ELSE
11.   q = NODO(NULL,NULL, CINZA);
12.   FOR i=0 TO 3
13.     FILHO(q,i) = p[i];
14.     PAI(p[i]) = q;
15.   RETURN q;

# Polygonal Map Quadtrees

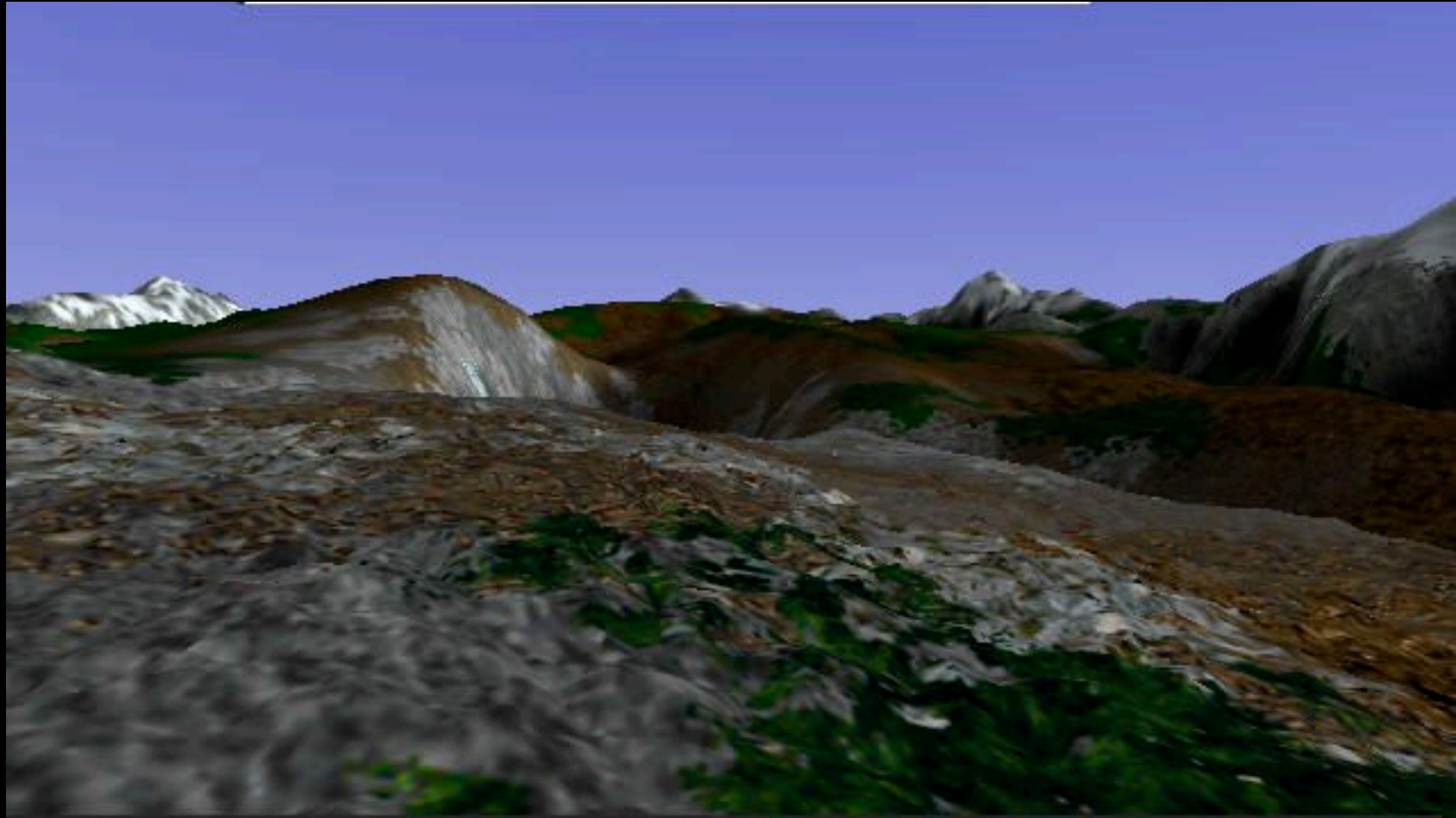


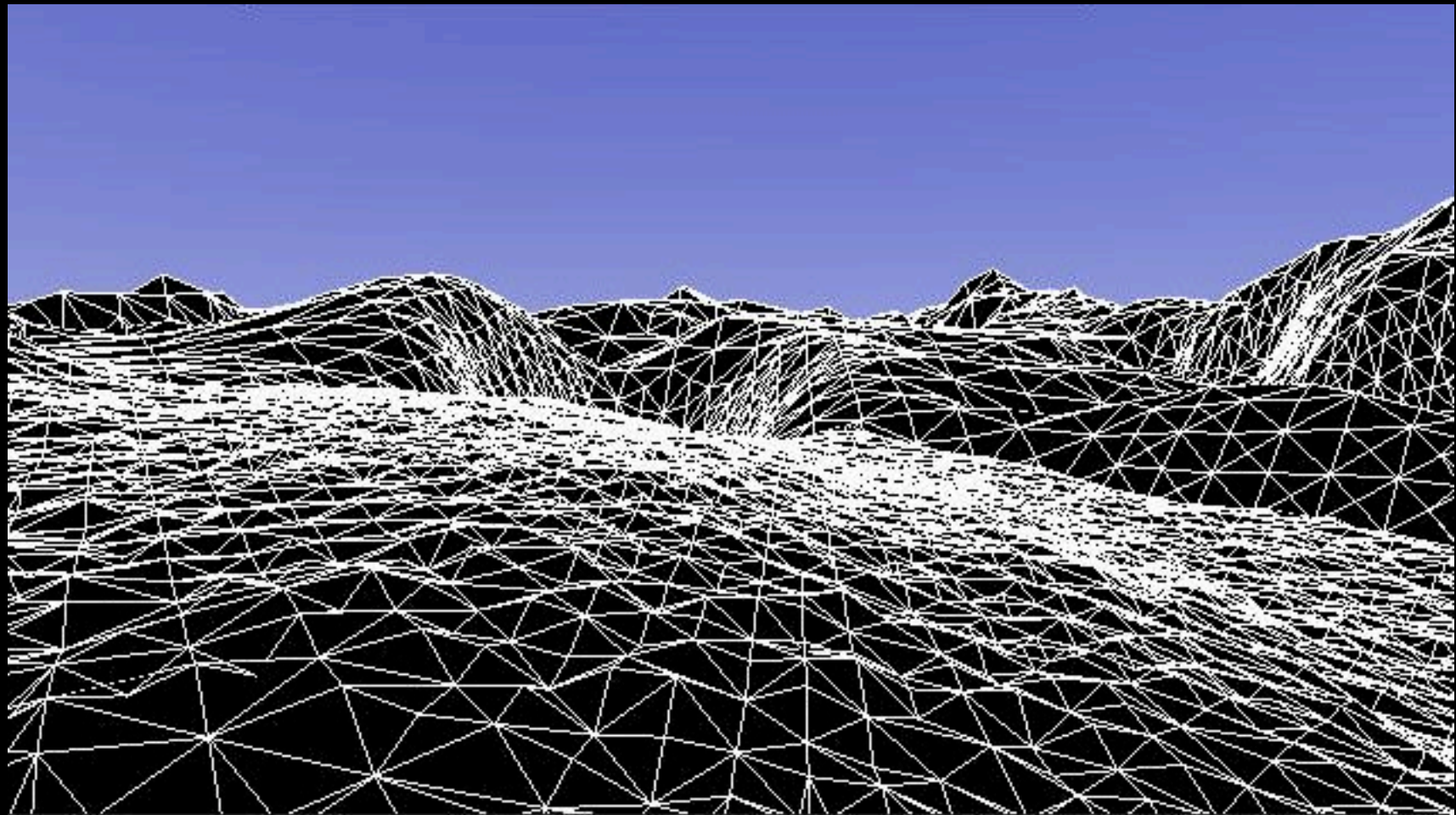


# Region Quadrees



# Simuladores

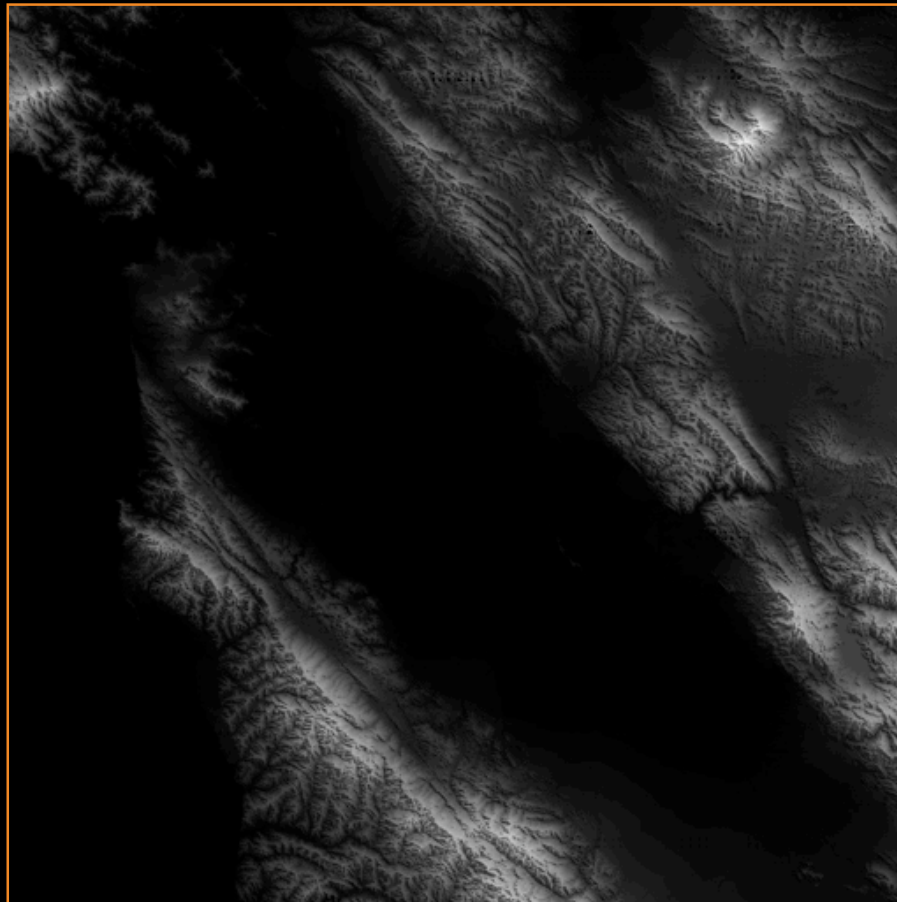




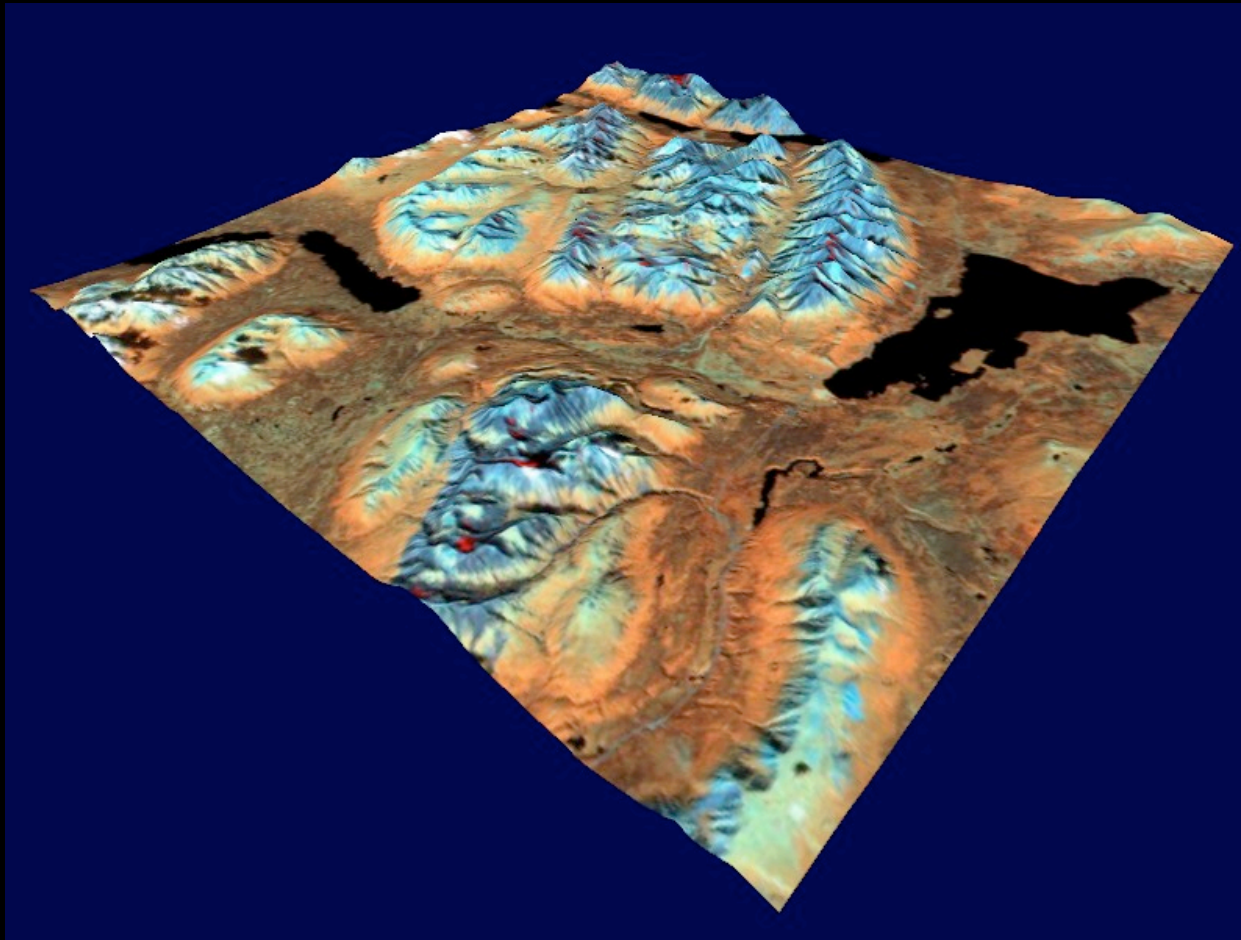


# Representation: Height Fields

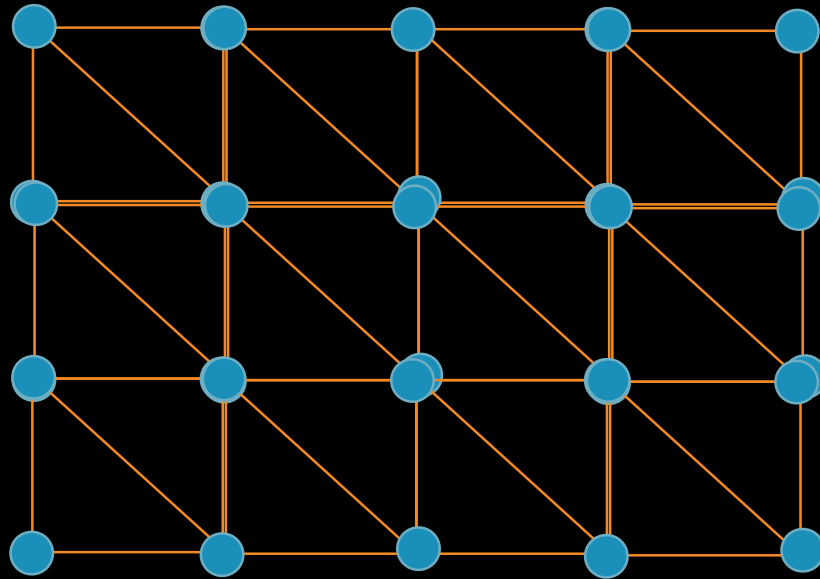
$$w(v) = (x, y, z(x, y))$$



# Height Fields



# Height fields



Brute force

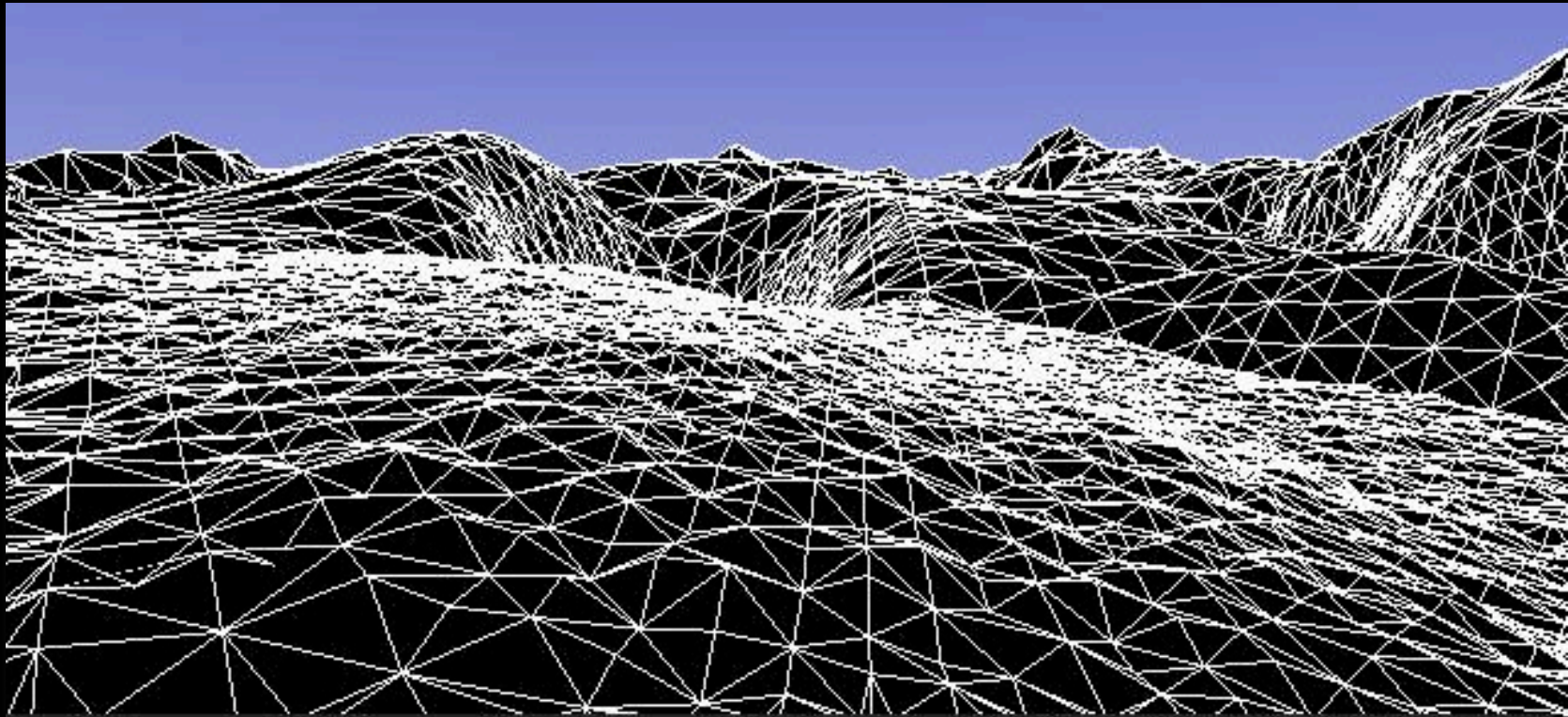
## Basic nature of LOD

**An ideally LOD'd scene: all polygons are roughly the same size in screen pixels.**

**By the nature of projection of 3D space, this means many more polygons are close to you than are far from you.**

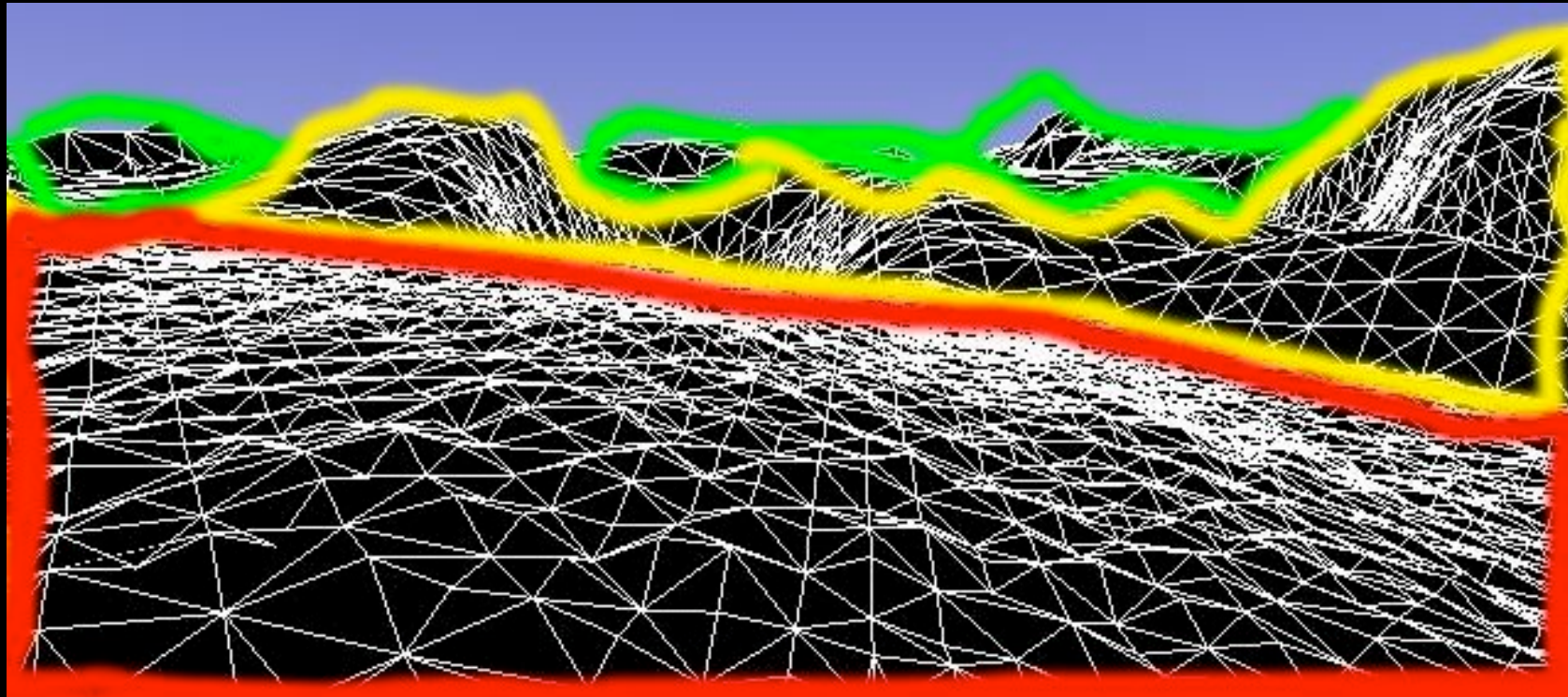


In an ideally LOD'd scene, all polygons are roughly the same size in screen pixels.





A large percentage of polygons  
are small and close (50%? 60%?)



# Terrain engine design goals

**Large terrain that looks good and is detailed**

**Can see forever (no walls of fog)**

**Runs at decent frame rates**

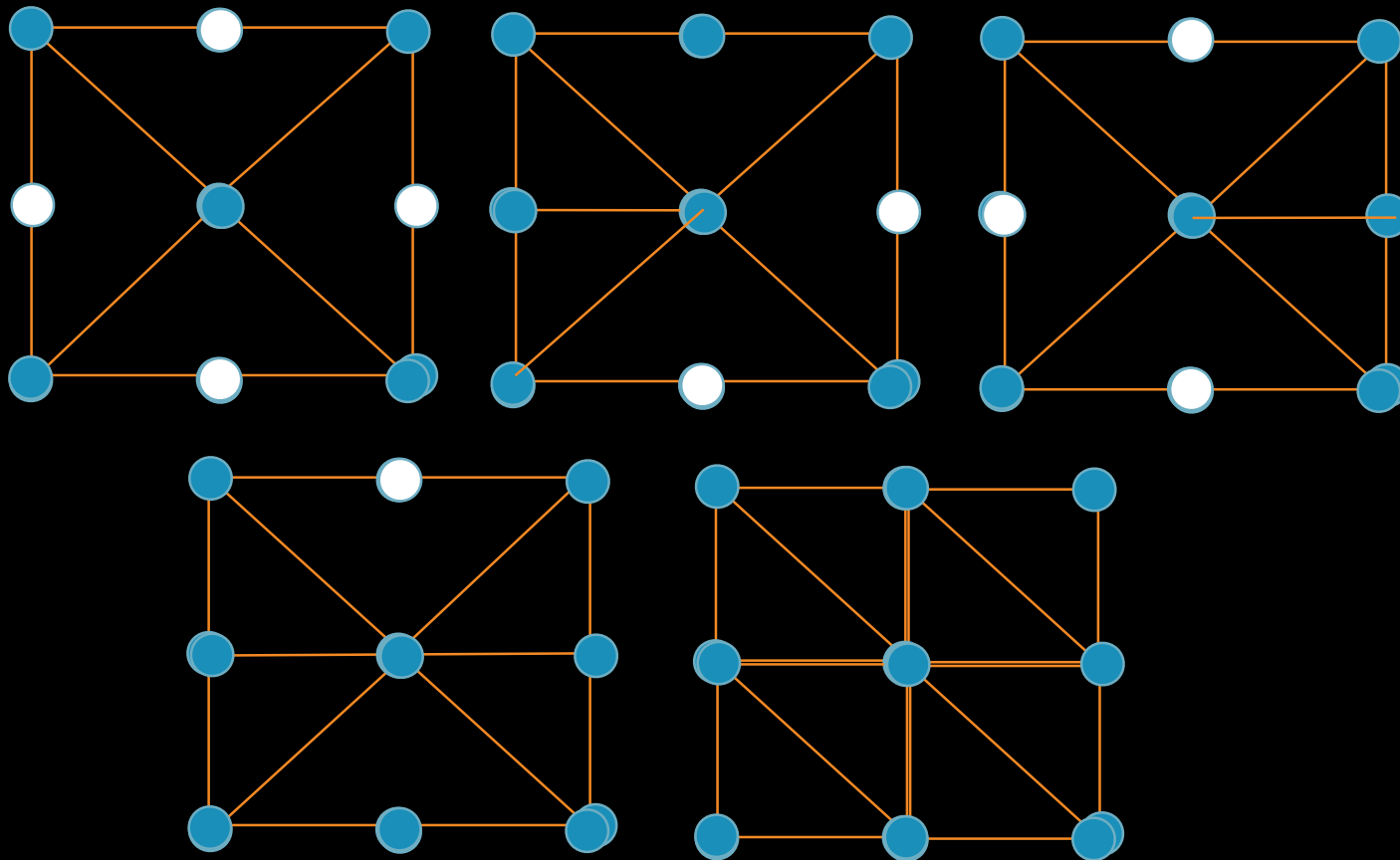
# Lindstrom's algorithm

**First presented at SIGGRAPH '96; paper available on the Web.**

**Bottom-up, works on a height field (elevation map)**

# Lindstrom's algorithm

Choosing which vertices to render

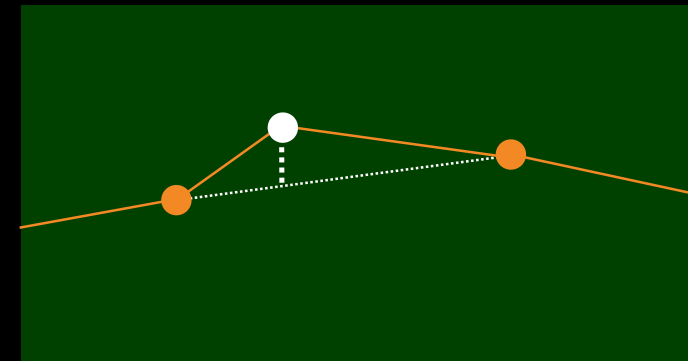
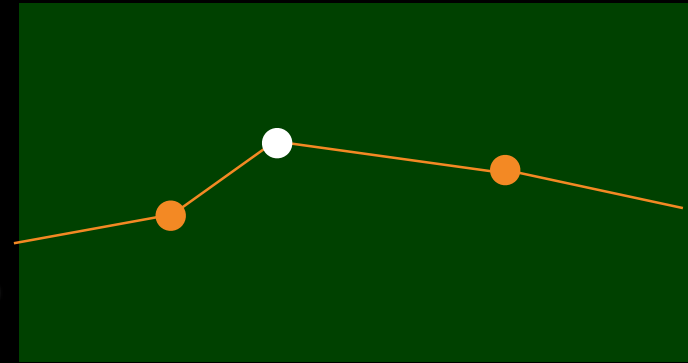


# Lindstrom's algorithm

Each vertex has an associated “error height”

We estimate the size of this height projected to the screen.

If it exceeds some threshold, we “enable” the vertex.

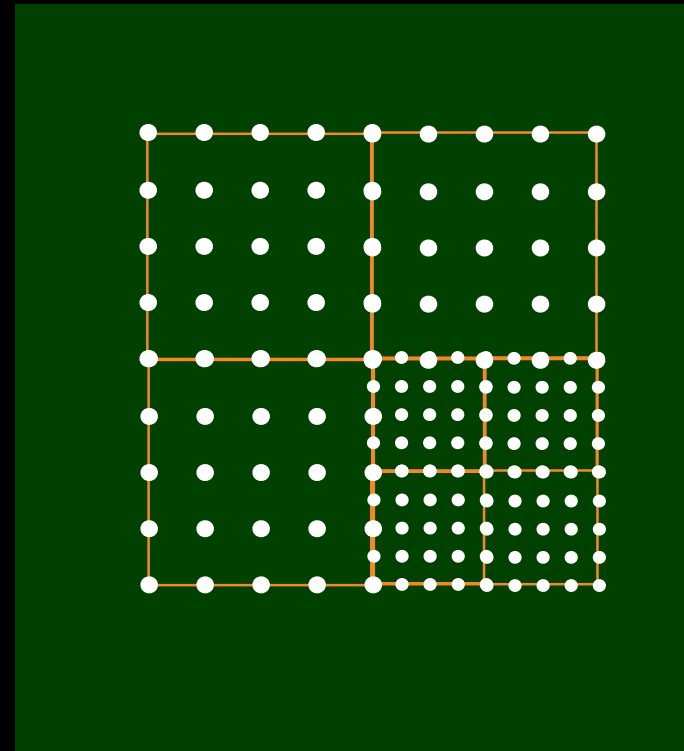


# Lindstrom's algorithm

Vertices are grouped into blocks, sorted by error value.

Frame coherence is used to limit the range of vertices that are tested each frame.

This gives Lindstrom much of its speed.

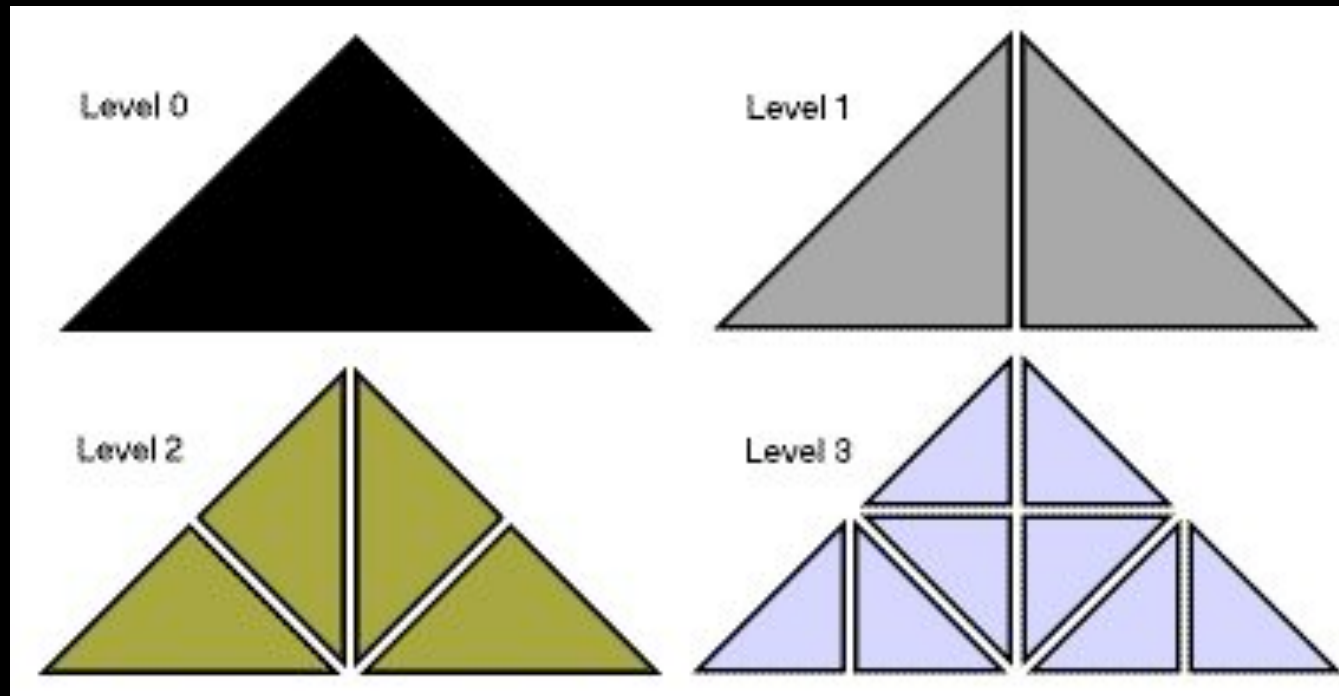


# ROAM algorithm

**Presented at IEEE Visualization '97, paper  
available on Web**

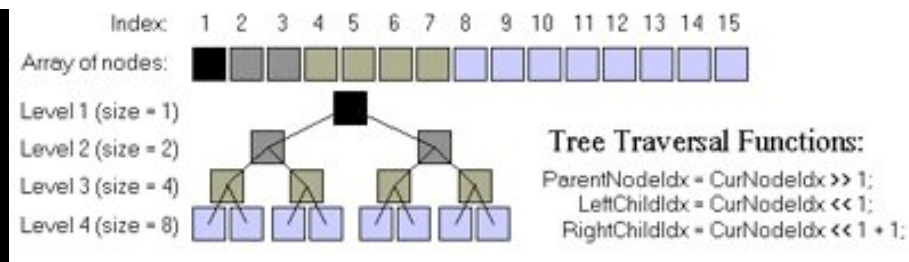
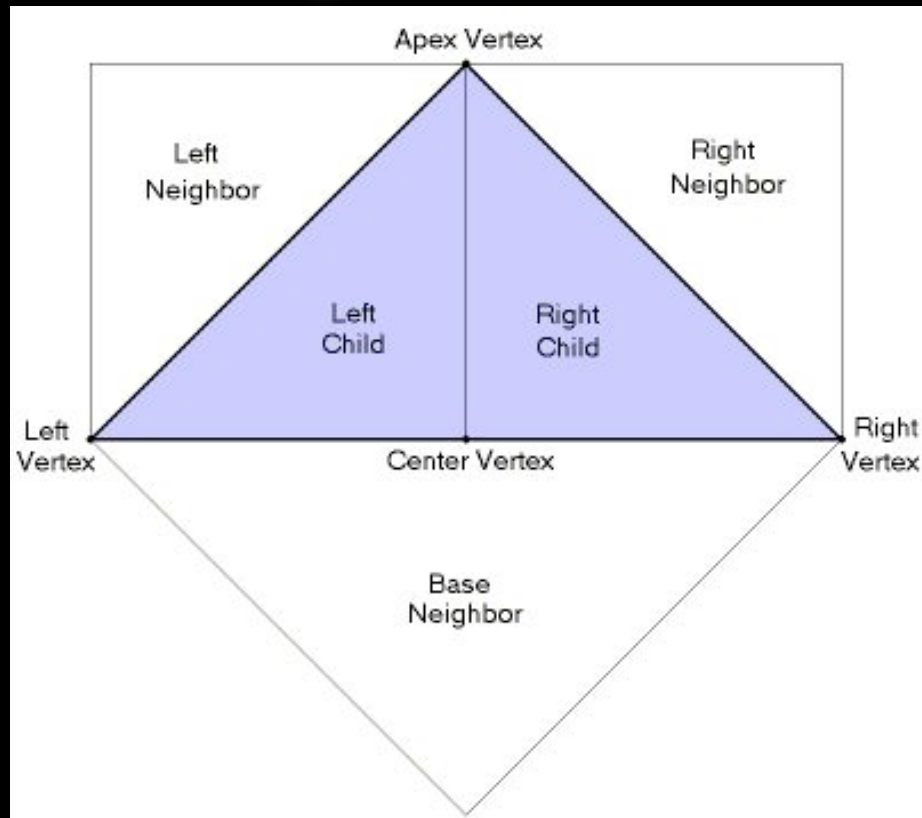
**Top-down; progressively refines bounding  
volumes**

# Triangular Bintree

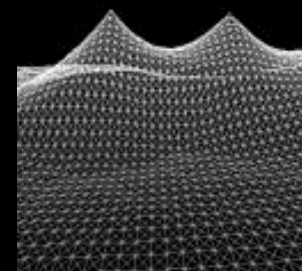
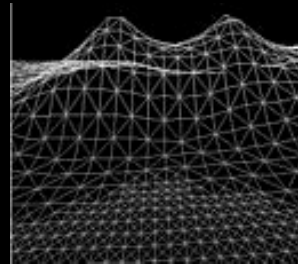
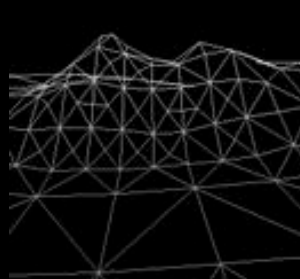
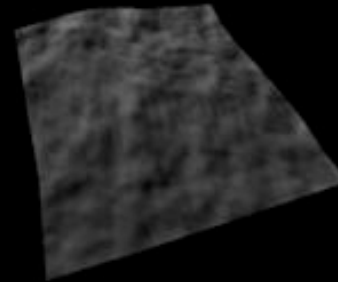
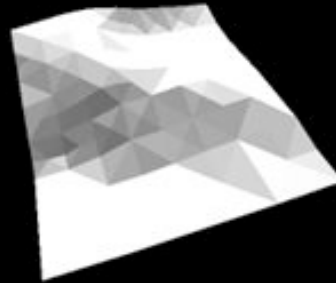
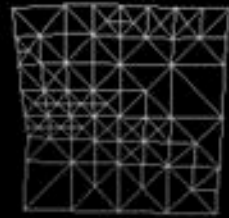




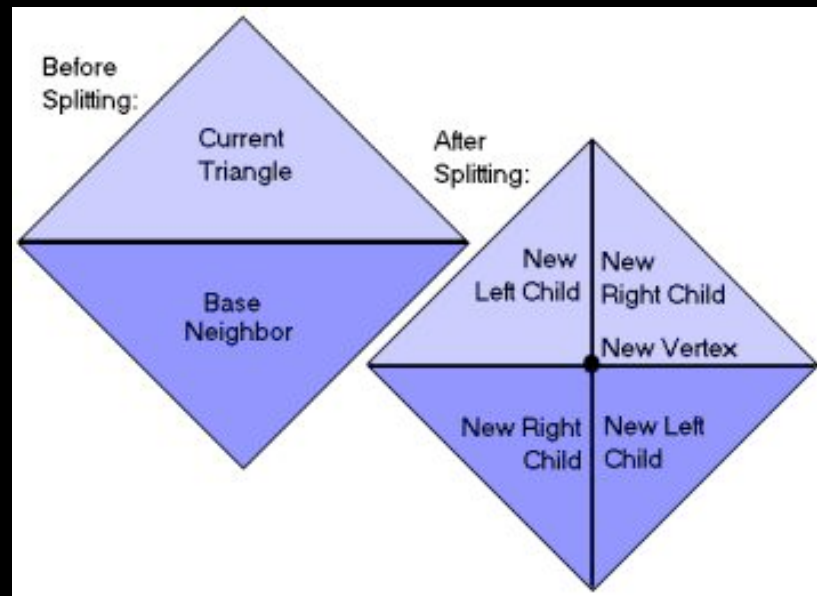
# ROAM algorithm



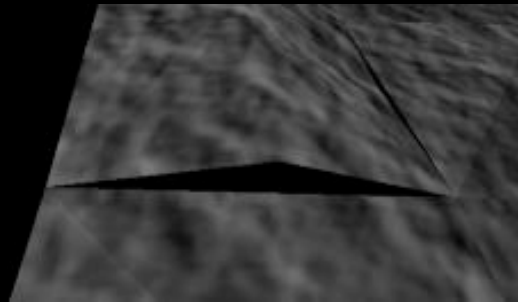
# ROAM algorithm



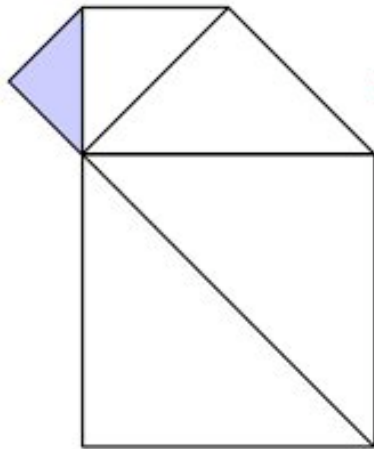
# ROAM algorithm



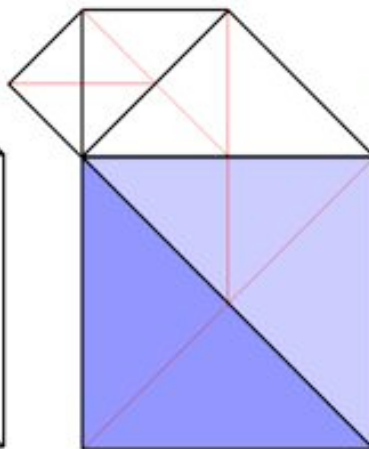
# ROAM algorithm



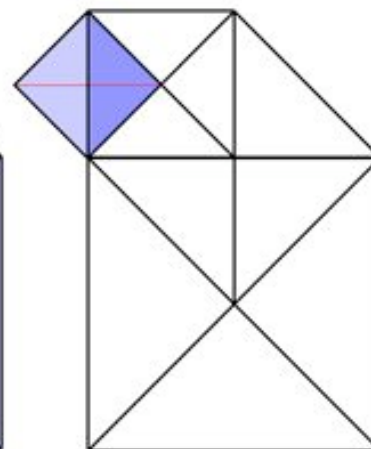
Split operation begins, but current triangle is not part of a diamond.



Recursively force-split the base neighbor until a diamond is found.



Original triangle can now be split.



# ROAM algorithm

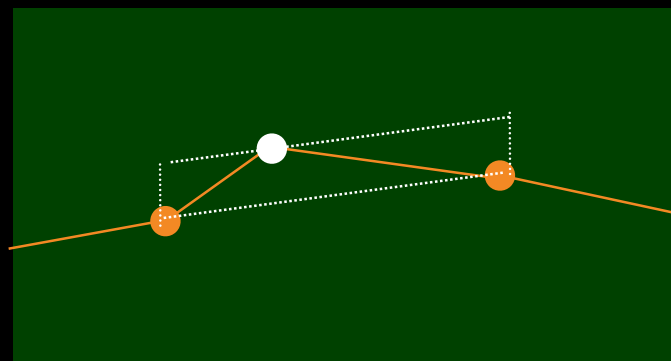
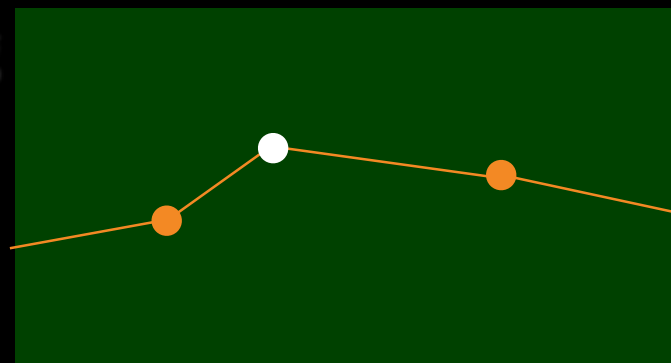
1. Find the highest priority triangle T in the queue
2. Force split T
3. Update the queue by removing T and other split triangles
4. Add any new triangles to the queue

# ROAM algorithm

The thickness of each bounding volume, projected to the screen, controls when it is subdivided

No block structure

These bounding volumes are prioritized; priorities decay as the viewpoint moves.



# Metrics

- Backface detail reduction
- Normal distortions
- Texture-coordinate distortion
- Silhouette edges
- View Frustum
- Atmospheric Obscurance
- Object Positioning