Learning

- Learning agents
- Inductive learning
 - Different Learning Scenarios
 - Evaluation
- Neural Networks
 - Perceptrons
 - Multilayer Perceptrons
- Reinforcement Learning
 - Temporal Differences
 - Q-Learning
 - SARSA

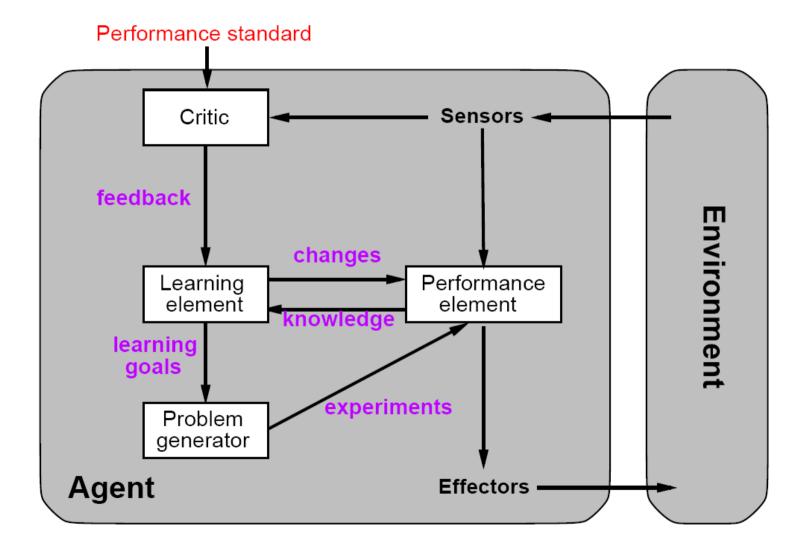
Material from Russell & Norvig, chapters 18.1, 18.2, 20.5 and 21

Slides based on Slides by Russell/Norvig, Ronald Williams, and Torsten Reil

Learning

- Learning is essential for unknown environments,
 - i.e., when designer lacks omniscience
- Learning is useful as a system construction method,
 - i.e., expose the agent to reality rather than trying to write it down
- Learning modifies the agent's decision mechanisms to improve performance

Learning Agents



Learning Element

- Design of a learning element is affected by
 - Which components of the performance element are to be learned
 - What feedback is available to learn these components
 - What representation is used for the components
- Type of feedback:
 - Supervised learning:
 - correct answers for each example
 - Unsupervised learning:
 - correct answers not given
 - Reinforcement learning:
 - occasional rewards for good actions

Different Learning Scenarios

Supervised Learning

- A teacher provides the value for the target function for all training examples (labeled examples)
- concept learning, classification, regression

Reinforcement Learning

 The teacher only provides feedback but not example values

Semi-supervised Learning

 Only a subset of the training examples are labeled

Unsupervised Learning

- There is no information except the training examples
- clustering, subgroup discovery, association rule discovery

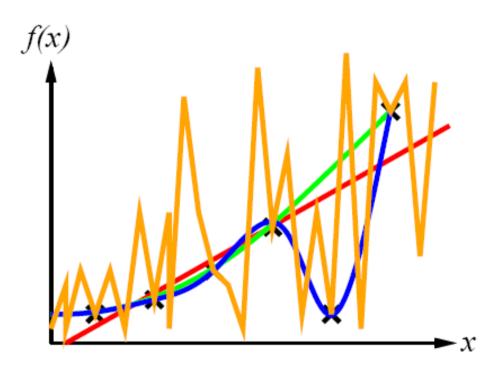
Inductive Learning

Simplest form: learn a function from examples

- f is the target function
- An example is a pair (x, f(x))
- Problem: find a hypothesis h
 - given a training set of examples
 - such that $h \approx f$
 - on all examples
 - i.e. the hypothesis must generalize from the training examples
- This is a highly simplified model of real learning:
 - Ignores prior knowledge
 - Assumes examples are given

Inductive Learning Method

- Construct/adjust h to agree with f on training set
 - h is consistent if it agrees with f on all examples
- Example:
 - curve fitting

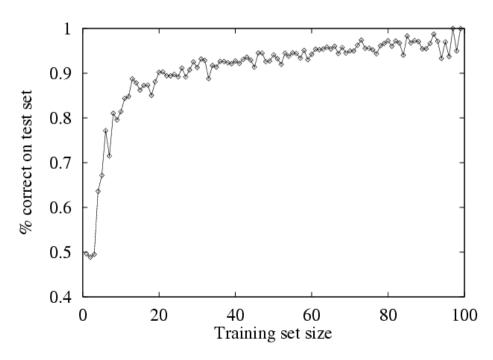


- Ockham's Razor
 - The best explanation is the simplest explanation that fits the data
- Overfitting Avoidance
 - maximize a combination of consistency and simplicity

Performance Measurement

- How do we know that $h \approx f$?
 - Use theorems of computational/statistical learning theory
 - Or try h on a new test set of examples where f is known (use same distribution over example space as training set)

Learning curve = % correct on test set over training set size



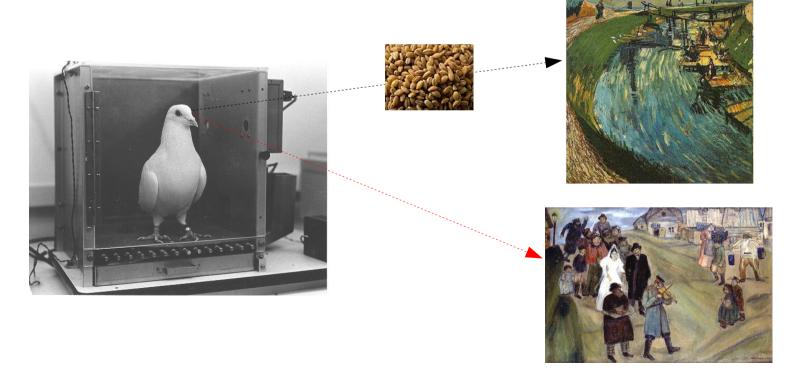
What are Neural Networks?

- Models of the brain and nervous system
- Highly parallel
 - Process information much more like the brain than a serial computer
- Learning
- Very simple principles
- Very complex behaviours
- Applications
 - As powerful problem solvers
 - As biological models

Pigeons as Art Experts

Famous experiment (Watanabe et al. 1995, 2001)

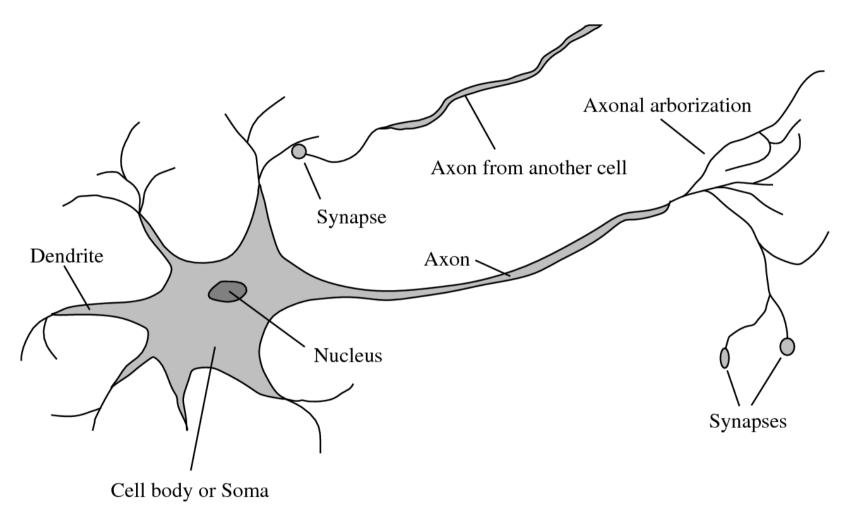
- Pigeon in Skinner box
- Present paintings of two different artists (e.g. Chagall / Van Gogh)
- Reward for pecking when presented a particular artist



Results

- Pigeons were able to discriminate between Van Gogh and Chagall with 95% accuracy
 - when presented with pictures they had been trained on
- Discrimination still 85% successful for previously unseen paintings of the artists
- Pigeons do not simply memorise the pictures
- They can extract and recognise patterns (the 'style')
- They generalise from the already seen to make predictions
- This is what neural networks (biological and artificial) are good at (unlike conventional computer)

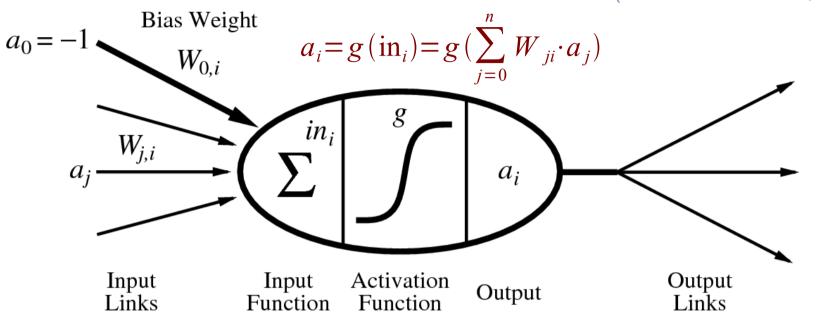
A Biological Neuron



- Neurons are connected to each other via synapses
- If a neuron is activated, it spreads its activation to all connected neurons

An Artificial Neuron

(McCulloch-Pitts, 1943)

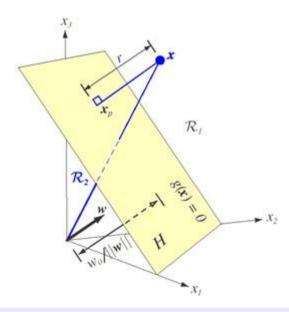


- Neurons correspond to nodes or units
- A link from unit i to unit j propagates activation a_j from j to i
- The weight $W_{i,j}$ of the link determines the strength and sign of the connection
- The total input activation is the sum of the input activations
- The output activation is determined by the activiation function g

Perceptron

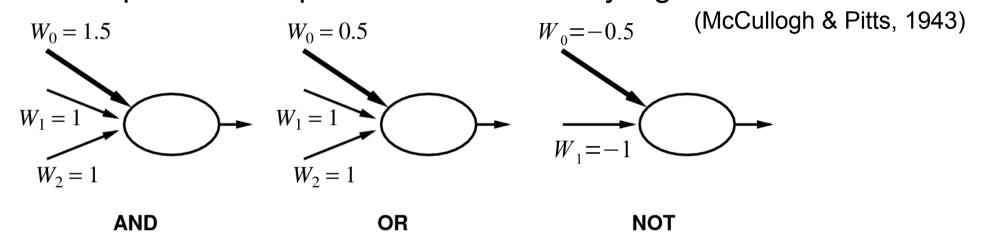
(Rosenblatt 1957, 1960)

- A single node
 - connecting n input signals with one output signal
 - typically signals are −1 or +1
- Activation function
 - A simple threshold function: $a_i = \begin{cases} a_i = 0 \\ 1 & \text{if } \sum_{i=0}^n W_i \cdot a_i > 0 \end{cases}$
- Thus it implements a linear separator
 - i.e., a hyperplane that divides n-dimensional space into a region with output -1 and a region with output 1

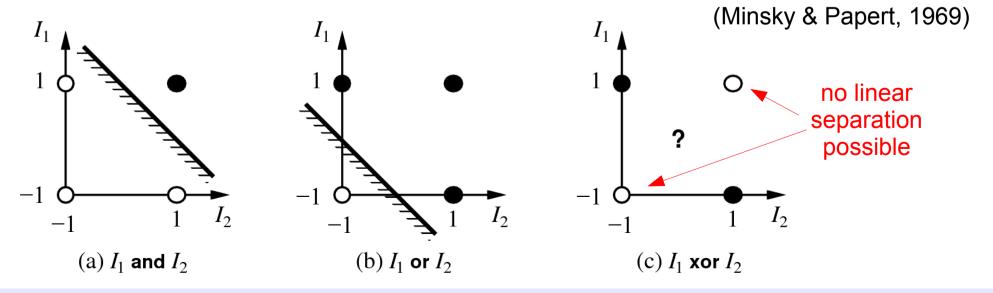


Perceptrons and Boolean Fucntions

a Perceptron can implement all elementary logical functions

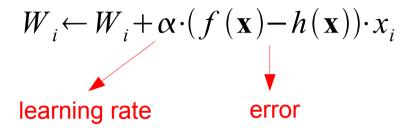


more complex functions like XOR cannot be modeled

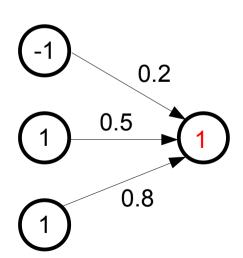


Perceptron Learning

Perceptron Learning Rule for Supervised Learning



Example:



Computation of output signal h(x)

$$in(x) = -1.0.2 + 1.0.5 + 1.0.8 = 1.1$$

 $h(x) = 1$ because $in(x) > 0$

Assume target value
$$f(x) = -1$$
 (and $\alpha = 0.5$)

$$W_0 \leftarrow 0.2 + 0.5 \cdot (-1 - 1) \cdot -1 = 0.2 + 1 = 1.2$$

 $W_1 \leftarrow 0.5 + 0.5 \cdot (-1 - 1) \cdot 1 = 0.5 - 1 = -0.5$
 $W_2 \leftarrow 0.8 + 0.5 \cdot (-1 - 1) \cdot 1 = 0.8 - 1 = -0.2$

Measuring the Error of a Network

- The error for one training example x can be measured by the squared error
 - the squared difference of the output value h(x) and the desired target value f(x)

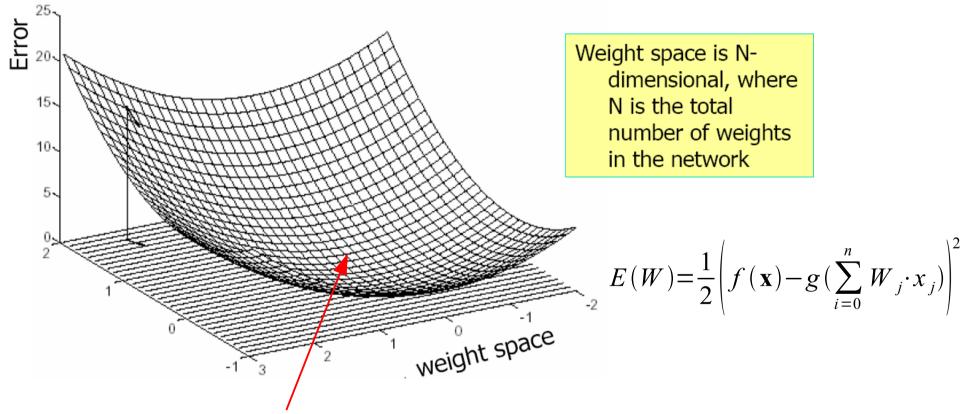
$$E(\mathbf{x}) = \frac{1}{2} Err^{2} = \frac{1}{2} (f(\mathbf{x}) - h(\mathbf{x}))^{2} = \frac{1}{2} \left| f(\mathbf{x}) - g(\sum_{i=0}^{n} W_{i} \cdot x_{j}) \right|^{2}$$

 For evaluating the performance of a network, we can try the network on a set of datapoints and average the value (= sum of squared errors)

$$E(Network) = \sum_{i=1}^{N} E(\mathbf{x}_{i})$$

Error Landscape

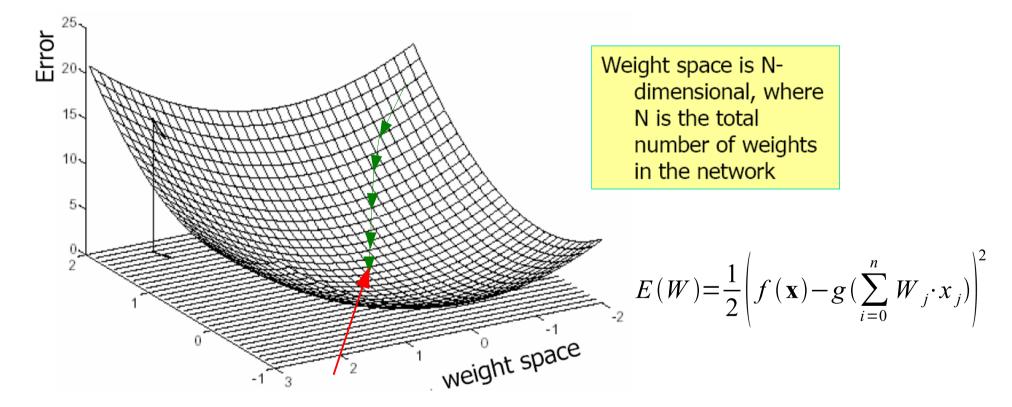
 The error function for one training example may be considered as a function in a multi-dimensional weight space



 The best weight setting for one example is where the error measure for this example is minimal

Error Minimization via Gradient Descent

- In order to find the point with the minimal error:
 - go downhill in the direction where it is steepest



... but make small steps, or you might step over the target

Error Minimization

It is easy to derive a perceptron training algorithm that minimizes the squared error

$$E = \frac{1}{2} Err^{2} = \frac{1}{2} (f(\mathbf{x}) - h(\mathbf{x}))^{2} = \frac{1}{2} \left| f(\mathbf{x}) - g(\sum_{i=0}^{n} W_{i} \cdot x_{i}) \right|^{2}$$

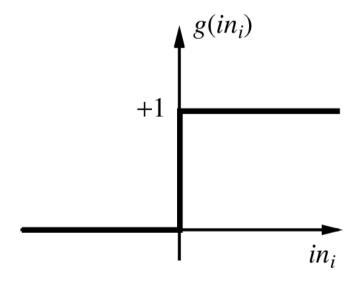
 Change weights into the direction of the steepest descent of the error function

$$\frac{\partial E}{\partial W_{j}} = Err \cdot \frac{\partial Err}{\partial W_{j}} = Err \cdot \frac{\partial}{\partial W_{j}} \left| f(\mathbf{x}) - g(\sum_{i=0}^{n} W_{j} \cdot x_{j}) \right| = -Err \cdot g'(\text{in}) \cdot x_{j}$$

- To compute this, we need a continuous and differentiable activation function g!
- Weight update with learning rate α : $W_j = W_j + \alpha \cdot Err \cdot g'(\text{in}) \cdot x_j$
 - positive error → increase network output
 - increase weights of nodes with positive input
 - decrease weights of nodes with negative input

Threshold Activation Function

- The regular threshold activation function is problematic
 - g'(x) = 0, therefore $\frac{\partial E}{\partial W_j} = -Err \cdot g'(\text{in}) \cdot x_j = 0$
 - → no weight changes!

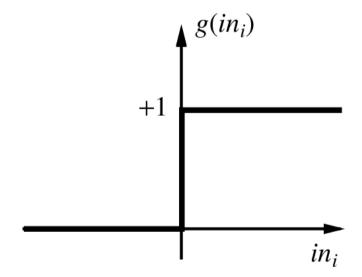


$$g(x) = \begin{cases} 0 & \text{if } x \le 0 \\ 1 & \text{if } x > 0 \end{cases}$$

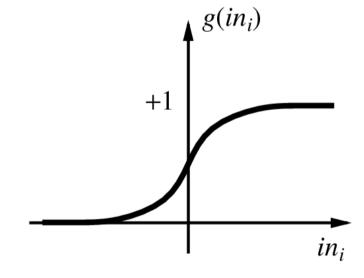
$$g'(x)=0$$

Sigmoid Activation Function

- A commonly used activation function is the sigmoid function
 - similar to the threshold function
 - easy to differentiate
 - non-linear



$$g(x) = \begin{cases} 0 & \text{if } x \le 0 \\ 1 & \text{if } x > 0 \end{cases}$$
$$g'(x) = 0$$

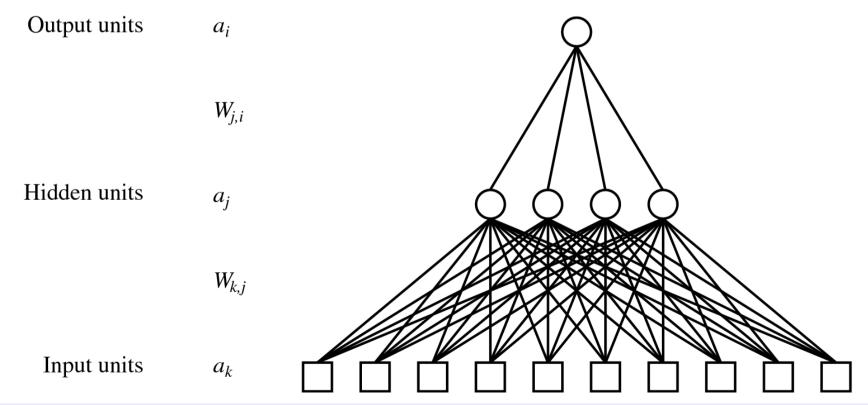


$$g(x) = \frac{1}{1 + e^{-x}}$$

$$g'(x) = g(x)(1 - g(x))$$

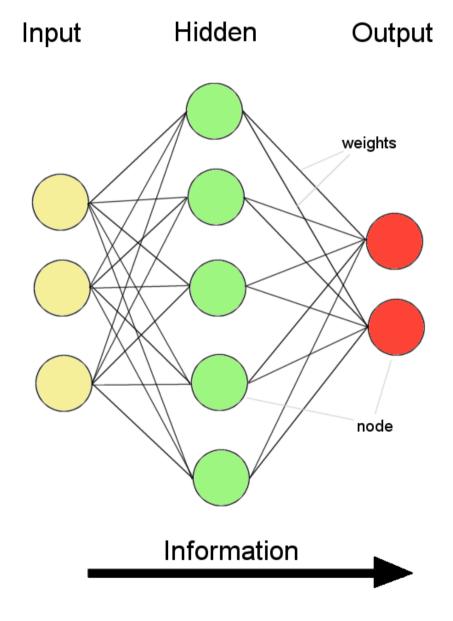
Multilayer Perceptrons

- Perceptrons may have multiple output nodes
 - may be viewed as multiple parallel perceptrons
- The output nodes may be combined with another perceptron
 - which may also have multiple output nodes
- The size of this hidden layer is determined manually



Multilayer Perceptrons

- Information flow is unidirectional
 - Data is presented to Input layer
 - Passed on to *Hidden Layer*
 - Passed on to Output layer
- Information is distributed
- Information processing is parallel



Expressiveness of MLPs

- Every continuous function can be modeled with three layers
 - i.e., with one hidden layer
- Every function can be modeled with four layers
 - i.e., with two hidden layers

Backpropagation Learning

The output nodes are trained like a normal perceptron

$$W_{ji} \leftarrow W_{ji} + \alpha \cdot Err_i \cdot g'(\text{in}_i) \cdot x_j = W_{ji} + \alpha \cdot \Delta_i \cdot x_j$$

- Δ_i is the error term of output node i times the derivation of its inputs
- the error term Δ_i of the output layers is propagated back to the hidden layer

$$\Delta_{j} = \left(\sum_{i} W_{ji} \cdot \Delta_{i}\right) \cdot g'(\operatorname{in}_{j}) \qquad W_{kj} = W_{kj} + \alpha \cdot \Delta_{j} \cdot x_{k}$$

 the training signal of hidden layer node j is the weighted sum of the errors of the output nodes

Minimizing the Network Error

- The error landscape for the entire network may be thought of as the sum of the error functions of all examples
 - will yield many local minima → hard to find global minimum
- Minimizing the error for one training example may destroy what has been learned for other examples

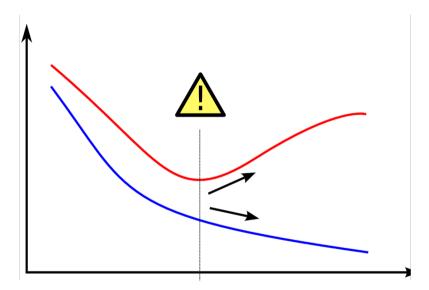
 a good location in weight space for one example may be a bad location for another examples

- Training procedure:
 - try all examples in turn
 - make small adjustments for each example
 - repeat until convergence
- One Epoch = One iteration through all examples



Overfitting

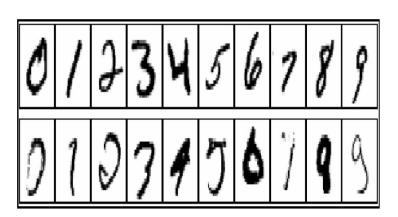
- Training Set Error continues to decrease with increasing number of training examples / number of epochs
 - an epoch is a complete pass through all training examples
- Test Set Error will start to increase because of overfitting



- Simple training protocol:
 - keep a separate validation set to watch the performance
 - validation set is different from training and test sets!
 - stop training if error on validation set gets down

Wide Variety of Applications

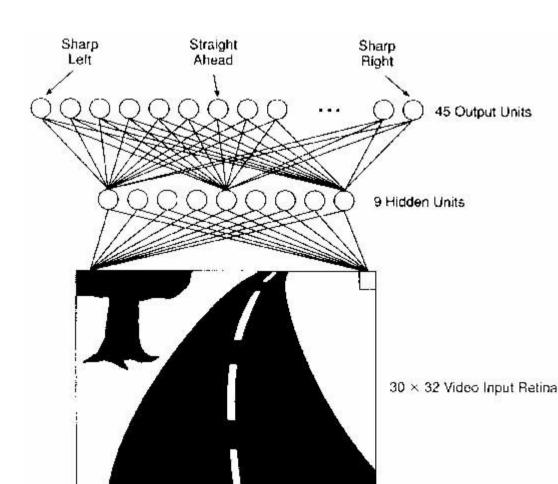
- Speech Recognition
- Autonomous Driving
- Handwritten Digit Recognition
- Credit Approval
- Backgammon
- etc.



- Good for problems where the final output depends on combinations of many input features
 - rule learning is better when only a few features are relevant
- Bad if explicit representations of the learned concept are needed
 - takes some effort to interpret the concepts that form in the hidden layers

Autonomous Land Vehicle In a Neural Network (ALVINN)

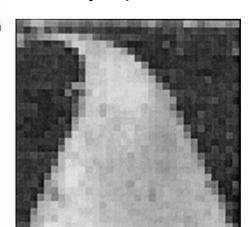
(Dean Pomerleau)

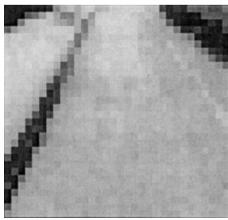


Training Data: Human Driver on real roads and simulator



Sensory input is directly fed into the network





Multilayer Network Control Unit for Navl.ab (From Kanade et al., 1994. © 1994 ACM. Couriesy of the authors.)