EEC 686/785 Modeling & Performance Evaluation of Computer Systems

Lecture 6

Wenbing Zhao

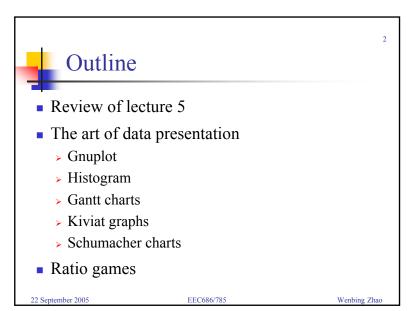
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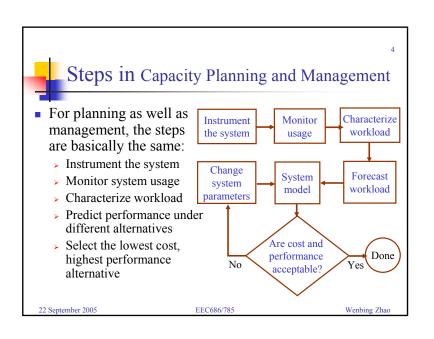


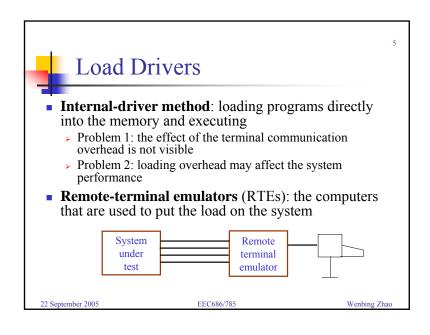
Terminology

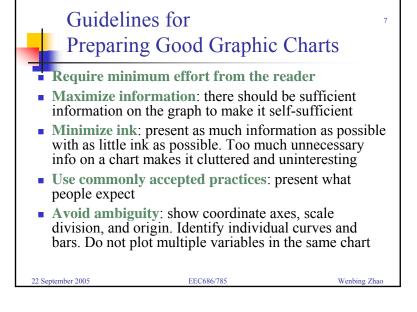
- Capacity planning: ensuring that adequate computer resources will be available to meet the future workload demands in a cost-effective manner while meeting the performance objectives
- Capacity management: ensuring that the currently available computing resources are used to provide the highest performance
- Capacity management is concerned with the present while capacity planning is concerned with the future
- **Benchmarking**: to compare the performance of two competing systems in an objective manner, benchmarks are run on these systems using automatic load drivers

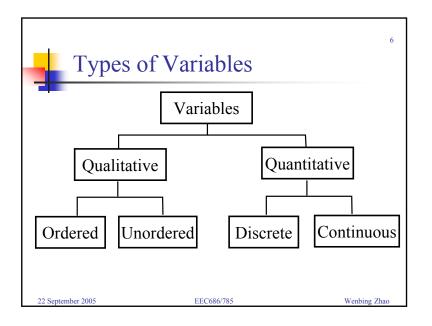
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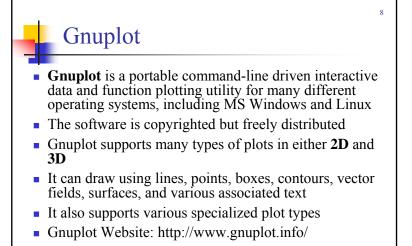












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Histogram

- A histogram is defined as a bar graph that shows frequency data
- Differences between histograms and bar graphs
 - > Think of histograms as sorting bins
 - Given one variable, sort data by this variable by placing them into "bins"
 - Then count how many pieces of data are in each bin. The height of the rectangle on top of each bin is proportional to the number of pieces in that bin

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Histogram

- Bar graphs show the comparison of several measurements of different items
- The main question a histogram answers is: "How many measurements are there in each of the classes of measurements?"
- ➤ The main question a bar graph answers is: "What is the measurement for each item?"

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Gantt Charts

- Gantt chart can be used to show the relative duration of any number of Boolean conditions, i.e., conditions that are either true or false
 - A resource being used or being idle is an example of a Boolean condition
 - Each condition is shown to be a set of horizontal line segments
 - The total length of the line segments represents the relative duration of the condition
 - The position of various segments is arranged such that the overlap between different lines represents the overlap between the conditions

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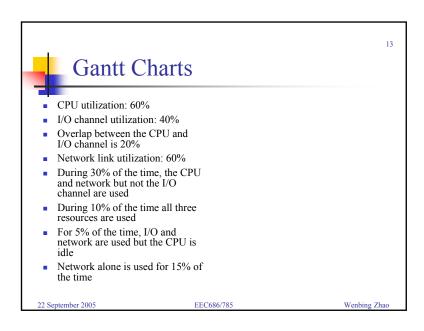


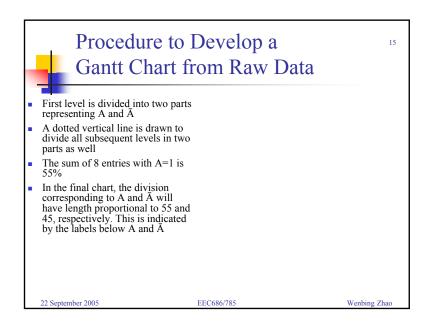
Gantt Charts

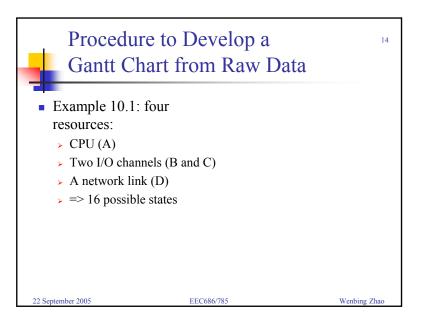
- Gantt chart is particularly useful to show the utilization profiles of the overlap among different resources
 - > Any resource whose utilization is too high is a bottleneck and may degrade the performance
 - > A resource with very low utilization represents inefficiency in the system
 - The overlap of utilization of different resources is a good thing

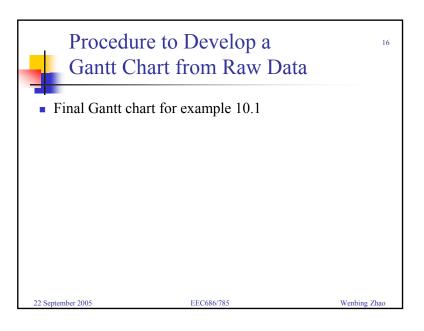
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Kiviat Graphs

- Kiviat graph: a circular graph in which several different performance metrics are plotted along radial lines
 - In the most popular version of the graph, an even number of metrics are used.
 - > Half of these metrics are HB metrics so that a higher value of the metrics is considered better.
 - > The other half of the metrics measure are LB metrics, and a lower value is considered better
 - > Kiviat graph for an ideal system is star

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Example 10.2

- Eight different metrics
 - > **Any channel busy** a HB metric
 - ➤ **CPU wait** CPU waiting for I/O completion, resource is wasted, an LB metric
 - > CPU in problem state indicates time used executing the user's program, a HB metric
 - > CPU in supervisor state indicates the time spent executing the operating system code, an LB metric

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Example 10.2

- Eight different metrics
 - CPU busy percentage of time CPU busy, i.e., CPU utilization, a HB metric (the resource is being used and not wasted)
 - ➤ **CPU only busy** percentage of time CPU only is busy, measures the fraction of time when only the CPU is used and none of the I/O channels are used, an LB metric
 - ➤ CPU/channel overlap measures the percentage of time the CPU is busy along with at least one I/O channel, a HB metric
 - ➤ Channel only busy measures the time when the channel is being used but the CPU is idle. The CPU must be waiting for the I/O, an LB metric

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Example 10.2

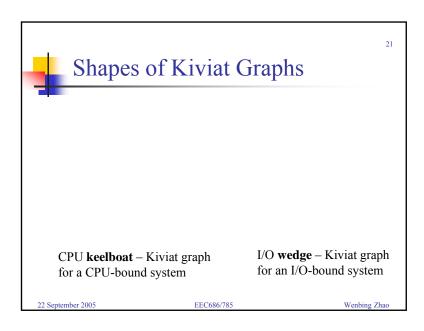
- Kiviat graph for a balanced system
- Problem with this set of metrics: only 4 independent metrics
 - > CPU busy = problem state + supervisor state
 - ➤ CPU wait = 100 CPU busy
 - ➤ Channel only = any busy CPU/channel overlap
 - ➤ CPU only = CPU busy CPU/channel overlap

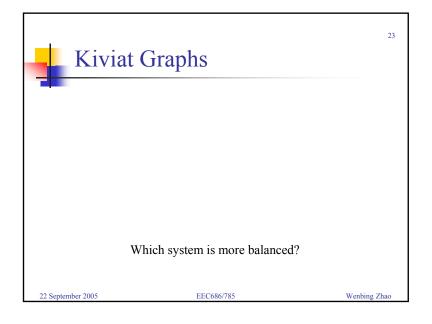
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Shapes of Kiviat Graphs

I/O **arrow** – Kiviat graph for a CPU- and I/O-bound system

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Figure of Merit

- The square root of the area of the reversed Kiviat graph can be used to compare the overall goodness of systems
- Consider a Kiviat graph with 2n axes.
 - > Let the percentage of performance values for a system be $\{x_1, x_2, ..., x_{2n}\}$, where odd values $x_1, x_3, ..., x_{2n-1}$ represent good metrics and the even values represent bad metrics
 - \rightarrow All x_i 's are percentages and lie between 0 and 100
 - > Figure of Merit (FOM) is computed as follows:

$$FOM = \left[\frac{1}{2n}\sum_{i=1}^{n} (x_{2i-1} + x_{2i+1})(100 - x_{2i})\right]^{1/2}$$

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Example 10.3

System	x_1	x_2	x_3	x_4	<i>x</i> ₅	x_6	x_7	x_8
A	100	60	40	0	40	0	40	60
В	70	30	40	30	70	30	40	30

$$FOM_A = \left[\frac{1}{8} \{ (100 + 40)(100 - 60) + (40 + 40)(100 - 0) + (40 + 40)(100 - 0) + (40 + 100)(100 - 60) \} \right]^{1/2}$$

$$= \left[(5600 + 8000 + 8000 + 5600) / 8 \right]^{1/2} = \sqrt{28200/8} = 58$$

$$FOM_B = \left[\frac{1}{8} \{ (70+40)(100-30) + (40+70)(100-30) + (70+40)(100-30) + (40+70)(100-30) \} \right]^{1/2}$$
$$= \left[(7700+7700+7700+7700)/8 \right]^{1/2} = \sqrt{30800/8} = 62$$

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Application of Kiviat Graphs

 Most of the literature on Kiviat graphs is on data processing systems

 Kiviat graph can be extended to networks, databases, and other types of computer systems

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Application of Kiviat Graphs

Schumacher Charts

- Schumacher Chart: another reporting format to show daily, weekly, monthly, quarterly, or yearly resource usage
- Any number of performance metrics can be plotted in tabular form
- The values are normalized with respect to the long-term mean and standard deviation
- Any observations that are beyond the mean plus or minus one standard deviation need to be explained

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Decision Maker's Games

- Even if the performance analysis is correctly done and presented, it may not be enough to persuade your audience – the decision makers – to follow your recommendations
- Reasons for rejection:
 - > The problem needs more analysis
 - Workload/metrics/configuration/deta is always based on past measurements, their applicability to the current or future environment can always be questioned

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Ratio Games

- Take an average of each individual system's performance and then take a ratio
- Normalize each system's performance on each workload by that of system A and then take an average of ratios
- Normalize each system's performance on each workload by that of system B and then take an average of ratios

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Ratio Games

- Ratios provide good opportunities for playing performance games with competitors
- Ratios have a *numerator* and *denominator* (base)
- Two ratios with different bases are not comparable
- However, many examples in published literature where computer scientists have knowingly or unknowingly compared ratios with different bases
- Ratio game: the technique of using ratios with incomparable bases and combining them to one's advantage

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Example of Ratio Games

- Ratio of totals: 6502 is worse. It takes 4.7% more time
- With 6502 as a base: 6502 is better (1% more time)
- With 8080 as a base: 6502 is worse (6% more time)

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Example of Ratio Games

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• Sum: Z8002 requires 9% less code than RISC-I

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Example of Ratio Games

RISC-I as base: Z8002 has 18% more code than RISC-I

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Using an Appropriate Ratio Metric

 Another form in which ratio games are used to show better performance is by choosing a suitable performance metric which is a ratio of two different metrics

Network	Throughput	Response	
A	10	2	
В	4	1	

Network	Throughput	Response	Power
A	10	2	5
В	4	1	4

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Using Relative Performance Enhancement

If the performance metric is already specified, it is possible to show that relative increase in the performance is better using one type of enhancement than another *provided the two are tried on different machines* (correct way to compare is to try on the same machine)

Alternative	Without	With	
Floating-point accelerator A on X	2	4	
Floating-point accelerator B on Y	3	5	

Alternative	Without	With	Ratio
A on X	2	4	2.00
B on Y	3	5	1.66

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Ratio Games with Percentages

- Percentages are basically ratios. They allow playing ratio games in ways that do not look like ratios
- Example 11.3. =>
- In fact, neither comparison used compatible bases:
 - > (a) number of tests used in each test as base
 - > (b) number of tests combined as base

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Ratio Games with Percentages

- Other ways to misuse percentages
 - > They can be used to have a psychological impact on the reader.
 - For example, 1000% improvement in performance sounds more impressive than an 11-time improvement
 - This is particularly useful when the performance before the improvement and the absolute increase in the performance are not impressive

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Ratio Games with Percentages

- Other ways to misuse percentages
 - > Small sample sizes can be neatly disguised by specifying the percentage.
 - Saying that 83.3% of the universities in town use system
 X is more impressive than saying that 5 out of 6
 universities use the system
 - ▶ The base in the percentage should be the initial value
 - The memory prices have gone done 400% as if they are now paying you to buy memory it should be the current price is 1/5 of the original

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Strategies for Winning a Ratio Game

 If one system is better on all benchmarks, contradicting conclusion cannot be drawn by any ratio game technique

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Strategies for Winning a Ratio Game

- Even if one system is better than the other on all benchmarks, a better relative performance can be shown by selecting the appropriate base
 - ➤ In table 11.9, A is 40% better than B using raw data, 43% better using A as base, 42% better using B as base
 - A designer would prefer to use the raw-data averages

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Strategies for Winning a Ratio Game

- If one system is better on some benchmarks and worse on others, contradicting conclusions can be drawn in some cases
 - The easiest way to verify whether a contradictory conclusion can be drawn for a particular data set is to try all possible bases
 - > The next several rules may help select the base

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Strategies for Winning a Ratio Game

- If the performance metric is an LB metric, it is better to use your system as the base
 - The execution time is an LB metric, and as shown in table 11.9, system A designers would be better off using system A as the base. B designers would prefer to use B as the base

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- If the performance metric is an HB metric, it is better to use your opponent as the base
 - > The throughputs, efficiency, MPS, and MFLOPS are examples of HB metrics
 - A higher average ratio would be obtained for A if B is used as a base

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Strategies for Winning a Ratio Game

- Those benchmarks that perform better on your system should be elongated and those that perform worse should be shortened
 - > The time duration of the benchmarks is often adjustable
 - > For example, in Sieve benchmark, the number of prime numbers to be generated can be set by the experimenter
 - > Elongating a benchmark in effect increases the weight on the favorable benchmark

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Derivation of the Rules

Assume the performance metric is an HB metric.

Consider the case of two systems A and B on two benchmarks I and J etc. as shown in table 11.10

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Derivation of the Rules

• Using raw data, A is better if and only if:

$$y < -\frac{a}{b}x + \frac{a+b}{b}$$

• Using A as base, A is considered better if and only if:

$$y < 2 - x$$

• Using B as base, A is considered better if and only if:

$$y < \frac{x}{2x-1}$$

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Derivation of the Rules

 This explains why it is better to use your opponent's system as base for HB metric

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Correct Analysis

- The main reason why the analysis of ratios results in contradicting results is that the approach of taking a mean of the ratio is wrong
- The approach completely ignores the fact that the performance is affected by several factors and by experimental errors
- A statement about one factor can be made only if the effects of different factors and errors are first isolated
- The isolation requires developing a model of the way these factors and experimental errors interact with each other
- Techniques for this require knowledge of several probabilistic, statistical, and experimental design concepts

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