

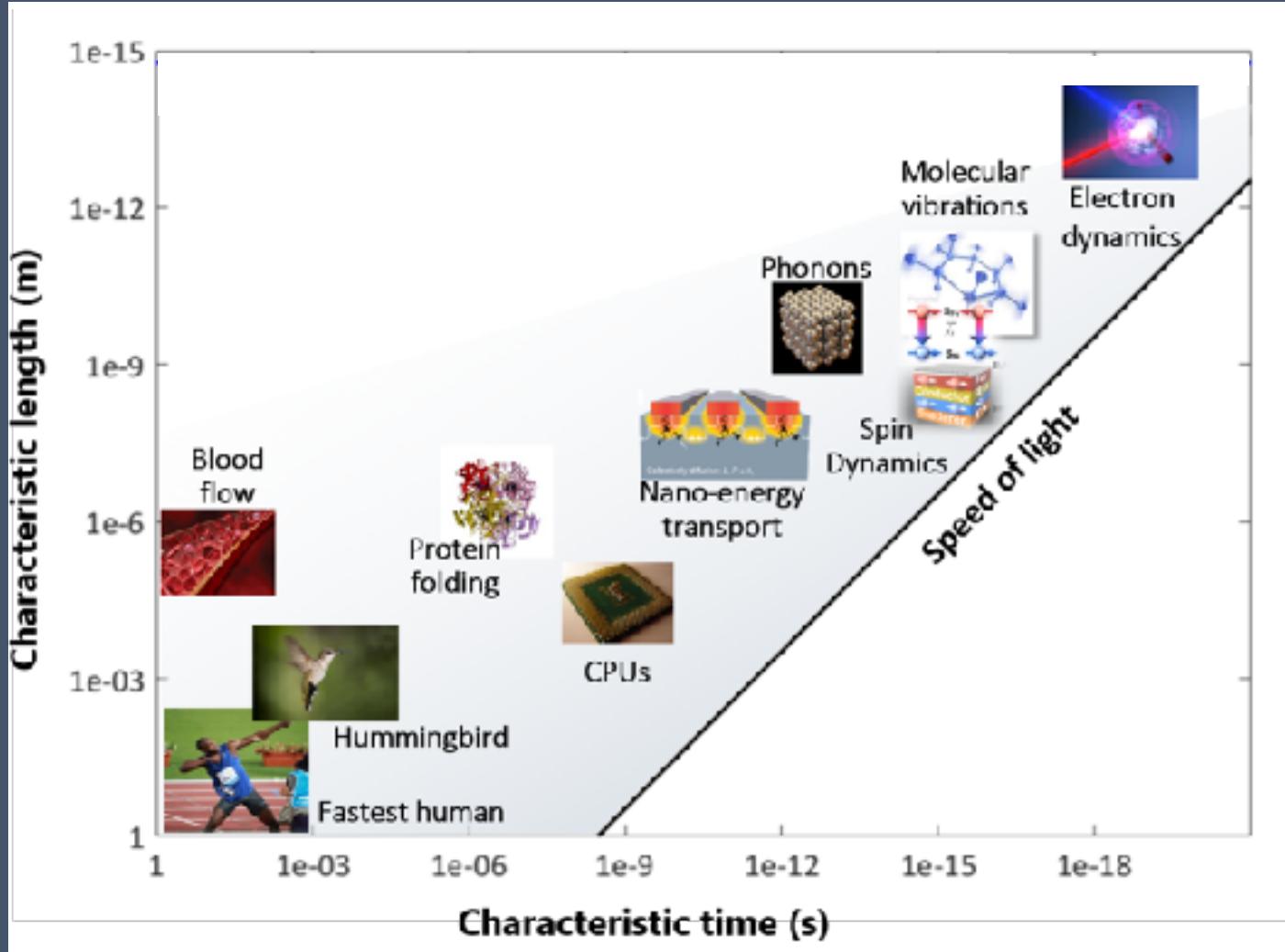
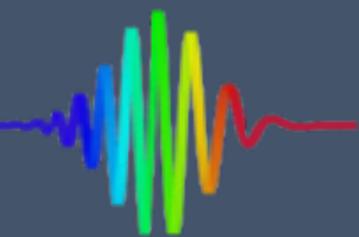
Attosecond, High-Harmonic Optical Vortices with Tailored Spin and Orbital Angular Momentum

Kevin M. Dorney

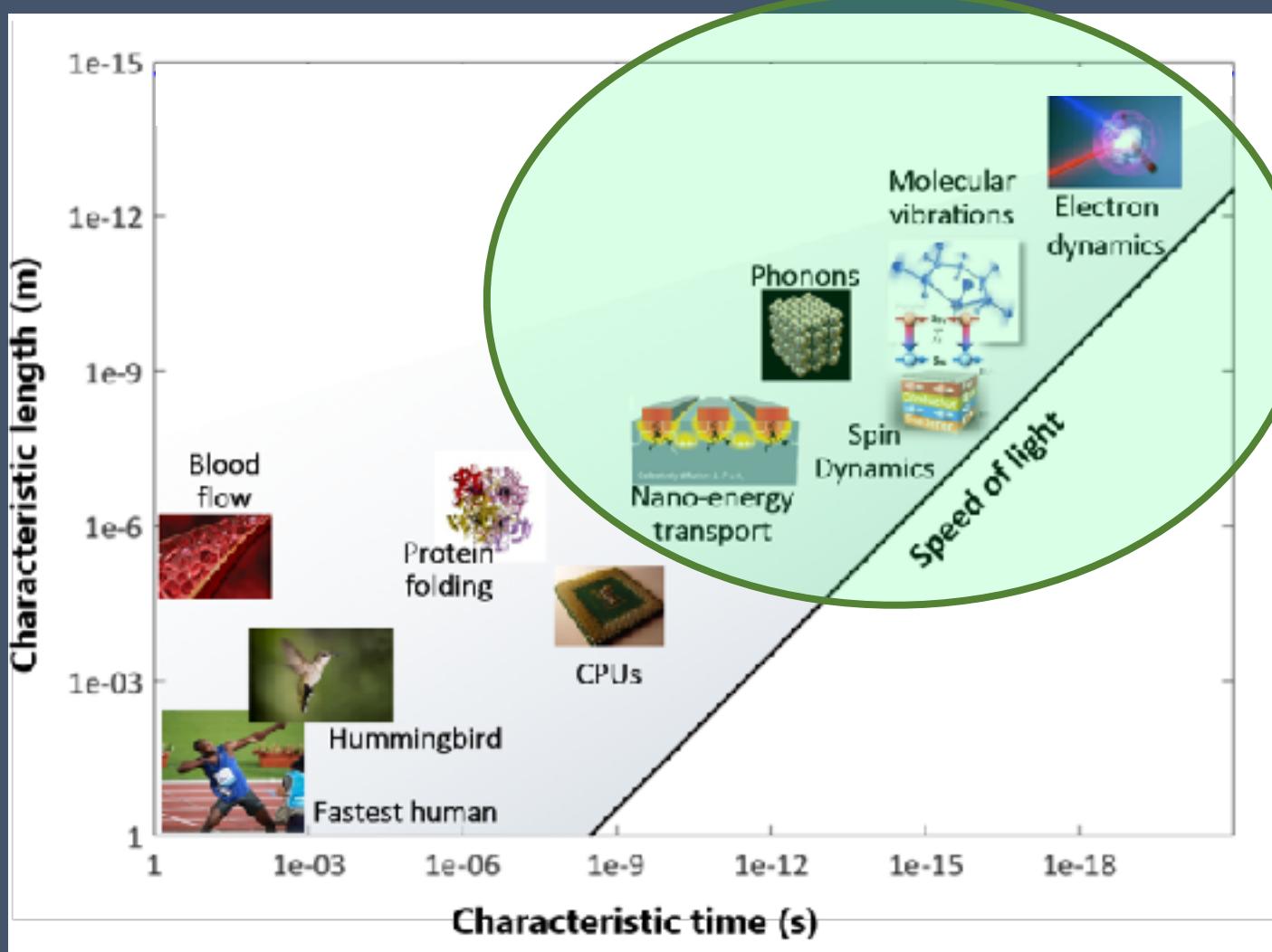
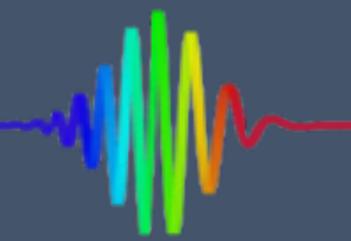
Kapteyn-Murnane Group,
JILA – University of Colorado Boulder



Life in the Fast Lane: The Nanoscale, Ultrafast Dynamics Underlying Emerging Technologies and Nature



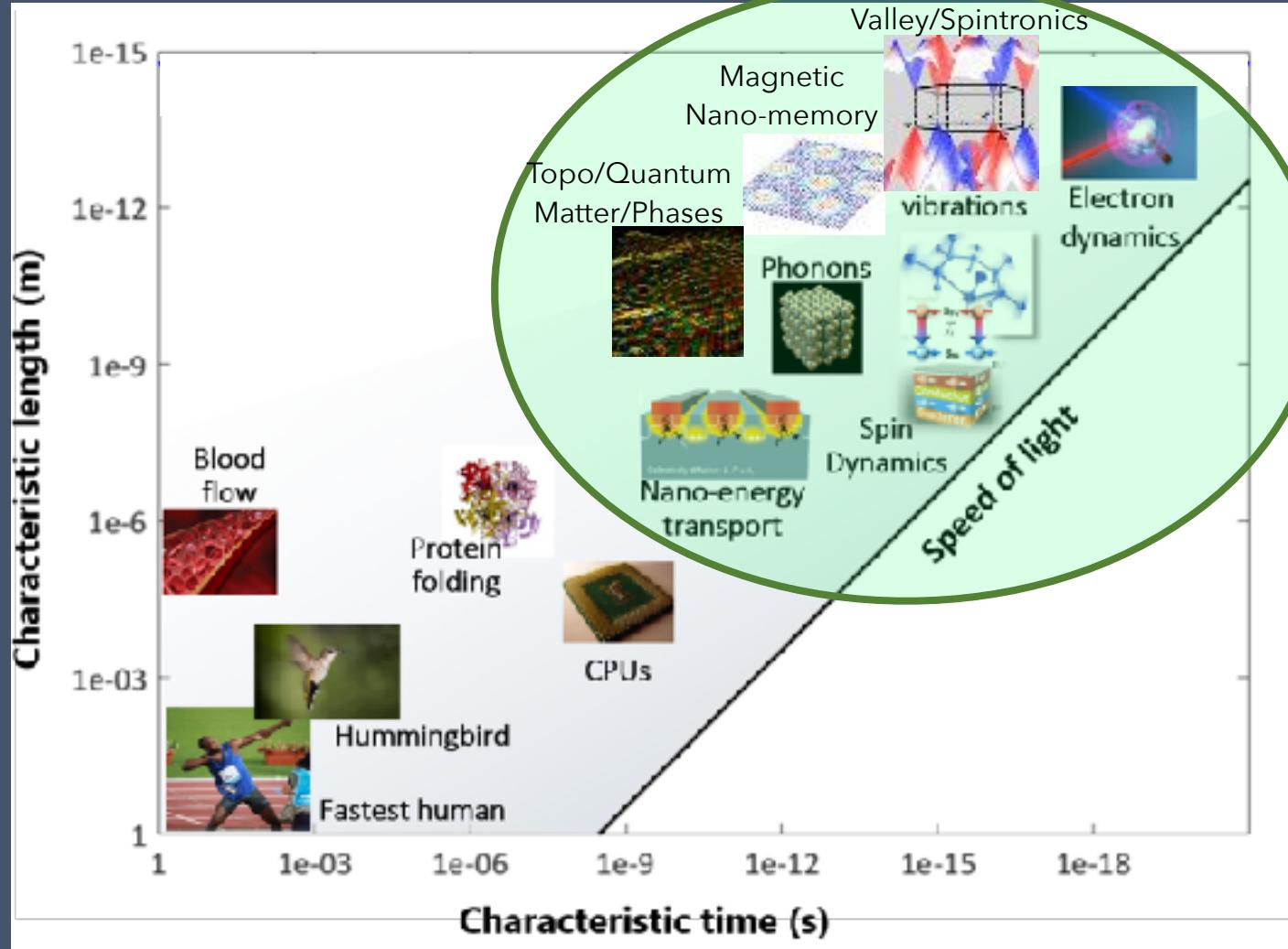
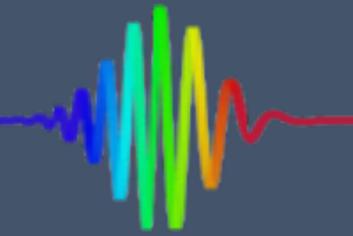
Life in the Fast Lane: The Nanoscale, Ultrafast Dynamics Underlying Emerging Technologies and Nature



Ultrafast, Short Wavelength Light is an Ideal Probe of the Nano-Quantum World

- ✓ Elemental, chemical, spin specificity
- ✓ Short wavelength yields high-resolution 3D images of structure
- ✓ Ultrafast nature of x-rays captures dynamics relevant to function
- ✓ Nondestructive/non-invasive; "x-ray" vision

Life in the Fast Lane: The Nanoscale, Ultrafast Dynamics Underlying Emerging Technologies and Nature



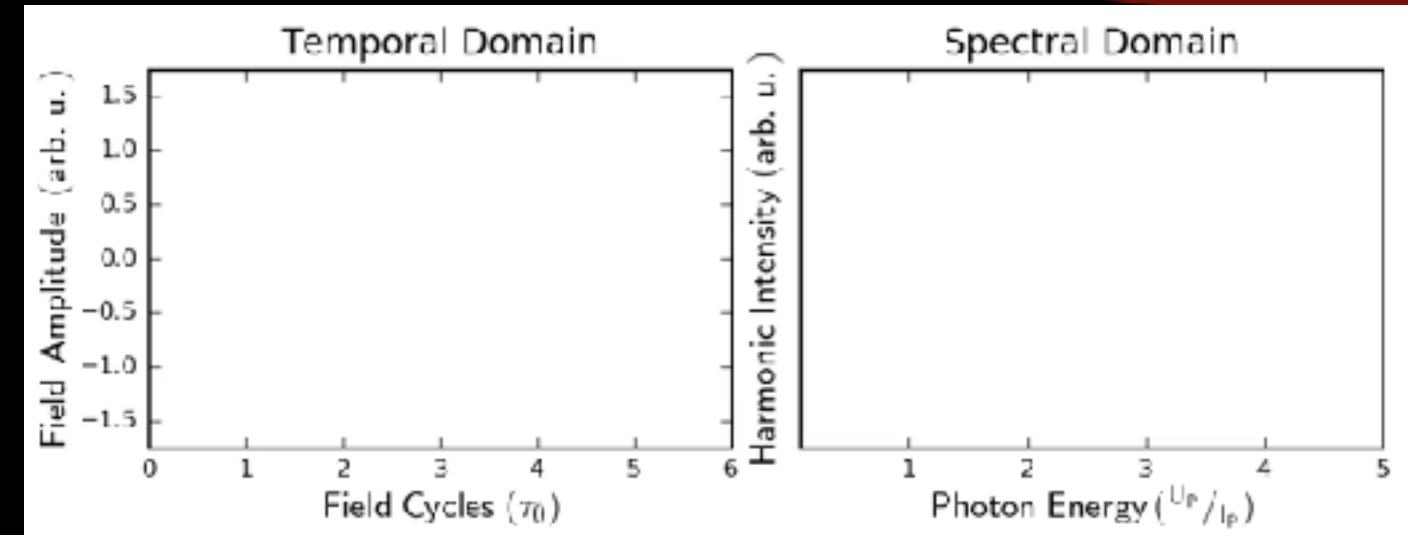
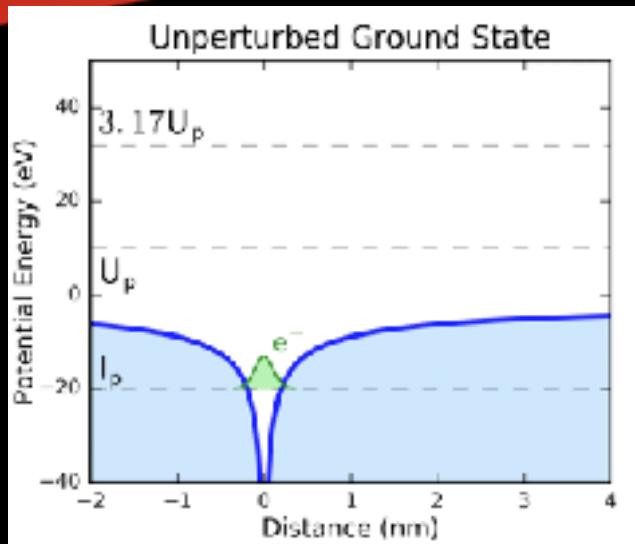
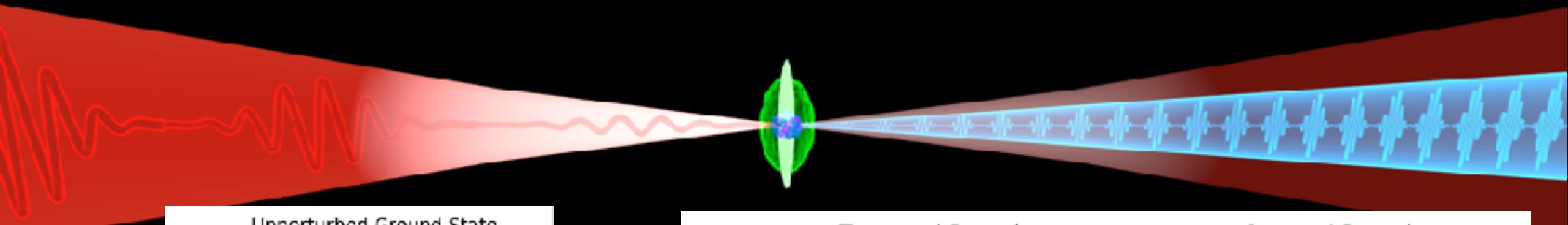
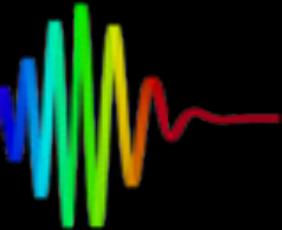
Ultrafast, Short Wavelength Light is an Ideal Probe of the Nano-Quantum World

- ✓ Elemental, chemical, spin specificity
- ✓ Short wavelength yields high-resolution 3D images of structure
- ✓ Ultrafast nature of x-rays captures dynamics relevant to function
- ✓ Nondestructive/non-invasive; “x-ray” vision

Future is Fast, Small, and Highly Structured!

- Many next-gen technologies are based on **chiral/topological materials**.
- Demands a need for ultrafast, **structured/chiral**, short-wavelength light!

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum. PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

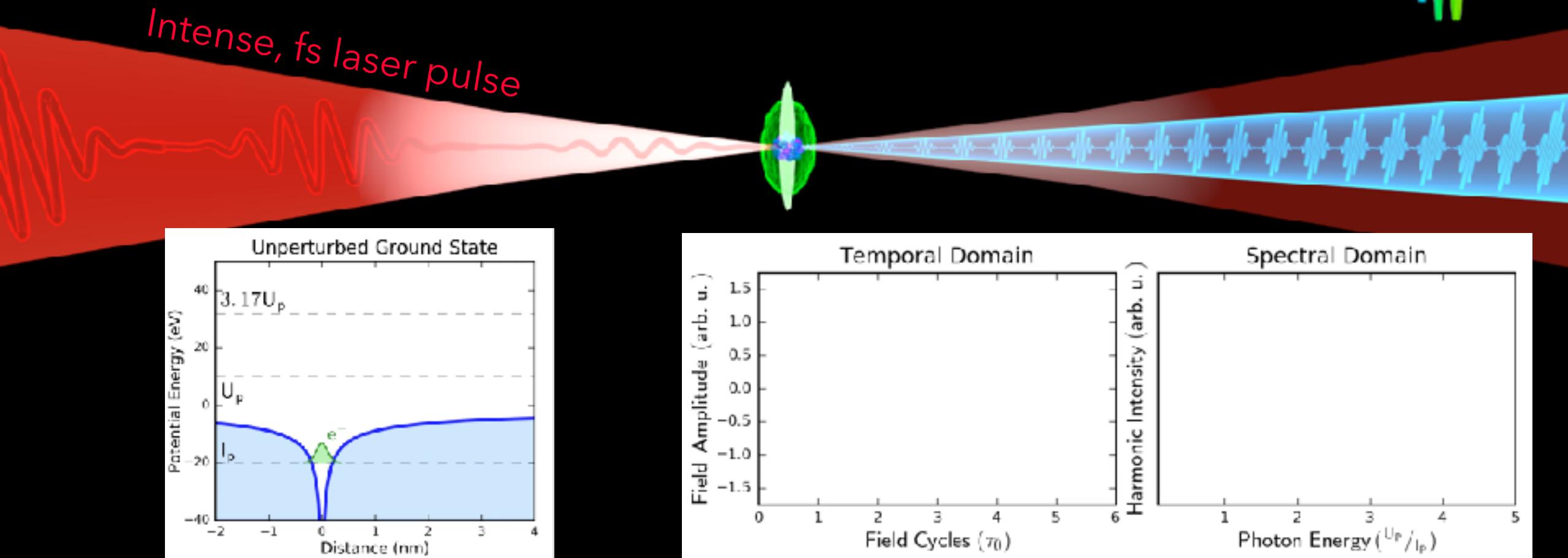
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum, PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

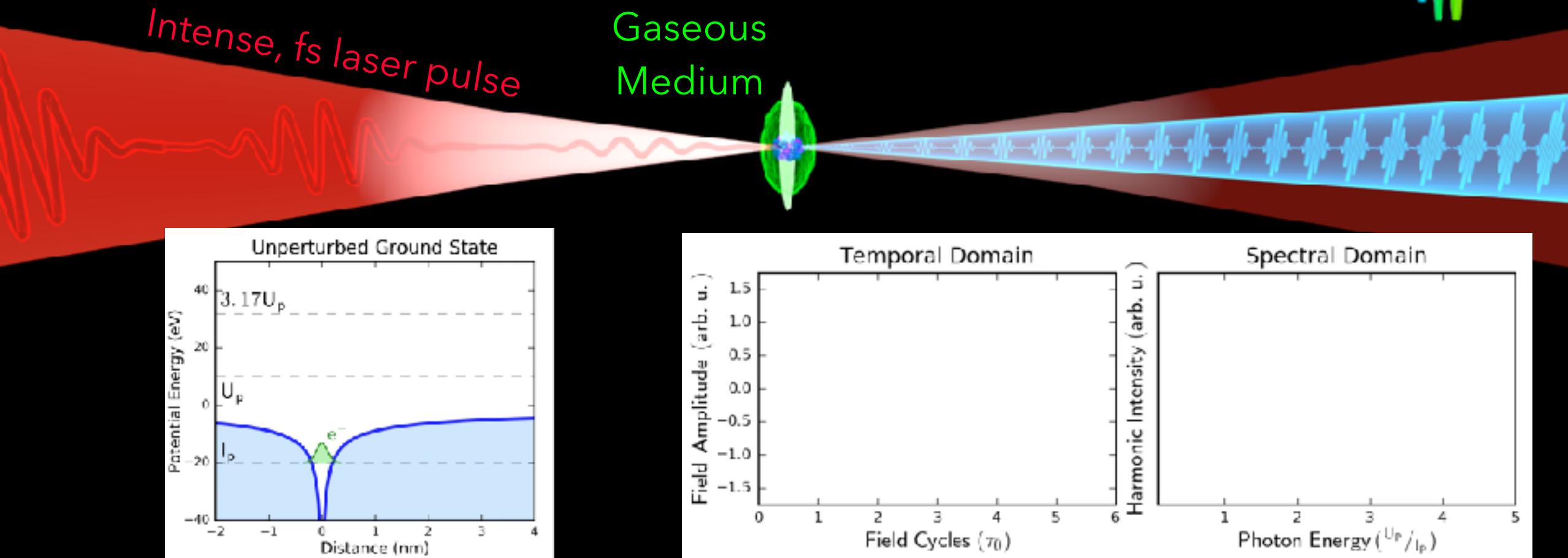
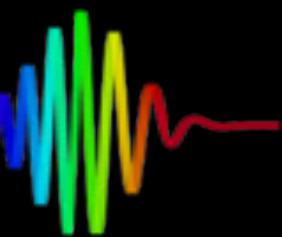
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum, PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

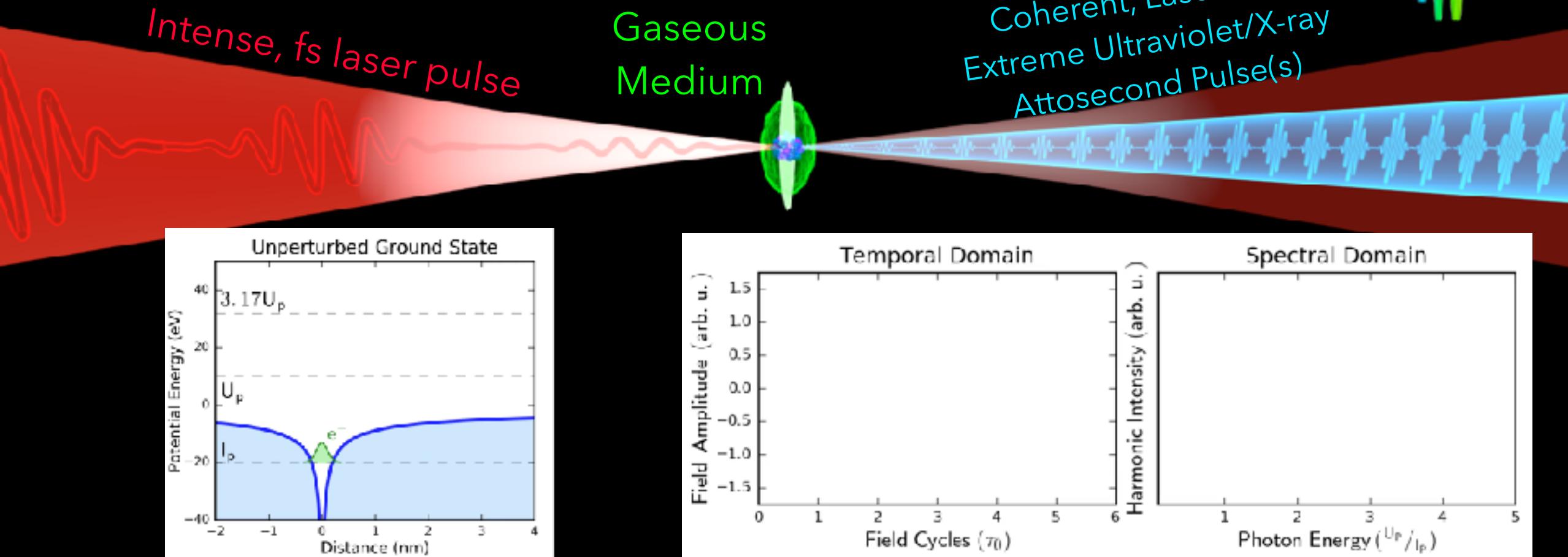
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum, PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

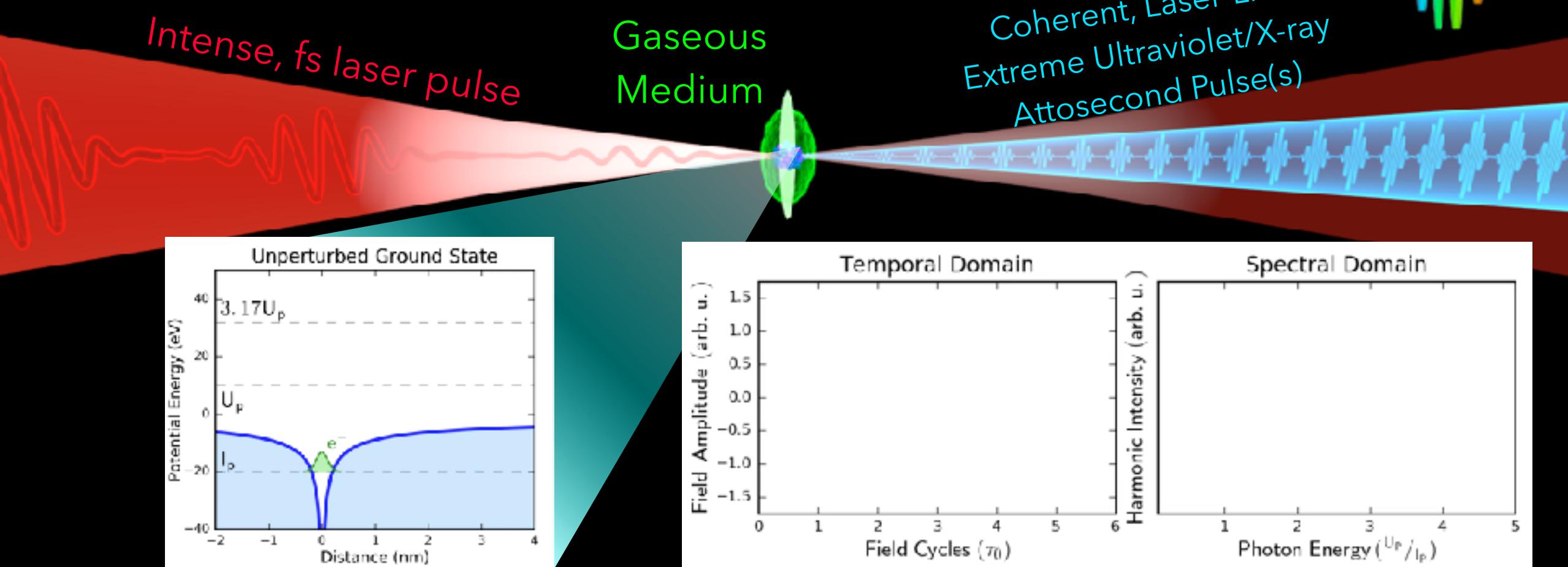
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum, PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

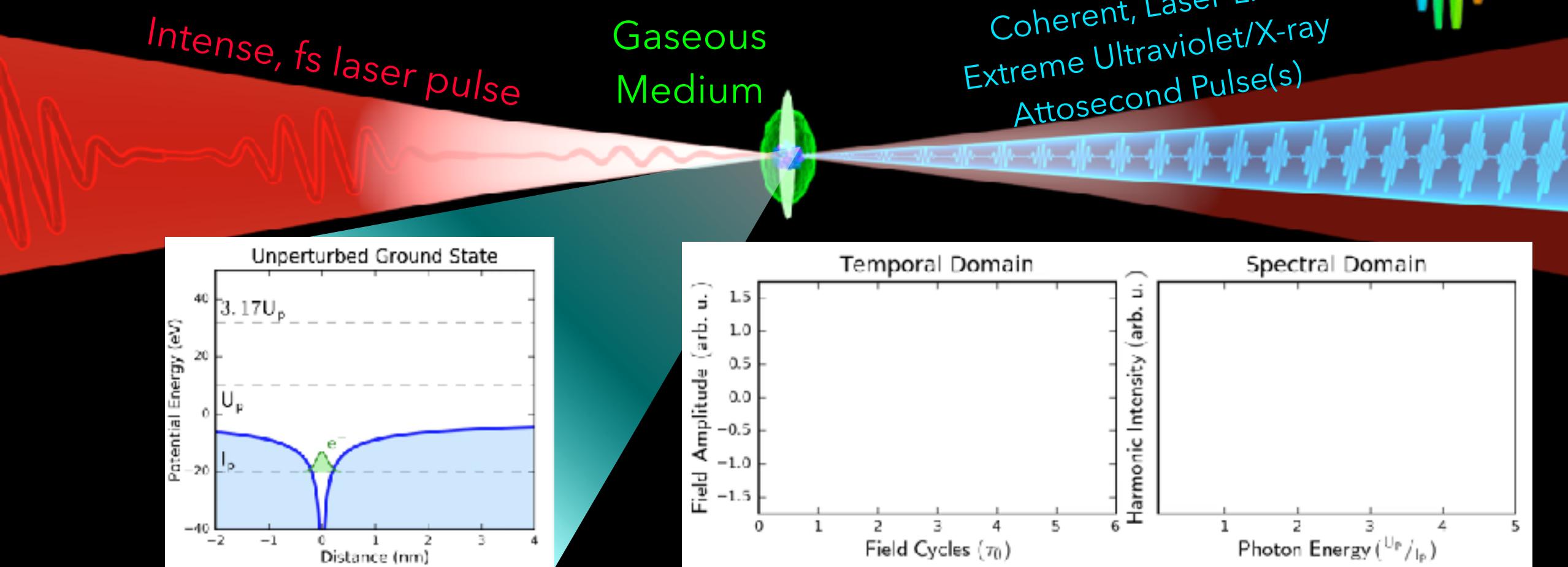
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum, PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

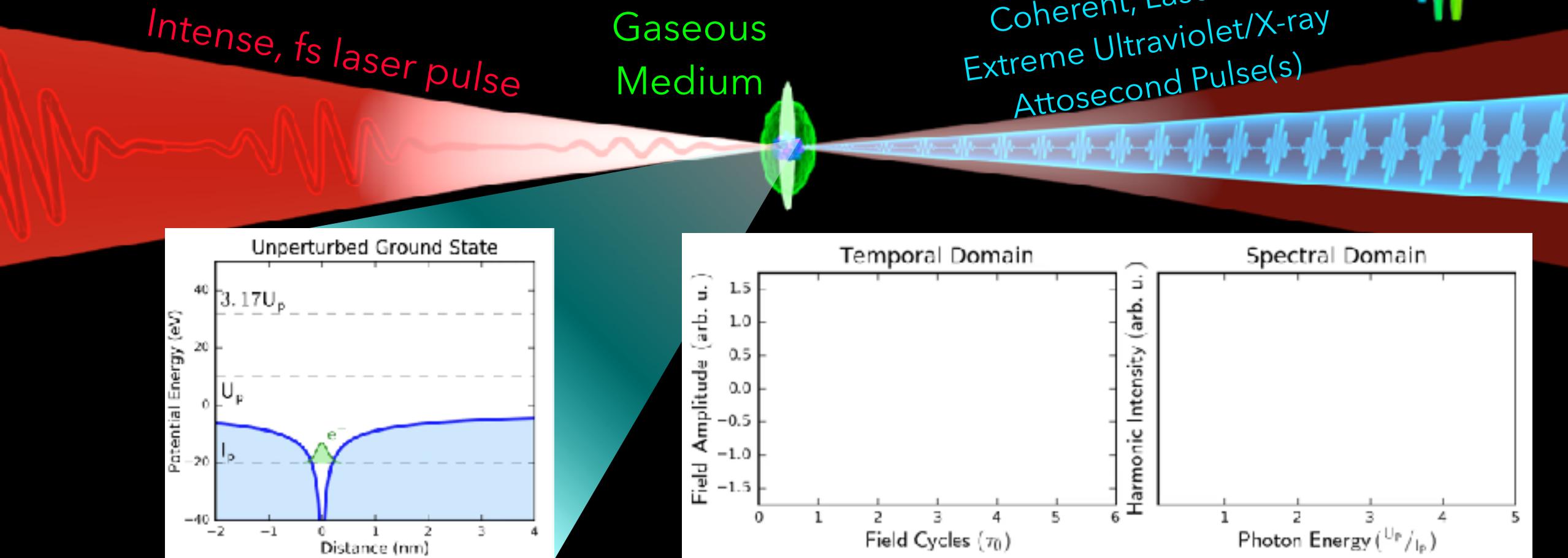
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum, PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

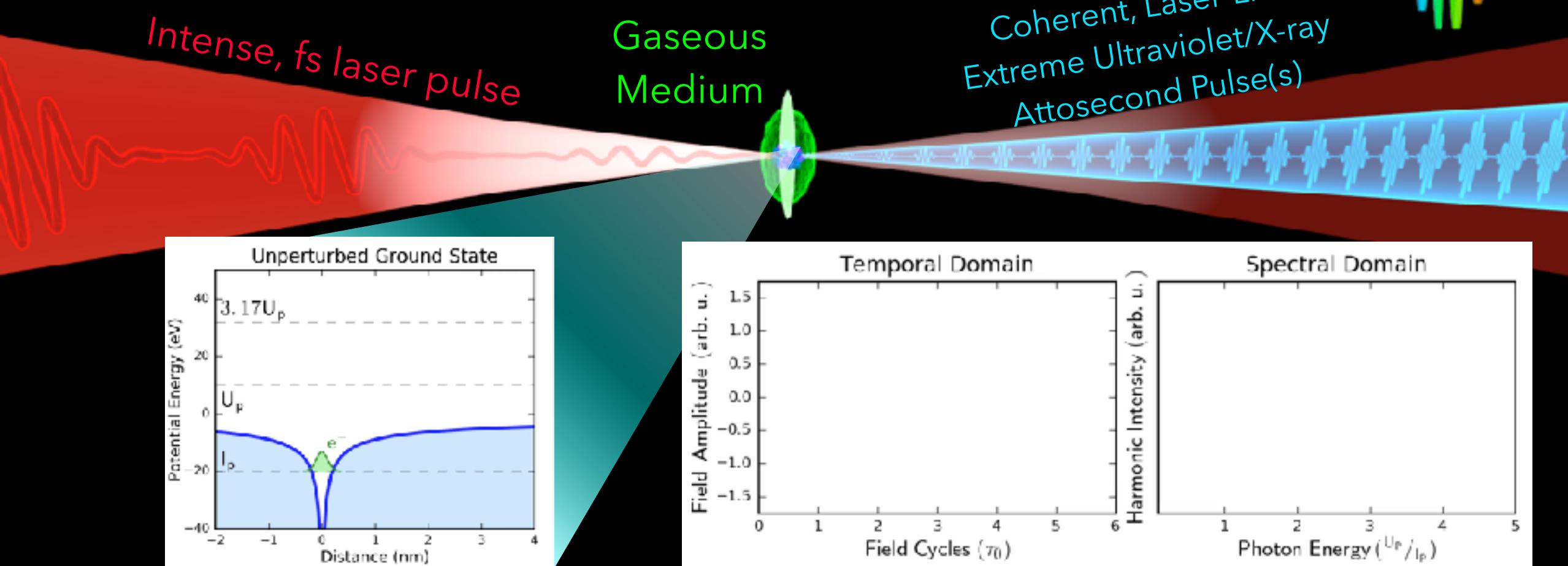
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

High-Harmonic Generation (HHG): A Quantum Technology for Capturing the Fastest Dynamics in Nature



Kuchiev, JETP, **45**, 404 1987

QM: Kulander, Schafer, Krause. SILAP 1992

Classical: Corkum, PRL, **71** 1993

Semi-Classical: Lewenstein et al, PRA **49**, 1994

McPherson et al, JOSA B, **4**, 595 1987

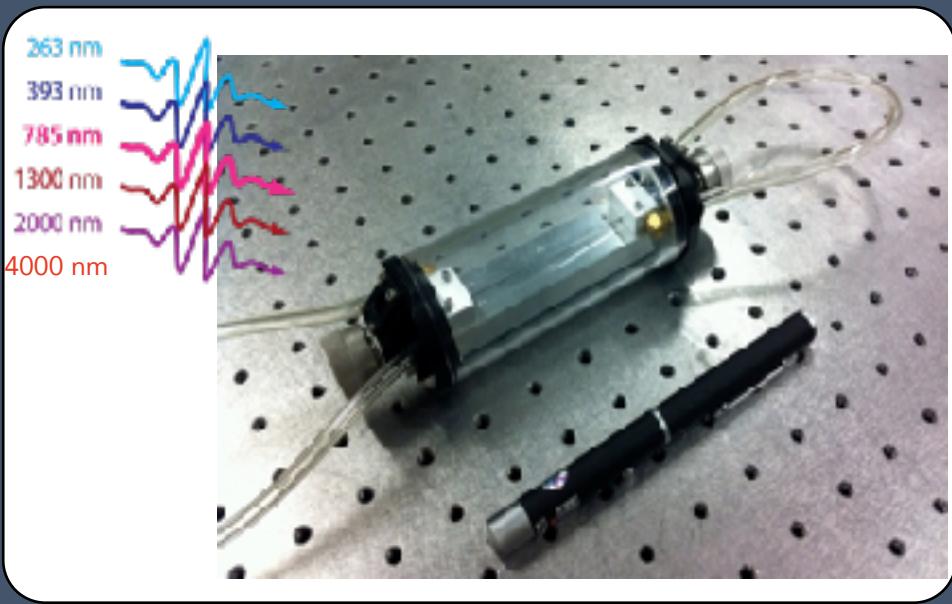
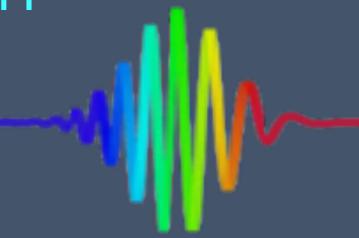
Ferry, et al. J. Phys. B., **21**, 1998

Rundquist et al., Science, **5368**, 1998

Zhou et al., PRL, **76**, 752 1996

Popmintchev et al., Science **336**, 1287 2012

HHG in the Lab: Tailored EUV and Soft X-ray Beams with Laser-Like Spatiotemporal Coherence on a Tabletop



¹Rundquist, et al. *Science*, **280**, 1998

²Bartels, et al. *Science* **297**, 2002

³Zhang, et al. *Opt. Lett.* **29**, 2004

⁴Popmintchev, et al. *Science*, **350**, 2015 (**UV drivers**)

⁵Chen, et al. *PRL*, **105**, 2010

⁶Popmintchev, et al. *Science*, **336**, 2012 (**mid-IR drivers**)

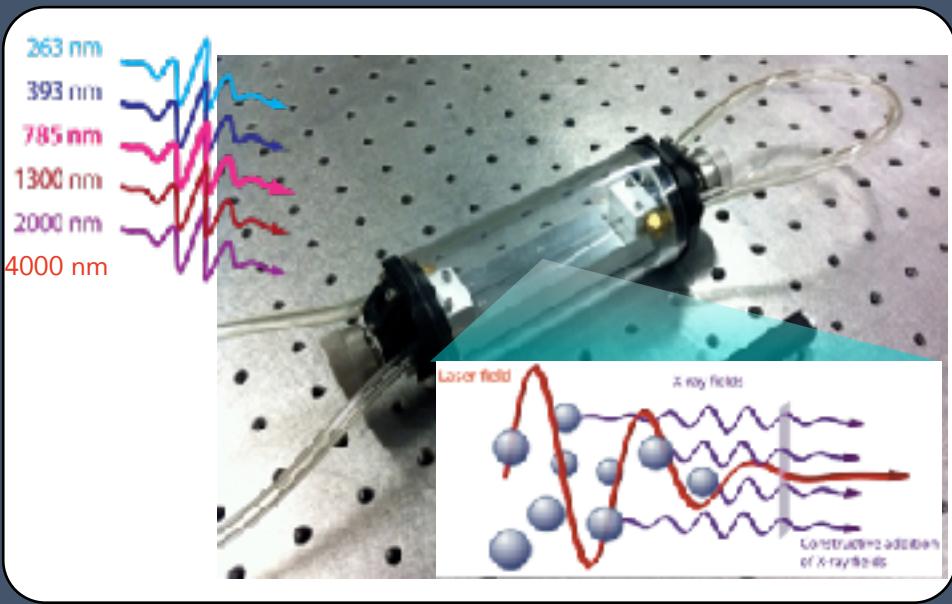
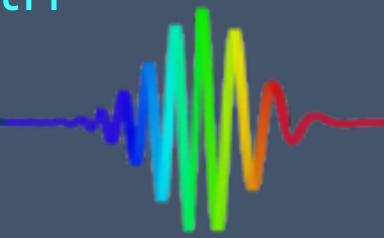
⁷Kfir, et al. *Nat. Photon.*, **9**, 2015

⁸Dorney, et al. *PRL*, **119**, 2017

⁹Dorney, et al. *Nat. Photon.* **1**, 2019

¹⁰Rego and Dorney, et al. *Science*, **364**, 2019

HHG in the Lab: Tailored EUV and Soft X-ray Beams with Laser-Like Spatiotemporal Coherence on a Tabletop



¹Rundquist, et al. *Science*, **280**, 1998

²Bartels, et al. *Science* **297**, 2002

³Zhang, et al. *Opt. Lett.* **29**, 2004

⁴Popmintchev, et al. *Science*, **350**, 2015 (**UV drivers**)

⁵Chen, et al. *PRL*, **105**, 2010

⁶Popmintchev, et al. *Science*, **336**, 2012 (**mid-IR drivers**)

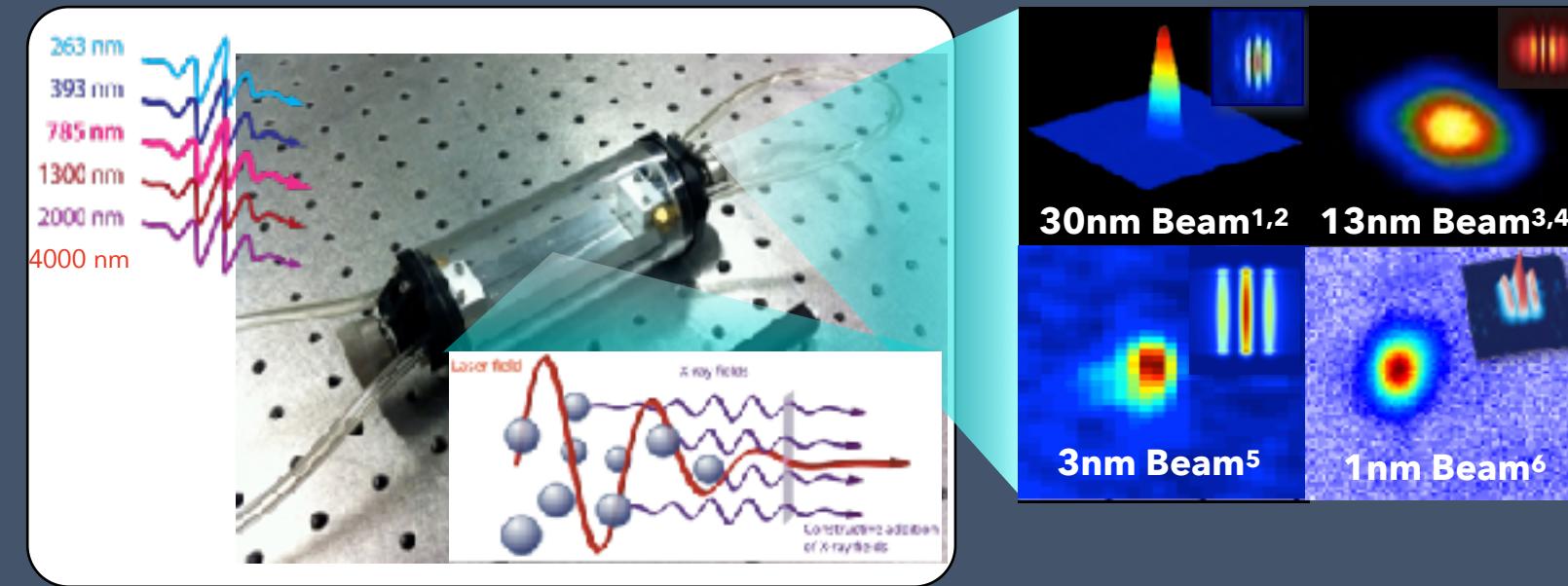
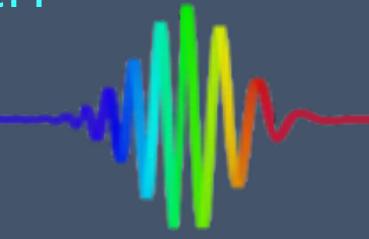
⁷Kfir, et al. *Nat. Photon.*, **9**, 2015

⁸Dorney, et al. *PRL*, **119**, 2017

⁹Dorney, et al. *Nat. Photon.* **1**, 2019

¹⁰Rego and Dorney, et al. *Science*, **364**, 2019

HHG in the Lab: Tailored EUV and Soft X-ray Beams with Laser-Like Spatiotemporal Coherence on a Tabletop



¹Rundquist, et al. *Science*, **280**, 1998

²Bartels, et al. *Science* **297**, 2002

³Zhang, et al. *Opt. Lett.* **29**, 2004

⁴Popmintchev, et al. *Science*, **350**, 2015 (**UV drivers**)

⁵Chen, et al. *PRL*, **105**, 2010

⁶Popmintchev, et al. *Science*, **336**, 2012 (**mid-IR drivers**)

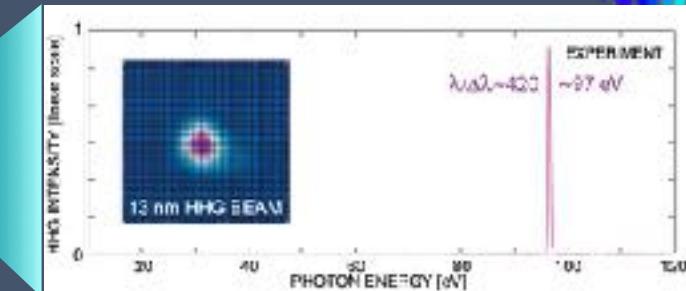
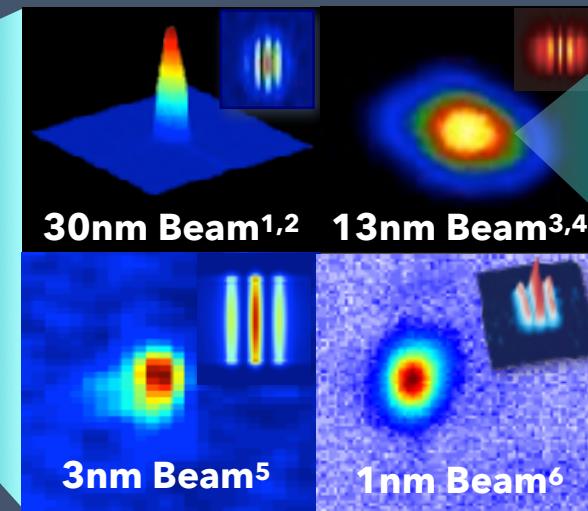
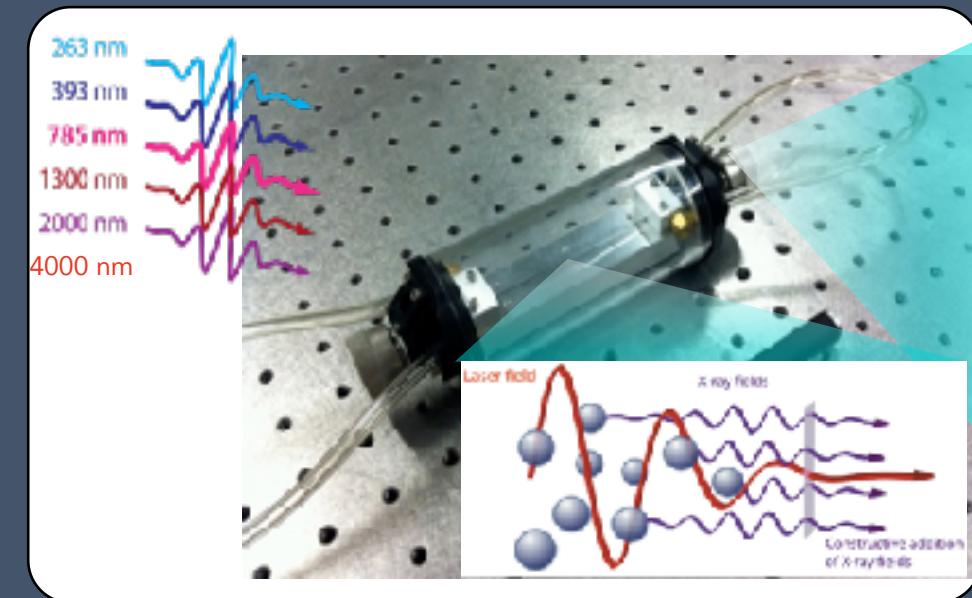
⁷Kfir, et al. *Nat. Photon.*, **9**, 2015

⁸Dorney, et al. *PRL*, **119**, 2017

⁹Dorney, et al. *Nat. Photon.* **1**, 2019

¹⁰Rego and Dorney, et al. *Science*, **364**, 2019

HHG in the Lab: Tailored EUV and Soft X-ray Beams with Laser-Like Spatiotemporal Coherence on a Tabletop



¹Rundquist, et al. *Science*, **280**, 1998

²Bartels, et al. *Science* **297**, 2002

³Zhang, et al. *Opt. Lett.* **29**, 2004

⁴Popmintchev, et al. *Science*, **350**, 2015 (**UV drivers**)

⁵Chen, et al. *PRL*, **105**, 2010

⁶Popmintchev, et al. *Science*, **336**, 2012 (**mid-IR drivers**)

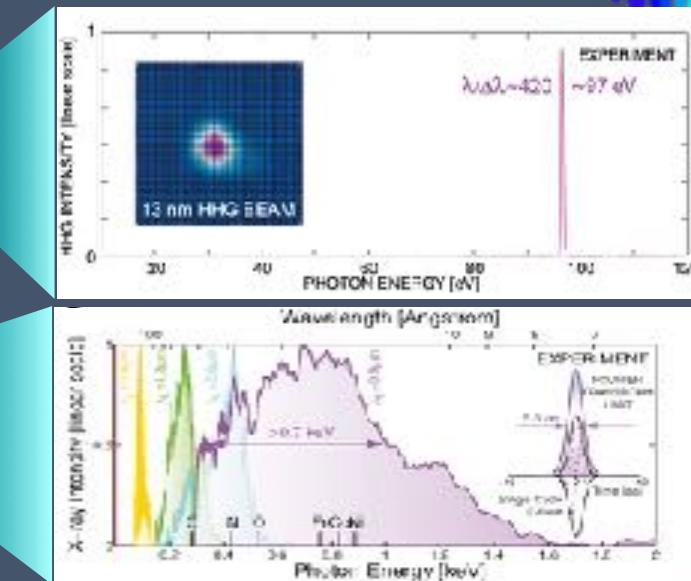
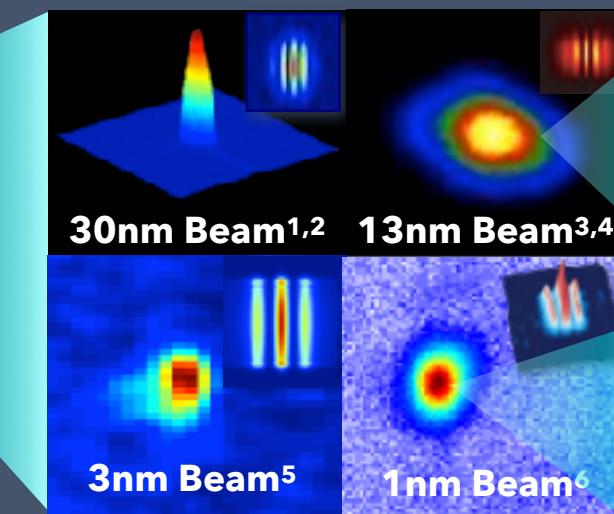
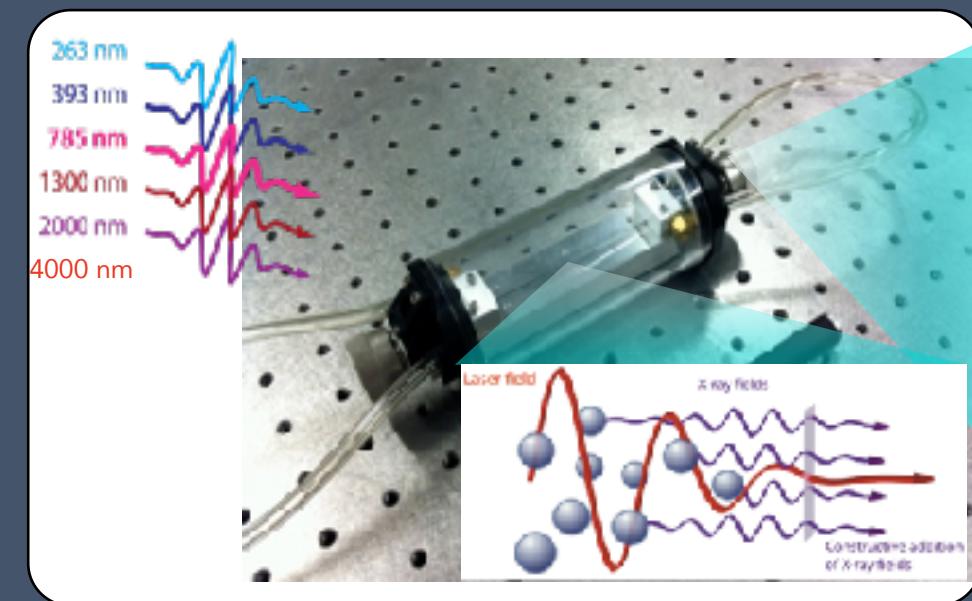
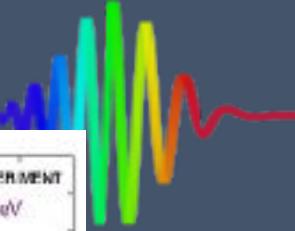
⁷Kfir, et al. *Nat. Photon.*, **9**, 2015

⁸Dorney, et al. *PRL*, **119**, 2017

⁹Dorney, et al. *Nat. Photon.* **1**, 2019

¹⁰Rego and Dorney, et al. *Science*, **364**, 2019

HHG in the Lab: Tailored EUV and Soft X-ray Beams with Laser-Like Spatiotemporal Coherence on a Tabletop



¹Rundquist, et al. *Science*, **280**, 1998

²Bartels, et al. *Science* **297**, 2002

³Zhang, et al. *Opt. Lett.* **29**, 2004

⁴Popmintchev, et al. *Science*, **350**, 2015 (**UV drivers**)

⁵Chen, et al. *PRL*, **105**, 2010

⁶Popmintchev, et al. *Science*, **336**, 2012 (**mid-IR drivers**)

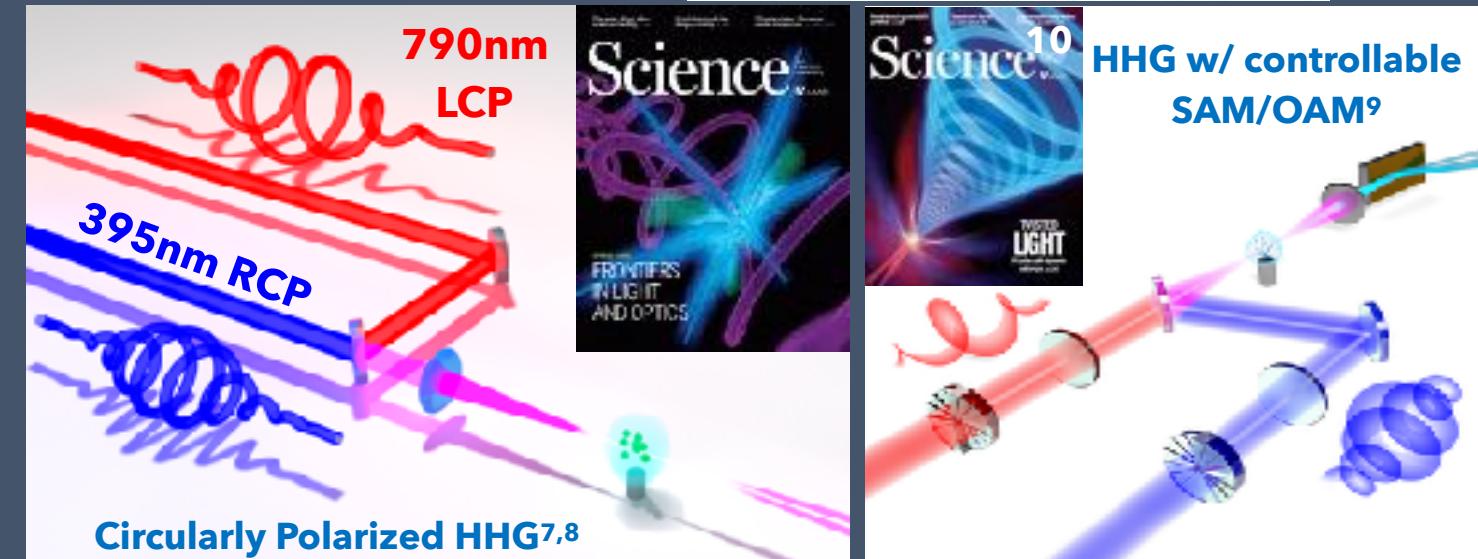
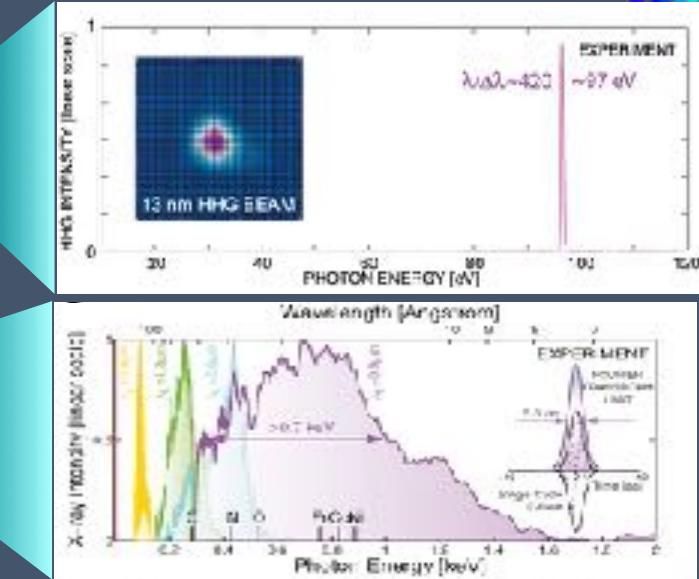
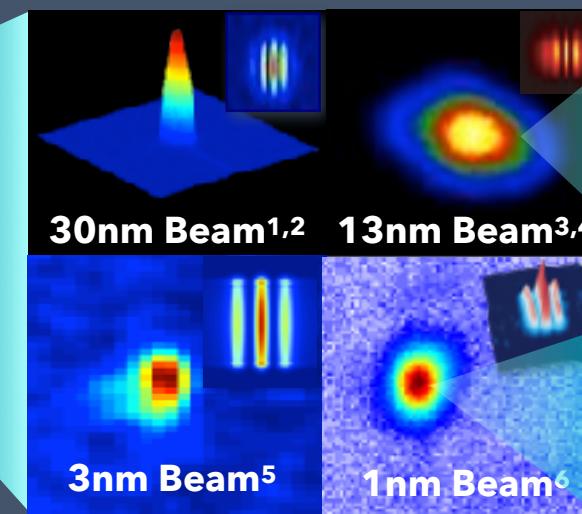
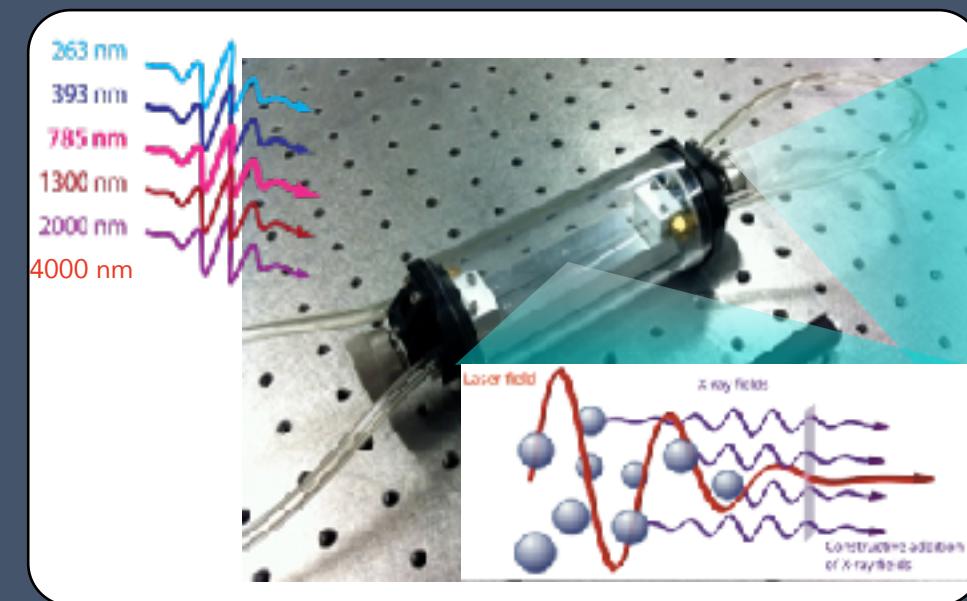
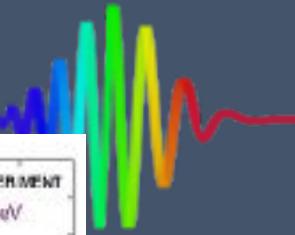
⁷Kfir, et al. *Nat. Photon.*, **9**, 2015

⁸Dorney, et al. *PRL*, **119**, 2017

⁹Dorney, et al. *Nat. Photon.* **1**, 2019

¹⁰Rego and Dorney, et al. *Science*, **364**, 2019

HHG in the Lab: Tailored EUV and Soft X-ray Beams with Laser-Like Spatiotemporal Coherence on a Tabletop



¹Rundquist, et al. *Science*, **280**, 1998

²Bartels, et al. *Science* **297**, 2002

³Zhang, et al. *Opt. Lett.* **29**, 2004

⁴Popmintchev, et al. *Science*, **350**, 2015 (**UV drivers**)

⁵Chen, et al. *PRL*, **105**, 2010

⁶Popmintchev, et al. *Science*, **336**, 2012 (**mid-IR drivers**)

⁷Kfir, et al. *Nat. Photon.*, **9**, 2015

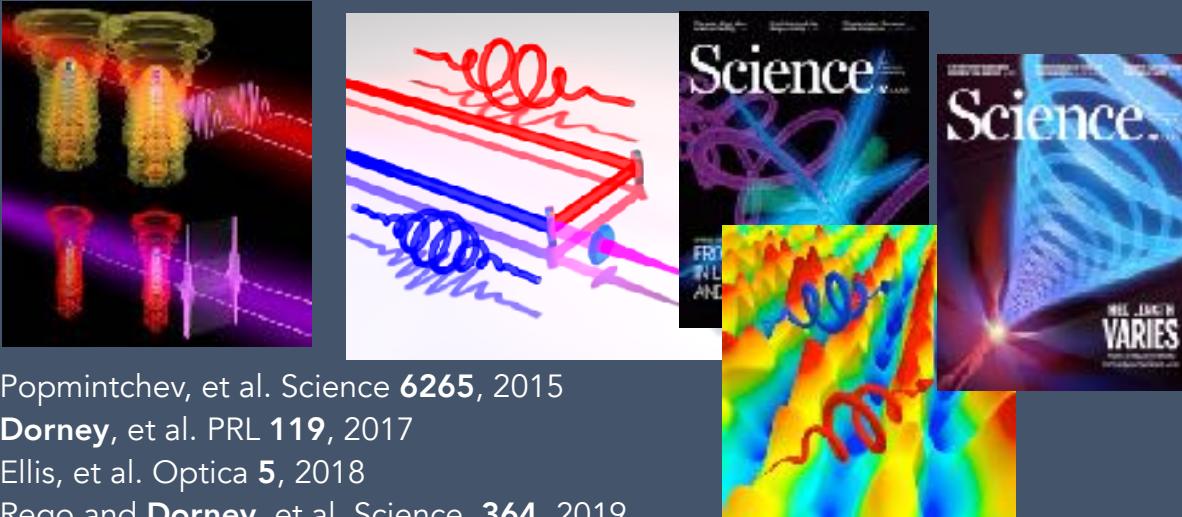
⁸Dorney, et al. *PRL*, **119**, 2017

⁹Dorney, et al. *Nat. Photon.* **1**, 2019

¹⁰Rego and Dorney, et al. *Science*, **364**, 2019

Light and Materials Science in the KM Group: AMO Dynamics at Extreme Spatial and Temporal Scales

New Paradigms in Attosecond Nonlinear Optics



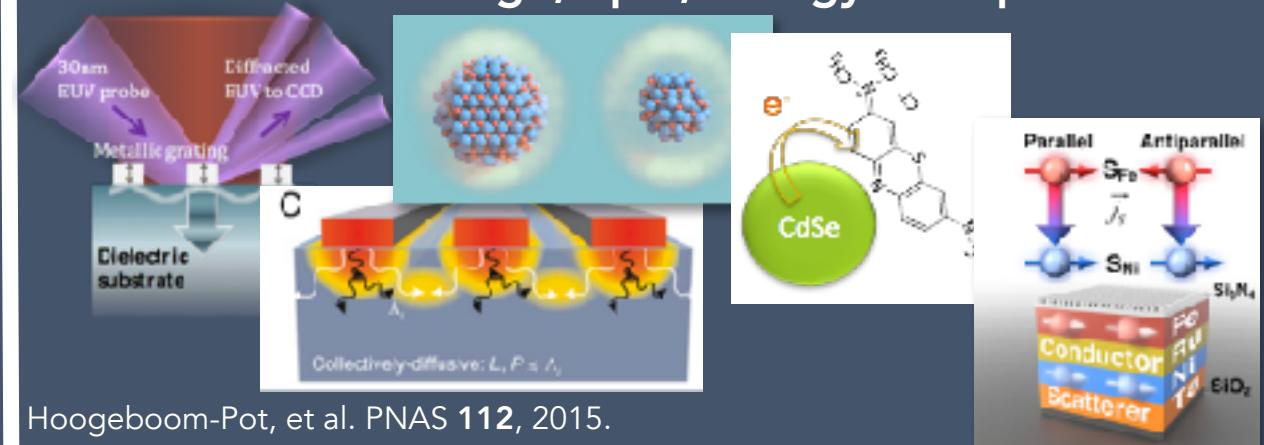
Ultrafast Coherent X-ray Imaging



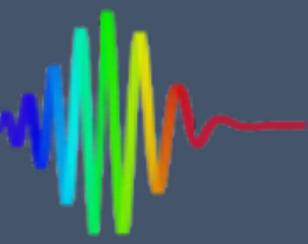
Uncovering New Ultrafast Materials Science



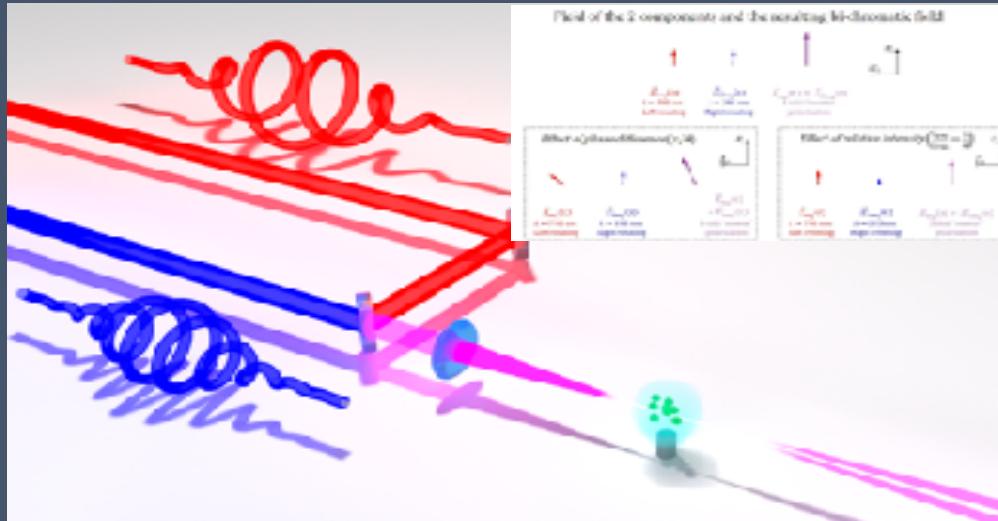
Nanoscale Charge, Spin, Energy Transport



Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG



Spin Angular Momentum (SAM) in HHG



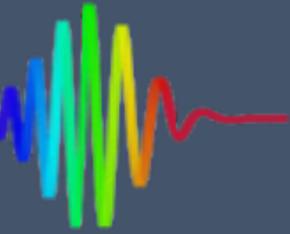
Eichmann, et al. PRA **51**, 1995

Long, et al. PRA **52**, 1995

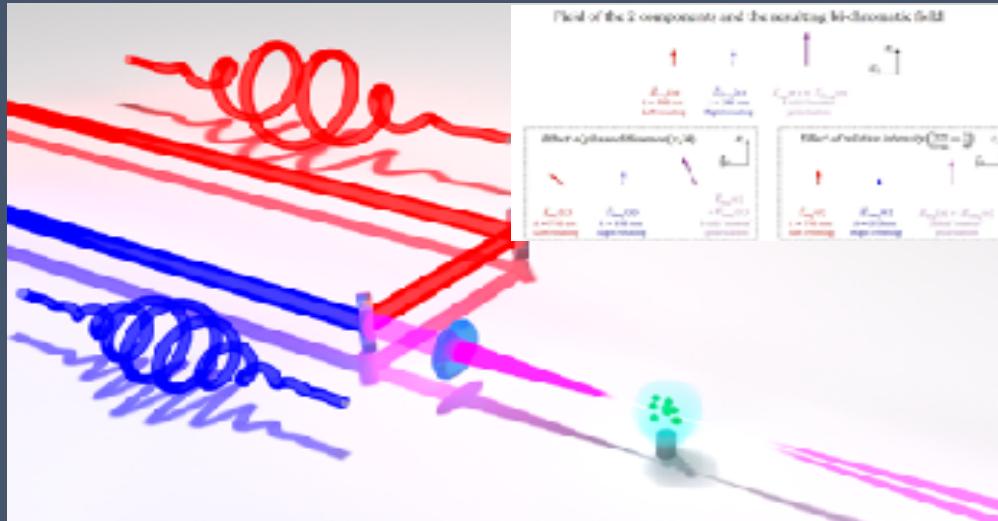
Milosevic & Becker. PRA, **62**, 2000

Kfir, et al. Nat. Photon. **9**, 2015

Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG

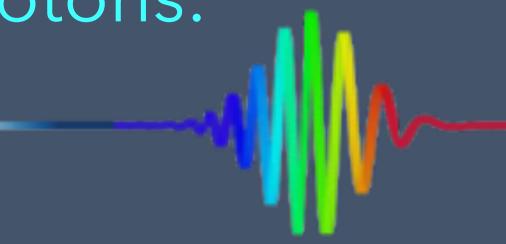


Spin Angular Momentum (SAM) in HHG

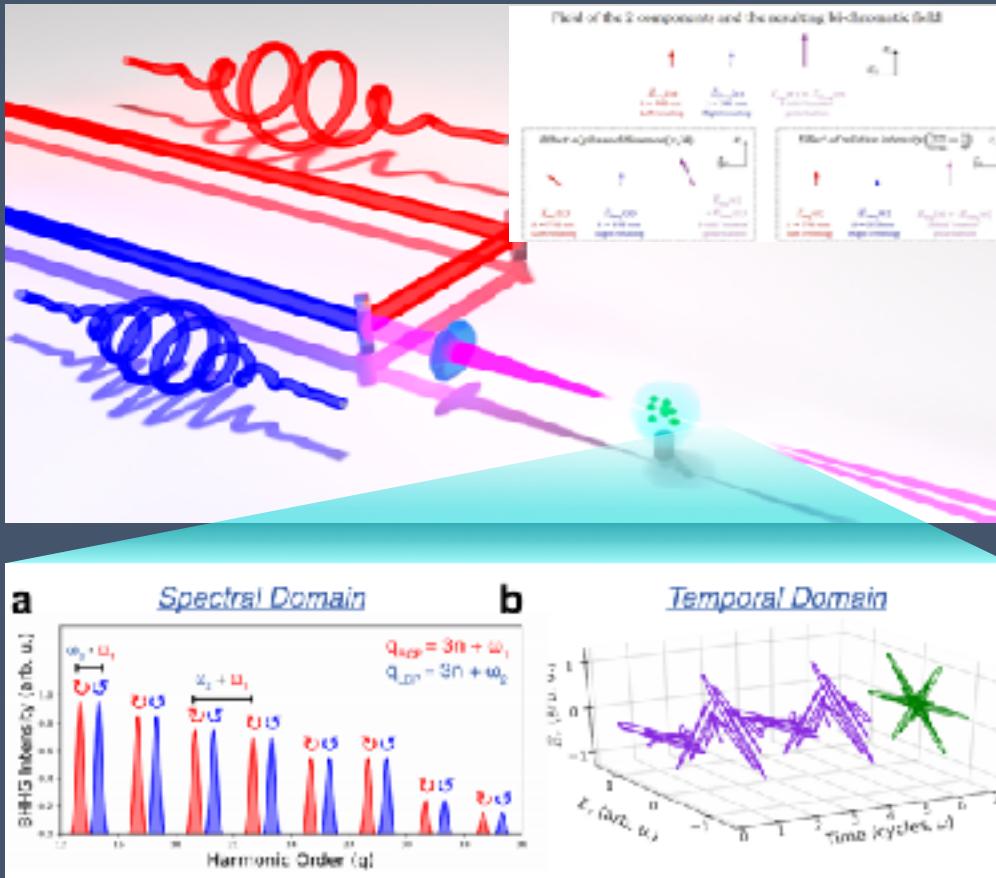


Eichmann, et al. PRA **51**, 1995
Long, et al. PRA **52**, 1995
Milosevic & Becker. PRA, **62**, 2000
Kfir, et al. Nat. Photon. **9**, 2015

Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG



Spin Angular Momentum (SAM) in HHG



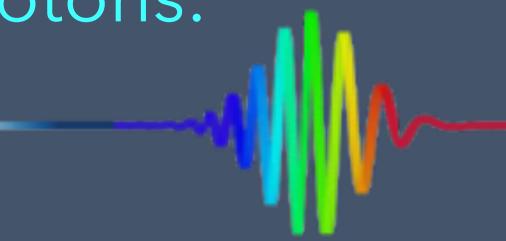
Eichmann, et al. PRA **51**, 1995

Long, et al. PRA **52**, 1995

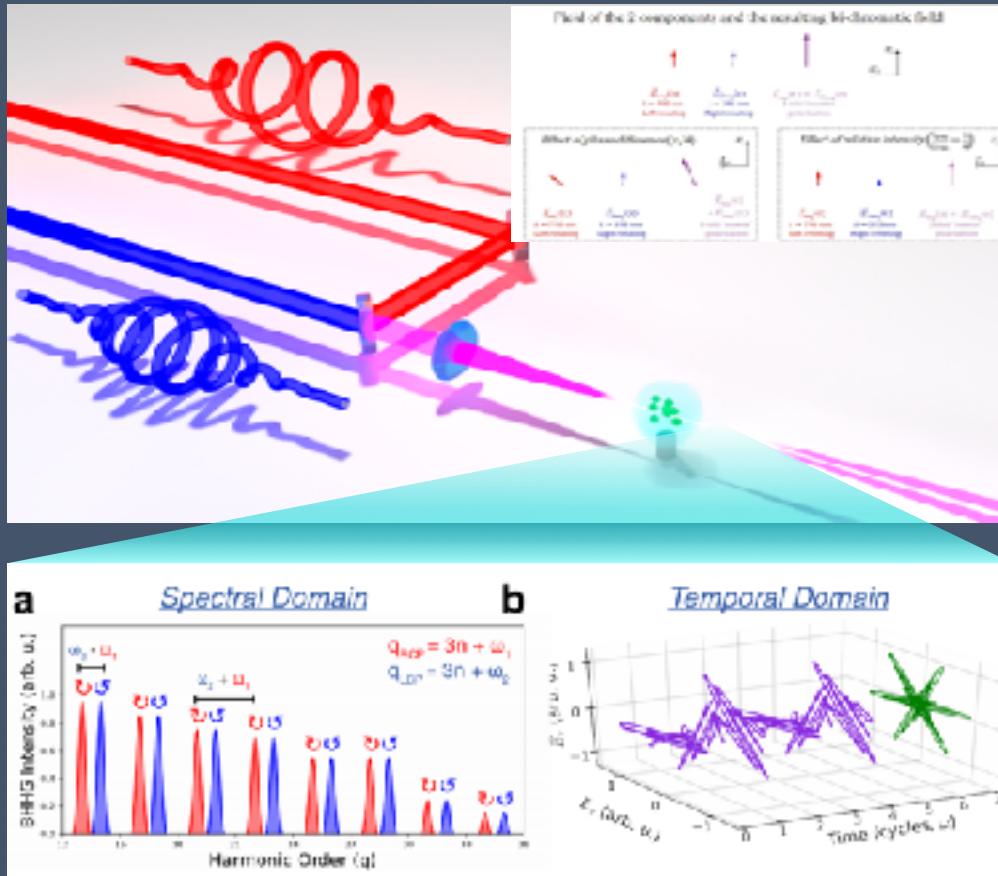
Milosevic & Becker. PRA, **62**, 2000

Kfir, et al. Nat. Photon. **9**, 2015

Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG



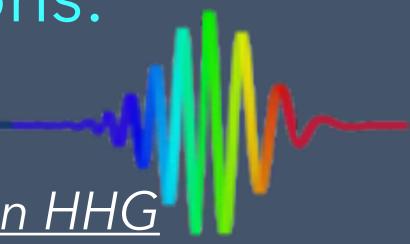
Spin Angular Momentum (SAM) in HHG



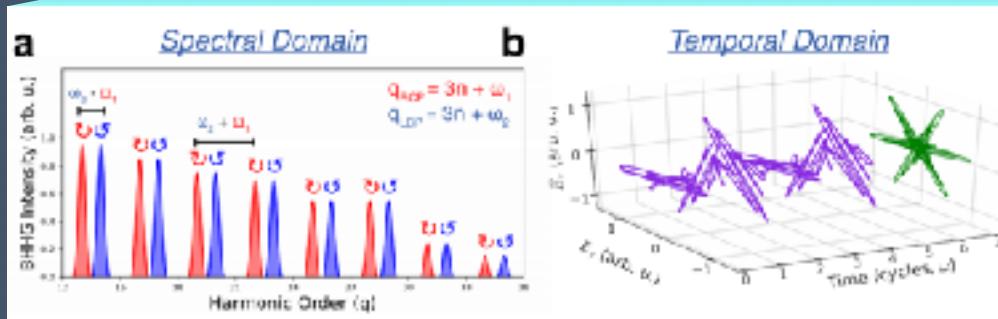
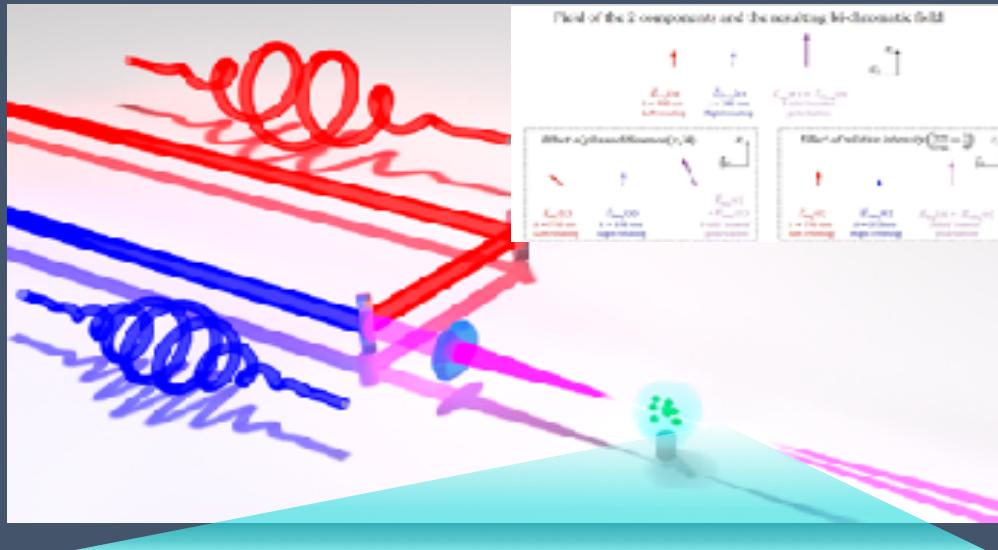
Eichmann, et al. PRA **51**, 1995
Long, et al. PRA **52**, 1995
Milosevic & Becker. PRA, **62**, 2000
Kfir, et al. Nat. Photon. **9**, 2015

Many, many more!
“Circularly polarized HHG”
>170 papers (>2015, G-Scholar)

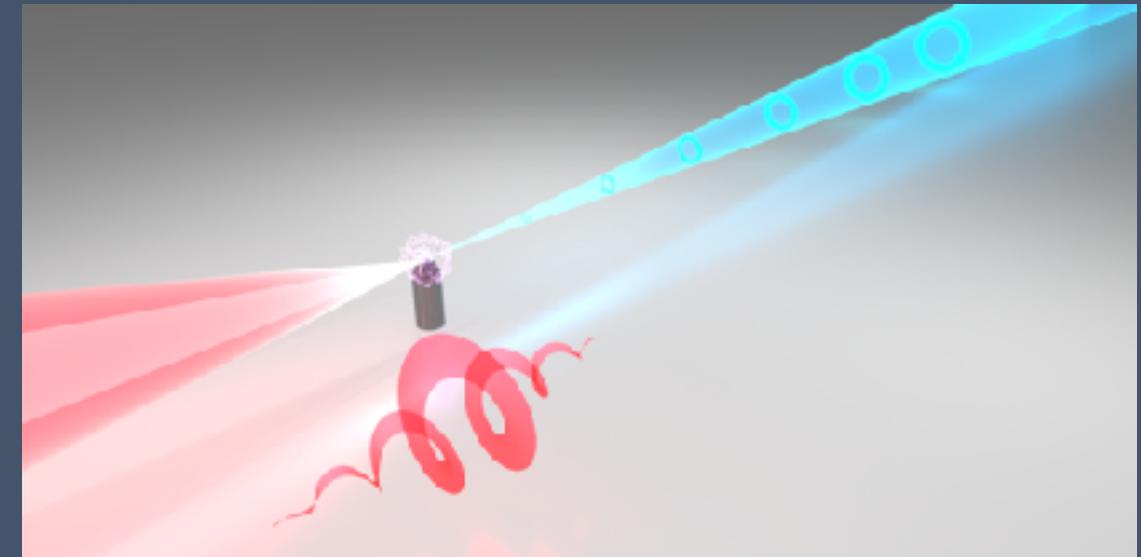
Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG



Spin Angular Momentum (SAM) in HHG



Orbital Angular Momentum (OAM) in HHG

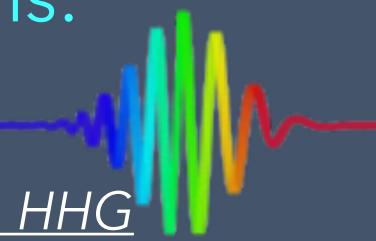


Eichmann, et al. PRA **51**, 1995
 Long, et al. PRA **52**, 1995
 Milosevic & Becker. PRA, **62**, 2000
 Kfir, et al. Nat. Photon. **9**, 2015

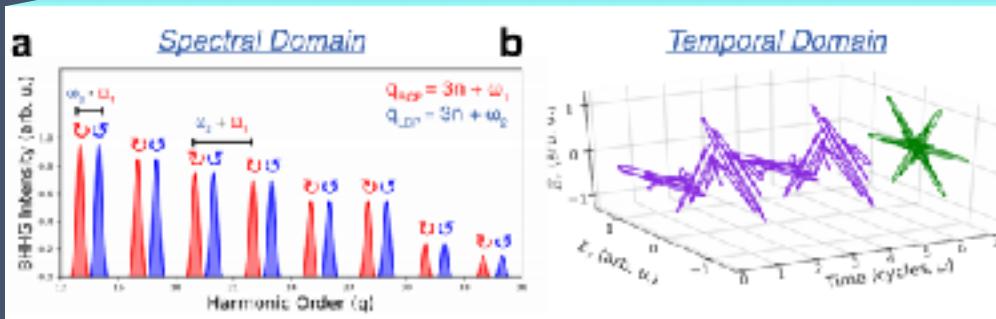
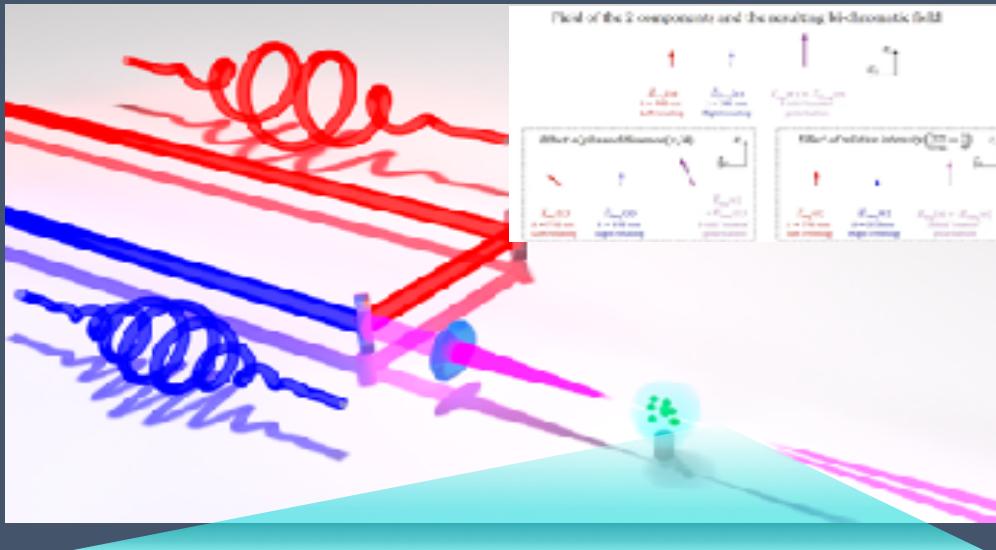
Many, many more!

"Circularly polarized HHG"
>170 papers (>2015, G-Scholar)

Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG



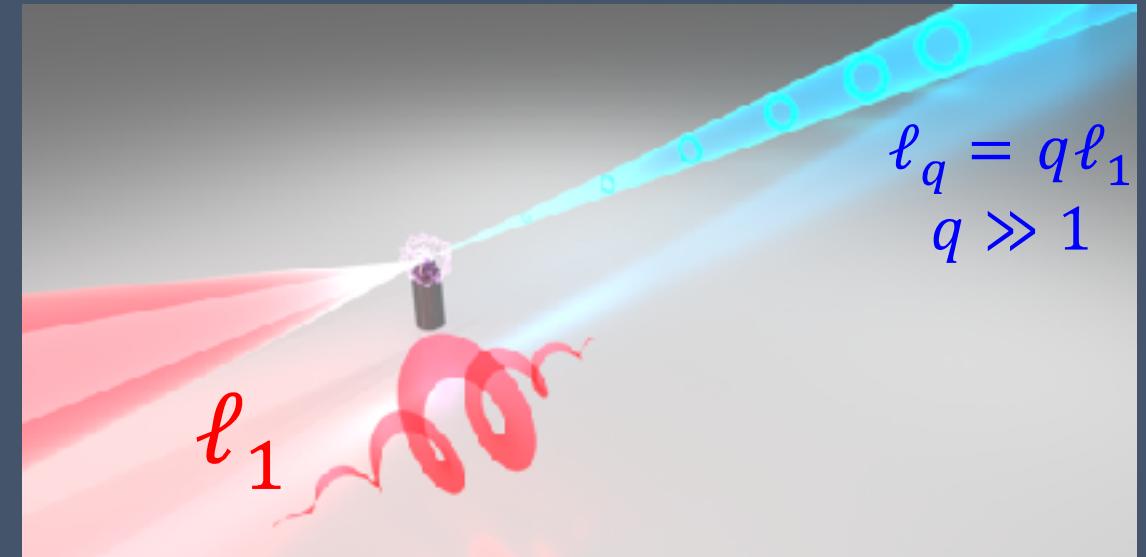
Spin Angular Momentum (SAM) in HHG



Eichmann, et al. PRA **51**, 1995
 Long, et al. PRA **52**, 1995
 Milosevic & Becker. PRA, **62**, 2000
 Kfir, et al. Nat. Photon. **9**, 2015

Many, many more!
"Circularly polarized HHG"
>170 papers (>2015, G-Scholar)

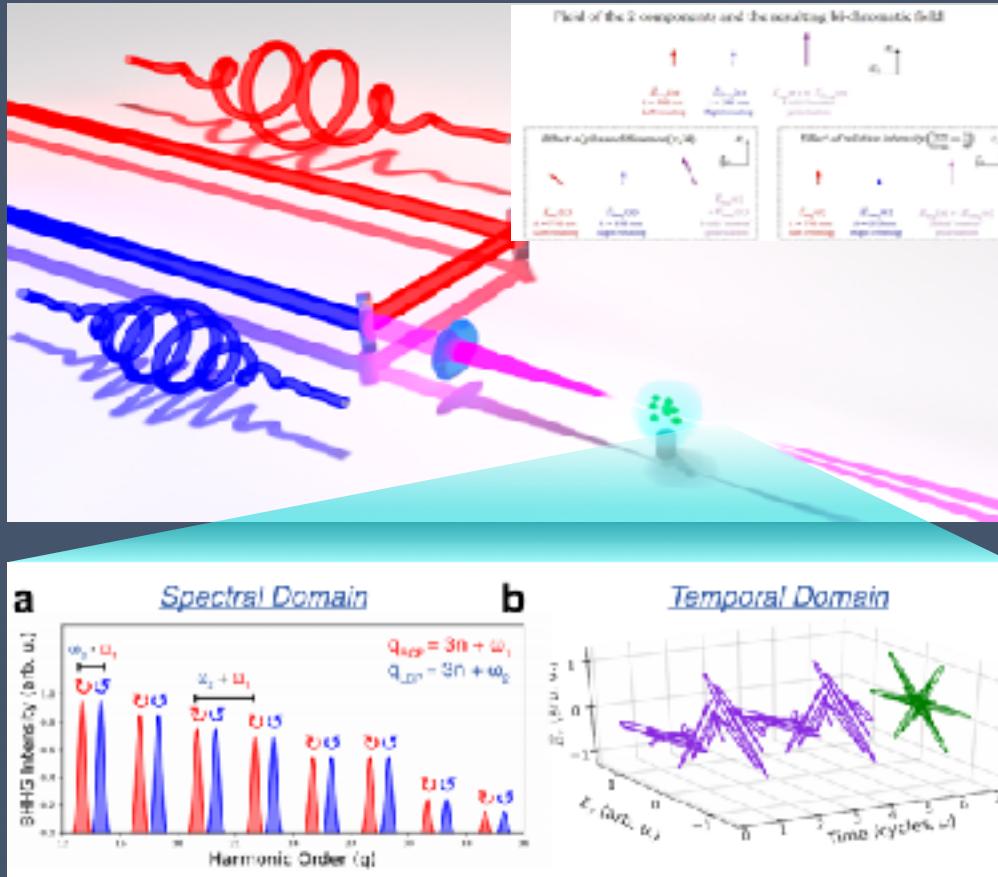
Orbital Angular Momentum (OAM) in HHG



- Zürch, et al. *Nat. Phys.* **8**, 2012
 Hernández-García, et al. *PRL*, **111**, 2013
 Gareipy, et al. *PRL* **113**, 2014
 Rego et al. *PRL*, **116**, 2016
 Géneaux, et al. *Nat. Commun.* **7**, 2016
 Kong, et al. *Nat. Commun.* **8**, 2017
 Gauthier, et al. *Nat. Commun.* **8**, 2017
 Dorney, et al. *Nat. Photon.* **1**, 2019
 Rego and Dorney, et al. *Science*, **364** 2019

Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG

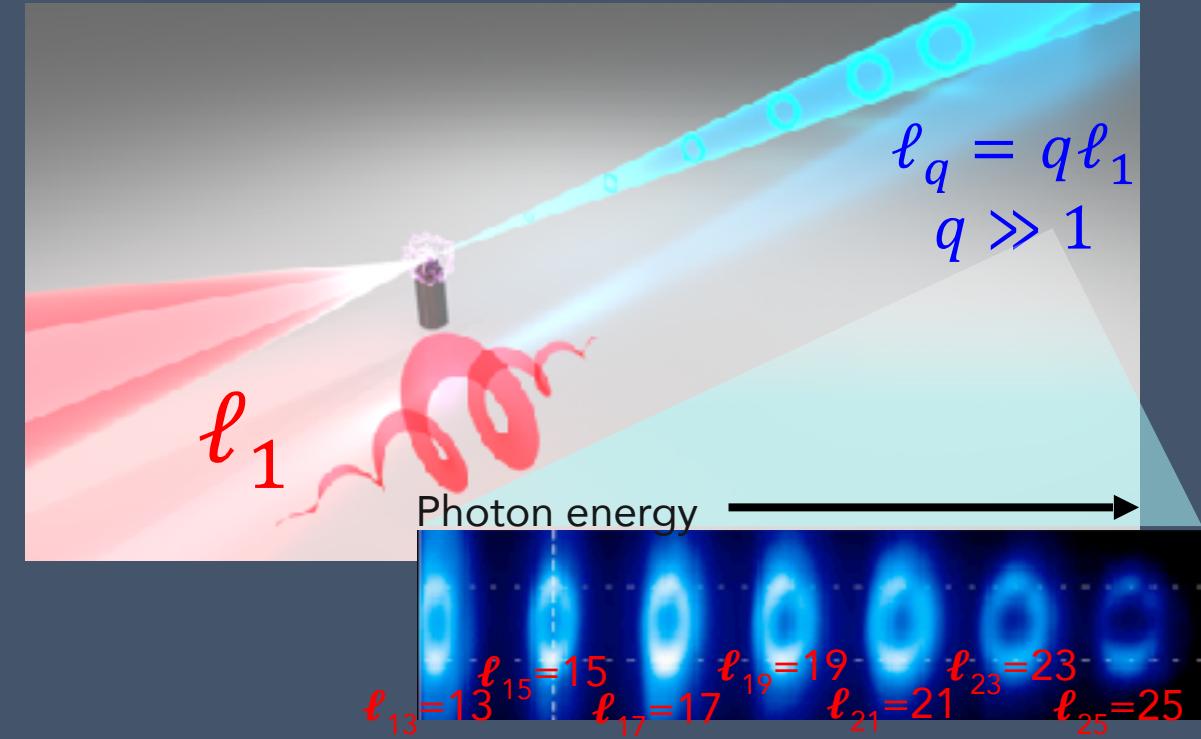
Spin Angular Momentum (SAM) in HHG



Eichmann, et al. PRA **51**, 1995
 Long, et al. PRA **52**, 1995
 Milosevic & Becker. PRA, **62**, 2000
 Kfir, et al. Nat. Photon. **9**, 2015

Many, many more!
"Circularly polarized HHG"
>170 papers (>2015, G-Scholar)

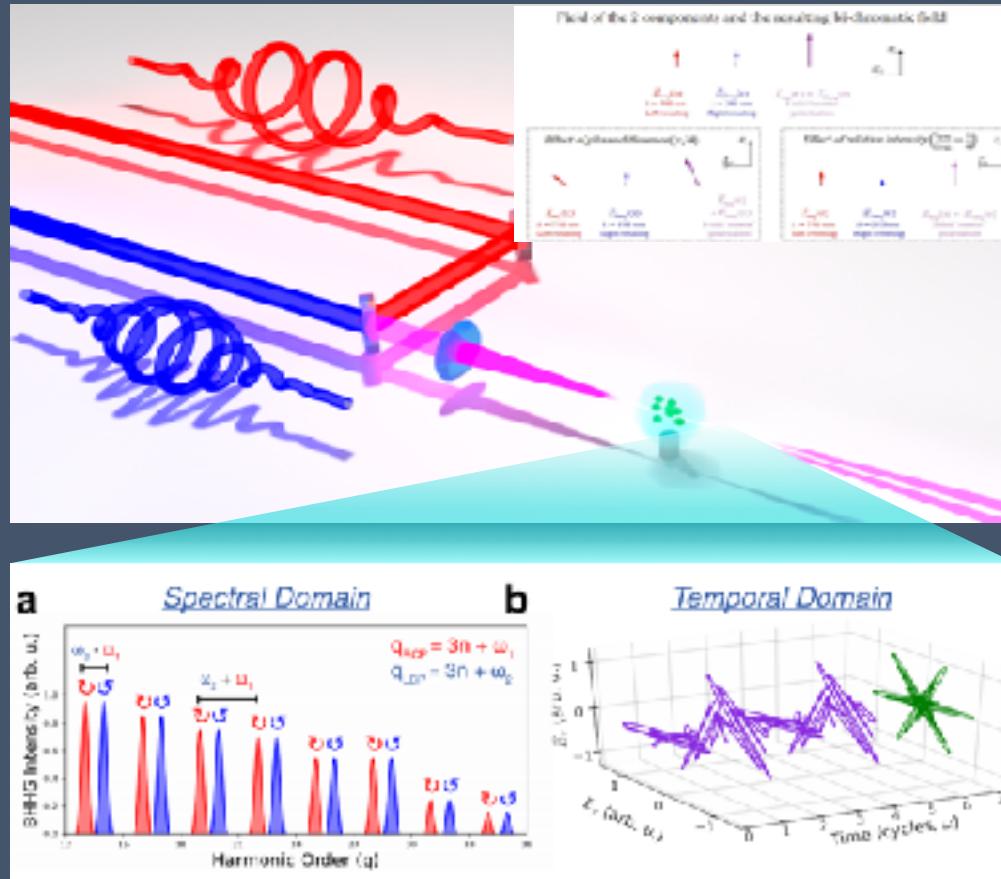
Orbital Angular Momentum (OAM) in HHG



Zürch, et al. *Nat. Phys.* **8**, 2012
 Hernández-García, et al. *PRL*, **111**, 2013
 Gareipy, et al. *PRL* **113**, 2014
 Rego et al. *PRL*, **116**, 2016
 Géneaux, et al. *Nat. Commun.* **7**, 2016
 Kong, et al. *Nat. Commun.* **8**, 2017
 Gauthier, et al. *Nat. Commun.* **8**, 2017
 Dorney, et al. *Nat. Photon.* **1**, 2019
 Rego and Dorney, et al. *Science*, **364** 2019

Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG

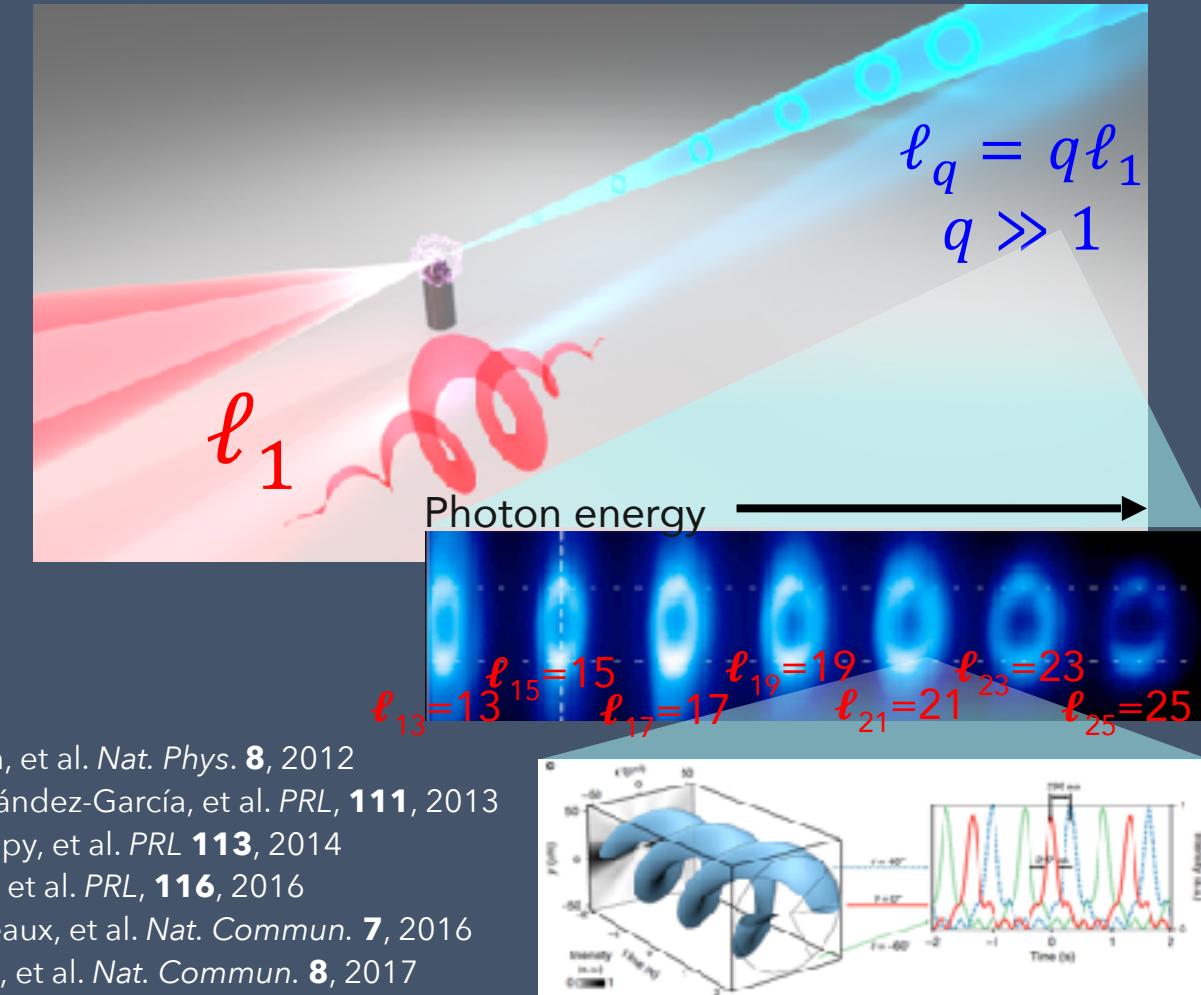
Spin Angular Momentum (SAM) in HHG



Eichmann, et al. PRA **51**, 1995
 Long, et al. PRA **52**, 1995
 Milosevic & Becker. PRA, **62**, 2000
 Kfir, et al. Nat. Photon. **9**, 2015

Many, many more!
"Circularly polarized HHG"
>170 papers (>2015, G-Scholar)

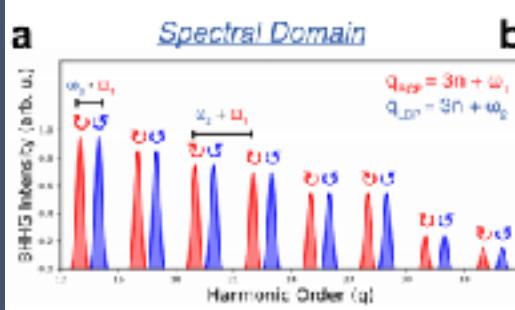
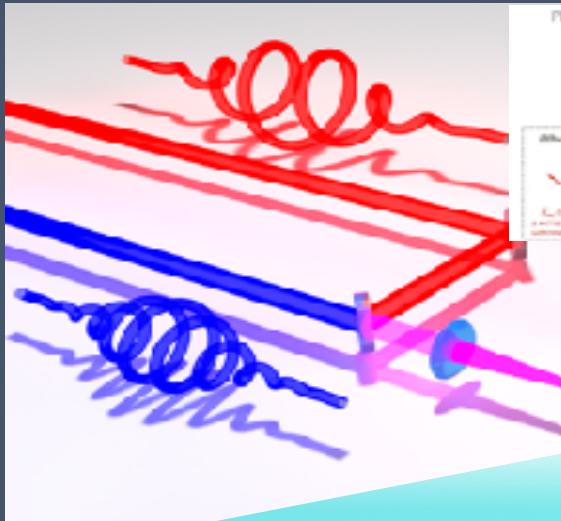
Orbital Angular Momentum (OAM) in HHG



Zürch, et al. Nat. Phys. **8**, 2012
 Hernández-García, et al. PRL, **111**, 2013
 Gareipy, et al. PRL **113**, 2014
 Rego et al. PRL, **116**, 2016
 Géneaux, et al. Nat. Commun. **7**, 2016
 Kong, et al. Nat. Commun. **8**, 2017
 Gauthier, et al. Nat. Commun. **8**, 2017
Dorney, et al. Nat. Photon. **1**, 2019
 Rego and **Dorney**, et al. Science, **364** 2019

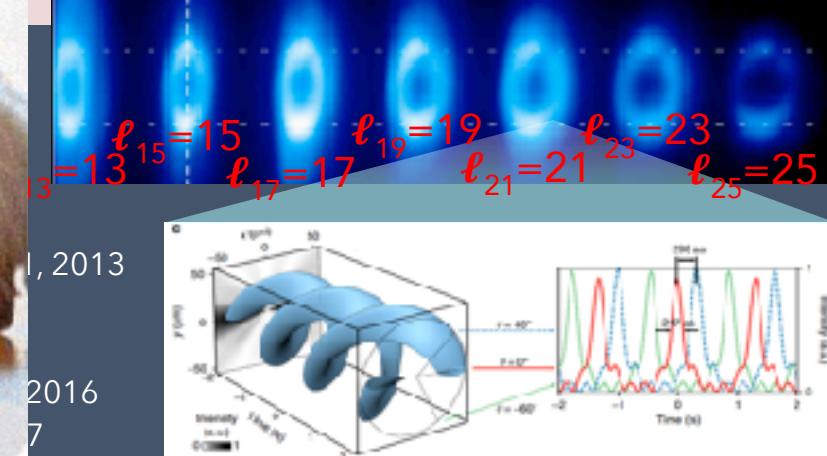
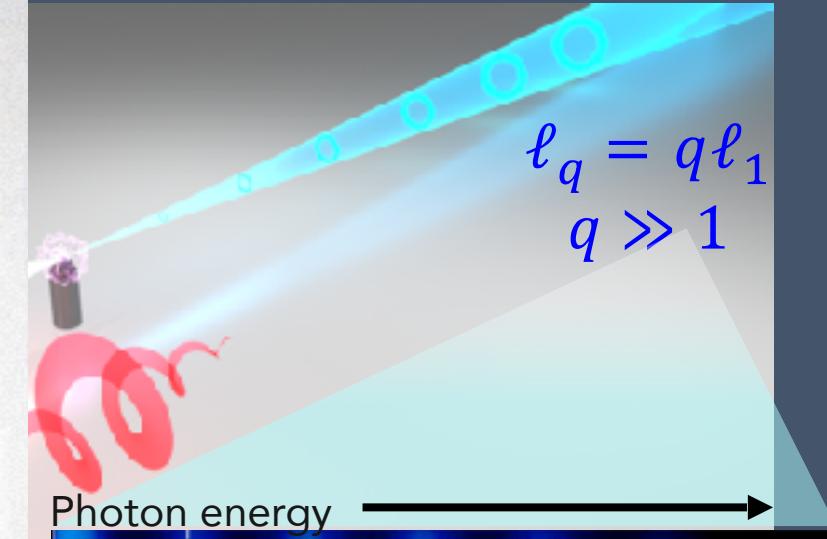
Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG

Spin Angular Momentum (SAM) in HHG



"Circularly polarized HHG"
>170 papers (>2015, G-Scholar)

Orbital Angular Momentum (OAM) in HHG



Eichmann, et al. PRA **51**, 1995

Long, et al. PRA **52**, 1995

Milosevic & Becker. PRA, **62**, 2000

Kfir, et al. Nat. Photon. **9**, 2015

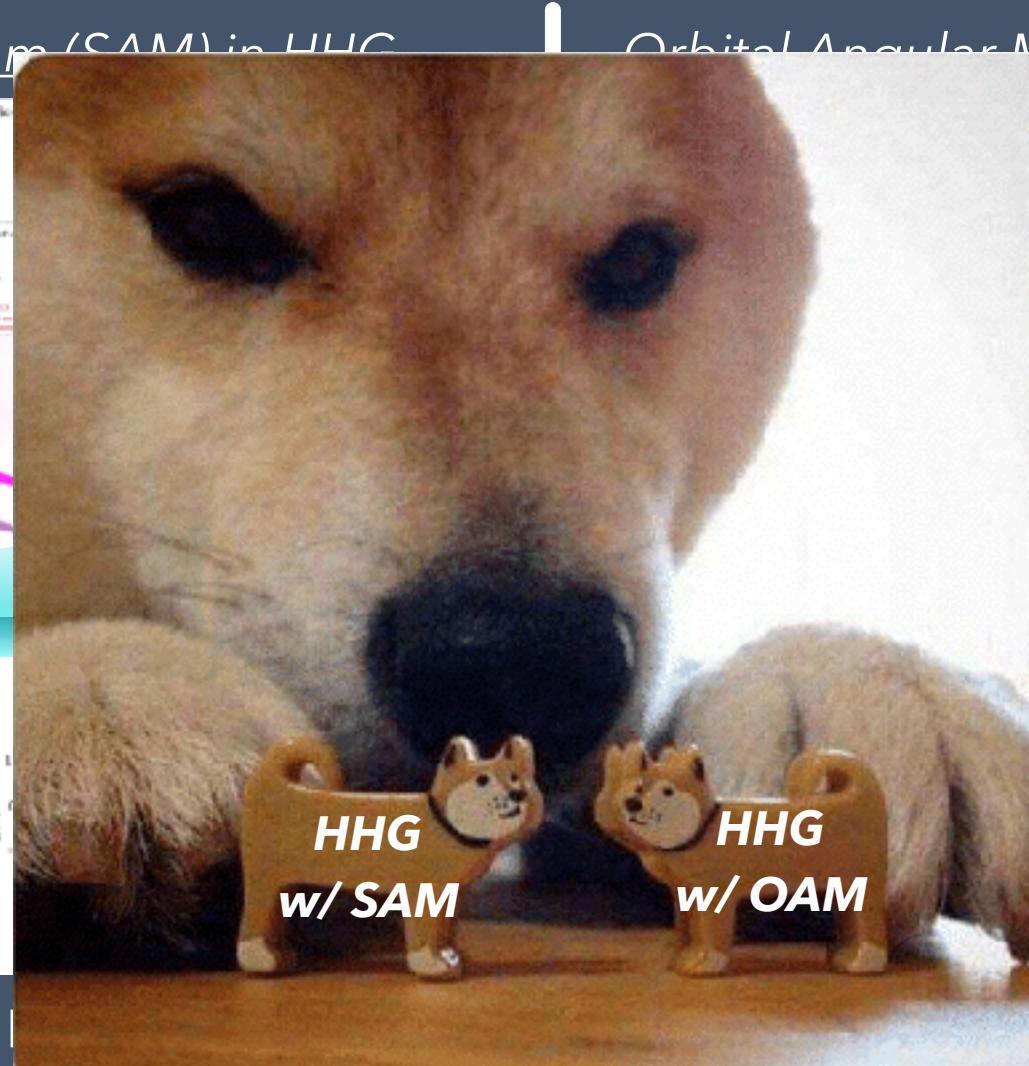
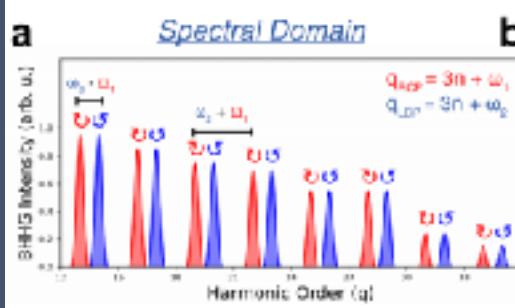
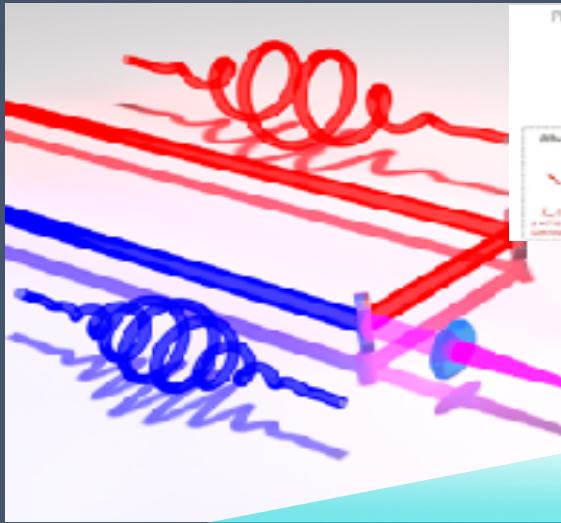
Gauthier, et al. Nat. Commun. **8**, 2017

Dorney, et al. Nat. Photon. **1**, 2019

Rego and Dorney, et al. Science, **364** 2019

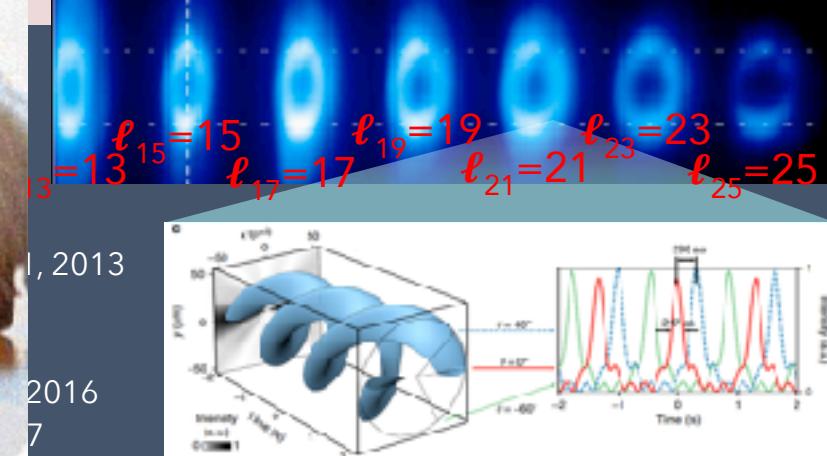
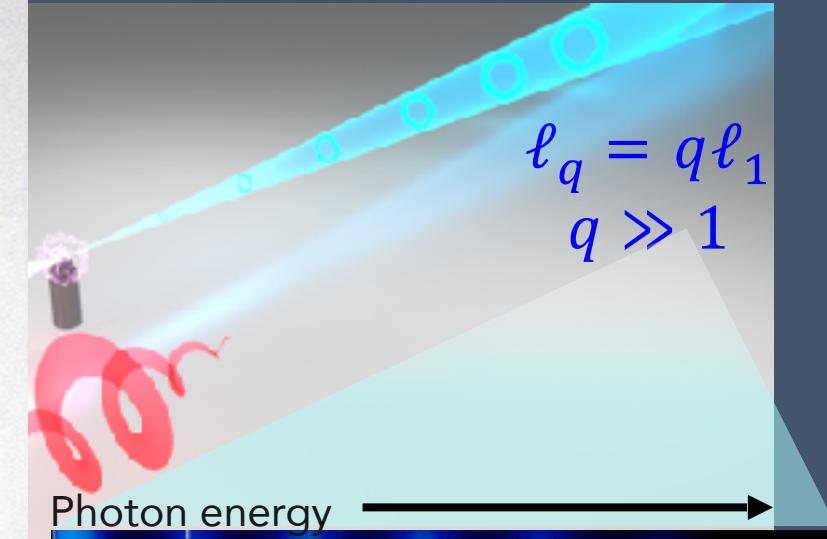
Attosecond Helical Field Lines and Twisted EUV Photons: Spin and Orbital Angular Momentum in HHG

Spin Angular Momentum (SAM) in HHG



"Circularly polarized HHG"
>170 papers (>2015, G-Scholar)

Orbital Angular Momentum (OAM) in HHG



Eichmann, et al. PRA **51**, 1995

Long, et al. PRA **52**, 1995

Milosevic & Becker. PRA, **62**, 2000

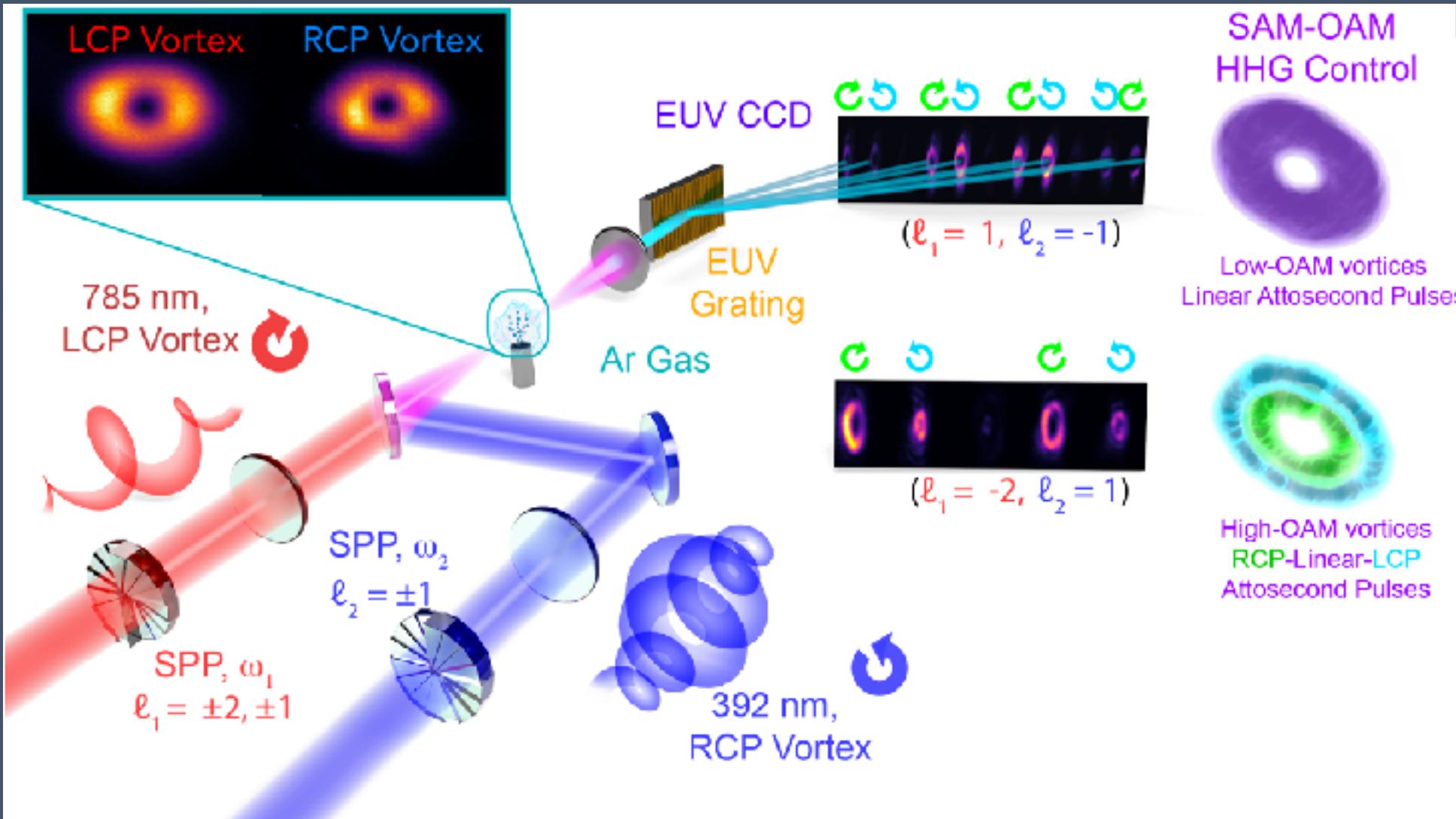
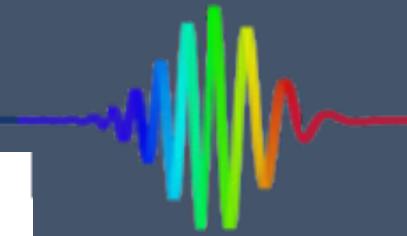
Kfir, et al. Nat. Photon. **9**, 2015

Gauthier, et al. Nat. Commun. **8**, 2017

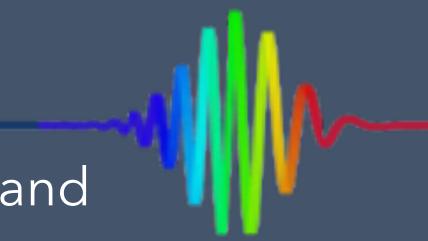
Dorney, et al. Nat. Photon. **1**, 2019

Rego and Dorney, et al. Science, **364** 2019

Two-Color HHG in the Presence of SAM and OAM: Exquisite Control of Attosecond, EUV Vortex Beams



Two-Color HHG in the Presence of SAM and OAM: Exquisite Control of Attosecond, EUV Vortex Beams



- High-harmonic generation is a parametric process, and thus must conserve energy and momentum (including SAM and OAM)

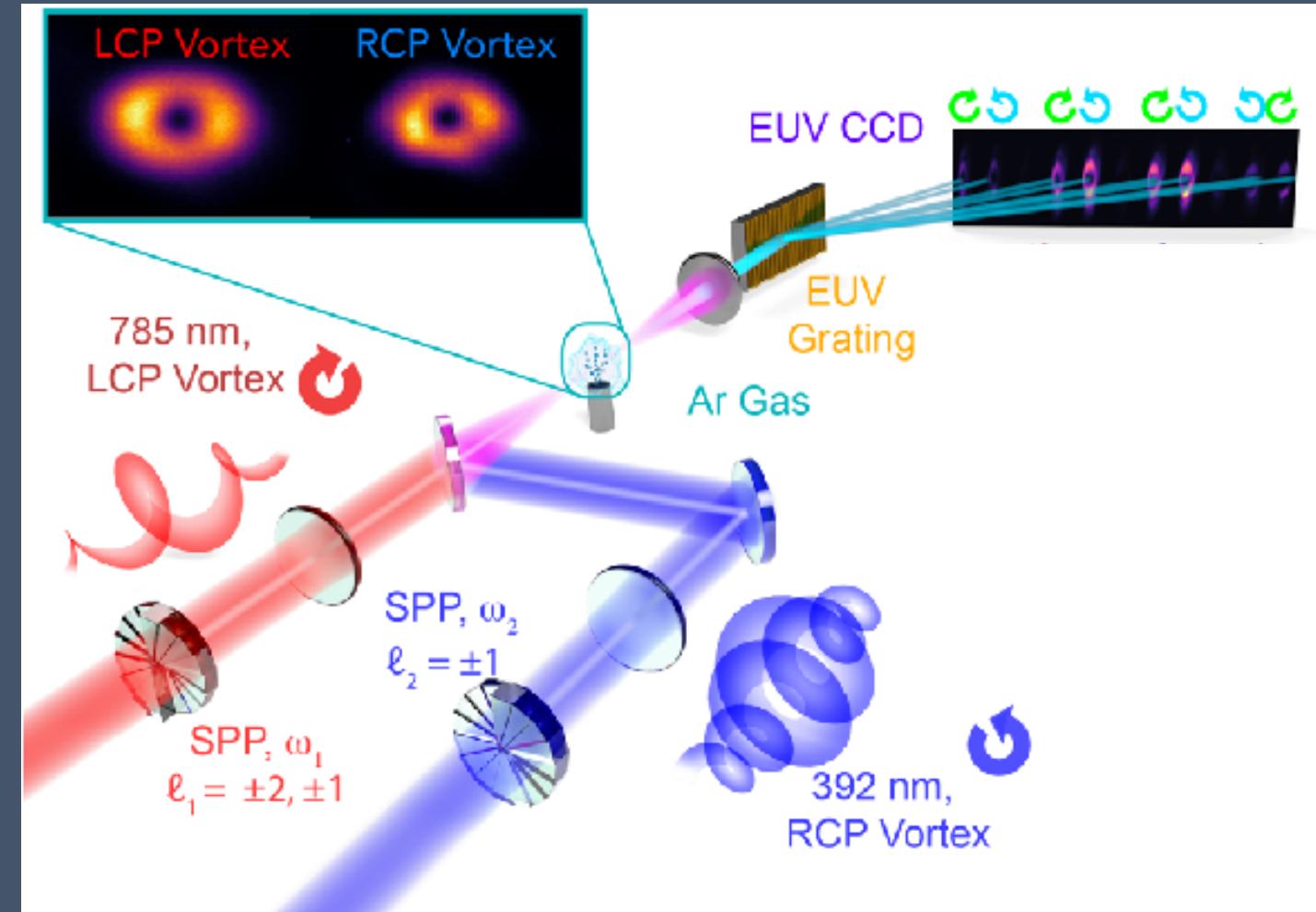
Constrain OAM via SAM!

$$\sigma_q = \mathbf{n}_1 \sigma_1 + \mathbf{n}_2 \sigma_2 \quad (\text{SAM})$$

$$\omega_q = \mathbf{n}_1 \omega_1 + \mathbf{n}_2 \omega_2 \quad (\text{Lin. Momentum})$$

$$\mathbf{n}_2 = \mathbf{n}_1 - \sigma_q \sigma_1 \quad (\text{Parity})$$

$$\ell_{q,q+1} = \frac{q + 2\sigma_q \sigma_{1,2}}{3} (\ell_1 + \ell_2) - \sigma_q \sigma_{1,2} \ell_{2,1}$$

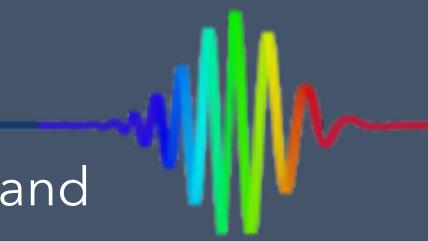


Paufler, et al. *PRA* **98**, 2018

Dorney, et al. *Nat. Photon.* **1**, 2019

Pisanty, et al. *PRL* **122**, 2019

Two-Color HHG in the Presence of SAM and OAM: Exquisite Control of Attosecond, EUV Vortex Beams



- High-harmonic generation is a parametric process, and thus must conserve energy and momentum (including SAM and OAM)

Constrain OAM via SAM!

$$\sigma_q = \mathbf{n}_1 \sigma_1 + \mathbf{n}_2 \sigma_2 \quad (\text{SAM})$$

$$\omega_q = \mathbf{n}_1 \omega_1 + \mathbf{n}_2 \omega_2 \quad (\text{Lin. Momentum})$$

$$\mathbf{n}_2 = \mathbf{n}_1 - \sigma_q \sigma_1 \quad (\text{Parity})$$

$$\ell_{q,q+1} = \frac{q + 2\sigma_q \sigma_{1,2}}{3} (\ell_1 + \ell_2) - \sigma_q \sigma_{1,2} \ell_{2,1}$$

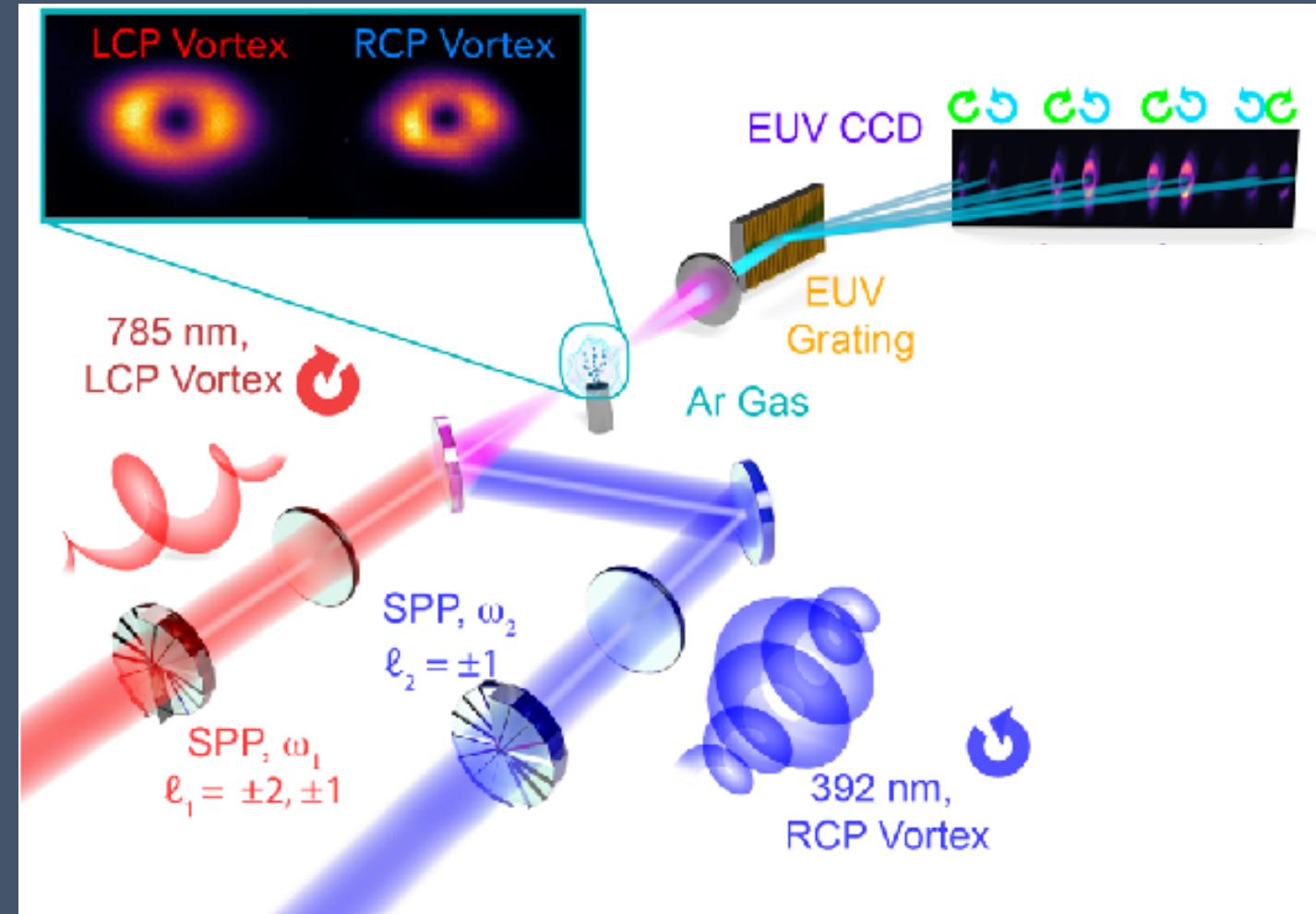
Torus-Knot Angular Momentum

$$J_\gamma = L + \gamma S = q \frac{\ell_1 + \ell_2}{3} \quad \therefore \gamma = \frac{2\ell_1 - \ell_2}{3}$$

Paufler, et al. *PRA* **98**, 2018

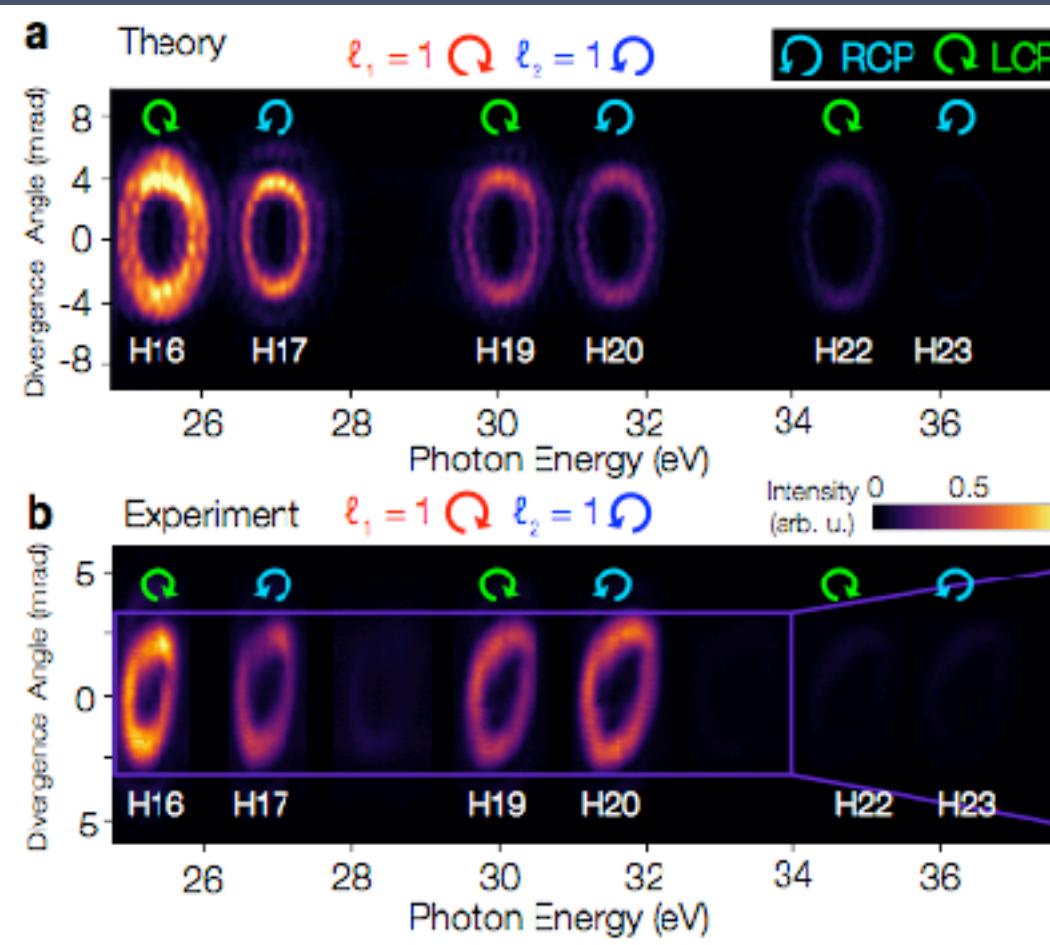
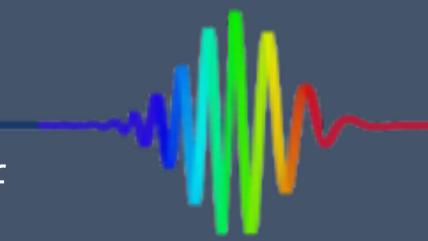
Dorney, et al. *Nat. Photon.* **1**, 2019

Pisanty, et al. *PRL* **122**, 2019



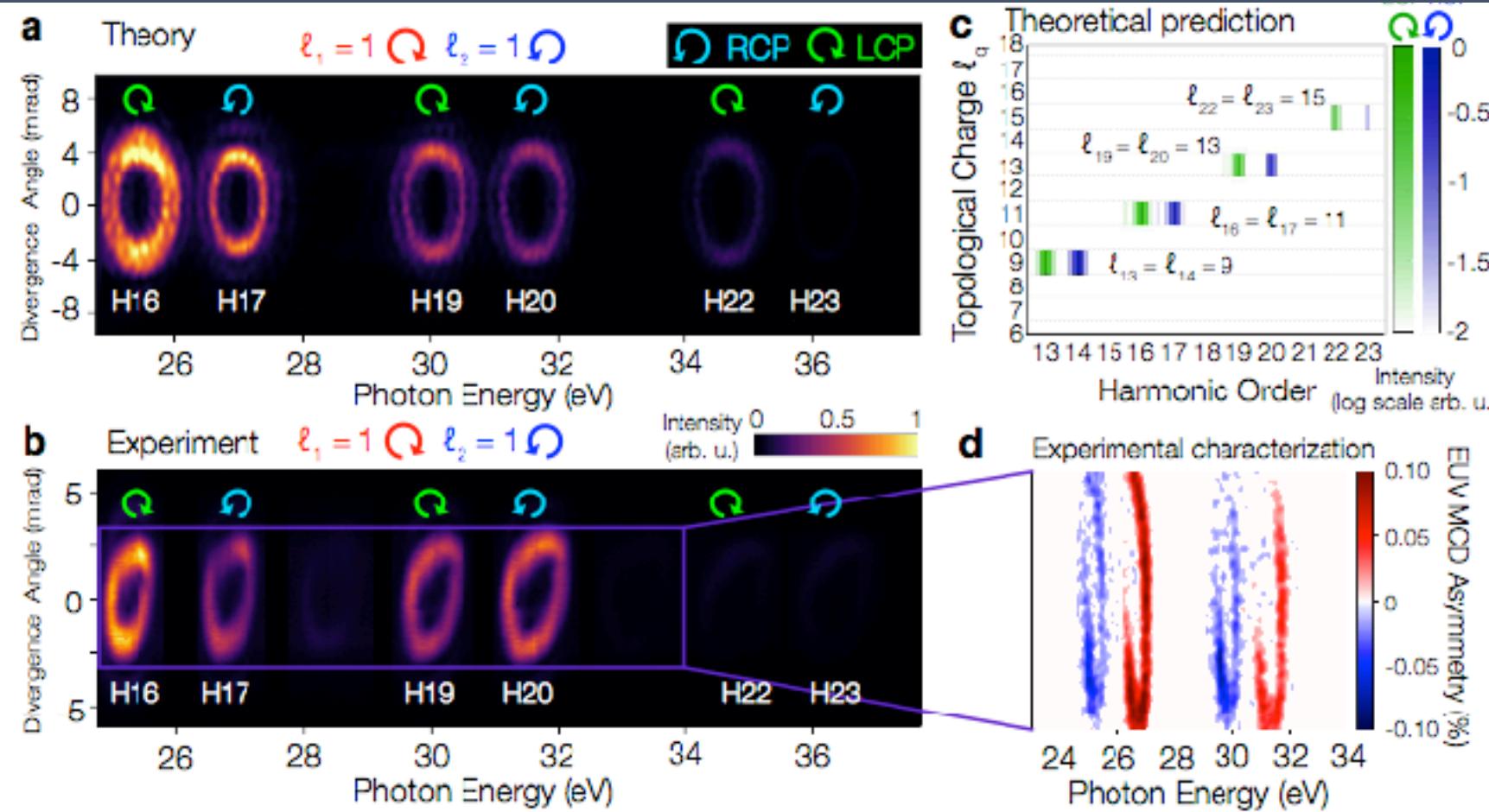
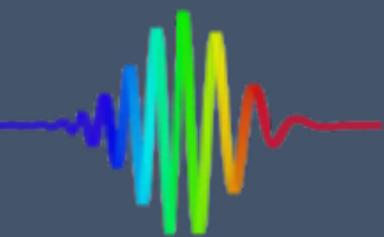
SAM-OAM HHG with Degenerate OAM Drivers: EUV Doughnuts with Same Twist, Opposite Helicity

- Driving the HHG process with a bicircular field with degenerate OAM yields pairs of EUV "doughnuts" with opposite helicity.



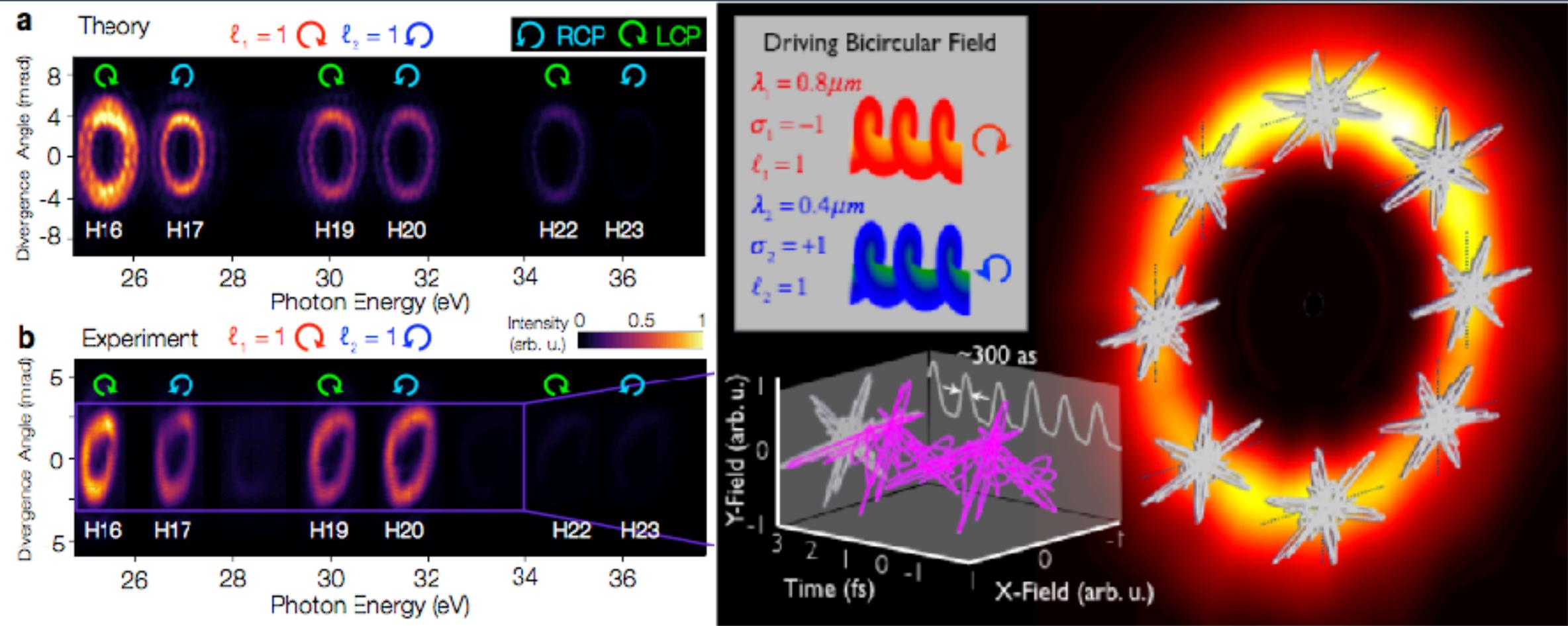
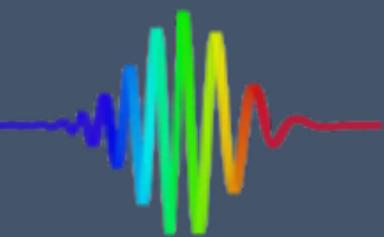
SAM-OAM HHG with Degenerate OAM Drivers: EUV Doughnuts with Same Twist, Opposite Helicity

- Driving the HHG process with a bicircular field with degenerate OAM yields pairs of EUV "doughnuts" with opposite helicity.

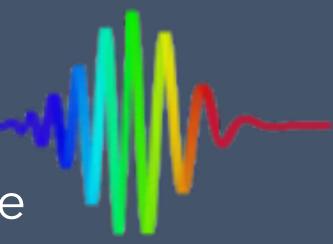


SAM-OAM HHG with Degenerate OAM Drivers: EUV Doughnuts with Same Twist, Opposite Helicity

- Driving the HHG process with a bicircular field with degenerate OAM yields pairs of EUV "doughnuts" with opposite helicity.

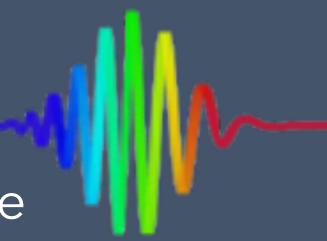


Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices



- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?

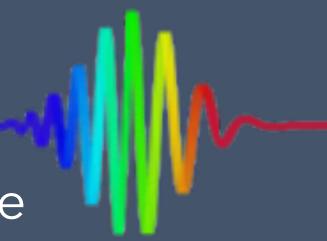
Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices



- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?

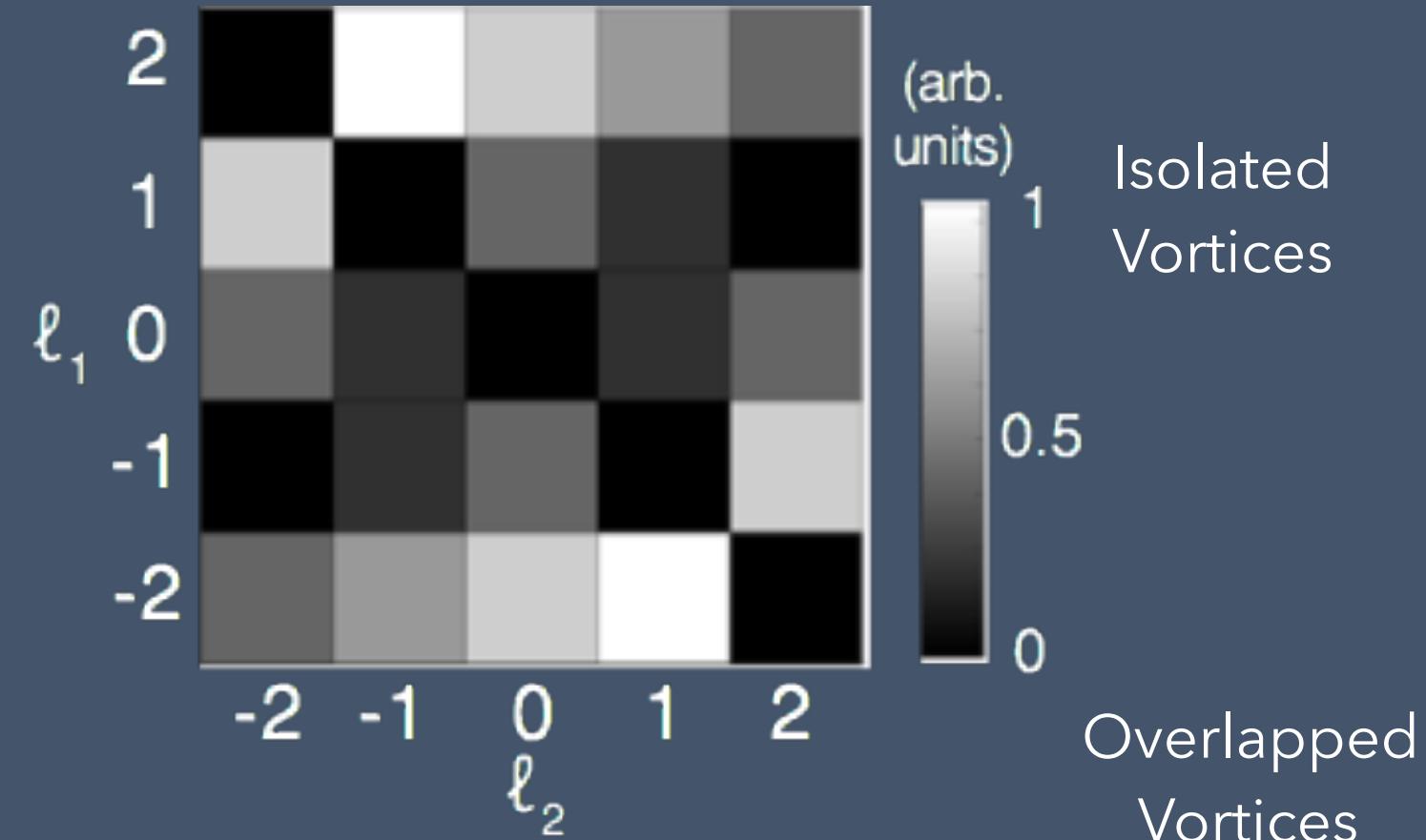
$$\Delta\beta \propto \frac{\ell_2\omega_1 - \ell_1\omega_2}{\omega_1 + \omega_2} \frac{|\ell_1 + \ell_2|}{\ell_1 + \ell_2}$$

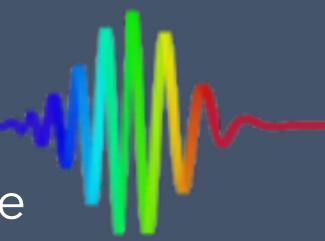
Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices



- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?

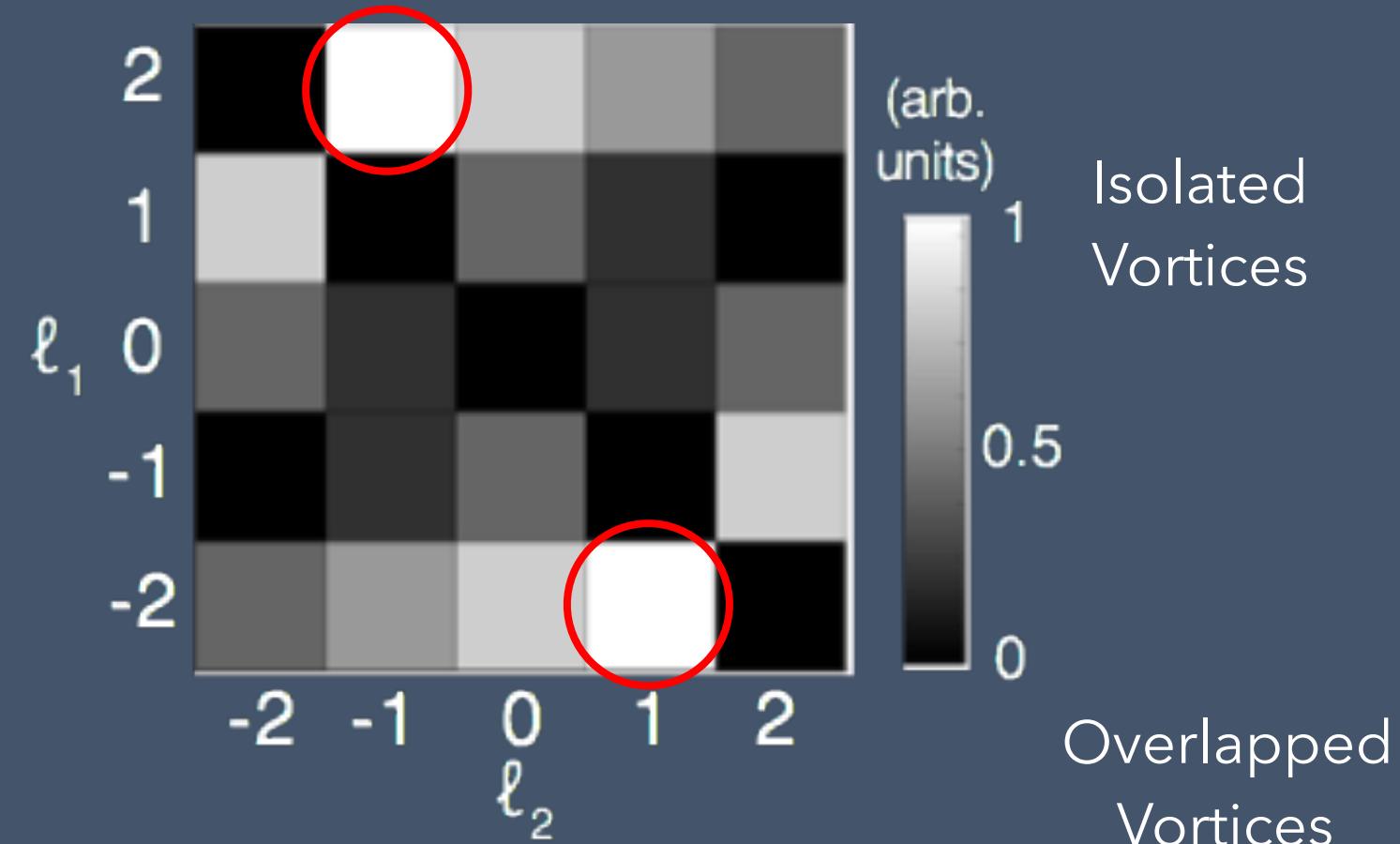
$$\Delta\beta \propto \frac{\ell_2\omega_1 - \ell_1\omega_2}{\omega_1 + \omega_2} \frac{|\ell_1 + \ell_2|}{\ell_1 + \ell_2}$$



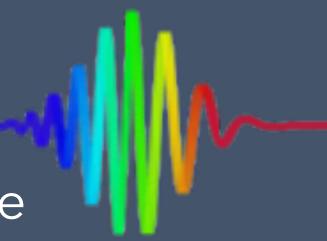
Controlling Divergence and Polarization in SAM-OAM HHG:
Spatially Isolated, Circularly Polarized, Attosecond Vortices

- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?

$$\Delta\beta \propto \frac{\ell_2\omega_1 - \ell_1\omega_2}{\omega_1 + \omega_2} \frac{|\ell_1 + \ell_2|}{\ell_1 + \ell_2}$$



Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices

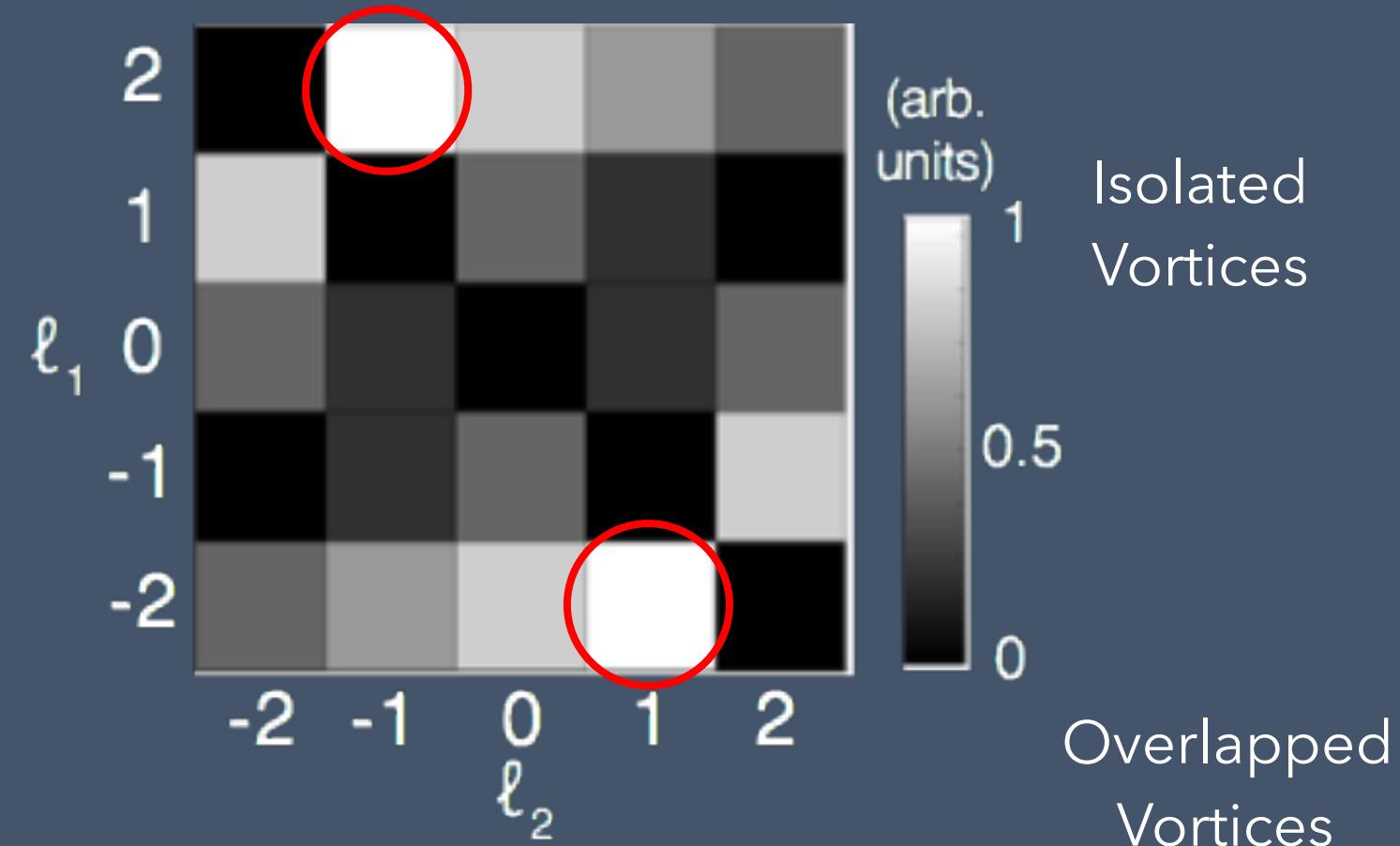


- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?

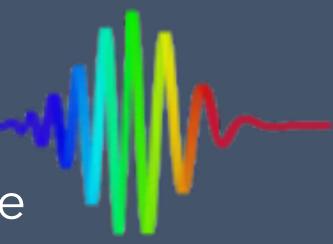
$$\Delta\beta \propto \frac{\ell_2\omega_1 - \ell_1\omega_2}{\omega_1 + \omega_2} \frac{|\ell_1 + \ell_2|}{\ell_1 + \ell_2}$$

Divergence of HHG is maximized when:

- 1) OAM of drivers are opposite in sign
- 2) OAM of drivers differs by 1

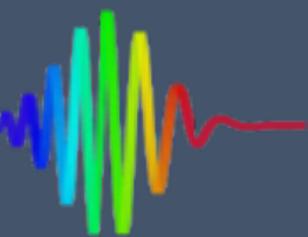


Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices

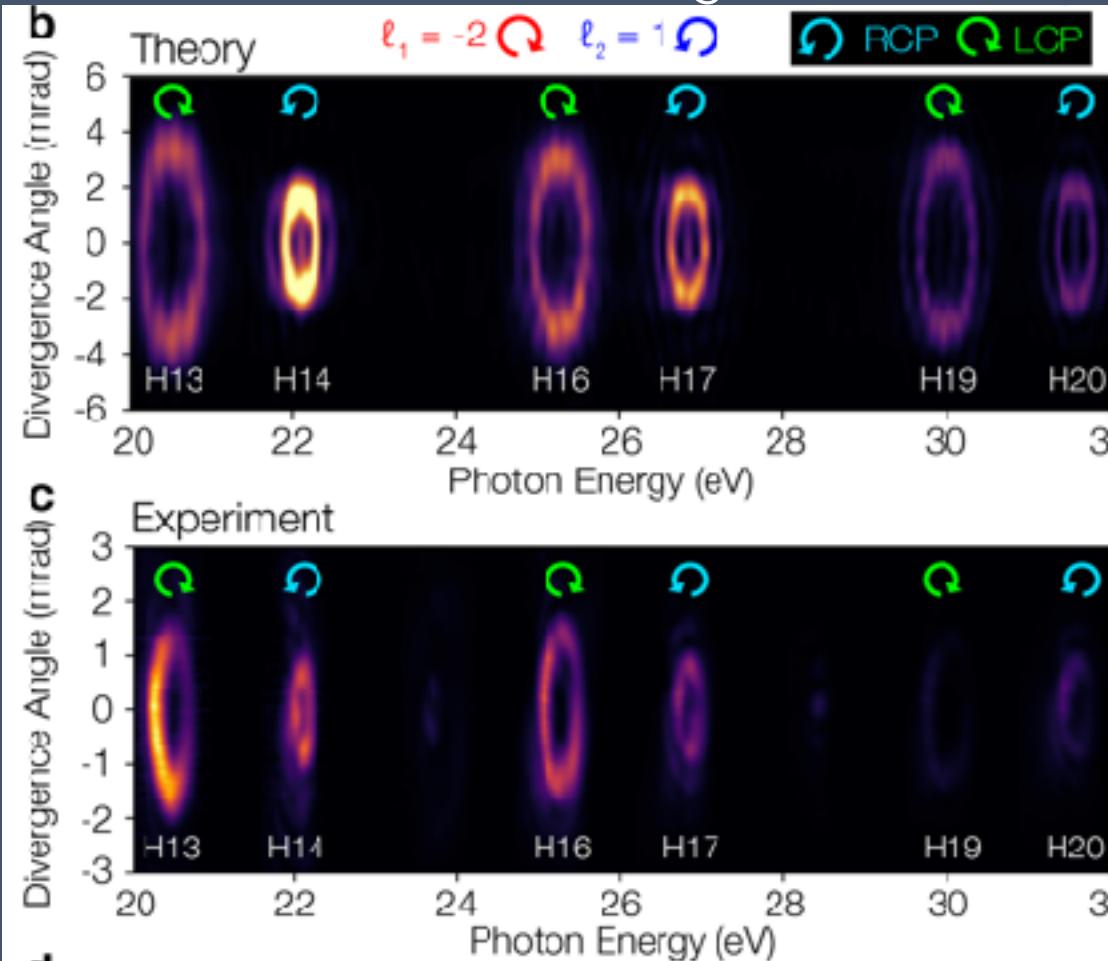


- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?

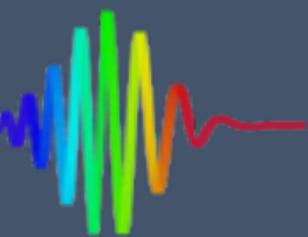
Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices



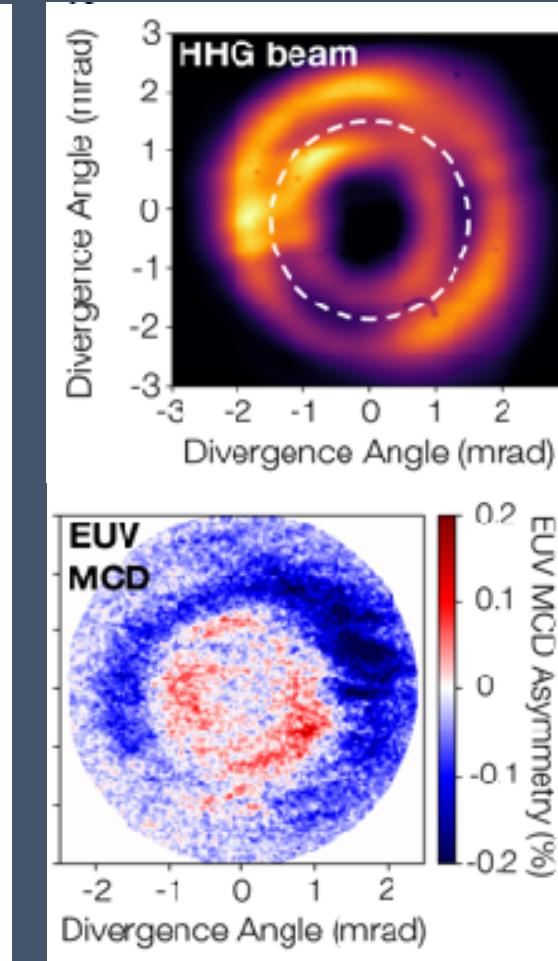
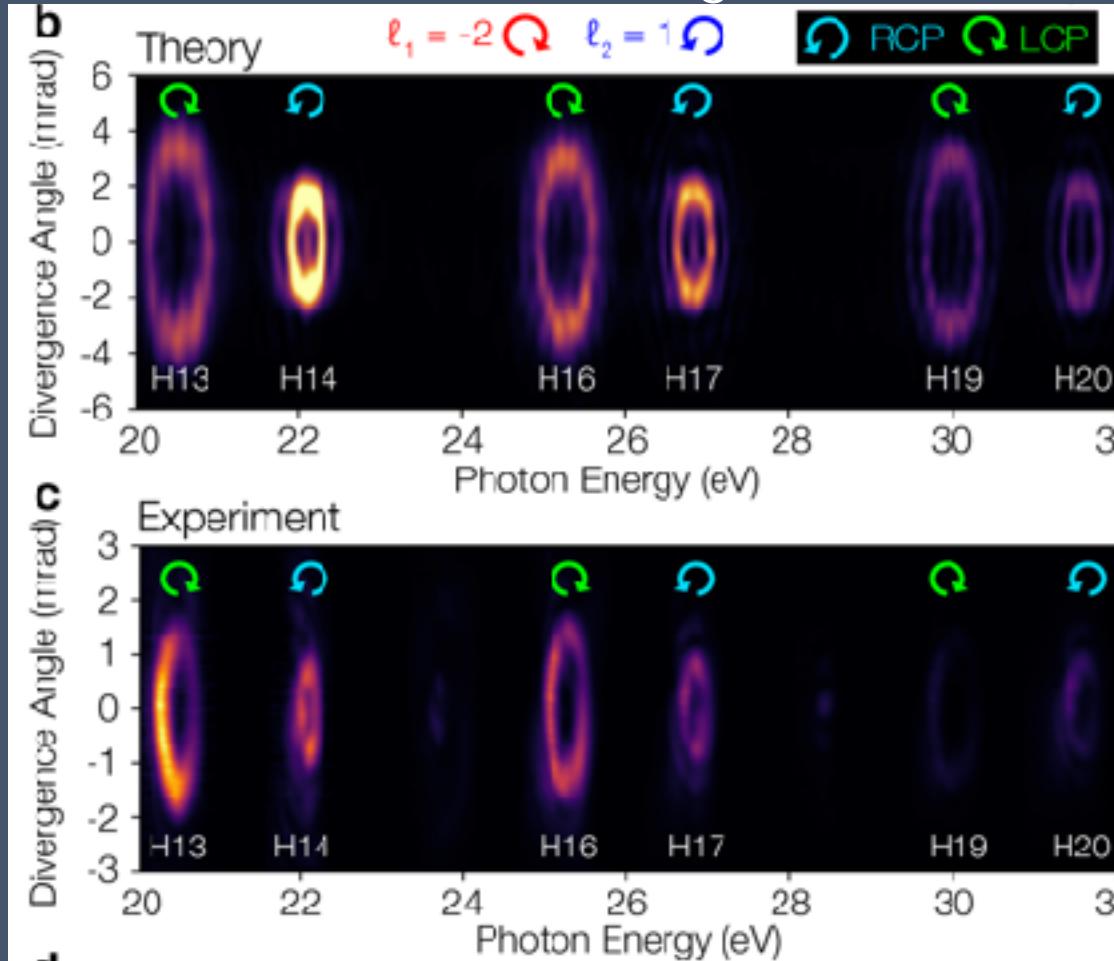
- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?



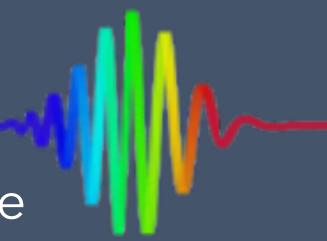
Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices



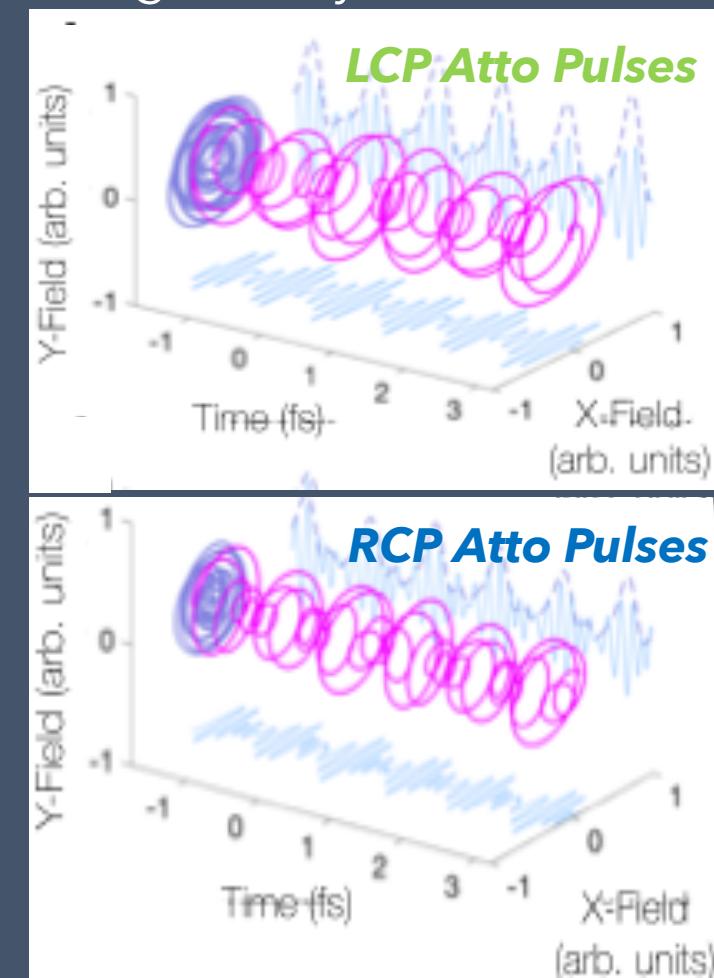
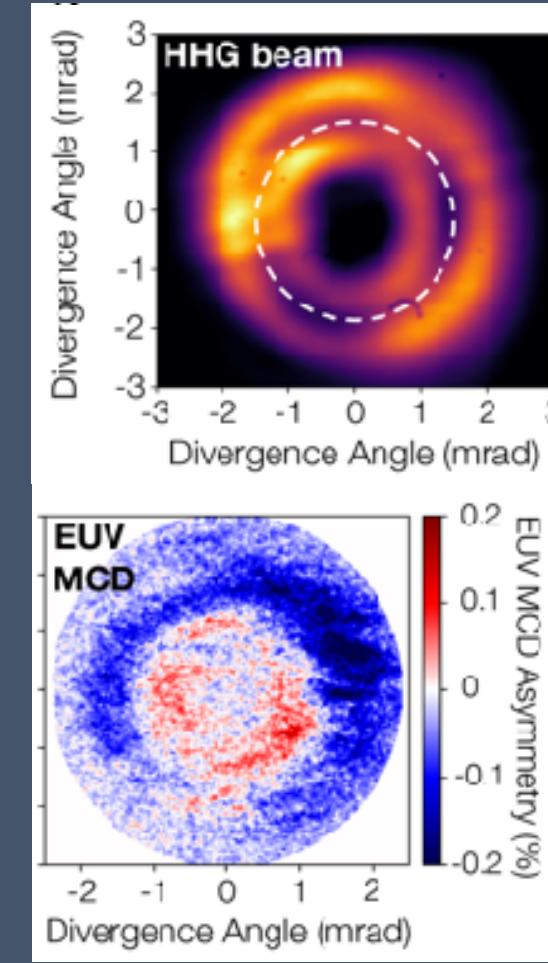
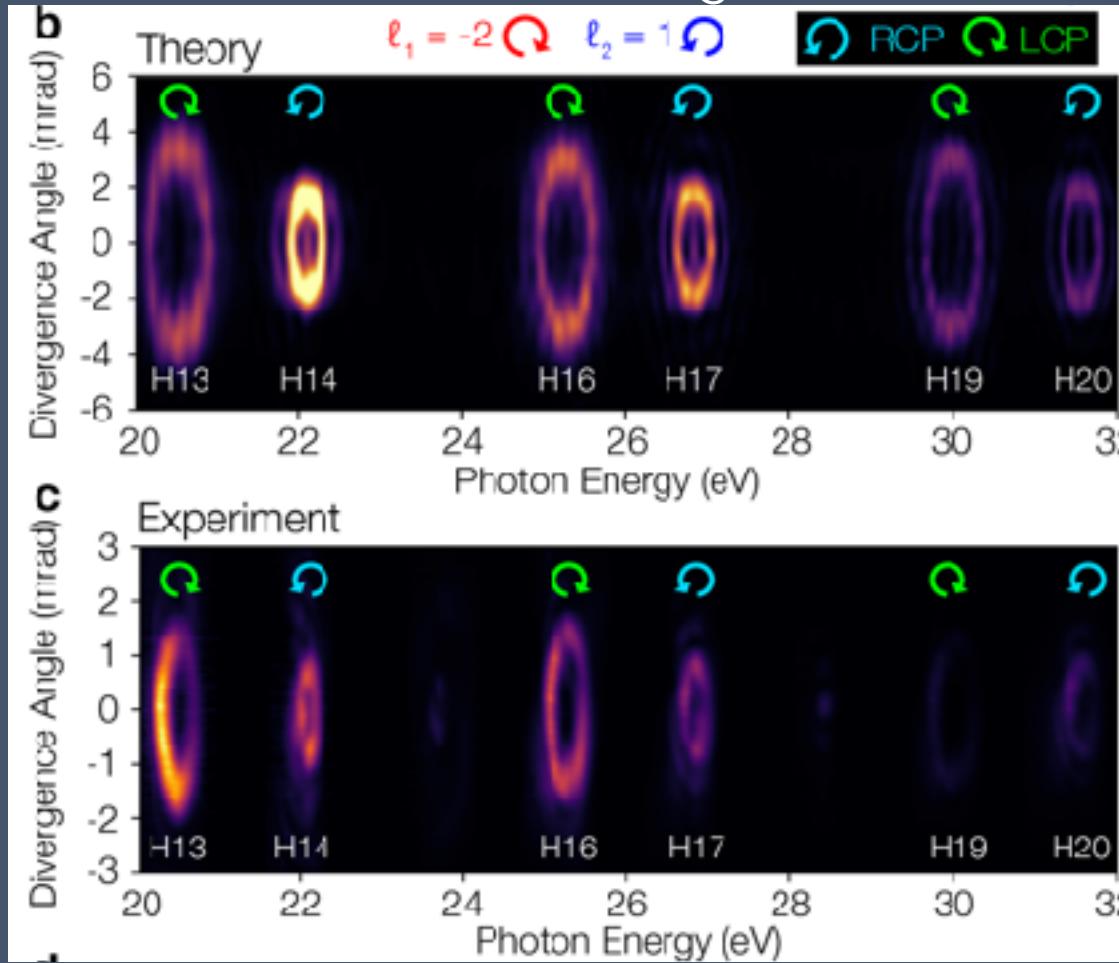
- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?



Controlling Divergence and Polarization in SAM-OAM HHG: Spatially Isolated, Circularly Polarized, Attosecond Vortices



- The presence of SAM constrains the allowed OAM values of the high-harmonics, and the OAM determines the divergence of the EUV vortices... Can we break the degeneracy?

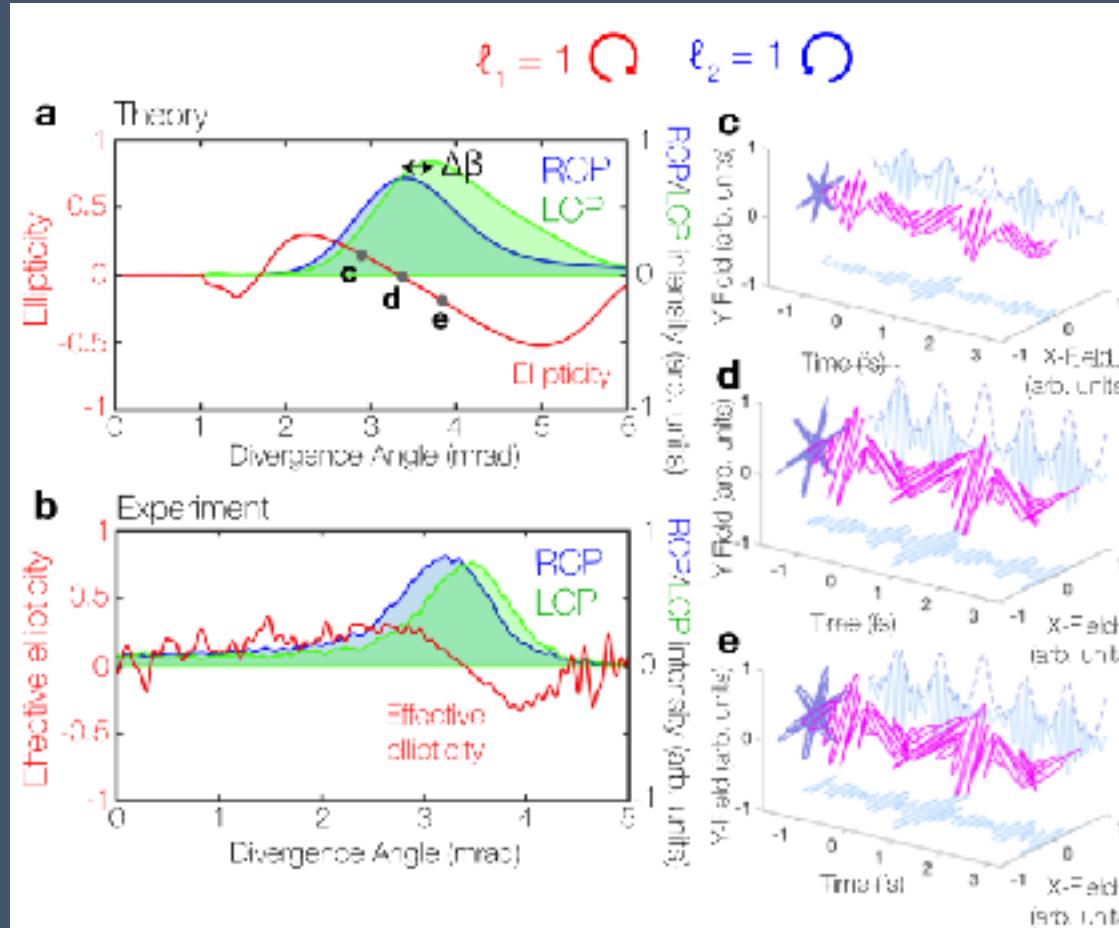


Entwined SAM-OAM Conservation in HHG:

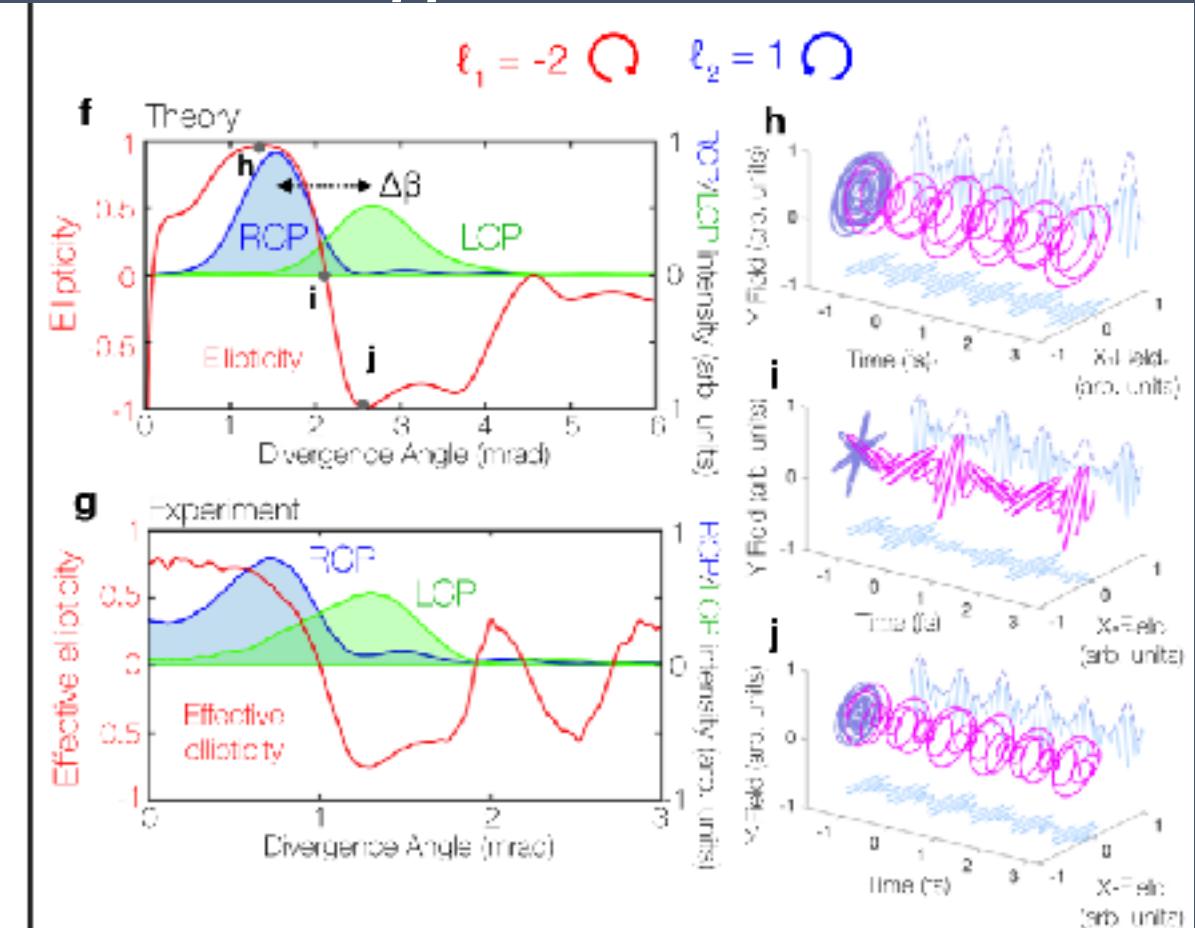
Attosecond Pulses from RCP to Linear to LCP



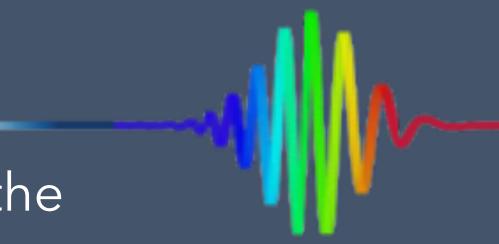
**EUV Vortices with Same OAM,
Opposite SAM (but overlapped)**



**EUV Vortices with Large OAM Difference,
Opposite SAM**



Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices



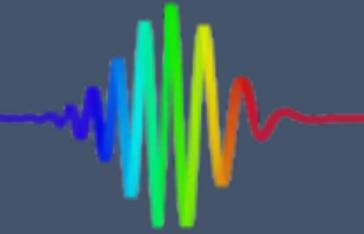
- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...

**OAM Conservation w/
Single-Color Drivers**

$$\ell_q = \ell_1 n_1$$

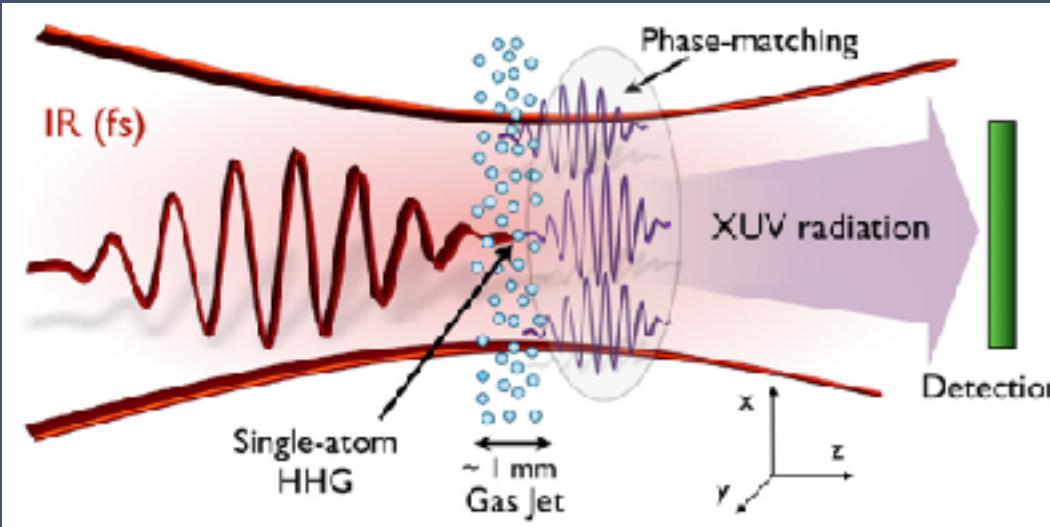
Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...



OAM Conservation w/ Single-Color Drivers

$$\ell_q = \ell_1 n_1$$

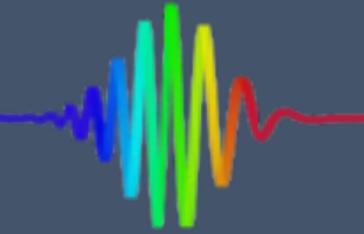


Dorney, et. al. *Nat. Photon.* **1**, 2019

Pisanty, et al. *PRL* **122**, 2019

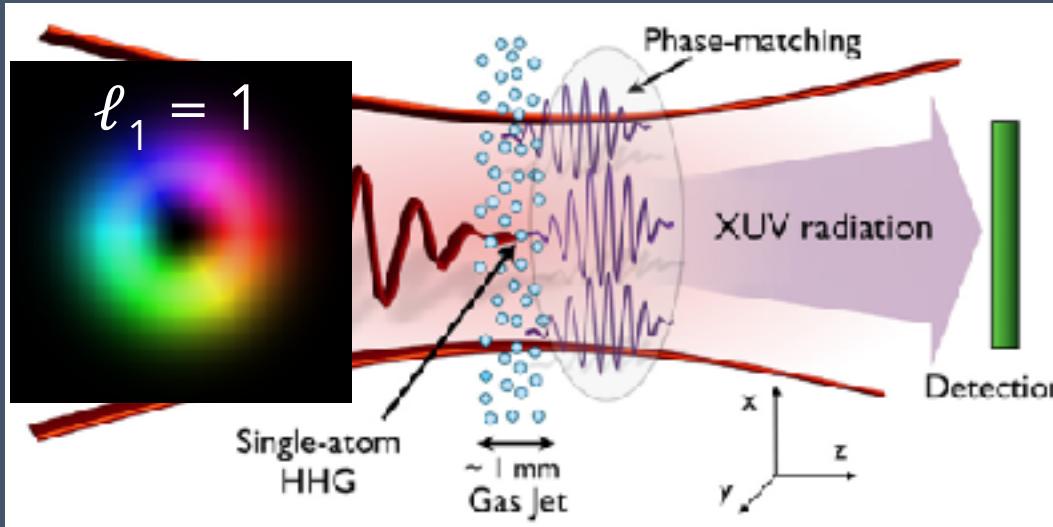
Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...



OAM Conservation w/ Single-Color Drivers

$$\ell_q = \ell_1 n_1$$

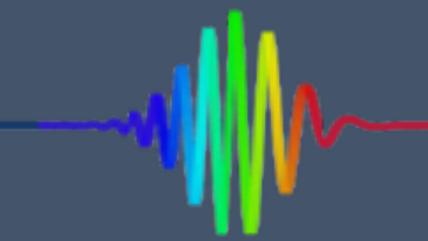


Dorney, et. al. *Nat. Photon.* **1**, 2019

Pisanty, et al. *PRL* **122**, 2019

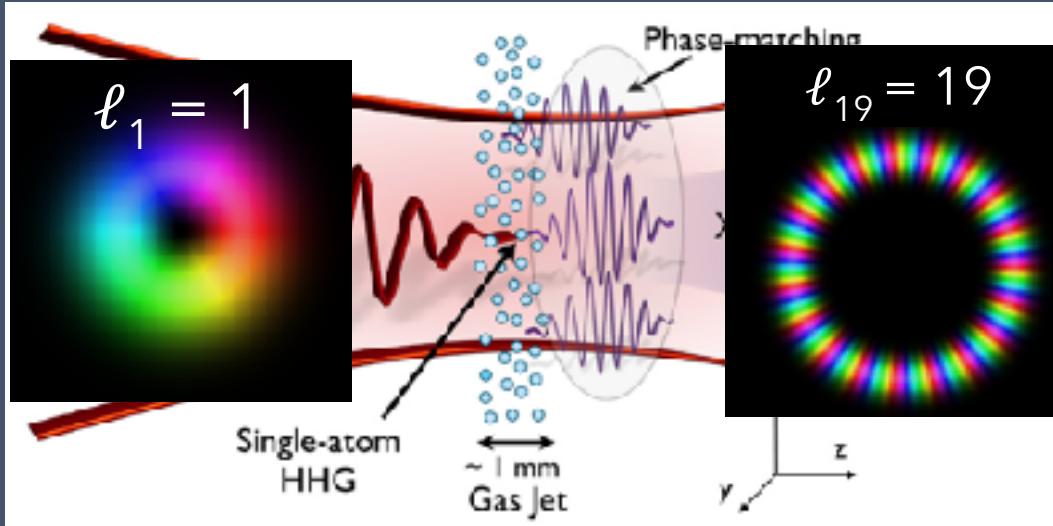
Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...



OAM Conservation w/ Single-Color Drivers

$$\ell_q = \ell_1 n_1$$



Dorney, et. al. *Nat. Photon.* **1**, 2019

Pisanty, et al. *PRL* **122**, 2019

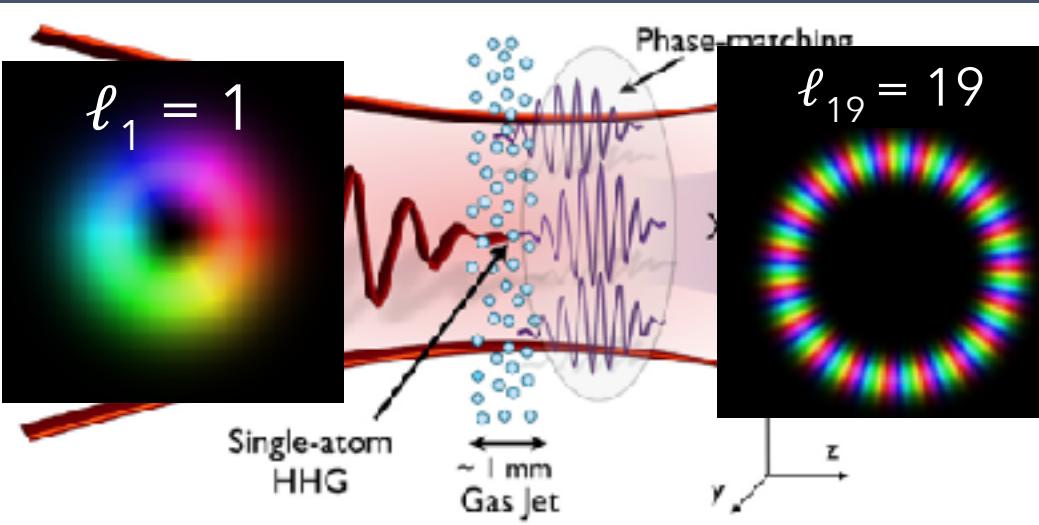
Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...

Gariepy, et al. PRL, 113, 2014

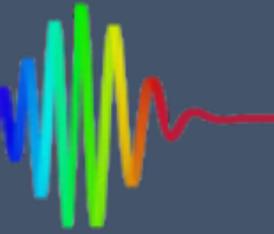
OAM Conservation w/ Single-Color Drivers

$$\ell_q = \ell_1 n_1$$



Dorney, et. al. *Nat. Photon.* **1**, 2019

Pisanty, et al. *PRL* **122**, 2019



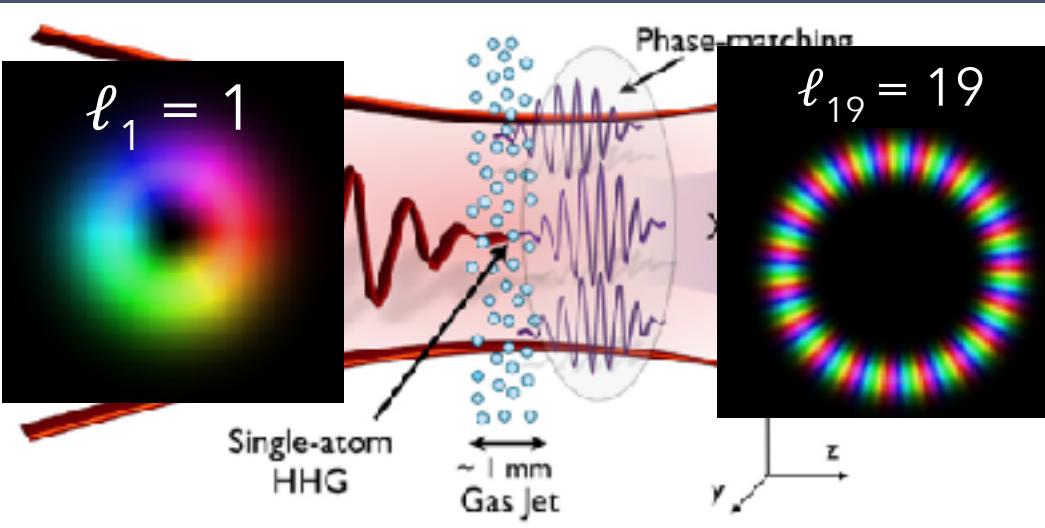
Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...

Gariepy, et al. PRL, 113, 2014

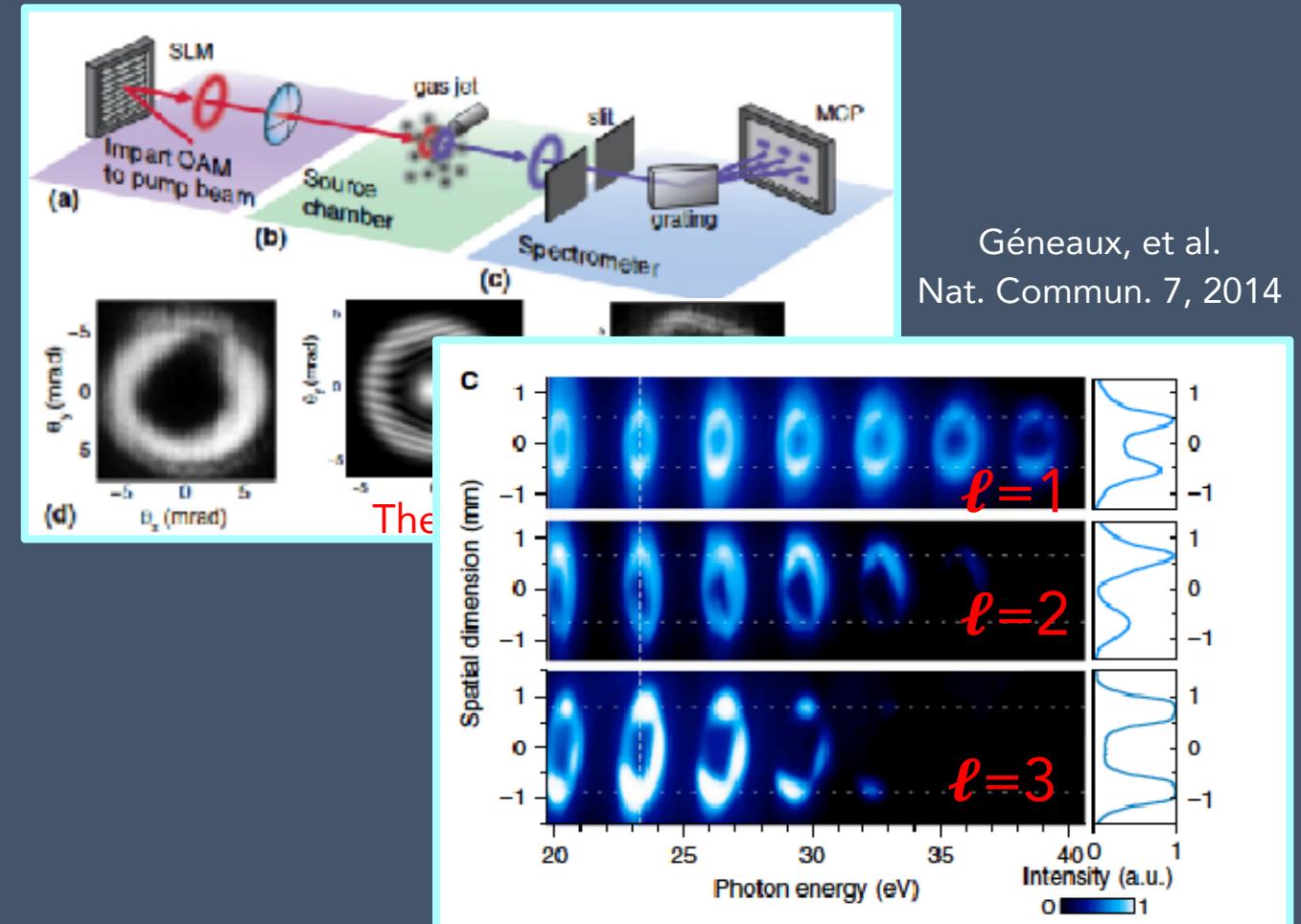
OAM Conservation w/ Single-Color Drivers

$$\ell_q = \ell_1 n_1$$



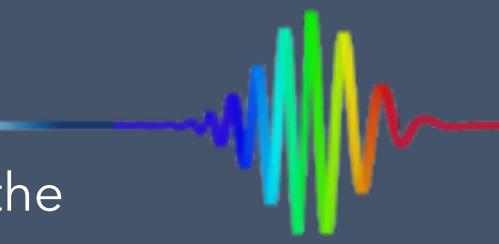
Dorney, et. al. Nat. Photon. 1, 2019

Pisanty, et al. PRL 122, 2019



Géneaux, et al.
Nat. Commun. 7, 2014

Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices



- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...

OAM Conservation w/

Bicircular Driver

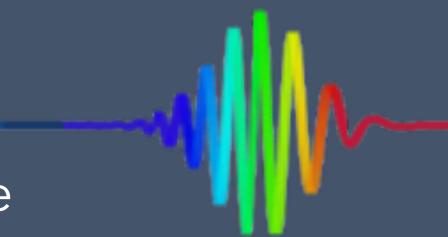
$$\ell_q = \frac{q + 2\sigma_q \sigma_1}{3} (\ell_1 + \ell_2) - \sigma_q \sigma_1 \ell_2$$

$$\ell_1 = 1 \quad \ell_2 = -1$$

$$\sigma_1 = 1 \quad \sigma_2 = -1$$

Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...



OAM Conservation w/

Bicircular Driver

$$\ell_q = \frac{q + 2\sigma_q \sigma_1}{3} (\ell_1 + \ell_2) - \sigma_q \sigma_1 \ell_2$$

$$\ell_1 = 1 \quad \ell_2 = -1$$

$$\sigma_1 = 1 \quad \sigma_2 = -1$$

$$\ell_q = \sigma_1 \quad \ell_{q+1} = \sigma_2$$

Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...

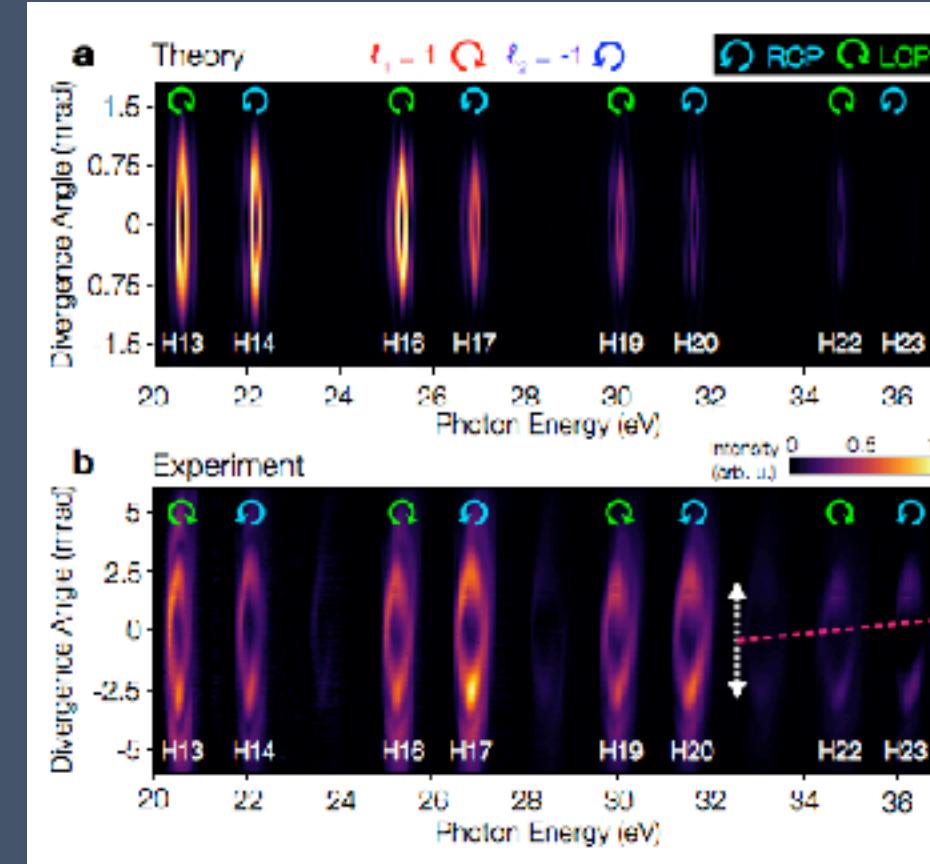
**OAM Conservation w/
Bicircular Driver**

$$\ell_q = \frac{q + 2\sigma_q \sigma_1}{3} (\ell_1 + \ell_2) - \sigma_q \sigma_1 \ell_2$$

$$\ell_1 = 1 \quad \ell_2 = -1$$

$$\sigma_1 = 1 \quad \sigma_2 = -1$$

$$\ell_q = \sigma_1 \quad \ell_{q+1} = \sigma_2$$



Dorney, et. al. *Nat. Photon.* **1**, 2019

Pisanty, et al. *PRL* **122**, 2019

Controlling the OAM in SAM-OAM HHG: High-Energy, Low-OAM Attosecond Vortices

- For most practical applications, we actually want **low** OAM high harmonics, but the physics of OAM HHG makes this difficult...

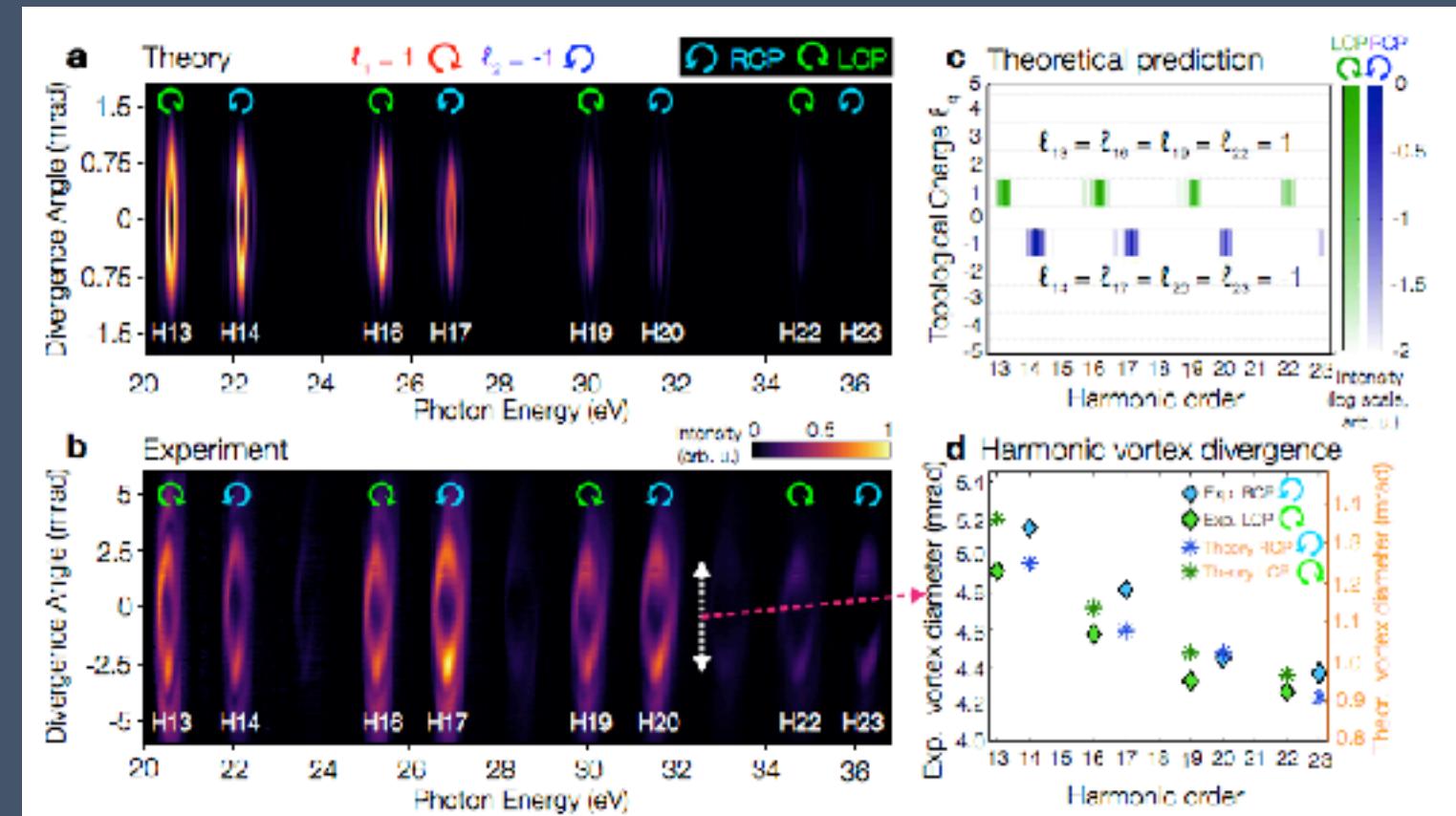
OAM Conservation w/ Bicircular Driver

$$\ell_q = \frac{q + 2\sigma_q \sigma_1}{3} (\ell_1 + \ell_2) - \sigma_q \sigma_1 \ell_2$$

$$\ell_1 = 1 \quad \ell_2 = -1$$

$$\sigma_1 = 1 \quad \sigma_2 = -1$$

$$\ell_q = \sigma_1 \quad \ell_{q+1} = \sigma_2$$



Dorney, et. al. *Nat. Photon.* **1**, 2019

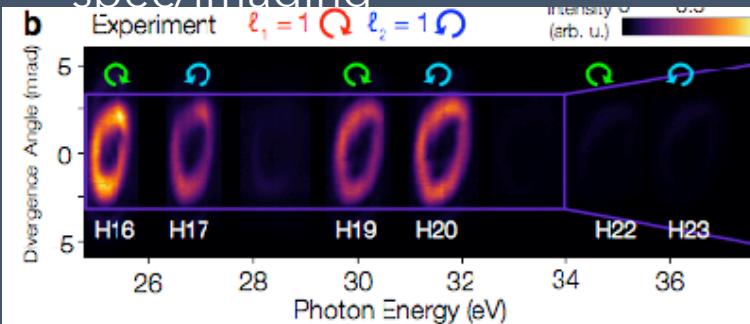
Pisanty, et al. *PRL* **122**, 2019

HHG with Simultaneous SAM-OAM Conservation: Structured EUV Light with Designer SAM, OAM, Divergence



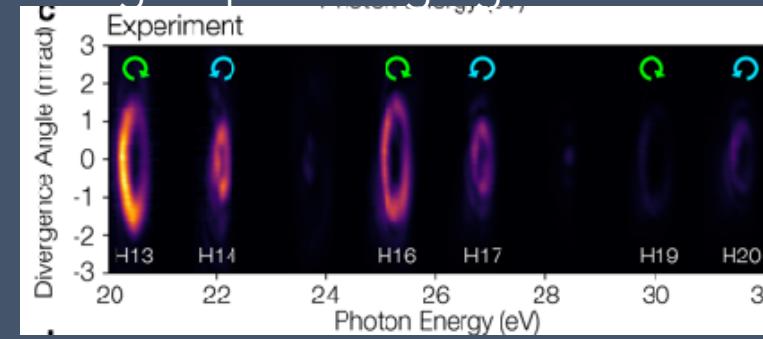
High OAM Vortices w/ Same OAM, Different SAM

- Linear atto pulses,
- OAM-mediated dichroic spec/imaging



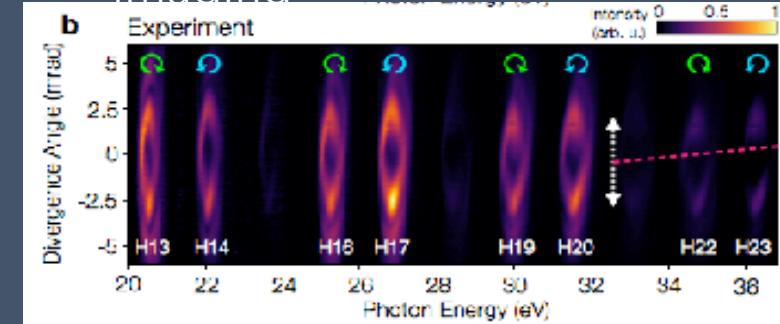
Spatially Isolated Vortices w/ Opposite SAM

- Circular atto pulses
- Spatially resolved, structured light spec/imaging



Low OAM Vortices w/ Opposite SAM

- Linear atto pulses
- Low OAM for controlled spec/imaging

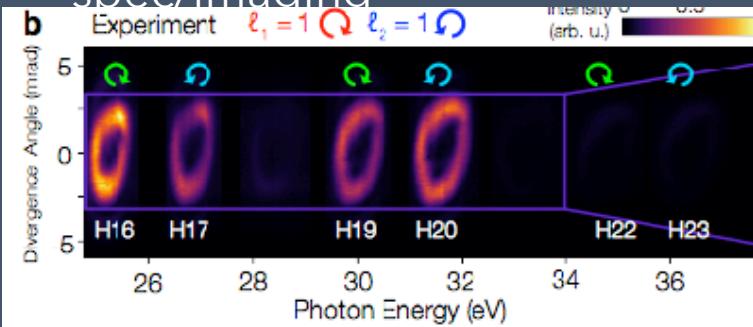


HHG with Simultaneous SAM-OAM Conservation: Structured EUV Light with Designer SAM, OAM, Divergence



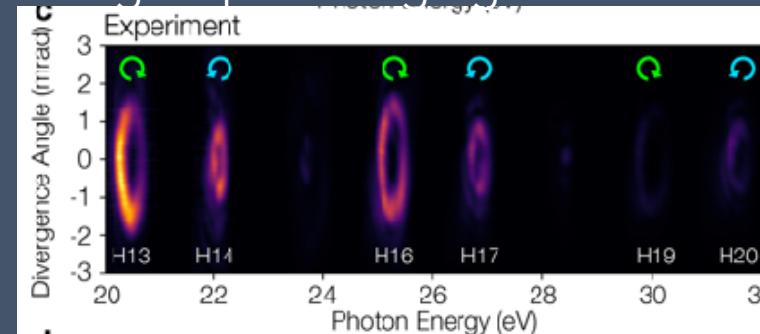
High OAM Vortices w/ Same OAM, Different SAM

- Linear atto pulses,
- OAM-mediated dichroic spec/imaging



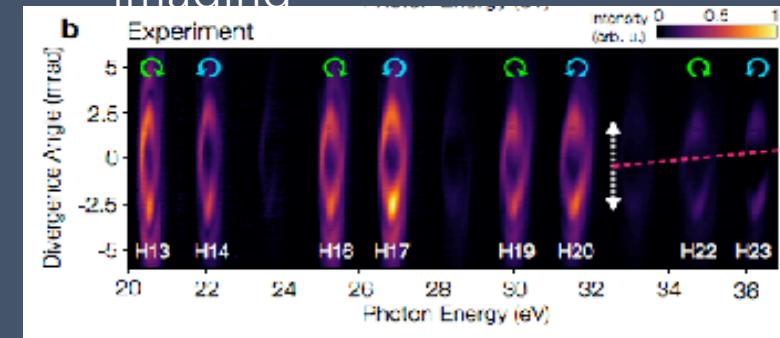
Spatially Isolated Vortices w/ Opposite SAM

- Circular atto pulses
- Spatially resolved, structured light spec/imaging

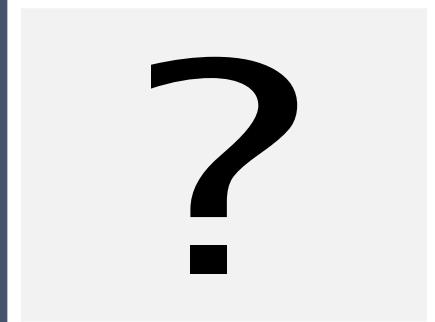


Low OAM Vortices w/ Opposite SAM

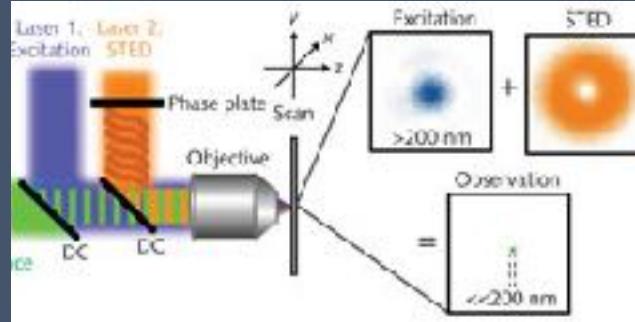
- Linear atto pulses
- Low OAM for controlled spec/imaging



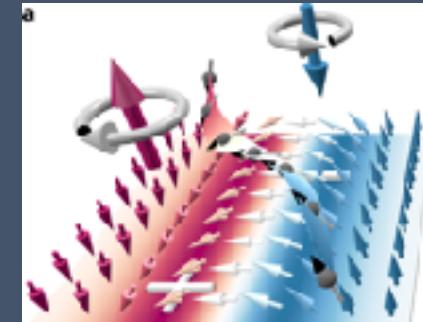
Mag Imaging/Control



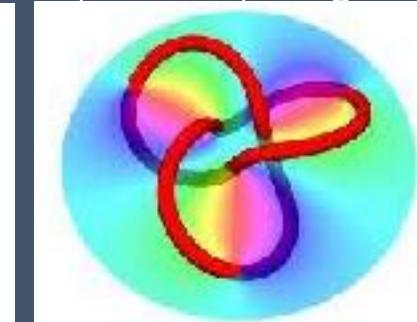
EUV-based STED



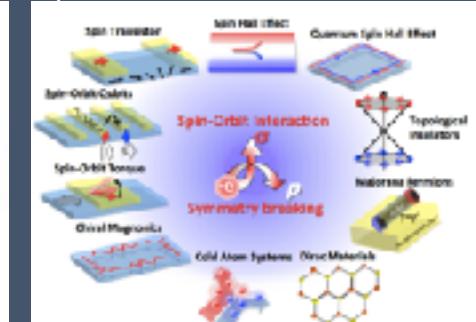
Orbital Magnetism



Optical Topologies



Spin/Orbit Interactions



High OAM Vortices w/Spatially Isolated VorticesLow OAM Vortices

Sar

> L

> C

S

b
Divergence Angle (mrad)
6
5
4
3
2
1
0
-1
-2
-3
-4
-5
-6

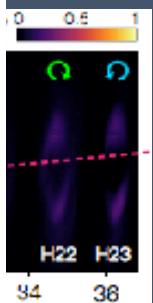
Mac

nature
photonics

ARTICLES

<https://doi.org/10.1038/s41566-018-0304-3>

spec/



Controlling the polarization and vortex charge of attosecond high-harmonic beams via simultaneous spin-orbit momentum conservation

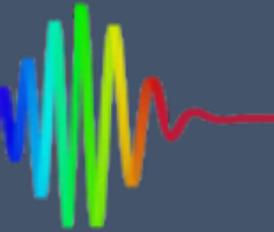
Kevin M. Dorney ^{1*}, Laura Rego ², Nathan J. Brooks ¹, Julio San Román ², Chen-Ting Liao ¹, Jennifer L. Ellis ¹, Dmitriy Zusin ¹, Christian Gentry ¹, Quynh L. Nguyen ¹, Justin M. Shaw ³, Antonio Picón ^{2,4}, Luis Plaja ², Henry C. Kapteyn ¹, Margaret M. Murnane ¹ and Carlos Hernández-García ^{2*}



actions

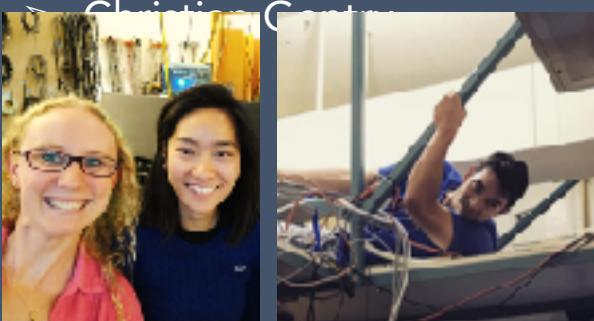


Excellent Group of Students, Collaborators and Advisors: Both at Home and Abroad!



JILA/NIST/CU Boulder (USA)

- Nathan Brooks
- Dr. Chen-Ting Liao
- Dr. Jennifer L. Ellis
- Dr. Dmitriy Zusin
- Christian Gauthier



- Quynh L. Nguyen
- Justin M. Shaw (NIST)
- **Prof. Henry Kapteyn**
- **Prof. Margaret Murnane**



\$\$\$\$
\$\$\$\$
\$\$\$\$



University of Salamanca (ESP)

- Laura Rego
- Dr. Julio San Román
- Dr. Antonio Picón



- **Dr. Carlos Hernández-García**
- **Prof. Luis Plaja**

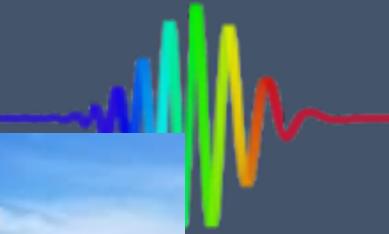


ICFO (ESP)

- Dr. Emilio Pisanty
- **Prof. Maciej Lewenstein**



Thanks to Organizers, Support Staff, Advisors
And... Of Course YOU!!!



Waipi'o Beach



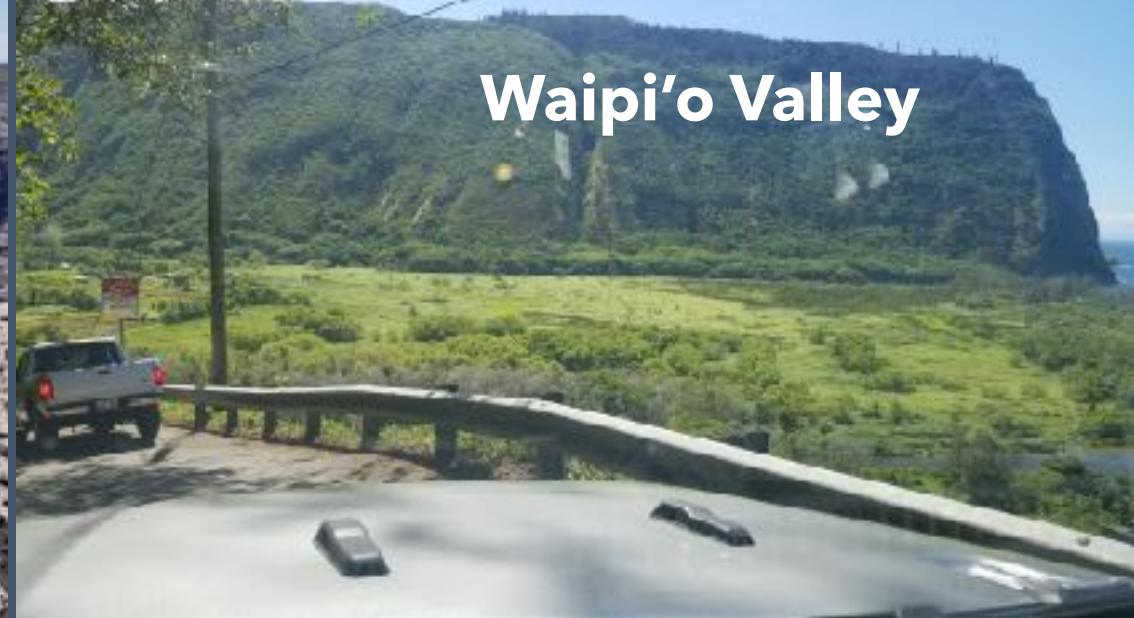
Green Sand Beach



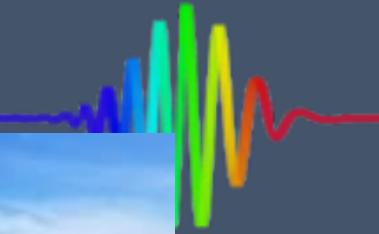
Holei Sea Arch



Waipi'o Valley



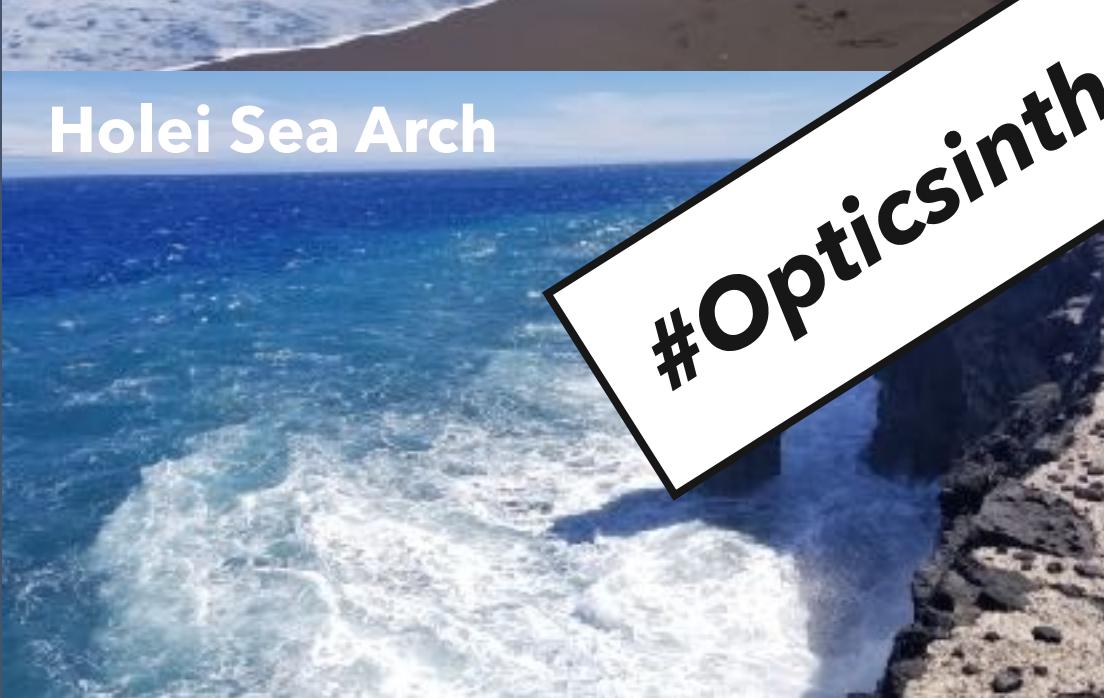
Thanks to Organizers, Support Staff, Advisors
And... Of Course YOU!!!



Waipi'o Beach



Holei Sea Arch

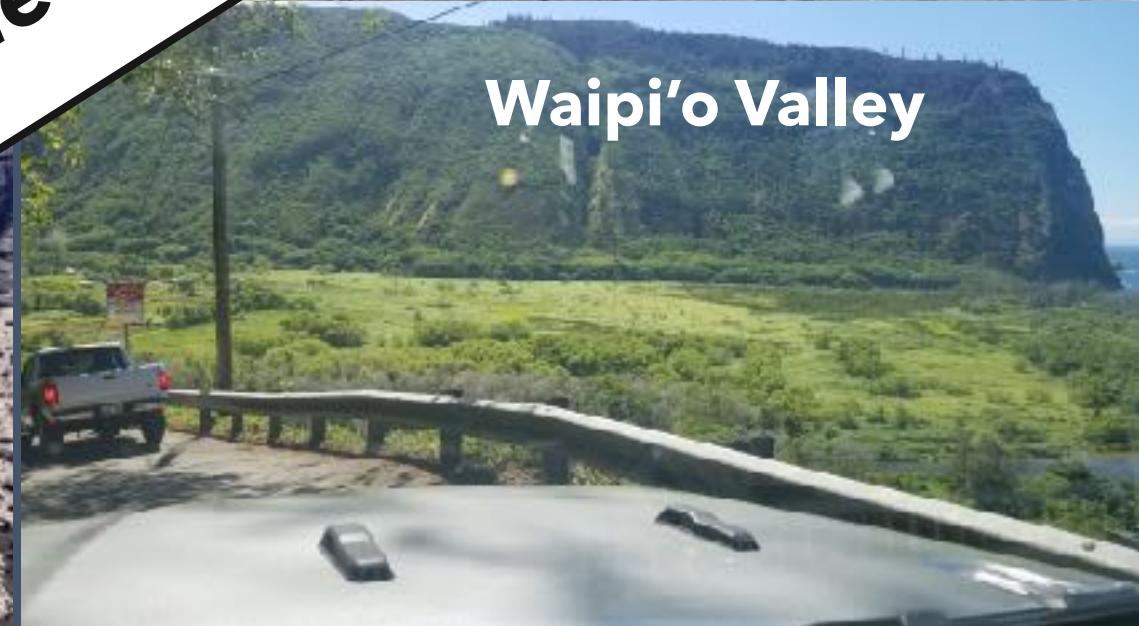


#OpticsintheTropics2019

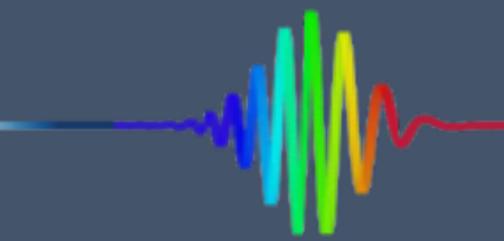
Green Sand Beach



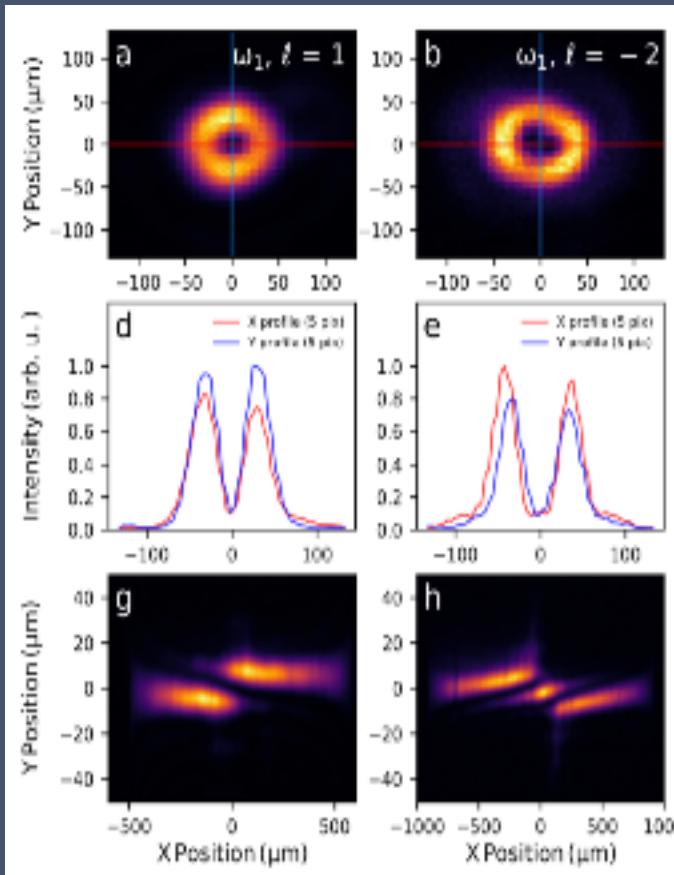
Waipi'o Valley



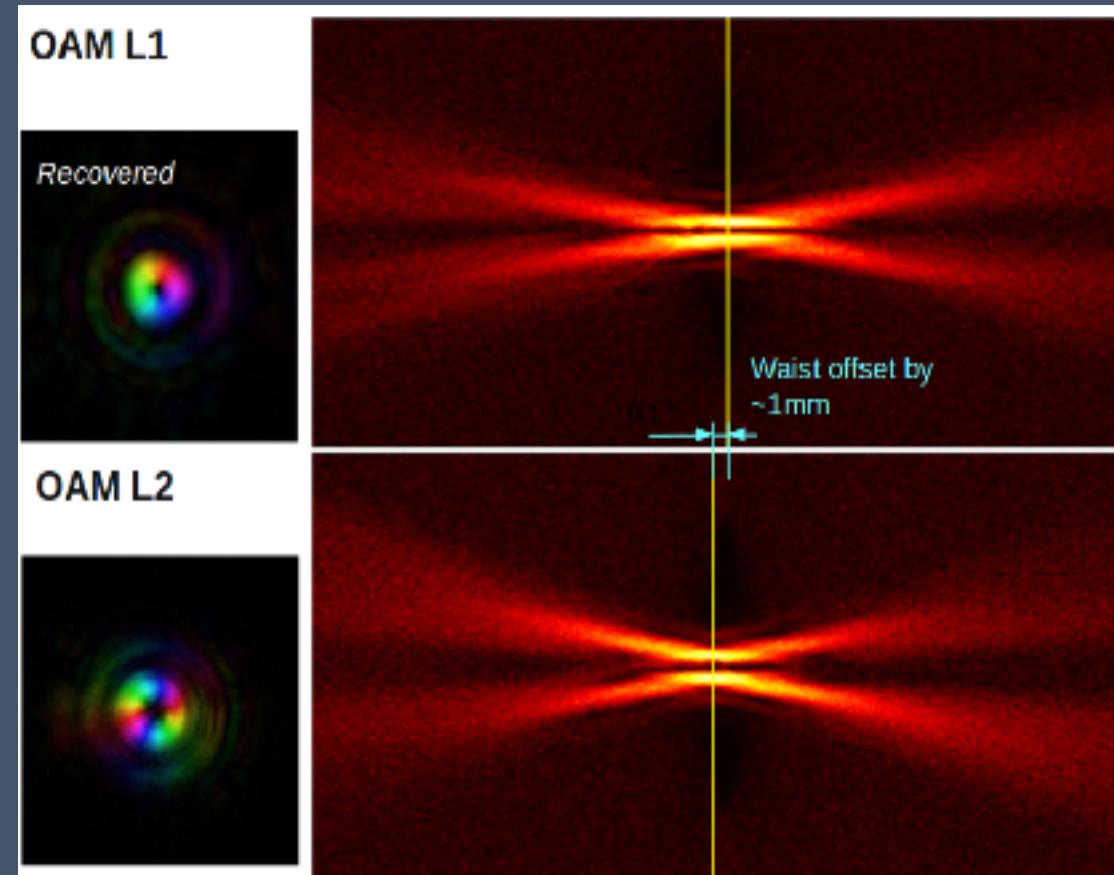
Generating and Quantifying High-Quality, Intense, Femtosecond Vortex Beams



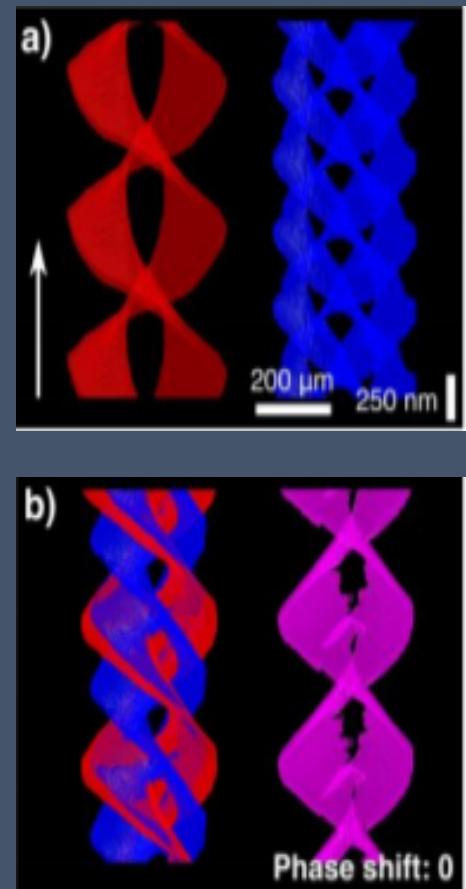
Cylindrical Lens Analyzer¹



Gerchberg-Saxton Phase Retrieval²⁻⁴



Ptychography^{5,6}



¹Alperin, et al. *Opt. Lett.* **41**, 2016

²Fu, et al. *Opt. Lett.* **41**, 2016

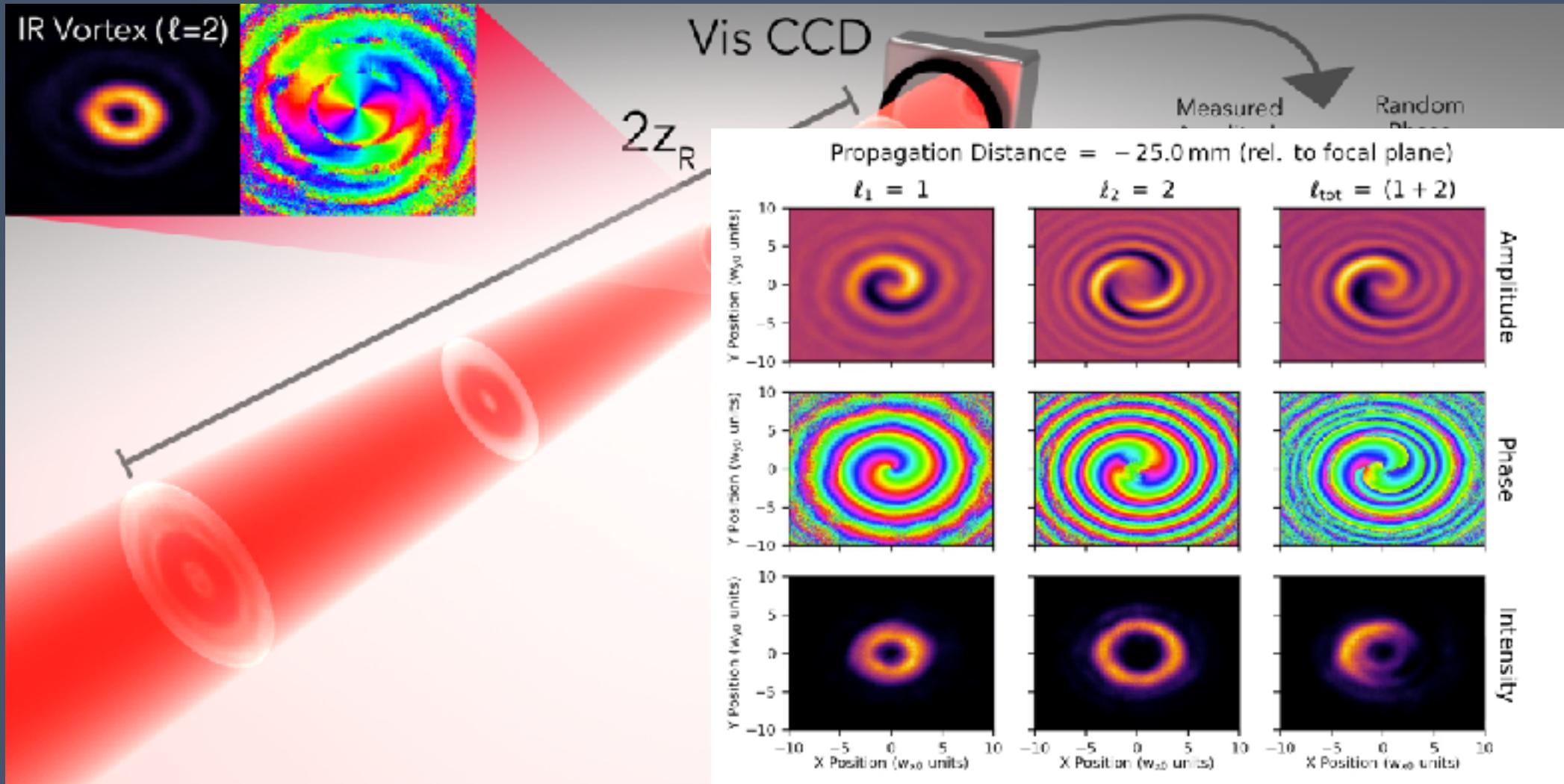
³Chang, et al. *Opt. Commun.* **405**, 2017

⁴Rego and Dorney, et al. *Science*, **364**, 2019

⁵Saito, et al. *Jpn. J. Appl. Phys.* **56**, 2017

⁶Esashi, et al. *Opt. Exp.* **26**, 2018

Generating and Quantifying High-Quality, Intense, Mixed OAM Vortex Beams

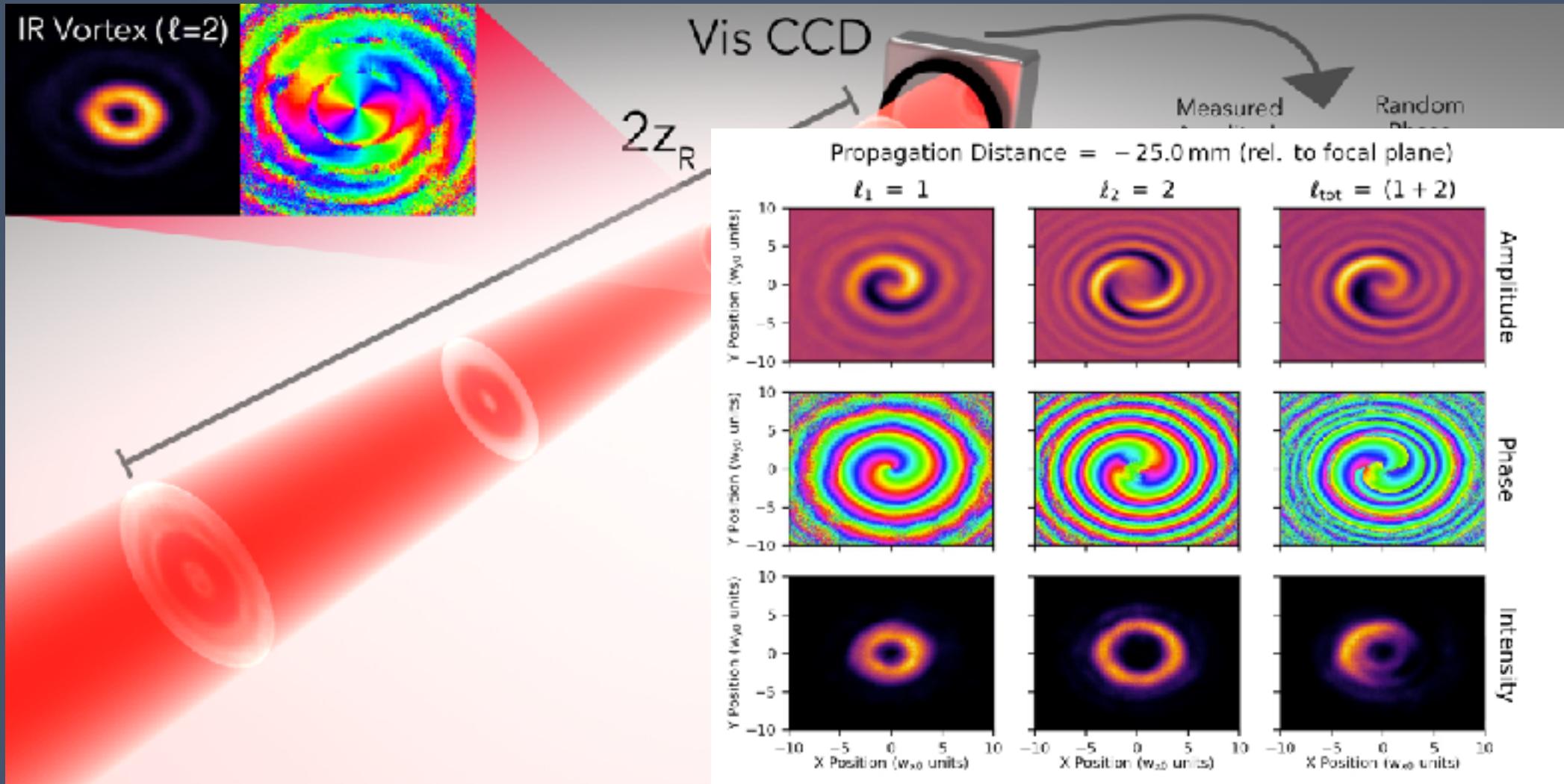


Fu, et al. *Opt. Lett.* **41**, 2016

Chang, et al. *Opt. Commun.* **405**, 2017

Rego and Dorney, et al. *Science*, **364**, 2019

Generating and Quantifying High-Quality, Intense, Mixed OAM Vortex Beams

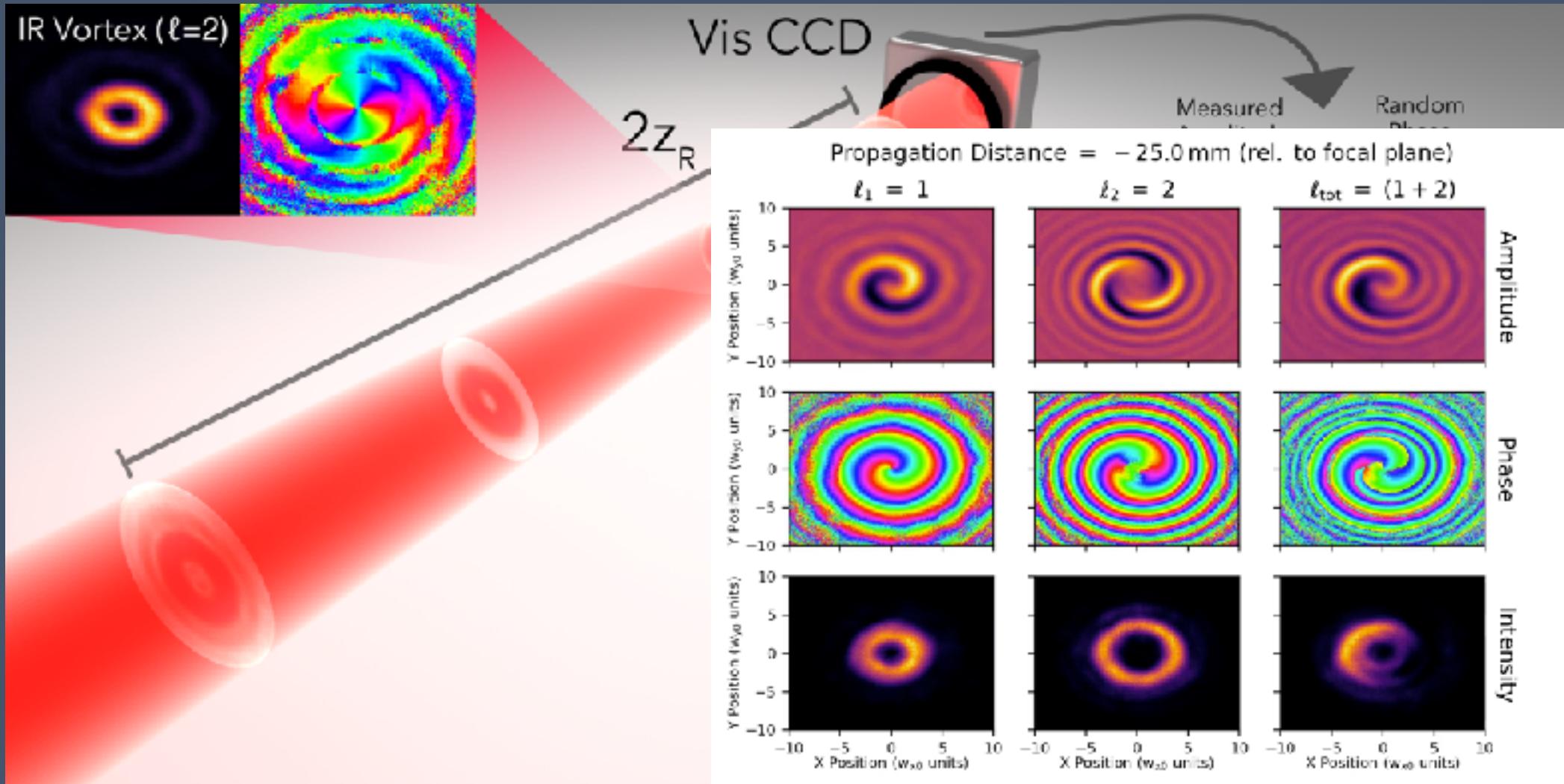


Fu, et al. Opt. Lett. **41**, 2016

Chang, et al. Opt. Commun. **405**, 2017

Rego and Dorney, et al. Science, **364**, 2019

Generating and Quantifying High-Quality, Intense, Mixed OAM Vortex Beams



Fu, et al. Opt. Lett. **41**, 2016

Chang, et al. Opt. Commun. **405**, 2017

Rego and Dorney, et al. Science, **364**, 2019



Backup Slide Title Goes Here...

