

1. A tank contains 8733 lbs of water at room temperature. How many hours would it take to empty the tank if a pump removes 2.5 gallons of water from the tank every minute.

First, let's figure out how many gallons of water we have.

$$V = \frac{w}{\gamma} = \frac{8733 \text{ lb}}{62.21 \text{ lb/ft}^3} = 140.4 \text{ ft}^3 \times \left(\frac{7.48 \text{ gal}}{\text{ft}^3} \right) = 1050 \text{ gal}$$

If we remove 2.5 gallons of water every minute it would take

$$(1050 \text{ gal}) / (2.5 \text{ gal/min}) = 420 \text{ min} \times \left(\frac{1 \text{ hr}}{60 \text{ min}} \right) = 7 \text{ hr}$$

2. If 400 L/min of fluid flows through a DN 50 Schedule 80 steel pipe what is the resulting average velocity (in m/s) of flow?

$$A_{\text{flow}} = 1905 \text{ mm}^2 = 1.905 \times 10^{-3} \text{ m}^2$$

$$Q = 400 \text{ L/min} \times \frac{1 \text{ m}^3/\text{s}}{60,000 \text{ L/min}} = 6.67 \times 10^{-3} \text{ m}^3/\text{s}$$

$$v = \frac{Q}{A_{\text{flow}}} = \frac{6.67 \times 10^{-3} \text{ m}^3/\text{s}}{1.905 \times 10^{-3} \text{ m}^2} = 3.5 \text{ m/s}$$

3. What is the smallest size standard Schedule 40 steel pipe that would carry 2.80 L/min of oil with a an average flow velocity below 0.3 m/s? Report your answer as a metric Nominal Pipe Size (DN).

First find the area required to transport the fluid exactly as specified.

$$Q = 2.80 \text{ L/min} \times \frac{1 \text{ m}^3/\text{s}}{60,000 \text{ L/min}} = 4.67 \times 10^{-5} \text{ m}^3/\text{s}$$

$$A = \frac{Q}{v} = \frac{4.67 \times 10^{-5} \text{ m}^3/\text{s}}{0.3 \text{ m/s}} = 1.56 \times 10^{-4} \text{ m}^2 = 155.56 \text{ mm}^2$$

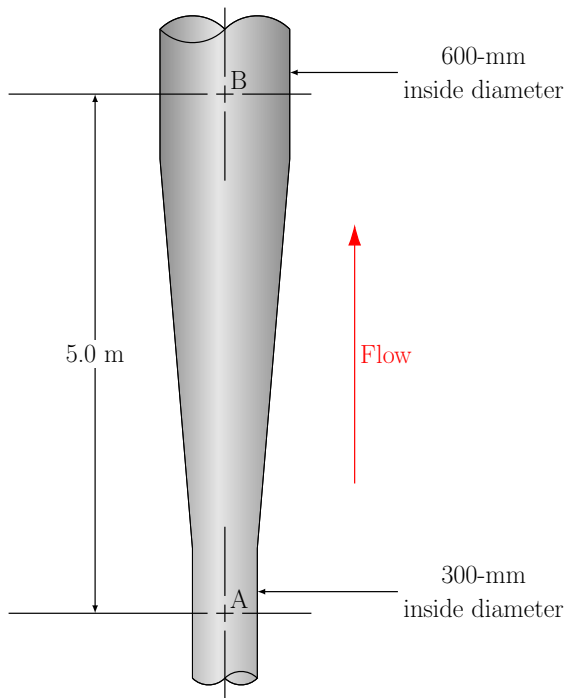
If we made the area any smaller the flow velocity would go above the 0.3 m/s. We therefore must go with DN15 pipe which has an area of 196 mm². If we went with the DN10 the flow velocity would be 0.38 m/s. Going with the DN15 results in a flow velocity of 0.24 m/s.

4. An aneurysm is an abnormal enlargement of a blood vessel such as the aorta. A patient's abdominal CT scan reveals an abnormal abdominal aortic diameter of 5.0 cm compared to their normal aortic diameter of 2.5 cm. If blood of density 1060 kg/m^3 travels through the normal portion of the aorta at a speed of 40 cm/s by how much does the pressure in the abnormal region exceed that of the normal region? Report your answer in kPa.

$$\Delta p = \frac{\rho}{2} (v_1^2 - v_2^2) = \frac{\rho v_1^2}{2} \left(1 - \left(\frac{d_1}{d_2} \right)^4 \right)$$

$$\Delta p = 0.5 (1060 \text{ kg/m}^3) (0.40 \text{ m/s})^2 (1 - 0.0625) = 79.5 \text{ Pa}$$

5. Turpentine is flowing at $0.45 \text{ m}^3/\text{s}$ in the fabricated tube shown below. If the pressure before the enlargement at A is 500 kPa what is the pressure at point B?



$$p_B = p_A + \frac{\rho}{2} (v_A^2 - v_B^2) - \gamma(z_B - z_A)$$

$$v_A = 6.37 \text{ m/s} \quad v_B = 1.59 \text{ m/s}$$

$$p_B = 500 \text{ kPa} + \frac{870}{2} (6.37^2 - 1.59^2) - 8.53(5 \text{ m})$$

$$p_B = 500 \text{ kPa} + 16.55 \text{ kPa} - 42.64 \text{ kPa} = 474 \text{ kPa}$$

6. Octane is flowing at 10 gpm from a standard 1-in Schedule 40 steel pipe to a standard 2-in Schedule 40 steel pipe. The pipes are horizontal. What is the difference in pressure (in psi) between the two pipes?

$$v_{1 \text{ in}} = 10 \text{ gpm} \frac{1 \text{ ft}^3/\text{s}}{449 \text{ gpm}} \frac{1}{0.006002 \text{ ft}^2} = 3.71 \text{ ft/s}$$

$$v_{2 \text{ in}} = 10 \text{ gpm} \frac{1 \text{ ft}^3/\text{s}}{449 \text{ gpm}} \frac{1}{0.02330 \text{ ft}^2} = 0.956 \text{ ft/s}$$

$$\Delta p = \frac{\rho}{2} (v_1^2 - v_2^2)$$

$$\begin{aligned} \Delta p &= 0.5 \times 1.36 \times (3.71^2 - 0.956^2) \text{ slug}/(\text{ft} \cdot \text{s}^2) \\ &= 8.74 \text{ lb}/\text{ft}^2 = 0.06 \text{ psi} \end{aligned}$$