



# The Elements of Linear Algebra Volume One: Livre des Lignes Droites

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### CONTENTS

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## The Equation of a Line in the Plane

#### Outline

- points vs physics vectors vs math vectors
- the idea of R2
- sketching points and vectors in the plane
- vector algebra in R2
- lines in R2 as parametric objects: through the origin, and not
- sketching lines in R2
- lengths, angles, and the dot product in R2
- normal vector to a line in R2
- equation of a line, three methods: elimination, from two pts via similar triangles, from geometry of dot product
- families of parallel lines
- sketching a line from an equation
- the big theorem with duality







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THE EQUATION OF A LINE IN THE PLANE









## The Equations of a Line in Space

#### Outline

- points, vectors in space
- -R3
- vector algebra
- planes in R3 parametrically: through the origin, not
- dot product in R3
- normal vector to a plane
- the equation of a plane: by elimination, by dot product
- families of parallel planes
- sketching from an equation
- big theorem with duality for planes
- LINES in R3 as intersection of two planes







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THE EQUATIONS OF A LINE IN SPACE









## Systems of Lines in the Plane

#### Outline

- note about how we understand one line in the plane, what about two?
- idea of three possible outcomes
- $-\,$  translations into matrix algebra equation: matrix-vector multiplication
- idea of a solution to a system
- questions: how can we characterize the three options in terms of the matrix
- $-\,$  use normals to answer, linear independence...
- characterization of column space bit??
- write "solution" as parametric form of the line, or as just point
- algorithmic solution stuff







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Systems of Lines in the Plane







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Systems of Planes in Space

### Outline

- to-do







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Systems of Planes in Space







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The Algebra of Square Matrices







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THE ALGEBRA OF SQUARE MATRICES







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Approximate Solutions to Unsolvable Systems







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### Approximate Solutions to Unsolvable Systems







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# Matrices as Transformations



