

SOLUTIONS MANUAL

CRYPTOGRAPHY AND NETWORK SECURITY

PRINCIPLES AND PRACTICE

FIFTH EDITION

Do Not Post on Web

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NOTICE

This manual contains solutions to the review questions and homework problems in *Cryptography and Network Security, Fifth Edition*. If you spot an error in a solution or in the wording of a problem, I would greatly appreciate it if you would forward the information via email to ws@shore.net. An errata sheet for this manual, if needed, is available at <http://www.box.net/shared/nh8hti5167> . File name is S-Crypto5e-mmyy

W.S.

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CHAPTER 1 INTRODUCTION

ANSWERS TO QUESTIONS

- 1.1 The OSI Security Architecture is a framework that provides a systematic way of defining the requirements for security and characterizing the approaches to satisfying those requirements. The document defines security attacks, mechanisms, and services, and the relationships among these categories.
- 1.2 **Passive attacks** have to do with eavesdropping on, or monitoring, transmissions. Electronic mail, file transfers, and client/server exchanges are examples of transmissions that can be monitored. **Active attacks** include the modification of transmitted data and attempts to gain unauthorized access to computer systems.
- 1.3 **Passive attacks:** release of message contents and traffic analysis. **Active attacks:** masquerade, replay, modification of messages, and denial of service.
- 1.4 **Authentication:** The assurance that the communicating entity is the one that it claims to be.
Access control: The prevention of unauthorized use of a resource (i.e., this service controls who can have access to a resource, under what conditions access can occur, and what those accessing the resource are allowed to do).
Data confidentiality: The protection of data from unauthorized disclosure.
Data integrity: The assurance that data received are exactly as sent by an authorized entity (i.e., contain no modification, insertion, deletion, or replay).
Nonrepudiation: Provides protection against denial by one of the entities involved in a communication of having participated in all or part of the communication.
Availability service: The property of a system or a system resource being accessible and usable upon demand by an authorized system entity, according to performance specifications for the system (i.e., a system is available if it provides services according to the system design whenever users request them).
- 1.5 See Table 1.3.

ANSWERS TO PROBLEMS

- 1.1 The system must keep personal identification numbers confidential, both in the host system and during transmission for a transaction. It must protect the integrity of account records and of individual transactions. Availability of the host system is important to the economic well being of the bank, but not to its fiduciary responsibility. The availability of individual teller machines is of less concern.

- 1.2** The system does not have high requirements for integrity on individual transactions, as lasting damage will not be incurred by occasionally losing a call or billing record. The integrity of control programs and configuration records, however, is critical. Without these, the switching function would be defeated and the most important attribute of all - availability - would be compromised. A telephone switching system must also preserve the confidentiality of individual calls, preventing one caller from overhearing another.
- 1.3**
- a.** The system will have to assure confidentiality if it is being used to publish corporate proprietary material.
 - b.** The system will have to assure integrity if it is being used to laws or regulations.
 - c.** The system will have to assure availability if it is being used to publish a daily paper.
- 1.4**
- a.** An organization managing public information on its web server determines that there is no potential impact from a loss of confidentiality (i.e., confidentiality requirements are not applicable), a moderate potential impact from a loss of integrity, and a moderate potential impact from a loss of availability.
 - b.** A law enforcement organization managing extremely sensitive investigative information determines that the potential impact from a loss of confidentiality is high, the potential impact from a loss of integrity is moderate, and the potential impact from a loss of availability is moderate.
 - c.** A financial organization managing routine administrative information (not privacy-related information) determines that the potential impact from a loss of confidentiality is low, the potential impact from a loss of integrity is low, and the potential impact from a loss of availability is low.
 - d.** The management within the contracting organization determines that: (i) for the sensitive contract information, the potential impact from a loss of confidentiality is moderate, the potential impact from a loss of integrity is moderate, and the potential impact from a loss of availability is low; and (ii) for the routine administrative information (non-privacy-related information), the potential impact from a loss of confidentiality is low, the potential impact from a loss of integrity is low, and the potential impact from a loss of availability is low.
 - e.** The management at the power plant determines that: (i) for the sensor data being acquired by the SCADA system, there is no potential impact from a loss of confidentiality, a high potential impact from a loss of integrity, and a high potential impact from a loss of availability; and (ii) for the administrative information being processed by the system, there is a low potential impact from a loss of confidentiality, a low potential impact from a loss of integrity, and a low potential impact from a loss of availability. Examples from FIPS 199.

1.5	Release of message contents	Traffic analysis	Masquerade	Replay	Modification of messages	Denial of service
Peer entity authentication			Y			
Data origin authentication			Y			
Access control			Y			
Confidentiality	Y					
Traffic flow confidentiality		Y				
Data integrity				Y	Y	
Non-repudiation			Y			
Availability						Y

1.6	Release of message contents	Traffic analysis	Masquerade	Replay	Modification of messages	Denial of service
Encipherment	Y					
Digital signature			Y	Y	Y	
Access control	Y	Y	Y	Y		Y
Data integrity				Y	Y	
Authentication exchange	Y		Y	Y		Y
Traffic padding		Y				
Routing control	Y	Y				Y
Notarization			Y	Y	Y	

CHAPTER 2 CLASSICAL ENCRYPTION TECHNIQUES

ANSWERS TO QUESTIONS

- 2.1 Plaintext, encryption algorithm, secret key, ciphertext, decryption algorithm.
- 2.2 Permutation and substitution.
- 2.3 One key for symmetric ciphers, two keys for asymmetric ciphers.
- 2.4 A **stream cipher** is one that encrypts a digital data stream one bit or one byte at a time. A **block cipher** is one in which a block of plaintext is treated as a whole and used to produce a ciphertext block of equal length.
- 2.5 Cryptanalysis and brute force.
- 2.6 **Ciphertext only.** One possible attack under these circumstances is the brute-force approach of trying all possible keys. If the key space is very large, this becomes impractical. Thus, the opponent must rely on an analysis of the ciphertext itself, generally applying various statistical tests to it. **Known plaintext.** The analyst may be able to capture one or more plaintext messages as well as their encryptions. With this knowledge, the analyst may be able to deduce the key on the basis of the way in which the known plaintext is transformed. **Chosen plaintext.** If the analyst is able to choose the messages to encrypt, the analyst may deliberately pick patterns that can be expected to reveal the structure of the key.
- 2.7 An encryption scheme is **unconditionally secure** if the ciphertext generated by the scheme does not contain enough information to determine uniquely the corresponding plaintext, no matter how much ciphertext is available. An encryption scheme is said to be **computationally secure** if: (1) the cost of breaking the cipher exceeds the value of the encrypted information, and (2) the time required to break the cipher exceeds the useful lifetime of the information.
- 2.8 The **Caesar cipher** involves replacing each letter of the alphabet with the letter standing k places further down the alphabet, for k in the range 1 through 25.
- 2.9 A **monoalphabetic substitution cipher** maps a plaintext alphabet to a ciphertext alphabet, so that each letter of the plaintext alphabet maps to a single unique letter of the ciphertext alphabet.
- 2.10 The **Playfair algorithm** is based on the use of a 5×5 matrix of letters constructed using a keyword. Plaintext is encrypted two letters at a time using this matrix.

- 2.11 A **polyalphabetic substitution cipher** uses a separate monoalphabetic substitution cipher for each successive letter of plaintext, depending on a key.
- 2.12 1. There is the practical problem of making large quantities of random keys. Any heavily used system might require millions of random characters on a regular basis. Supplying truly random characters in this volume is a significant task.
2. Even more daunting is the problem of key distribution and protection. For every message to be sent, a key of equal length is needed by both sender and receiver. Thus, a mammoth key distribution problem exists.
- 2.13 A **transposition cipher** involves a permutation of the plaintext letters.
- 2.14 Steganography involves concealing the existence of a message.

ANSWERS TO PROBLEMS

- 2.1 a. No. A change in the value of b shifts the relationship between plaintext letters and ciphertext letters to the left or right uniformly, so that if the mapping is one-to-one it remains one-to-one.
b. 2, 4, 6, 8, 10, 12, 13, 14, 16, 18, 20, 22, 24. Any value of a larger than 25 is equivalent to $a \bmod 26$.
c. The values of a and 26 must have no common positive integer factor other than 1. This is equivalent to saying that a and 26 are relatively prime, or that the greatest common divisor of a and 26 is 1. To see this, first note that $E(a, p) = E(a, q)$ ($0 \leq p < q < 26$) if and only if $a(p - q)$ is divisible by 26. 1. Suppose that a and 26 are relatively prime. Then, $a(p - q)$ is not divisible by 26, because there is no way to reduce the fraction $a/26$ and $(p - q)$ is less than 26. 2. Suppose that a and 26 have a common factor $k > 1$. Then $E(a, p) = E(a, q)$, if $q = p + m/k \neq p$.
- 2.2 There are 12 allowable values of a (1, 3, 5, 7, 9, 11, 15, 17, 19, 21, 23, 25). There are 26 allowable values of b , from 0 through 25). Thus the total number of distinct affine Caesar ciphers is $12 \times 26 = 312$.
- 2.3 Assume that the most frequent plaintext letter is e and the second most frequent letter is t. Note that the numerical values are $e = 4$; $B = 1$; $t = 19$; $U = 20$. Then we have the following equations:
- $$1 = (4a + b) \bmod 26$$
- $$20 = (19a + b) \bmod 26$$
- Thus, $19 = 15a \bmod 26$. By trial and error, we solve: $a = 3$.
Then $1 = (12 + b) \bmod 26$. By observation, $b = 15$.
- 2.4 A good glass in the Bishop's hostel in the Devil's seat—twenty-one degrees and thirteen minutes—northeast and by north—main branch seventh limb east side—shoot from the left eye of the death's head— a bee line from the tree through the shot fifty feet out. (from *The Gold Bug*, by Edgar Allan Poe)

- 2.5 a. The first letter t corresponds to A, the second letter h corresponds to B, e is C, s is D, and so on. Second and subsequent occurrences of a letter in the key sentence are ignored. The result

ciphertext: SIDKHKDM AF HCRKIABIE SHIMC KD LFEAILA
plaintext: basilisk to leviathan blake is contact

- b. It is a monoalphabetic cipher and so easily breakable.
c. The last sentence may not contain all the letters of the alphabet. If the first sentence is used, the second and subsequent sentences may also be used until all 26 letters are encountered.

- 2.6 The cipher refers to the words in the page of a book. The first entry, 534, refers to page 534. The second entry, C2, refers to column two. The remaining numbers are words in that column. The names DOUGLAS and BIRLSTONE are simply words that do not appear on that page. Elementary! (from *The Valley of Fear*, by Sir Arthur Conan Doyle)

- 2.7 a.

2	8	10	7	9	6	3	1	4	5
C	R	Y	P	T	O	G	A	H	I
B	E	A	T	T	H	E	T	H	I
R	D	P	I	L	L	A	R	F	R
O	M	T	H	E	L	E	F	T	O
U	T	S	I	D	E	T	H	E	L
Y	C	E	U	M	T	H	E	A	T
R	E	T	O	N	I	G	H	T	A
T	S	E	V	E	N	I	F	Y	O
U	A	R	E	D	I	S	T	R	U
S	T	F	U	L	B	R	I	N	G
T	W	O	F	R	I	E	N	D	S

4	2	8	10	5	6	3	7	1	9
N	E	T	W	O	R	K	S	C	U
T	R	F	H	E	H	F	T	I	N
B	R	O	U	Y	R	T	U	S	T
E	A	E	T	H	G	I	S	R	E
H	F	T	E	A	T	Y	R	N	D
I	R	O	L	T	A	O	U	G	S
H	L	L	E	T	I	N	I	B	I
T	I	H	I	U	O	V	E	U	F
E	D	M	T	C	E	S	A	T	W
T	L	E	D	M	N	E	D	L	R
A	P	T	S	E	T	E	R	F	O

ISRNG BUTLF RRAFR LIDL P FTIYO NVSEE TBEHI HTETA
EYHAT TUCME HRGTA IOENT TUSRU IEADR FOETO LHMET
NTEDS IFWRO HUTEL EITDS

- b. The two matrices are used in reverse order. First, the ciphertext is laid out in columns in the second matrix, taking into account the order dictated by the second memory word. Then, the contents of the second matrix are read left to right, top to bottom and laid out in columns in the first matrix, taking into account the order dictated by the first memory word. The plaintext is then read left to right, top to bottom.
- c. Although this is a weak method, it may have use with time-sensitive information and an adversary without immediate access to good cryptanalysis (e.g., tactical use). Plus it doesn't require anything more than paper and pencil, and can be easily remembered.

2.8 SPUTNIK

2.9 PT BOAT ONE OWE NINE LOST IN ACTION IN BLACKETT STRAIT TWO MILES SW MERESU COVE X CREW OF TWELVE X REQUEST ANY INFORMATION

2.10 a.

L	A	R	G	E
S	T	B	C	D
F	H	I/J	K	M
N	O	P	Q	U
V	W	X	Y	Z

b.

O	C	U	R	E
N	A	B	D	F
G	H	I/J	K	L
M	P	Q	S	T
V	W	X	Y	Z

- 2.11 a. UZTBDLGZPNNWLGTGTUEROVLDBDUHFPERHWQSRZ
 - b. UZTBDLGZPNNWLGTGTUEROVLDBDUHFPERHWQSRZ
 - c. A cyclic rotation of rows and/or columns leads to equivalent substitutions. In this case, the matrix for part a of this problem is obtained from the matrix of Problem 2.10a, by rotating the columns by one step and the rows by three steps.
- 2.12 a. $25! \approx 2^{84}$
 - b. Given any 5x5 configuration, any of the four row rotations is equivalent, for a total of five equivalent configurations. For each of these five configurations, any of the four column rotations is equivalent. So each configuration in fact represents 25 equivalent configurations. Thus, the total number of unique keys is $25!/25 = 24!$

2.13 A mixed Caesar cipher. The amount of shift is determined by the keyword, which determines the placement of letters in the matrix.

2.14 a. We need an even number of letters, so append a "q" to the end of the message. Then convert the letters into the corresponding alphabetic positions:

M	e	e	t	m	e	a	t	t	h	e	u	s	u	a	l
13	5	5	20	13	5	1	20	20	8	5	21	19	21	1	12
P	l	a	c	e	a	t	t	e	n	r	a	t	h	e	r
16	12	1	3	5	1	20	20	5	14	18	1	20	8	5	18
T	h	a	n	e	i	g	h	t	o	c	l	o	c	k	q
20	8	1	14	5	9	7	8	20	15	3	12	15	3	11	17

The calculations proceed two letters at a time. The first pair:

$$\begin{pmatrix} C_1 \\ C_2 \end{pmatrix} = \begin{pmatrix} 9 & 4 \\ 5 & 7 \end{pmatrix} \begin{pmatrix} 13 \\ 5 \end{pmatrix} \bmod 26 = \begin{pmatrix} 137 \\ 100 \end{pmatrix} \bmod 26 = \begin{pmatrix} 7 \\ 22 \end{pmatrix}$$

The first two ciphertext characters are alphabetic positions 7 and 22, which correspond to GV. The complete ciphertext:

GVUIGVKODZYPUHEKJHUZWFWZFSJSDZMUDZMYCJQMFWWUQRKR

b. We first perform a matrix inversion. Note that the determinate of the encryption matrix is $(9 \times 7) - (4 \times 5) = 43$. Using the matrix inversion formula from the book:

$$\begin{pmatrix} 9 & 4 \\ 5 & 7 \end{pmatrix}^{-1} = \frac{1}{43} \begin{pmatrix} 7 & -4 \\ -5 & 9 \end{pmatrix} \bmod 26 = 23 \begin{pmatrix} 7 & -4 \\ -5 & 9 \end{pmatrix} \bmod 26 = \begin{pmatrix} 161 & -92 \\ -115 & 9 \end{pmatrix} \bmod 26 = \begin{pmatrix} 5 & 12 \\ 15 & 25 \end{pmatrix}$$

Here we used the fact that $(43)^{-1} = 23$ in Z_{26} . Once the inverse matrix has been determined, decryption can proceed. Source: [LEWA00].

2.15 Consider the matrix \mathbf{K} with elements k_{ij} to consist of the set of column vectors \mathbf{K}_j , where:

$$\mathbf{K} = \begin{pmatrix} k_{11} & \cdots & k_{1n} \\ \vdots & \vdots & \vdots \\ k_{n1} & \cdots & k_{nn} \end{pmatrix} \quad \text{and} \quad \mathbf{K}_j = \begin{pmatrix} k_{1j} \\ \vdots \\ k_{nj} \end{pmatrix}$$

The ciphertext of the following chosen plaintext n -grams reveals the columns of \mathbf{K} :

$$\begin{aligned} (B, A, A, \dots, A, A) &\leftrightarrow \mathbf{K}_1 \\ (A, B, A, \dots, A, A) &\leftrightarrow \mathbf{K}_2 \\ &\vdots \\ (A, A, A, \dots, A, B) &\leftrightarrow \mathbf{K}_n \end{aligned}$$

- 2.16 a. 7×13^4
 b. 7×13^4
 c. 13^4
 d. 10×13^4
 e. $2^4 \times 13^2$
 f. $2^4 \times (13^2 - 1) \times 13$
 g. 37648
 h. 23530
 i. 157248

2.17 key: *legleglegle*
 plaintext: *explanation*
 ciphertext: *PBVWETLXOZR*

2.18 a.

s	e	n	d	m	o	r	e	m	o	n	e	y
18	4	13	3	12	14	17	4	12	14	13	4	24
9	0	1	7	23	15	21	14	11	11	2	8	9
1	4	14	10	9	3	12	18	23	25	15	12	7
B	E	C	K	J	D	M	S	X	Z	P	M	H

b.

c	a	s	h	n	o	t	n	e	e	d	e	d
2	0	18	7	13	14	19	13	4	4	3	4	3
25	4	22	3	22	15	19	5	19	21	12	8	4
1	4	14	10	9	3	12	18	23	25	15	12	7
B	E	C	K	J	D	M	S	X	Z	P	M	H

2.19 your package ready Friday 21st room three Please destroy this immediately.

2.20 a. Lay the message out in a matrix 8 letters across. Each integer in the key tells you which letter to choose in the corresponding row. Result:

He sitteth between the cherubims. The isles may be glad thereof. As the rivers in the south.

- b. Quite secure. In each row there is one of eight possibilities. So if the ciphertext is $8n$ letters in length, then the number of possible plaintexts is 8^n .
 c. Not very secure. Lord Peter figured it out. (from *The Nine Tailors*)

CHAPTER 3 BLOCK CIPHERS AND THE DATA ENCRYPTION STANDARD

ANSWERS TO QUESTIONS

- 3.1 Most symmetric block encryption algorithms in current use are based on the Feistel block cipher structure. Therefore, a study of the Feistel structure reveals the principles behind these more recent ciphers.
- 3.2 A **stream cipher** is one that encrypts a digital data stream one bit or one byte at a time. A **block cipher** is one in which a block of plaintext is treated as a whole and used to produce a ciphertext block of equal length.
- 3.3 If a small block size, such as $n = 4$, is used, then the system is equivalent to a classical substitution cipher. For small n , such systems are vulnerable to a statistical analysis of the plaintext. For a large block size, the size of the key, which is on the order of $n \times 2^n$, makes the system impractical.
- 3.4 In a product cipher, two or more basic ciphers are performed in sequence in such a way that the final result or product is cryptographically stronger than any of the component ciphers.
- 3.5 In **diffusion**, the statistical structure of the plaintext is dissipated into long-range statistics of the ciphertext. This is achieved by having each plaintext digit affect the value of many ciphertext digits, which is equivalent to saying that each ciphertext digit is affected by many plaintext digits. **Confusion** seeks to make the relationship between the statistics of the ciphertext and the value of the encryption key as complex as possible, again to thwart attempts to discover the key. Thus, even if the attacker can get some handle on the statistics of the ciphertext, the way in which the key was used to produce that ciphertext is so complex as to make it difficult to deduce the key. This is achieved by the use of a complex substitution algorithm.
- 3.6 **Block size:** Larger block sizes mean greater security (all other things being equal) but reduced encryption/decryption speed. **Key size:** Larger key size means greater security but may decrease encryption/decryption speed. **Number of rounds:** The essence of the Feistel cipher is that a single round offers inadequate security but that multiple rounds offer increasing security. **Subkey generation algorithm:** Greater complexity in this algorithm should lead to greater difficulty of cryptanalysis. **Round function:** Again, greater complexity generally means greater resistance to cryptanalysis. **Fast software encryption/decryption:** In many cases, encryption is embedded in applications or utility functions in such a way as to preclude a hardware implementation. Accordingly, the speed of execution of the

algorithm becomes a concern. **Ease of analysis:** Although we would like to make our algorithm as difficult as possible to cryptanalyze, there is great benefit in making the algorithm easy to analyze. That is, if the algorithm can be concisely and clearly explained, it is easier to analyze that algorithm for cryptanalytic vulnerabilities and therefore develop a higher level of assurance as to its strength.

- 3.7 The S-box is a substitution function that introduces nonlinearity and adds to the complexity of the transformation.
- 3.8 The avalanche effect is a property of any encryption algorithm such that a small change in either the plaintext or the key produces a significant change in the ciphertext.
- 3.9 **Differential cryptanalysis** is a technique in which chosen plaintexts with particular XOR difference patterns are encrypted. The difference patterns of the resulting ciphertext provide information that can be used to determine the encryption key. **Linear cryptanalysis** is based on finding linear approximations to describe the transformations performed in a block cipher.

ANSWERS TO PROBLEMS

- 3.1
 - a. For an n -bit block size are 2^n possible different plaintext blocks and 2^n possible different ciphertext blocks. For both the plaintext and ciphertext, if we treat the block as an unsigned integer, the values are in the range 0 through $2^n - 1$. For a mapping to be reversible, each plaintext block must map into a unique ciphertext block. Thus, to enumerate all possible reversible mappings, the block with value 0 can map into anyone of 2^n possible ciphertext blocks. For any given mapping of the block with value 0, the block with value 1 can map into any one of $2^n - 1$ possible ciphertext blocks, and so on. Thus, the total number of reversible mappings is $(2^n)!$.
 - b. In theory, the key length could be $\log_2(2^n)!$ bits. For example, assign each mapping a number, from 1 through $(2^n)!$ and maintain a table that shows the mapping for each such number. Then, the key would only require $\log_2(2^n)!$ bits, but we would also require this huge table. A more straightforward way to define the key is to have the key consist of the ciphertext value for each plaintext block, listed in sequence for plaintext blocks 0 through $2^n - 1$. This is what is suggested by Table 3.1. In this case the key size is $n \times 2^n$ and the huge table is not required.
- 3.2 Because of the key schedule, the round functions used in rounds 9 through 16 are mirror images of the round functions used in rounds 1 through 8. From this fact we see that encryption and decryption are identical. We are given a ciphertext c . Let $m' = c$. Ask the encryption oracle to encrypt m' . The ciphertext returned by the oracle will be the decryption of c .
- 3.3
 - a. We need only determine the probability that for the remaining $N - t$ plaintexts P_i , we have $E[K, P_i] \neq E[K', P_i]$. But $E[K, P_i] = E[K', P_i]$ for all the remaining P_i with probability $1 - 1/(N - t)!$.

- b. Without loss of generality we may assume the $E[K, P_i] = P_i$ since $E_K(\bullet)$ is taken over all permutations. It then follows that we seek the probability that a permutation on $N - t$ objects has exactly t' fixed points, which would be the additional t' points of agreement between $E(K, \bullet)$ and $E(K', \bullet)$. But a permutation on $N - t$ objects with t' fixed points is equal to the number of ways t' out of $N - t$ objects can be fixed, while the remaining $N - t - t'$ are not fixed. Then using Problem 3.4 we have that

$$\begin{aligned} \Pr(t' \text{ additional fixed points}) &= \binom{N-t}{t'} \times \Pr(\text{no fixed points in } N-t-t' \text{ objects}) \\ &= \frac{1}{(t')!} \times \sum_{k=0}^{N-t-t'} \frac{(-1)^k}{k!} \end{aligned}$$

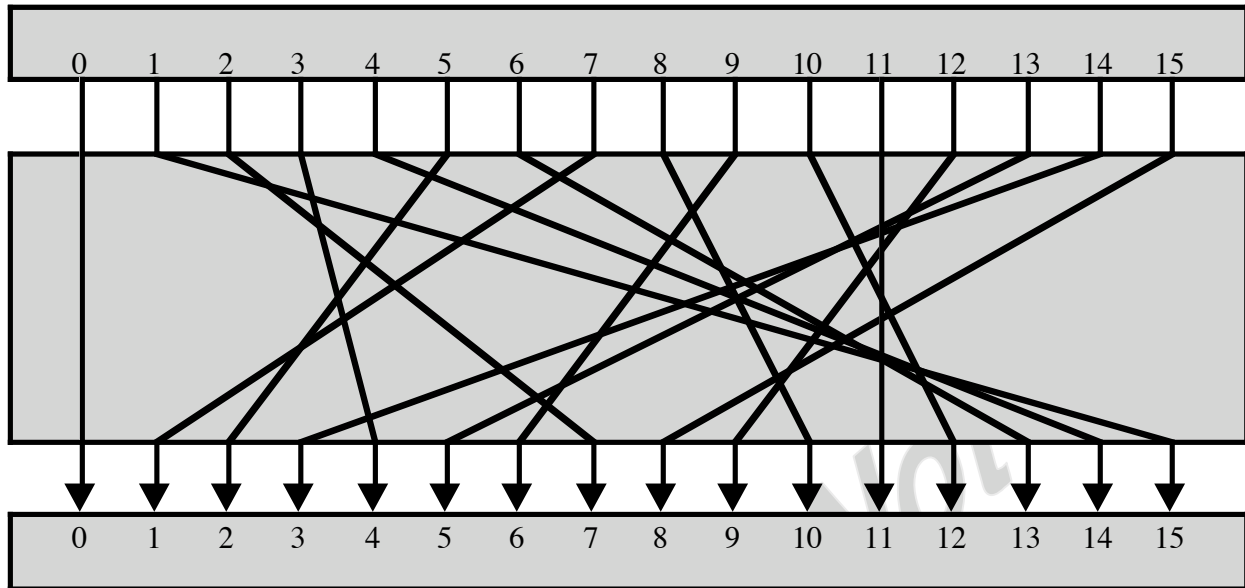
We see that this reduces to the solution to part (a) when $t' = N - t$.

- 3.4 Let S_{2^n} be the set of permutations on $[0, 1, \dots, 2^n - 1]$, which is referred to as the symmetric group on 2^n objects, and let $N = 2^n$. For $0 \leq i \leq N$, let A_i be all mappings $\pi \in S_{2^n}$ for which $\pi(i) = i$. It follows that $|A_i| = (N-1)!$ and $|\bigcap_{1 \leq i \leq k} A_i| = (N-k)!$. The inclusion-exclusion principle states that

$$\begin{aligned} \Pr(\text{no fixed points in } \pi) &= \frac{1}{N!} \sum_{k=0}^N \binom{N}{k} \times (N-k)! \times (-1)^k \\ &= \sum_{k=0}^N \frac{(-1)^k}{k!} \\ &= 1 - 1 + 1/2! - 1/3! + \dots + (-1)^N N \times 1/N! \\ &= e^{-1} + O\left(\frac{1}{N!}\right) \end{aligned}$$

Then since $e^{-1} \approx 0.368$, we find that for even small values of N , approximately 37% of permutations contain no fixed points.

3.5



3.6 Main key $K = 111\dots111$ (56 bits)
 Round keys $K_1 = K_2 = \dots = K_{16} = 1111\dots111$ (48 bits)
 Ciphertext $C = 1111\dots111$ (64 bits)
 Input to the first round of decryption =
 $LD_0RD_0 = RE_{16}LE_{16} = IP(C) = 1111\dots111$ (64 bits)
 $LD_0 = RD_0 = 1111\dots111$ (32 bits)

Output of the first round of decryption = LD_1RD_1
 $LD_1 = RD_0 = 1111\dots111$ (32 bits)

Thus, the bits no. 1 and 16 of the output are equal to '1'.

$RD_1 = LD_0 \oplus F(RD_0, K_{16})$

We are looking for bits no. 1 and 16 of RD_1 (33 and 48 of the entire output).

Based on the analysis of the permutation P , bit 1 of $F(RD_0, K_{16})$ comes from the fourth output of the S-box S_4 , and bit 16 of $F(RD_0, K_{16})$ comes from the second output of the S-box S_3 . These bits are XOR-ed with 1's from the corresponding positions of LD_0 .

Inside of the function F ,

$E(RD_0) \approx K_{16} = 0000\dots000$ (48 bits),

and thus inputs to all eight S-boxes are equal to "000000".

Output from the S-box $S_4 = "0111"$, and thus the fourth output is equal to '1',

Output from the S-box $S_3 = "1010"$, and thus the second output is equal to '0'.

From here, after the XOR, the bit no. 33 of the first round output is equal to '0', and the bit no. 48 is equal to '1'.

3.7 In the solution given below the following general properties of the XOR function are used:

$$\begin{aligned} A \oplus 1 &= A' \\ (A \oplus B)' &= A' \oplus B = A \oplus B' \\ A' \oplus B' &= A \oplus B \end{aligned}$$

Where A' = the bitwise complement of A .

a. $F(R_n, K_{n+1}) = 1$

We have

$$L_{n+1} = R_n; R_{n+1} = L_n \oplus F(R_n, K_{n+1}) = L_n \oplus 1 = L_n'$$

Thus

$$L_{n+2} = R_{n+1} = L_n'; R_{n+2} = L_{n+1} = R_n'$$

i.e., after each two rounds we obtain the bit complement of the original input, and every four rounds we obtain back the original input:

$$L_{n+4} = L_{n+2}' = L_n; R_{n+4} = R_{n+2}' = R_n$$

Therefore,

$$L_{16} = L_0; R_{16} = R_0$$

An input to the inverse initial permutation is $R_{16} L_{16}$.

Therefore, the transformation computed by the modified DES can be represented as follows:

$C = IP^{-1}(SWAP(IP(M)))$, where SWAP is a permutation exchanging the position of two halves of the input: $SWAP(A, B) = (B, A)$.

This function is linear (and thus also affine). Actually, this is a permutation, the product of three permutations IP, SWAP, and IP^{-1} . This permutation is however different from the identity permutation.

b. $F(R_n, K_{n+1}) = R_n'$

We have

$$L_{n+1} = R_n; R_{n+1} = L_n \oplus F(R_n, K_{n+1}) = L_n \oplus R_n'$$

$$L_{n+2} = R_{n+1} = L_n \oplus R_n'$$

$$R_{n+2} = L_{n+1} \oplus F(R_{n+1}, K_{n+2}) = R_n \approx (L_n \oplus R_n')' = R_n \oplus L_n \oplus R_n'' = L_n$$

$$L_{n+3} = R_{n+2} = L_n$$

$$R_{n+3} = L_{n+2} \oplus F(R_{n+2}, K_{n+3}) = (L_n \approx R_n') \oplus L_n' = R_n' \oplus 1 = R_n$$

i.e., after each three rounds we come back to the original input.

$$L_{15} = L_0; R_{15} = R_0$$

and

$$L_{16} = R_0 \quad (1)$$

$$R_{16} = L_0 \oplus R_0' \quad (2)$$

An input to the inverse initial permutation is $R_{16} L_{16}$.

A function described by (1) and (2) is affine, as bitwise complement is affine, and the other transformations are linear.

The transformation computed by the modified DES can be represented as follows:

$$C = IP^{-1}(FUN2(IP(M))), \text{ where } FUN2(A, B) = (A \oplus B', B).$$

This function is affine as a product of three affine functions.

In all cases decryption looks exactly the same as encryption.

- 3.8 a.** First, pass the 64-bit input through PC-1 (Table 3.4a) to produce a 56-bit result. Then perform a left circular shift separately on the two 28-bit halves. Finally, pass the 56-bit result through PC-2 (Table 3.4b) to produce the 48-bit K_1 :

in binary notation: 0000 1011 0000 0010 0110 0111
 1001 1011 0100 1001 1010 0101

in hexadecimal notation: 0 B 0 2 6 7 9 B 4 9 A 5

- b.** L_0, R_0 are derived by passing the 64-plaintext through IP (Table 3.2a):

$$L_0 = 1100 \ 1100 \ 0000 \ 0000 \ 1100 \ 1100 \ 1111 \ 1111$$

$$R_0 = 1111 \ 0000 \ 1010 \ 1010 \ 1111 \ 0000 \ 1010 \ 1010$$

- c.** The E table (Table 3.2c) expands R_0 to 48 bits:

$$E(R_0) = 01110 \ 100001 \ 010101 \ 010101 \ 011110 \ 100001 \ 010101 \ 010101$$

- d.** $A = 011100 \ 010001 \ 011100 \ 110010 \ 111000 \ 010101 \ 110011 \ 110000$

- e.** $S_1^{00}(1110) = S_1^0(14) = 0$ (base 10) = 0000 (base 2)
 $S_2^{01}(1000) = S_2^1(8) = 12$ (base 10) = 1100 (base 2)
 $S_3^{00}(1110) = S_3^0(14) = 2$ (base 10) = 0010 (base 2)
 $S_4^{10}(1001) = S_4^2(9) = 1$ (base 10) = 0001 (base 2)
 $S_5^{10}(1100) = S_5^2(12) = 6$ (base 10) = 0110 (base 2)
 $S_6^{01}(1010) = S_6^1(10) = 13$ (base 10) = 1101 (base 2)
 $S_7^{11}(1001) = S_7^3(9) = 5$ (base 10) = 0101 (base 2)
 $S_8^{10}(1000) = S_8^2(8) = 0$ (base 10) = 0000 (base 2)

- f.** $B = 0000 \ 1100 \ 0010 \ 0001 \ 0110 \ 1101 \ 0101 \ 0000$

- g.** Using Table 3.2d, $P(B) = 1001 \ 0010 \ 0001 \ 1100 \ 0010 \ 0000 \ 1001 \ 1100$

h. $R_1 = 0101\ 1110\ 0001\ 1100\ 1110\ 1100\ 0110\ 0011$

i. $L_1 = R_0$. The ciphertext is the concatenation of L_1 and R_1 . Source: [MEYE82]

3.9 The reasoning for the Feistel cipher, as shown in Figure 3.3, applies in the case of DES. We only have to show the effect of the IP and IP^{-1} functions. For encryption, the input to the final IP^{-1} is $RE_{16} \parallel LE_{16}$. The output of that stage is the ciphertext. On decryption, the first step is to take the ciphertext and pass it through IP. Because IP is the inverse of IP^{-1} , the result of this operation is just $RE_{16} \parallel LE_{16}$, which is equivalent to $LD_0 \parallel RD_0$. Then, we follow the same reasoning as with the Feistel cipher to reach a point where $LE_0 = RD_{16}$ and $RE_0 = LD_{16}$. Decryption is completed by passing $LD_0 \parallel RD_0$ through IP^{-1} . Again, because IP is the inverse of IP^{-1} , passing the plaintext through IP as the first step of encryption yields $LD_0 \parallel RD_0$, thus showing that decryption is the inverse of encryption.

3.10 a. Let us work this from the inside out.

$$T_{16}(L_{15} \parallel R_{15}) = L_{16} \parallel R_{16}$$

$$T_{17}(L_{16} \parallel R_{16}) = R_{16} \parallel L_{16}$$

$$IP [IP^{-1} (R_{16} \parallel L_{16})] = R_{16} \parallel L_{16}$$

$$TD_1(R_{16} \parallel L_{16}) = R_{15} \parallel L_{15}$$

b. $T_{16}(L_{15} \parallel R_{15}) = L_{16} \parallel R_{16}$

$$IP [IP^{-1} (L_{16} \parallel R_{16})] = L_{16} \parallel R_{16}$$

$$TD_1(R_{16} \parallel L_{16}) = R_{16} \parallel L_{16} \oplus f(R_{16}, K_{16}) \\ \neq L_{15} \parallel R_{15}$$

3.11 PC-1 is essentially the same as IP with every eighth bit eliminated. This would enable a similar type of implementation. Beyond that, there does not appear to be any particular cryptographic significance.

3.12

Round number	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Bits rotated	0	1	2	2	2	2	2	2	1	2	2	2	2	2	2	1

3.13 a. The equality in the hint can be shown by listing all 1-bit possibilities:

A	B	$A \oplus B$	$(A \oplus B)'$	$A' \oplus B$
0	0	0	1	1
0	1	1	0	0
1	0	1	0	0
1	1	0	1	1

We also need the equality $A \oplus B = A' \oplus B'$, which is easily seen to be true. Consider the two XOR operations in Figure 3.6. If the plaintext and key for an encryption are complemented, then the inputs to the first XOR are also complemented. The output, then, is the same as for the uncomplemented inputs. Further down, we see that only one of the two inputs to the second XOR is complemented, therefore, the output is the complement of the output that would be generated by uncomplemented inputs.

- b. In a chosen plaintext attack, if for chosen plaintext X , the analyst can obtain $Y_1 = E[K, X]$ and $Y_2 = E[K', X]$, then an exhaustive key search requires only 2^{55} rather than 2^{56} encryptions. To see this, note that $(Y_2)' = E[K', X]$. Now, pick a test value of the key T and perform $E[T, X]$. If the result is Y_1 , then we know that T is the correct key. If the result is $(Y_2)'$, then we know that T' is the correct key. If neither result appears, then we have eliminated two possible keys with one encryption.

- 3.14 The result can be demonstrated by tracing through the way in which the bits are used. An easy, but not necessary, way to see this is to number the 64 bits of the key as follows (read each vertical column of 2 digits as a number):

2113355-1025554-0214434-1123334-0012343-2021453-0202435-0110454-
1031975-1176107-2423401-7632789-7452553-0858846-6836043-9495226-

The first bit of the key is identified as 21, the second as 10, the third as 13, and so on. The eight bits that are not used in the calculation are unnumbered. The numbers 01 through 28 and 30 through 57 are used. The reason for this assignment is to clarify the way in which the subkeys are chosen. With this assignment, the subkey for the first iteration contains 48 bits, 01 through 24 and 30 through 53, in their natural numerical order. It is easy at this point to see that the first 24 bits of each subkey will always be from the bits designated 01 through 28, and the second 24 bits of each subkey will always be from the bits designated 30 through 57.

- 3.15 For $1 \leq i \leq 128$, take $c_i \in \{0, 1\}^{128}$ to be the string containing a 1 in position i and then zeros elsewhere. Obtain the decryption of these 128 ciphertexts. Let m_1, m_2, \dots, m_{128} be the corresponding plaintexts. Now, given any ciphertext c which does not consist of all zeros, there is a unique nonempty subset of the c_i 's which we can XOR together to obtain c . Let $I(c) \subseteq \{1, 2, \dots, 128\}$ denote this subset. Observe

$$c = \bigoplus_{i \in I(c)} c_i = \bigoplus_{i \in I(c)} E(m_i) = E\left(\bigoplus_{i \in I(c)} m_i\right)$$

Thus, we obtain the plaintext of c by computing $\bigoplus_{i \in I(c)} m_i$. Let $\mathbf{0}$ be the all-zero string. Note that $\mathbf{0} = \mathbf{0} \oplus \mathbf{0}$. From this we obtain $E(\mathbf{0}) = E(\mathbf{0} \oplus \mathbf{0}) = E(\mathbf{0}) \oplus E(\mathbf{0}) = \mathbf{0}$. Thus, the plaintext of $c = \mathbf{0}$ is $m = \mathbf{0}$. Hence we can decrypt every $c \in \{0, 1\}^{128}$.

- 3.16 a. This adds nothing to the security of the algorithm. There is a one-to-one reversible relationship between the 10-bit key and the output of the P10

function. If we consider the output of the P10 function as a new key, then there are still 2^{10} different unique keys.

b. By the same reasoning as (a), this adds nothing to the security of the algorithm.

3.17 $s = wxyz + wxy + wyz + wy + wz + yz + w + x + z$
 $t = wxz + wyz + wz + xz + yz + w + y$

3.18 OK

Please Do Not
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CHAPTER 4 BASIC CONCEPTS IN NUMBER THEORY AND FINITE FIELDS

ANSWERS TO QUESTIONS

- 4.1 A **group** is a set of elements that is closed under a binary operation and that is associative and that includes an identity element and an inverse element.
- 4.2 A **ring** is a set of elements that is closed under two binary operations, addition and subtraction, with the following: the addition operation is a group that is commutative; the multiplication operation is associative and is distributive over the addition operation.
- 4.3 A **field** is a ring in which the multiplication operation is commutative, has no zero divisors, and includes an identity element and an inverse element.
- 4.4 A nonzero b is a **divisor** of a if $a = mb$ for some m , where a , b , and m are integers. That is, b is a **divisor** of a if there is no remainder on division.
- 4.5 In modular arithmetic, all arithmetic operations are performed modulo some integer.
- 4.6 (1) Ordinary polynomial arithmetic, using the basic rules of algebra. (2) Polynomial arithmetic in which the arithmetic on the coefficients is performed over a finite field; that is, the coefficients are elements of the finite field. (3) Polynomial arithmetic in which the coefficients are elements of a finite field, and the polynomials are defined modulo a polynomial $M(x)$ whose highest power is some integer n .

ANSWERS TO PROBLEMS

- 4.1 a. $n!$
b. We can do this by example. Consider the set S_3 . We have $\{3, 2, 1\} \bullet \{1, 3, 2\} = \{2, 3, 1\}$, but $\{1, 3, 2\} \bullet \{3, 2, 1\} = \{3, 1, 2\}$.

4.2 Here are the addition and multiplication tables

+	0	1	2
0	0	1	2
1	1	2	0
2	2	0	1

×	0	1	2
0	0	0	0
1	0	1	2
2	0	2	1

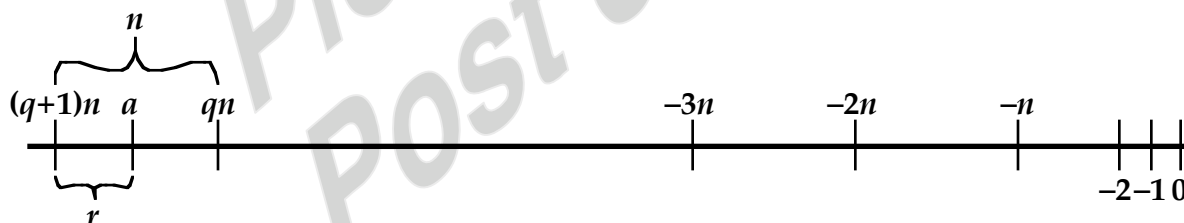
- a. Yes. The identity element is 0, and the inverses of 0, 1, 2 are respectively 0, 2, 1.
b. No. The identity element is 1, but 0 has no inverse.

4.3 S is a ring. We show using the axioms in Figure 4.2:

- (A1) Closure: The sum of any two elements in S is also in S.
(A2) Associative: S is associative under addition, by observation.
(A3) Identity element: a is the additive identity element for addition.
(A4) Inverse element: The additive inverses of a and b are b and a, respectively.
(A5) Commutative: S is commutative under addition, by observation.
(M1) Closure: The product of any two elements in S is also in S.
(M2) Associative: S is associative under multiplication, by observation.
(M3) Distributive laws: S is distributive with respect to the two operations, by observation.

4.4 The equation is the same. For integer $a < 0$, a will either be an integer multiple of n or fall between two consecutive multiples qn and $(q+1)n$, where $q < 0$. The remainder satisfies the condition $0 \leq r \leq n$.

4.5 In this diagram, q is a negative integer.



4.6 a. 2 b. 3 c. 4 There are other correct answers.

4.7 Section 4.3 defines the relationship: $a = n \times \lfloor a/n \rfloor + (a \bmod n)$. Thus, we can define the mod operator as: $a \bmod n = a - n \times \lfloor a/n \rfloor$.

- a. $5 \bmod 3 = 5 - 3 \lfloor 5/3 \rfloor = 2$
b. $5 \bmod -3 = 5 - (-3) \lfloor 5/(-3) \rfloor = -1$
c. $-5 \bmod 3 = -5 - 3 \lfloor (-5)/3 \rfloor = 1$
d. $-5 \bmod -3 = -5 - (-3) \lfloor (-5)/(-3) \rfloor = -2$

This example is from [GRAH94]

4.8 $a = b$

4.9 Recall Figure 4.1 and that any integer a can be written in the form

$$a = qn + r$$

where q is some integer and r one of the numbers

$$0, 1, 2, \dots, n-1$$

Using the second definition, no two of the remainders in the above list are congruent (mod n), because the difference between them is less than n and therefore n does not divide that difference. Therefore, two numbers that are not congruent (mod n) must have different remainders. So we conclude that n divides $(a-b)$ if and only if a and b are numbers that have the same remainder when divided by n .

4.10 1, 2, 4, 6, 16, 12

- 4.11** a. This is the definition of congruence as used in Section 4.3.
b. The first two statements mean

$$a - b = nk; \quad b - c = nm$$

so that

$$a - c = (a - b) + (b - c) = n(k + m)$$

- 4.12** a. Let $c = a \bmod n$ and $d = b \bmod n$. Then
 $c = a + kn; \quad d = b + mn; \quad c - d = (a - b) + (k - m)n$.
Therefore $(c - d) = (a - b) \bmod n$
b. Using the definitions of c and d from part (a),
 $cd = ab + n(kb + ma + kmn)$
Therefore $cd = (a \times b) \bmod n$

4.13 $1^{-1} = 1, 2^{-1} = 3, 3^{-1} = 2, 4^{-1} = 4$

4.14 We have $1 \equiv 1 \pmod{9}; 10 \equiv 1 \pmod{9}; 10^2 \equiv 10(10) \equiv 1(1) \equiv 1 \pmod{9}; 10^{n-1} \equiv 1 \pmod{9}$. Express N as $a_0 + a_1 10^1 + \dots + a_{n-1} 10^{n-1}$. Then $N \equiv a_0 + a_1 + \dots + a_{n-1} \pmod{9}$.

- 4.15** a. $\gcd(24140, 16762) = \gcd(16762, 7378) = \gcd(7378, 2006) = \gcd(2006, 1360) = \gcd(1360, 646) = \gcd(646, 68) = \gcd(68, 34) = \gcd(34, 0) = 34$
b. 35

- 4.16** a. We want to show that $m > 2r$. This is equivalent to $qn + r > 2r$, which is equivalent to $qn > r$. Since $n > r$, we must have $qn > r$.
b. If you study the pseudocode for Euclid's algorithm in the text, you can see that the relationship defined by Euclid's algorithm can be expressed as

$$A_i = q_i A_{i+1} + A_{i+2}$$

The relationship $A_{i+2} < A_i/2$ follows immediately from (a).

- c. From (b), we see that $A_3 < 2^{-1}A_1$, that $A_5 < 2^{-1}A_3 < 2^{-2}A_1$, and in general that $A_{2j+1} < 2^{-j}A_1$ for all integers j such that $1 < 2j + 1 \leq k + 2$, where k is the number

of steps in the algorithm. If k is odd, we take $j = (k + 1)/2$ to obtain $N > (k + 1)/2$, and if k is even, we take $j = k/2$ to obtain $N > k/2$. In either case $k < 2N$.

- 4.17 a. Euclid:** $\gcd(2152, 764) = \gcd(764, 624) = \gcd(624, 140) = \gcd(140, 64) = \gcd(64, 12) = \gcd(12, 4) = \gcd(4, 0) = 4$
Stein: $A_1 = 2152, B_1 = 764, C_1 = 1; A_2 = 1076, B_2 = 382, C_2 = 2; A_3 = 538, B_3 = 191, C_3 = 4; A_4 = 269, B_4 = 191, C_4 = 4; A_5 = 78, B_5 = 191, C_5 = 4; A_6 = 39, B_5 = 191, C_5 = 4; A_6 = 152, B_6 = 39, C_6 = 4; A_7 = 76, B_7 = 39, C_7 = 4; A_8 = 38, B_8 = 39, C_8 = 4; A_9 = 19, B_9 = 39, C_9 = 4; A_{10} = 20, B_{10} = 19, C_{10} = 4; A_{11} = 10, B_{11} = 19, C_{11} = 4; A_{12} = 5, B_{12} = 19, C_{12} = 4; A_{13} = 14, B_{13} = 5, C_{13} = 4; A_{14} = 7, B_{14} = 5, C_{14} = 4; A_{15} = 2, B_{15} = 5, C_{15} = 4; A_{16} = 1, B_{16} = 5, C_{16} = 4; A_{17} = 4, B_{17} = 1, C_{17} = 4; A_{18} = 2, B_{18} = 1, C_{18} = 4; A_{19} = 1, B_{19} = 1, C_{19} = 4; \gcd(2152, 764) = 1 \times 4 = 4$
- b.** Euclid's algorithm requires a "long division" at each step whereas the Stein algorithm only requires division by 2, which is a simple operation in binary arithmetic.
- 4.18 a.** If A_n and B_n are both even, then $2 \times \gcd(A_{n+1}, B_{n+1}) = \gcd(A_n, B_n)$. But $C_{n+1} = 2C_n$, and therefore the relationship holds.
 If one of A_n and B_n is even and one is odd, then dividing the even number does not change the gcd. Therefore, $\gcd(A_{n+1}, B_{n+1}) = \gcd(A_n, B_n)$. But $C_{n+1} = C_n$, and therefore the relationship holds.
 If both A_n and B_n are odd, we can use the following reasoning based on the rules of modular arithmetic. Let $D = \gcd(A_n, B_n)$. Then D divides $|A_n - B_n|$ and D divides $\min(A_n, B_n)$. Therefore, $\gcd(A_{n+1}, B_{n+1}) = \gcd(A_n, B_n)$. But $C_{n+1} = C_n$, and therefore the relationship holds.
- b.** If at least one of A_n and B_n is even, then at least one division by 2 occurs to produce A_{n+1} and B_{n+1} . Therefore, the relationship is easily seen to hold.
 Suppose that both A_n and B_n are odd; then A_{n+1} is even; in that case the relationship obviously holds.
- c.** By the result of (b), every 2 iterations reduces the AB product by a factor of 2. The AB product starts out at $< 2^{2N}$. There are at most $\log(2^{2N}) = 2N$ pairs of iterations, or at most $4N$ iterations.
- d.** At the very beginning, we have $A_1 = A, B_1 = B$, and $C_1 = 1$. Therefore $C_1 \times \gcd(A_1, B_1) = \gcd(A, B)$. Then, by (a), $C_2 \times \gcd(A_2, B_2) = C_1 \times \gcd(A_1, B_1) = \gcd(A, B)$. Generalizing, $C_n \times \gcd(A_n, B_n) = \gcd(A, B)$. The algorithm stops when $A_n = B_n$. But, for $A_n = B_n$, $\gcd(A_n, B_n) = A_n$. Therefore, $C_n \times \gcd(A_n, B_n) = C_n \times A_n = \gcd(A, B)$.
- 4.19 a.** 3239
b. $\gcd(40902, 24240) = 34 \neq 1$, so there is no multiplicative inverse.
c. 550

4.20

+	0	1	2	3	4
0	0	1	2	3	4
1	1	2	3	4	0
2	2	3	4	0	1
3	3	4	0	1	2
4	4	0	1	2	3

×	0	1	2	3	4
0	0	0	0	0	0
1	0	1	2	3	4
2	0	2	4	1	3
3	0	3	1	4	2
4	0	4	3	2	1

w	$-w$	w^{-1}
0	0	—
1	4	1
2	3	3
3	2	2
4	1	4

4.21 Let S be the set of polynomials whose coefficients form a field F . Recall that addition is defined as follows: For

$$f(x) = \sum_{i=0}^n a_i x^i; \quad g(x) = \sum_{i=0}^m b_i x^i; \quad n \geq m$$

then addition is defined as:

$$f(x) + g(x) = \sum_{i=0}^m (a_i + b_i) x^i + \sum_{i=m+1}^n a_i x^i$$

Using the axioms in Figure 4.2, we now examine the addition operation:

(A1) Closure: The sum of any two elements in S is also in S . This is so because the sum of any two coefficients is also a valid coefficient, because F is a field.

(A2) Associative: S is associative under addition. This is so because coefficient addition is associative.

(A3) Identity element: 0 is the additive identity element for addition.

(A4) Inverse element: The additive inverse of a polynomial $f(x)$ a polynomial with the coefficients $-a_i$.

(A5) Commutative: S is commutative under addition. This is so because coefficient addition is commutative.

Multiplication is defined as follows:

$$f(x) \times g(x) = \sum_{i=0}^{n+m} c_i x^i$$

where

$$c_k = a_0 b_k + a_1 b_{k-1} + \cdots + a_{k-1} b_1 + a_k b_0$$

In the last formula, we treat a_i as zero for $i > n$ and b_i as zero for $i > m$.

- (M1) Closure: The product of any two elements in S is also in S . This is so because the product of any two coefficients is also a valid coefficient, because F is a field.
- (M2) Associative: S is associative under multiplication. This is so because coefficient multiplication is associative.
- (M3) Distributive laws: S is distributive with respect to the two operations, by the field properties of the coefficients.

- 4.22 a. True. To see, this consider the equation for c_k , above, for $k = n + m$, where $f(x)$ and $g(x)$ are monic. The only nonzero term on the right of equation is $a_n b_m$, which has the value 1.
- b. True. We have $c_{n+m} = a_n b_m \neq 0$.
- c. True when $m \neq n$; in that case the highest degree coefficient is of degree $\max[m, n]$. But false in general when $m = n$, because the highest-degree coefficients might cancel (be additive inverses).
- 4.23 a. $9x^2 + 7x + 7$
- b. $5x^3 + 7x^2 + 2x + 6$
- 4.24 a. Reducible: $(x + 1)(x^2 + x + 1)$
- b. Irreducible. If you could factor this polynomial, one factor would be either x or $(x + 1)$, which would give you a root of $x = 0$ or $x = 1$ respectively. By substitution of 0 and 1 into this polynomial, it clearly has no roots.
- c. Reducible: $(x + 1)^4$
- 4.25 a. 1
- b. 1
- c. $x + 1$
- d. $x + 78$ Source: [KOBL94]

4.26 Polynomial Arithmetic Modulo ($x^2 + x + 1$):

		000 0	001 1	010 x	011 $x + 1$
000	0	0	1	x	$x + 1$
001	1	1	0	$x + 1$	x
010	x	x	$x + 1$	0	1
011	$x + 1$	$x + 1$	x	1	0

		000 0	001 1	010 x	011 $x + 1$
000	0	0	0	0	0
001	1	0	1	x	$x + 1$
010	x	0	x	$x + 1$	1
011	$x + 1$	0	$x + 1$	1	x

4.27 $x^2 + 1$

4.28 Generator for $GF(2^4)$ using $x^4 + x + 1$

Power Representation	Polynomial Representation	Binary Representation	Decimal (Hex) Representation
0	0	0000	0
$g^0 (= g^{15})$	1	0001	1
g^1	g	0010	2
g^2	g^2	0100	4
g^3	g^3	1000	8
g^4	$g + 1$	0011	3
g^5	$g^2 + g$	0110	6
g^6	$g^3 + g^2$	1100	12
g^7	$g^3 + g + 1$	1011	11
g^8	$g^2 + 1$	0101	5
g^9	$g^3 + g$	1010	10
g^{10}	$g^2 + g + 1$	0111	7
g^{11}	$g^3 + g^2 + g$	1110	14
g^{12}	$g^3 + g^2 + g + 1$	1111	15
g^{13}	$g^3 + g^2 + 1$	1101	13
g^{14}	$g^3 + 1$	1001	9

CHAPTER 5 ADVANCED ENCRYPTION STANDARD

ANSWERS TO QUESTIONS

- 5.1 **Security:** Actual security; randomness; soundness, other security factors.
Cost: Licensing requirements; computational efficiency; memory requirements.
Algorithm and Implementation Characteristics: Flexibility; hardware and software suitability; simplicity.
- 5.2 General security; software implementations; restricted-space environments; hardware implementations; attacks on implementations; encryption vs. decryption; key agility; other versatility and flexibility; potential for instruction-level parallelism.
- 5.3 Rijndael allows for block lengths of 128, 192, or 256 bits. AES allows only a block length of 128 bits.
- 5.4 The State array holds the intermediate results on the 128-bit block at each stage in the processing.
- 5.5
1. Initialize the S-box with the byte values in ascending sequence row by row. The first row contains {00}, {01}, {02}, etc., the second row contains {10}, {11}, etc., and so on. Thus, the value of the byte at row x , column y is $\{xy\}$.
 2. Map each byte in the S-box to its multiplicative inverse in the finite field $GF(2^8)$; the value {00} is mapped to itself.
 3. Consider that each byte in the S-box consists of 8 bits labeled $(b_7, b_6, b_5, b_4, b_3, b_2, b_1, b_0)$. Apply the following transformation to each bit of each byte in the S-box:

$$b'_i = b_i \oplus b_{(i+4) \bmod 8} \oplus b_{(i+5) \bmod 8} \oplus b_{(i+6) \bmod 8} \oplus b_{(i+7) \bmod 8} \oplus c_i$$

where c_i is the i th bit of byte c with the value {63}; that is, $(c_7c_6c_5c_4c_3c_2c_1c_0) = (01100011)$. The prime (') indicates that the variable is to be updated by the value on the right.

- 5.6 Each individual byte of **State** is mapped into a new byte in the following way: The leftmost 4 bits of the byte are used as a row value and the rightmost 4 bits are used as a column value. These row and column values serve as indexes into the S-box to select a unique 8-bit output value.
- 5.7 The first row of **State** is not altered. For the second row, a 1-byte circular left shift is performed. For the third row, a 2-byte circular left shift is performed. For the third row, a 3-byte circular left shift is performed.

- 5.8 12 bytes.
- 5.9 MixColumns operates on each column individually. Each byte of a column is mapped into a new value that is a function of all four bytes in that column.
- 5.10 The 128 bits of **State** are bitwise XORed with the 128 bits of the round key.
- 5.11 The AES key expansion algorithm takes as input a 4-word (16-byte) key and produces a linear array of 44 words (176 bytes). The expansion is defined by the pseudocode in Section 5.4.
- 5.12 SubBytes operates on State, with each byte mapped into a new byte using the S-box. SubWord operates on an input word, with each byte mapped into a new byte using the S-box.
- 5.13 ShiftRows is described in the answer to Question 5.8. RotWord performs a one-byte circular left shift on a word; thus it is equivalent to the operation of ShiftRows on the second row of State.
- 5.14 For the AES decryption algorithm, the sequence of transformations for decryption differs from that for encryption, although the form of the key schedules for encryption and decryption is the same. The equivalent version has the same sequence of transformations as the encryption algorithm (with transformations replaced by their inverses). To achieve this equivalence, a change in key schedule is needed.

ANSWERS TO PROBLEMS

- 5.1 We want to show that $d(x) = a(x) \times b(x) \bmod (x^4 + 1) = 1$. Substituting into Equation (5.12) in Appendix 5A, we have:

$$\begin{bmatrix} d_0 \\ d_1 \\ d_2 \\ d_3 \end{bmatrix} = \begin{bmatrix} a_0 & a_3 & a_2 & a_1 \\ a_1 & a_0 & a_3 & a_2 \\ a_2 & a_1 & a_0 & a_3 \\ a_3 & a_2 & a_1 & a_0 \end{bmatrix} \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \end{bmatrix} = \begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} 0E \\ 09 \\ 0D \\ 0B \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

But this is the same set of equations discussed in the subsection on the MixColumn transformation:

$$\begin{aligned} (\{0E\} \bullet \{02\}) \oplus \{0B\} \oplus \{0D\} \oplus (\{09\} \bullet \{03\}) &= \{01\} \\ (\{09\} \bullet \{02\}) \oplus \{0E\} \oplus \{0B\} \oplus (\{0D\} \bullet \{03\}) &= \{00\} \\ (\{0D\} \bullet \{02\}) \oplus \{09\} \oplus \{0E\} \oplus (\{0B\} \bullet \{03\}) &= \{00\} \\ (\{0B\} \bullet \{02\}) \oplus \{0D\} \oplus \{09\} \oplus (\{0E\} \bullet \{03\}) &= \{00\} \end{aligned}$$

The first equation is verified in the text. For the second equation, we have $\{09\} \bullet \{02\} = 00010010$; and $\{0D\} \bullet \{03\} = \{0D\} \oplus (\{0D\} \bullet \{02\}) = 00001101 \oplus 00011010 = 00010111$. Then

$$\begin{array}{rcl}
\{09\} \bullet \{02\} & = & 00010010 \\
\{0E\} & = & 00001110 \\
\{0B\} & = & 00001011 \\
\{0D\} \bullet \{03\} & = & \underline{00010111} \\
& & 00000000
\end{array}$$

For the third equation, we have $\{0D\} \bullet \{02\} = 00011010$; and $\{0B\} \bullet \{03\} = \{0B\} \oplus (\{0B\} \bullet \{02\}) = 00001011 \oplus 00010110 = 00011101$. Then

$$\begin{array}{rcl}
\{0D\} \bullet \{02\} & = & 00011010 \\
\{09\} & = & 00001001 \\
\{0E\} & = & 00001110 \\
\{0B\} \bullet \{03\} & = & \underline{00011101} \\
& & 00000000
\end{array}$$

For the fourth equation, we have $\{0B\} \bullet \{02\} = 00010110$; and $\{0E\} \bullet \{03\} = \{0E\} \oplus (\{0E\} \bullet \{02\}) = 00001110 \oplus 00011100 = 00010010$. Then

$$\begin{array}{rcl}
\{0B\} \bullet \{02\} & = & 00010110 \\
\{0D\} & = & 00001101 \\
\{09\} & = & 00001001 \\
\{0E\} \bullet \{03\} & = & \underline{00010010} \\
& & 00000000
\end{array}$$

5.2 a. $\{01\}$

b. We need to show that the transformation defined by Equation 5.2, when applied to $\{01\}^{-1}$, produces the correct entry in the S-box. We have

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \oplus \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \oplus \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 0 \end{bmatrix}$$

The result is $\{7C\}$, which is the same as the value for $\{01\}$ in the S-box (Table 5.2a).

5.3 $w(0) = \{00\ 00\ 00\ 00\}$; $w(1) = \{00\ 00\ 00\ 00\}$; $w(2) = \{00\ 00\ 00\ 00\}$; $w(3) = \{00\ 00\ 00\ 00\}$; $w(4) = \{62\ 63\ 63\ 63\}$; $w(5) = \{62\ 63\ 63\ 63\}$; $w(6) = \{62\ 63\ 63\ 63\}$; $w(7) = \{62\ 63\ 63\ 63\}$

5.4

00	04	08	0C
01	05	09	0D
02	06	0A	0E
03	07	0B	0F

a

01	05	09	0D
00	04	08	0C
03	07	0B	0F
02	06	0A	0E

b

7C	6B	01	D7
63	F2	30	FE
7B	C5	2B	76
77	6F	67	AB

c

7C	6B	01	D7
F2	30	FE	63
2B	76	7B	C5
AB	77	6F	67

d

75	87	0F	B2
55	E6	04	22
3E	2E	B8	8C
10	15	58	0A

e

5.5 It is easy to see that $x^4 \bmod (x^4 + 1) = 1$. This is so because we can write:

$$x^4 = [1 \times (x^4 + 1)] + 1$$

Recall that the addition operation is XOR. Then,

$$x^8 \bmod (x^4 + 1) = [x^4 \bmod (x^4 + 1)] \times [x^4 \bmod (x^4 + 1)] = 1 \times 1 = 1$$

So, for any positive integer a , $x^{4a} \bmod (x^4 + 1) = 1$. Now consider any integer i of the form $i = 4a + (i \bmod 4)$. Then,

$$\begin{aligned} x^i \bmod (x^4 + 1) &= [(x^{4a}) \times (x^{i \bmod 4})] \bmod (x^4 + 1) \\ &= [x^{4a} \bmod (x^4 + 1)] \times [x^{i \bmod 4} \bmod (x^4 + 1)] = x^{i \bmod 4} \end{aligned}$$

The same result can be demonstrated using long division.

- 5.6
- AddRoundKey
 - The MixColumn step, because this is where the different bytes interact with each other.
 - The ByteSub step, because it contributes nonlinearity to AES.
 - The ShiftRow step, because it permutes the bytes.
 - There is no wholesale swapping of rows or columns. AES does not require this step because: The MixColumn step causes every byte in a column to alter every other byte in the column, so there is not need to swap rows; The ShiftRow step moves bytes from one column to another, so there is no need to swap columns
- Source: These observations were made by John Savard

5.7 The primary issue is to assure that multiplications take a constant amount of time, independent of the value of the argument. This can be done by adding no-operation cycles as needed to make the times uniform.

5.8

$$\begin{bmatrix} e_{0,j} \\ e_{1,j} \\ e_{2,j} \\ e_{3,j} \end{bmatrix} = \begin{bmatrix} S[a_{0,j}] \\ S[a_{1,j-1}] \\ S[a_{2,j-2}] \\ S[a_{3,j-3}] \end{bmatrix} \oplus \begin{bmatrix} k_{0,j} \\ k_{1,j} \\ k_{2,j} \\ k_{3,j} \end{bmatrix}$$

5.9 Input = 67 89 AB CD.

$$\text{Output} = \begin{bmatrix} 2 & 3 & 1 & 1 \\ 1 & 2 & 3 & 1 \\ 1 & 1 & 2 & 3 \\ 3 & 1 & 1 & 2 \end{bmatrix} \begin{bmatrix} 67 \\ 89 \\ AB \\ CD \end{bmatrix} = \begin{bmatrix} 67 \cdot 2 + 89 \cdot 3 + AB + CD \\ 67 + 89 \cdot 2 + AB \cdot 3 + CD \\ 67 + 89 + AB \cdot 2 + CD \cdot 3 \\ 67 \cdot 3 + 89 + AB + CD \cdot 2 \end{bmatrix} = \begin{bmatrix} CE + 80 + AB + CD \\ 67 + 09 + E6 + CD \\ 67 + 89 + 4D + 4C \\ A9 + 89 + AB + 81 \end{bmatrix} = \begin{bmatrix} 28 \\ 45 \\ EF \\ 0A \end{bmatrix}$$

Verification with the Inverse Mix Column transformation gives

$$\text{Input}'' = \begin{bmatrix} E & B & D & 9 \\ 9 & E & B & D \\ D & 9 & E & B \\ B & D & 9 & E \end{bmatrix} \begin{bmatrix} 28 \\ 45 \\ EF \\ 0A \end{bmatrix} = \begin{bmatrix} 28 \cdot E + 45 \cdot B + EF \cdot D + 0A \cdot 9 \\ 28 \cdot 9 + 45 \cdot E + EF \cdot B + 0A \cdot D \\ 28 \cdot D + 45 \cdot 9 + EF \cdot E + 0A \cdot B \\ 28 \cdot B + 45 \cdot D + EF \cdot 9 + 0A \cdot E \end{bmatrix} = \begin{bmatrix} AB + D1 + 47 + 5A \\ 73 + 9B + 13 + 72 \\ D3 + 5B + 6D + 4E \\ 23 + 54 + D6 + 6C \end{bmatrix} = \begin{bmatrix} 67 \\ 89 \\ AB \\ CD \end{bmatrix}$$

After changing one bit in the input,

Input' = 77 89 AB CD,

and the corresponding output

$$\text{Output}' = \begin{bmatrix} 2 & 3 & 1 & 1 \\ 1 & 2 & 3 & 1 \\ 1 & 1 & 2 & 3 \\ 3 & 1 & 1 & 2 \end{bmatrix} \begin{bmatrix} 77 \\ 89 \\ AB \\ CD \end{bmatrix} = \begin{bmatrix} 77 \cdot 2 + 89 \cdot 3 + AB + CD \\ 77 + 89 \cdot 2 + AB \cdot 3 + CD \\ 77 + 89 + AB \cdot 2 + CD \cdot 3 \\ 77 \cdot 3 + 89 + AB + CD \cdot 2 \end{bmatrix} = \begin{bmatrix} EE + 80 + AB + CD \\ 77 + 89 + E6 + CD \\ 77 + 89 + 4D + 4C \\ C7 + 89 + AB + 81 \end{bmatrix} = \begin{bmatrix} 08 \\ 55 \\ FF \\ 3A \end{bmatrix}$$

The number of bits that changed in the output as a result of a single-bit change in the input is 5.

5.10 Key expansion:

W0 = 1010 0111 W1 = 0011 1011 W2 = 0001 1100 W3 = 0010 0111

W4 = 0111 0110 W5 = 0101 0001

Round 0:

After Add round key: 1100 1000 0101 0000

Round 1:

After Substitute nibbles: 1100 0110 0001 1001

After Shift rows: 1100 1001 0001 0110

After Mix columns: 1110 1100 1010 0010

After Add round key: 1110 1100 1010 0010

Round 2:

After Substitute nibbles: 1111 0000 1000 0101

After Shift rows: 0111 0001 0110 1001

After Add round key: 0000 0111 0011 1000

$$5.11 \begin{bmatrix} x^3 + 1 & x \\ x & x^3 + 1 \end{bmatrix} \begin{bmatrix} 1 & x^2 \\ x^2 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

To get the above result, observe that $(x^5 + x^2 + x) \bmod (x^4 + x + 1) = 0$

5.12 The decryption process should be the reverse of the encryption process.

5.13 For convenience, we drop the "j" subscript. We show the equivalence for the first equation; the rest are shown in the same fashion. From Equation (5.8), we have

$$s'_0 = (2 \bullet s_0) \oplus (3 \bullet s_1) \oplus s_2 \oplus s_3$$

From Equation (5.9), we have

$$\begin{aligned} s'_0 &= s_0 \oplus \text{Tmp} \oplus [2 \bullet (s_0 \oplus s_1)] \\ &= s_0 \oplus (s_0 \oplus s_1 \oplus s_2 \oplus s_3) \oplus [2 \bullet (s_0 \oplus s_1)] && \text{substituting for Tmp} \\ &= s_0 \oplus s_0 \oplus s_1 \oplus s_2 \oplus s_3 \oplus (2 \bullet s_0) \oplus (2 \bullet s_1) && \text{expanding the final term} \\ &= s_0 \oplus s_0 \oplus (2 \bullet s_0) \oplus s_1 \oplus (2 \bullet s_1) \oplus s_2 \oplus s_3 && \text{rearranging terms} \\ &= (2 \bullet s_0) \oplus s_1 \oplus (2 \bullet s_1) \oplus s_2 \oplus s_3 && \text{cancelling first two terms} \\ &= (2 \bullet s_0) \oplus (3 \bullet s_1) \oplus s_2 \oplus s_3 && \text{using the identity referenced} \\ & && \text{just before Equation (5.9)} \end{aligned}$$

CHAPTER 6 BLOCK CIPHER OPERATION

ANSWERS TO QUESTIONS

- 6.1 With triple encryption, a plaintext block is encrypted by passing it through an encryption algorithm; the result is then passed through the same encryption algorithm again; the result of the second encryption is passed through the same encryption algorithm a third time. Typically, the second stage uses the decryption algorithm rather than the encryption algorithm.
- 6.2 This is an attack used against a double encryption algorithm and requires a known (plaintext, ciphertext) pair. In essence, the plaintext is encrypted to produce an intermediate value in the double encryption, and the ciphertext is decrypted to produce an intermediation value in the double encryption. Table lookup techniques can be used in such a way to dramatically improve on a brute-force try of all pairs of keys.
- 6.3 Triple encryption can be used with three distinct keys for the three stages; alternatively, the same key can be used for the first and third stage.
- 6.4 There is no cryptographic significance to the use of decryption for the second stage. Its only advantage is that it allows users of 3DES to decrypt data encrypted by users of the older single DES by repeating the key.
- 6.5 In some modes, the plaintext does not pass through the encryption function, but is XORed with the output of the encryption function. The math works out that for decryption in these cases, the encryption function must also be used.

ANSWERS TO PROBLEMS

- 6.1 a. If the IVs are kept secret, the 3-loop case has more bits to be determined and is therefore more secure than 1-loop for brute force attacks.
- b. For software implementations, the performance is equivalent for most measurements. One-loop has two fewer XORs per block. three-loop might benefit from the ability to do a large set of blocks with a single key before switching. The performance difference from choice of mode can be expected to be smaller than the differences induced by normal variation in programming style.

For hardware implementations, three-loop is three times faster than one-loop, because of pipelining. That is: Let P_i be the stream of input plaintext blocks, X_i

the output of the first DES, Y_i the output of the second DES and C_i the output of the final DES and therefore the whole system's ciphertext.

In the 1-loop case, we have:

$$\begin{aligned} X_i &= \text{DES}(\text{XOR}(P_i, C_{i-1})) \\ Y_i &= \text{DES}(X_i) \\ C_i &= \text{DES}(Y_i) \end{aligned}$$

[where C_0 is the single IV]

If P_1 is presented at $t=0$ (where time is measured in units of DES operations), X_1 will be available at $t=1$, Y_1 at $t=2$ and C_1 at $t=3$. At $t=1$, the first DES is free to do more work, but that work will be:

$$X_2 = \text{DES}(\text{XOR}(P_2, C_1))$$

but C_1 is not available until $t=3$, therefore X_2 can not be available until $t=4$, Y_2 at $t=5$ and C_2 at $t=6$.

In the 3-loop case, we have:

$$\begin{aligned} X_i &= \text{DES}(\text{XOR}(P_i, X_{i-1})) \\ Y_i &= \text{DES}(\text{XOR}(X_i, Y_{i-1})) \\ C_i &= \text{DES}(\text{XOR}(Y_i, C_{i-1})) \end{aligned}$$

[where X_0 , Y_0 and C_0 are three independent IVs]

If P_1 is presented at $t=0$, X_1 is available at $t=1$. Both X_2 and Y_1 are available at $t=4$. X_3 , Y_2 and C_1 are available at $t=3$. X_4 , Y_3 and C_2 are available at $t=4$.

Therefore, a new ciphertext block is produced every 1 tick, as opposed to every 3 ticks in the single-loop case. This gives the three-loop construct a throughput three times greater than the one-loop construct.

6.2 Instead of $\text{CBC}[\text{CBC}(\text{CBC}(X))]$, use $\text{ECB}[\text{CBC}(\text{CBC}(X))]$. The final IV was not needed for security. The lack of feedback loop prevents the chosen-ciphertext differential cryptanalysis attack. The extra IVs still become part of a key to be determined during any known plaintext attack.

6.3 The Merkle-Hellman attack finds the desired two keys K_1 and K_2 by finding the plaintext-ciphertext pair such that intermediate value A is 0. The first step is to create a list of all of the plaintexts that could give $A = 0$:

$$P_i = D[i, 0] \quad \text{for } i = 0. 1. \dots, 2^{56} - 1$$

Then, use each P_i as a chosen plaintext and obtain the corresponding ciphertexts C_i :

$$C_i = E[i, P_i] \quad \text{for } i = 0. 1. \dots, 2^{56} - 1$$

The next step is to calculate the intermediate value B_i for each C_i using $K_3 = K_1 = i$.

$$B_i = D[i, C_i] \quad \text{for } i = 0. 1. \dots, 2^{56} - 1$$

A table of triples of the following form is constructed: $(P_i \text{ or } B_i, i, \text{flag})$, where *flag* indicates either a P-type or B-type triple. Note that the 256 values P_i are also potentially intermediate values B . All P_i and B_i values are placed in the table, and the table is sorted on the first entry in each triple, and then search to find consecutive P and B values such that $B_i = P_j$. For each such equality, i, j is a candidate for the desired pair of keys K_1 and K_4 . Each candidate pair of keys is tested on a few other plaintext-ciphertext pairs to filter out false alarms.

- 6.4 a. No. For example, suppose C_1 is corrupted. The output block P_3 depends only on the input blocks C_2 and C_3 .
 b. An error in P_1 affects C_1 . But since C_1 is input to the calculation of C_2 , C_2 is affected. This effect carries through indefinitely, so that all ciphertext blocks are affected. However, at the receiving end, the decryption algorithm restores the correct plaintext for blocks except the one in error. You can show this by writing out the equations for the decryption. Therefore, the error only effects the corresponding decrypted plaintext block.
- 6.5 In CBC encryption, the input block to each forward cipher operation (except the first) depends on the result of the previous forward cipher operation, so the forward cipher operations cannot be performed in parallel. In CBC decryption, however, the input blocks for the inverse cipher function (i.e., the ciphertext blocks) are immediately available, so that multiple inverse cipher operations can be performed in parallel.
- 6.6 After decryption, the last byte of the last block is used to determine the amount of padding that must be stripped off. Therefore there must be at least one byte of padding.
- 6.7 For this padding method, the padding bits can be removed unambiguously, provided the receiver can determine that the message is indeed padded. One way to ensure that the receiver does not mistakenly remove bits from an unpadded message is to require the sender to pad every message, including messages in which the final block is already complete. For such messages, an entire block of padding is appended.
- 6.8 Nine plaintext characters are affected. The plaintext character corresponding to the ciphertext character is obviously altered. In addition, the altered ciphertext character enters the shift register and is not removed until the next eight characters are processed.

- 6.9** Let message M1 have plaintext blocks $P1_j$ and ciphertext blocks $C1_j$. Similarly for message M2. If the same IV and key are used in OFB mode for both messages, then both messages have the same output blocks O_j . Suppose an attacker can observe the ciphertext blocks for M1 and M2 and that the attacker knows the exact contents of $P1_q$.

Then,

$$\begin{aligned}
 C1_q &= P1_q \oplus O_q && \text{by definition of OFB} \\
 C1_q \oplus P1_q &= P1_q \oplus O_q \oplus P1_q && \text{add to both sides} \\
 O_q \oplus P1_q \oplus P1_q &= C1_q \oplus P1_q && \text{rearrange} \\
 O_q &= C1_q \oplus P1_q && \text{cancel terms} \\
 C2_q &= P2_q \oplus O_q && \text{by definition of OFB} \\
 C2_q \oplus O_q &= P2_q \oplus O_q \oplus O_q && \text{add to both sides} \\
 P2_q &= C2_q \oplus O_q && \text{add to both sides}
 \end{aligned}$$

6.10 $O_i = C_i \oplus P_i$

- 6.11 a.** Assume that the last block of plaintext is only L bytes long, where $L < 2w/8$. The encryption sequence is as follows (The description in RFC 2040 has an error; the description here is correct.):

1. Encrypt the first $(N - 2)$ blocks using the traditional CBC technique.
2. XOR P_{N-1} with the previous ciphertext block C_{N-2} to create Y_{N-1} .
3. Encrypt Y_{N-1} to create E_{N-1} .
4. Select the first L bytes of E_{N-1} to create C_N .
5. Pad P_N with zeros at the end and exclusive-OR with E_{N-1} to create Y_N .
6. Encrypt Y_N to create C_{N-1} .

The last two blocks of the ciphertext are C_{N-1} and C_N .

- b.** $P_{N-1} = C_{N-2} \oplus D(K, [C_N \parallel X])$
 $P_N \parallel X = (C_N \parallel 00\dots 0) \oplus D(K, [C_{N-1}])$
 P_N = left-hand portion of $(P_N \parallel X)$
 where \parallel is the concatenation function

- 6.12 a.** Assume that the last block (P_N) has j bits. After encrypting the last full block (P_{N-1}), encrypt the ciphertext (C_{N-1}) again, select the leftmost j bits of the encrypted ciphertext, and XOR that with the short block to generate the output ciphertext.
- b.** While an attacker cannot recover the last plaintext block, he can change it systematically by changing individual bits in the ciphertext. If the last few bits of the plaintext contain essential information, this is a weakness.

CHAPTER 7 PSEUDORANDOM NUMBER GENERATION AND STREAM CIPHERS

ANSWERS TO QUESTIONS

- 7.1 Statistical randomness refers to a property of a sequence of numbers or letters, such that the sequence appears random and passes certain statistical tests that indicate that the sequence has the properties of randomness. If a statistically random sequence is generated by an algorithm, then the sequence is predictable by anyone knowing the algorithm and the starting point of the sequence. An unpredictable sequence is one in which knowledge of the sequence generation method is insufficient to determine the sequence.
- 7.2 1. The encryption sequence should have a large period. 2. The keystream should approximate the properties of a true random number stream as close as possible. 3. To guard against brute-force attacks, the key needs to be sufficiently long. The same considerations as apply for block ciphers are valid here. Thus, with current technology, a key length of at least 128 bits is desirable.
- 7.3 If two plaintexts are encrypted with the same key using a stream cipher, then cryptanalysis is often quite simple. If the two ciphertext streams are XORed together, the result is the XOR of the original plaintexts. If the plaintexts are text strings, credit card numbers, or other byte streams with known properties, then cryptanalysis may be successful.
- 7.4 The actual encryption involves only the XOR operation. Key stream generation involves the modulo operation and byte swapping.

ANSWERS TO PROBLEMS

- 7.1 We give the result for $a = 3$:
- 1, 3, 9, 27, 19, 26, 16, 17, 20, 29, 25, 13, 8, 24, 10, 30, 28, 22, 4, 12, 5, 15, 14, 11, 2, 6, 18, 23, 7, 21, 1
- 7.2 a. Maximum period is $2^{4-2} = 4$
b. a must be 3, 5, 11, or 13
c. The seed must be odd
- 7.3 When $m = 2^k$, the right-hand digits of X_n are much less random than the left-hand digits. See [KNUT98], page 13 for a discussion.

7.4 Let us start with an initial seed of 1. The first generator yields the sequence:

1, 6, 10, 8, 9, 2, 12, 7, 3, 5, 4, 11, 1, . . .

The second generator yields the sequence:

1, 7, 10, 5, 9, 11, 12, 6, 3, 8, 4, 2, 1, . . .

Because of the patterns evident in the second half of the latter sequence, most people would consider it to be less random than the first sequence.

7.5 Many packages make use of a linear congruential generator with $m = 2^k$. As discussed in the answer to Problem 5.6, this leads to results in which the right-hand digits are much less random than the left-hand digits. Now, if we use a linear congruential generator of the following form:

$$X_{n+1} = (aX_n + c) \bmod m$$

then it is easy to see that the scheme will generate all even integers, all odd integers, or will alternate between even and odd integers, depending on the choice for a and c . Often, a and c are chosen to create a sequence of alternating even and odd integers. This has a tremendous impact on the simulation used for calculating π . The simulation depends on counting the number of pairs of integers whose greatest common divisor is 1. With truly random integers, one-fourth of the pairs should consist of two even integers, which of course have a gcd greater than 1. This never occurs with sequences that alternate between even and odd integers. To get the correct value of π using Cesaro's method, the number of pairs with a gcd of 1 should be approximately 60.8%. When pairs are used where one number is odd and the other even, this percentage comes out too high, around 80%, thus leading to the too small value of π . For a further discussion, see Danilowicz, R. "Demonstrating the Dangers of Pseudo-Random Numbers," *SIGCSE Bulletin*, June 1989.

7.6 a.

Pair	Probability
00	$(0.5 - \partial)^2 = 0.25 - \partial + \partial^2$
01	$(0.5 - \partial) \times (0.5 + \partial) = 0.25 - \partial^2$
10	$(0.5 + \partial) \times (0.5 - \partial) = 0.25 - \partial^2$
11	$(0.5 + \partial)^2 = 0.25 + \partial + \partial^2$

- b. Because 01 and 10 have equal probability in the initial sequence, in the modified sequence, the probability of a 0 is 0.5 and the probability of a 1 is 0.5.
- c. The probability of any particular pair being discarded is equal to the probability that the pair is either 00 or 11, which is $0.5 + 2\partial^2$, so the expected number of input bits to produce x output bits is $x / (0.25 - \partial^2)$.
- d. The algorithm produces a totally predictable sequence of exactly alternating 1's and 0's.

7.7 a. For the sequence of input bits a_1, a_2, \dots, a_n , the output bit b is defined as:

$$b = a_1 \oplus a_2 \oplus \dots \oplus a_n$$

- b. $0.5 - 2\partial^2$
- c. $0.5 - 8\partial^4$
- d. The limit as n goes to infinity is 0.5.

7.8 Use a key of length 255 bytes. The first two bytes are zero; that is $K[0] = K[1] = 0$. Thereafter, we have: $K[2] = 255$; $K[3] = 254$; ... $K[255] = 2$.

- 7.9 a. Simply store i , j , and S , which requires $8 + 8 + (256 \times 8) = 2064$ bits
b. The number of states is $[256! \times 256^2] \approx 2^{1700}$. Therefore, 1700 bits are required.

- 7.10 a. By taking the first 80 bits of $v \parallel c$, we obtain the initialization vector, v . Since v , c , k are known, the message can be recovered (i.e., decrypted) by computing $RC4(v \parallel k) \oplus c$.
b. If the adversary observes that $v_i = v_j$ for distinct i, j then he/she knows that the same key stream was used to encrypt both m_i and m_j . In this case, the messages m_i and m_j may be vulnerable to the type of cryptanalysis carried out in part (a).
c. Since the key is fixed, the key stream varies with the choice of the 80-bit v , which is selected randomly. Thus, after approximately $\sqrt{\frac{\pi}{2}} 2^{80} \approx 2^{40}$ messages are sent, we expect the same v , and hence the same key stream, to be used more than once.
d. The key k should be changed sometime before 2^{40} messages are sent.

CHAPTER 8 INTRODUCTION TO NUMBER THEORY

ANSWERS TO QUESTIONS

- 8.1 An integer $p > 1$ is a prime number if and only if its only divisors are ± 1 and $\pm p$.
- 8.2 We say that a nonzero b divides a if $a = mb$ for some m , where a , b , and m are integers.
- 8.3 Euler's totient function, written $\phi(n)$, is the number of positive integers less than n and relatively prime to n .
- 8.4 The algorithm takes a candidate integer n as input and returns the result "composite" if n is definitely not a prime, and the result "inconclusive" if n may or may not be a prime. If the algorithm is repeatedly applied to a number and repeatedly returns inconclusive, then the probability that the number is actually prime increases with each inconclusive test. The probability required to accept a number as prime can be set as close to 1.0 as desired by increasing the number of tests made.
- 8.5 If r and n are relatively prime integers with $n > 0$, and if $\phi(n)$ is the least positive exponent m such that $a^m \equiv 1 \pmod{n}$, then r is called a primitive root modulo n .
- 8.6 The two terms are synonymous.

ANSWERS TO PROBLEMS

- 8.1 a. We are assuming that p_n is the largest of all primes. Because $X > p_n$, X is not prime. Therefore, we can find a prime number p_m that divides X .
- b. The prime number p_m cannot be any of p_1, p_2, \dots, p_n ; otherwise p_m would divide the difference $X - p_1 p_2 \dots p_n = 1$, which is impossible. Thus, $m > n$.
- c. This construction provides a prime number outside any finite set of prime numbers, so the complete set of prime numbers is not finite.
- d. We have shown that there is a prime number $> p_n$ that divides $X = 1 + p_1 p_2 \dots p_n$, so p_{n+1} is equal to or less than this prime. Therefore, since this prime divides X , it is $\leq X$ and therefore $p_{n+1} \leq X$.
- 8.2 a. $\gcd(a, b) = d$ if and only if a is a multiple of d and b is a multiple of d and $\gcd(a/d, b/d) = 1$. The probability that an integer chosen at random is a multiple of d is just $1/d$. Thus the probability that $\gcd(a, b) = d$ is equal to $1/d$ times $1/d$ times P , namely, P/d^2 .

b. We have

$$\sum_{d \geq 1} \Pr[\gcd(a, b) = d] = \sum_{d \geq 1} \frac{P}{d^2} = P \sum_{d \geq 1} \frac{1}{d^2} = P \times \frac{\pi^2}{6} = 1$$

To satisfy this equation, we must have $P = \frac{6}{\pi^2} = 0.6079$.

8.3 If p were any prime dividing n and $n + 1$ it would also have to divide

$$(n + 1) - n = 1$$

8.4 Fermat's Theorem states that if p is prime and a is a positive integer not divisible by p , then $a^{p-1} \equiv 1 \pmod{p}$. Therefore $3^{10} \equiv 1 \pmod{11}$. Therefore $3^{201} = (3^{10})^{20} \times 3 \equiv 3 \pmod{11}$.

8.5 12

8.6 6

8.7 1

8.8 6

8.9 If a is one of the integers counted in $\phi(n)$, that is, one of the integers not larger than n and prime to n , the $n - a$ is another such integer, because $\gcd(a, n) = \gcd(n - a, n)$. The two integers, a and $n - a$, are distinct, because $a = n - a$ gives $n = 2a$, which is inconsistent with the assumption that $\gcd(a, n) = 1$. Therefore, for $n > 2$, the integers counted in $\phi(n)$ can be paired off, and so the number of them must be even.

8.10 Only multiples of p have a factor in common with p^n , when p is prime. There are just p^{n-1} of these $\leq p^n$, so $\phi(p^n) = p^n - p^{n-1}$.

8.11 a. $\phi(41) = 40$, because 41 is prime

b. $\phi(27) = \phi(3^3) = 3^3 - 3^2 = 27 - 9 = 18$

c. $\phi(231) = \phi(3) \times \phi(7) \times \phi(11) = 2 \times 6 \times 10 = 120$

d. $\phi(440) = \phi(2^3) \times \phi(5) \times \phi(11) = (2^3 - 2^2) \times 4 \times 10 = 160$

8.12 It follows immediately from the result stated in Problem 8.10.

8.13 totient

8.14 a. For $n = 5$, $2^n - 2 = 30$, which is divisible by 5.

b. We can rewrite the Chinese test as $(2^n - 2) \equiv 0 \pmod{n}$, or equivalently, $2^n \equiv 2 \pmod{n}$. By Fermat's Theorem, this relationship is true if n is prime (Equation 8.2).

c. For $n = 15$, $2^n - 2 = 32,766$, which is divisible by 15.

d. $2^{10} = 1024 \equiv 1 \pmod{341}$

$2^{340} = (2^{10})^{34} \equiv (1 \pmod{341})$

$$2^{341} \equiv 2 \pmod{341}$$

8.15 First consider $a = 1$. In step 3 of TEST(n), the test is **if** $1^q \bmod n = 1$ **then** return("inconclusive"). This clearly returns "inconclusive." Now consider $a = n - 1$. In step 5 of TEST(n), for $j = 0$, the test is **if** $(n - 1)^q \bmod n = n - 1$ **then** return("inconclusive"). This condition is met by inspection.

8.16 In Step 1 of TEST(2047), we set $k = 1$ and $q = 1023$, because $(2047 - 1) = (2^1)(1023)$. In Step 2 we select $a = 2$ as the base. In Step 3, we have $a^q \bmod n = 2^{1023} \bmod 2047 = (2^{11})^{93} \bmod 2047 = (2048)^{93} \bmod 2047 = 1$ and so the test is passed.

8.17 There are many forms to this proof, and virtually every book on number theory has a proof. Here we present one of the more concise proofs. Define $M_i = M/m_i$. Because all of the factors of M are pairwise relatively prime, we have $\gcd(M_i, m_i) = 1$. Thus, there are solutions N_i of

$$N_i M_i \equiv 1 \pmod{m_i}$$

With these N_i , the solution x to the set of congruences is:

$$x \equiv a_1 N_1 M_1 + \dots + a_k N_k M_k \pmod{M}$$

To see this, we introduce the notation $\langle x \rangle_m$, by which we mean the least positive residue of x modulo m . With this notation, we have

$$\langle x \rangle_{m_i} \equiv a_i N_i M_i \equiv a_i \pmod{m_i}$$

because all other terms in the summation above that make up x contain the factor m_i and therefore do not contribute to the residue modulo m_i . Because $N_i M_i \equiv 1 \pmod{m_i}$, the solution is also unique modulo M , which proves this form of the Chinese Remainder Theorem.

8.18 We have $M = 3 \times 5 \times 7 = 105$; $M/3 = 35$; $M/5 = 21$; $M/7 = 15$. The set of linear congruences

$$35b_1 \equiv 1 \pmod{3}; \quad 21b_2 \equiv 1 \pmod{5}; \quad 15b_3 \equiv 1 \pmod{7}$$

has the solutions $b_1 = 2$; $b_2 = 1$; $b_3 = 1$. Then,

$$x \equiv 2 \times 2 \times 35 + 3 \times 1 \times 21 + 2 \times 1 \times 15 \equiv 233 \pmod{105} = 23$$

8.19 If the day in question is the x th (counting from and including the first Monday), then

$$x = 1 + 2K_1 = 2 + 3K_2 = 3 + 4K_3 = 4 + K_4 = 5 + 6K_5 = 6 + 5K_6 = 7K_7$$

where the K_i are integers; i.e.,

(1) $x \equiv 1 \pmod{2}$; (2) $x \equiv 2 \pmod{3}$; (3) $x \equiv 3 \pmod{4}$; (4) $x \equiv 4 \pmod{1}$; (5) $x \equiv 5 \pmod{6}$;
(6) $x \equiv 6 \pmod{5}$; (7) $x \equiv 0 \pmod{7}$

Of these congruences, (4) is no restriction, and (1) and (2) are included in (3) and (5). Of the two latter, (3) shows that x is congruent to 3, 7, or 11 (mod 12), and (5) shows the x is congruent to 5 or 11, so that (3) and (5) together are equivalent to $x \equiv 11 \pmod{12}$. Hence, the problem is that of solving:

$$\begin{array}{ll} x \equiv 11 \pmod{12}; & x \equiv 6 \pmod{5}; \quad x \equiv 0 \pmod{7} \\ \text{or} & x \equiv -1 \pmod{12}; \quad x \equiv 1 \pmod{5}; \quad x \equiv 0 \pmod{7} \end{array}$$

Then $m_1 = 12$; $m_2 = 5$; $m_3 = 7$; $M = 420$

$$M_1 = 35; M_2 = 84; M_3 = 60$$

Then,

$$x \equiv (-1)(-1)35 + (-1)1 \times 21 + 2 \times 0 \times 60 = -49 \equiv 371 \pmod{420}$$

The first x satisfying the condition is 371.

8.20 2, 3, 8, 12, 13, 17, 22, 23

8.21 a. $x = 2, 27 \pmod{29}$

b. $x = 9, 24 \pmod{29}$

c. $x = 8, 10, 12, 15, 18, 26, 27 \pmod{29}$

CHAPTER 9 PUBLIC-KEY CRYPTOGRAPHY AND RSA

ANSWERS TO QUESTIONS

- 9.1 Plaintext:** This is the readable message or data that is fed into the algorithm as input. **Encryption algorithm:** The encryption algorithm performs various transformations on the plaintext. **Public and private keys:** This is a pair of keys that have been selected so that if one is used for encryption, the other is used for decryption. The exact transformations performed by the encryption algorithm depend on the public or private key that is provided as input. **Ciphertext:** This is the scrambled message produced as output. It depends on the plaintext and the key. For a given message, two different keys will produce two different ciphertexts. **Decryption algorithm:** This algorithm accepts the ciphertext and the matching key and produces the original plaintext.
- 9.2** A user's private key is kept private and known only to the user. The user's public key is made available to others to use. The private key can be used to encrypt a signature that can be verified by anyone with the public key. Or the public key can be used to encrypt information that can only be decrypted by the possessor of the private key.
- 9.3 Encryption/decryption:** The sender encrypts a message with the recipient's public key. **Digital signature:** The sender "signs" a message with its private key. Signing is achieved by a cryptographic algorithm applied to the message or to a small block of data that is a function of the message. **Key exchange:** Two sides cooperate to exchange a session key. Several different approaches are possible, involving the private key(s) of one or both parties.
- 9.4 1.** It is computationally easy for a party B to generate a pair (public key PU_b , private key PR_b).
- 2.** It is computationally easy for a sender A, knowing the public key and the message to be encrypted, M , to generate the corresponding ciphertext:

$$C = E(PU_b, M)$$

- 3.** It is computationally easy for the receiver B to decrypt the resulting ciphertext using the private key to recover the original message:

$$M = D(PR_b, C) = D(PR_b, E(PU_b, M))$$

4. It is computationally infeasible for an opponent, knowing the public key, PU_b , to determine the private key, PR_b .
 5. It is computationally infeasible for an opponent, knowing the public key, PU_b , and a ciphertext, C , to recover the original message, M .
- 9.5 A **one-way function** is one that maps a domain into a range such that every function value has a unique inverse, with the condition that the calculation of the function is easy whereas the calculation of the inverse is infeasible:
- 9.6 A **trap-door one-way function** is easy to calculate in one direction and infeasible to calculate in the other direction unless certain additional information is known. With the additional information the inverse can be calculated in polynomial time.
- 9.7
1. Pick an odd integer n at random (e.g., using a pseudorandom number generator).
 2. Pick an integer $a < n$ at random.
 3. Perform the probabilistic primality test, such as Miller-Rabin. If n fails the test, reject the value n and go to step 1.
 4. If n has passed a sufficient number of tests, accept n ; otherwise, go to step 2.

ANSWERS TO PROBLEMS

- 9.1 This proof is discussed in the CESG report mentioned in Chapter 9 [ELLI99].

a. $M3 =$

5	2	1	4	5
1	4	3	2	2
3	1	2	5	3
4	3	4	1	4
2	5	5	3	1

- b. Assume a plaintext message p is to be encrypted by Alice and sent to Bob. Bob makes use of $M1$ and $M3$, and Alice makes use of $M2$. Bob chooses a random number, k , as his private key, and maps k by $M1$ to get x , which he sends as his public key to Alice. Alice uses x to encrypt p with $M2$ to get z , the ciphertext, which she sends to Bob. Bob uses k to decrypt z by means of $M3$, yielding the plaintext message p .
- c. If the numbers are large enough, and $M1$ and $M2$ are sufficiently random to make it impractical to work backwards, p cannot be found without knowing k .
- 9.2
- a. $n = 33$; $\phi(n) = 20$; $d = 3$; $C = 26$.
 - b. $n = 55$; $\phi(n) = 40$; $d = 27$; $C = 14$.
 - c. $n = 77$; $\phi(n) = 60$; $d = 53$; $C = 57$.
 - d. $n = 143$; $\phi(n) = 120$; $d = 11$; $C = 106$.
 - e. $n = 527$; $\phi(n) = 480$; $d = 343$; $C = 128$. For decryption, we have

$$\begin{aligned}
 128^{343} \bmod 527 &= 128^{256} \times 128^{64} \times 128^{16} \times 128^4 \times 128^2 \times 128^1 \bmod 527 \\
 &= 35 \times 256 \times 35 \times 101 \times 47 \times 128 = 2 \bmod 527 \\
 &= 2 \bmod 257
 \end{aligned}$$

- 9.3 5

- 9.4 By trial and error, we determine that $p = 59$ and $q = 61$. Hence $\phi(n) = 58 \times 60 = 3480$. Then, using the extended Euclidean algorithm, we find that the multiplicative inverse of 31 modulo $\phi(n)$ is 3031.
- 9.5 Suppose the public key is $n = pq$, e . Probably the order of e relative to $(p-1)(q-1)$ is small so that a small power of e gives us something congruent to $1 \bmod (p-1)(q-1)$. In the worst case where the order is 2 then e and d (the private key) are the same. Example: if $p = 7$ and $q = 5$ then $(p-1)(q-1) = 24$. If $e = 5$ then e squared is congruent to $1 \bmod (p-1)(q-1)$; that is, 25 is congruent to $24 \bmod 1$.
- 9.6 Yes. If a plaintext block has a common factor with n modulo n then the encoded block will also have a common factor with n modulo n . Because we encode blocks, which are smaller than pq , the factor must be p or q and the plaintext block must be a multiple of p or q . We can test each block for primality. If prime, it is p or q . In this case we divide into n to find the other factor. If not prime, we factor it and try the factors as divisors of n .
- 9.7 No, it is not safe. Once Bob leaks his private key, Alice can use this to factor his modulus, N . Then Alice can crack any message that Bob sends.

Here is one way to factor the modulus:

Let $k = ed - 1$. Then k is congruent to 0 mod $\phi(N)$ (where ' ϕ ' is the Euler totient function). Select a random x in the multiplicative group $Z(N)$. Then $x^k \equiv 1 \bmod N$, which implies that $x^{k/2}$ is a square root of 1 mod N . With 50% probability, this is a nontrivial square root of N , so that

$\gcd(x^{k/2} - 1, N)$ will yield a prime factor of N .

If $x^{k/2} \equiv 1 \bmod N$, then try $x^{k/4}$, $x^{k/8}$, etc...

This will fail if and only if $x^{k/2^i} \equiv -1$ for some i . If it fails, then choose a new x .

This will factor N in expected polynomial time.

- 9.8 Consider a set of alphabetic characters $\{A, B, \dots, Z\}$. The corresponding integers, representing the position of each alphabetic character in the alphabet, form a set of message block values $SM = \{0, 1, 2, \dots, 25\}$. The set of corresponding ciphertext block values $SC = \{0^e \bmod N, 1^e \bmod N, \dots, 25^e \bmod N\}$, and can be computed by everybody with the knowledge of the public key of Bob.

Thus, the most efficient attack against the scheme described in the problem is to compute $M^e \bmod N$ for all possible values of M , then create a look-up table with a ciphertext as an index, and the corresponding plaintext as a value of the appropriate location in the table.

- 9.9 a. We consider $n = 233, 235, 237, 239$, and 241 , and the base $a = 2$:
 $n = 233$
 $233 - 1 = 2^3 \times 29$, thus $k=3, q=29$

$a^q \bmod n = 2^{29} \bmod 233 = 1$
 test returns "inconclusive" ("probably prime")

$n = 235$

$235 - 1 = 2^1 \times 117$, thus $k=1$, $q=117$

$a^q \bmod n = 2^{117} \bmod 235 = 222$

$222 \neq 1$ and $222 \neq 235 - 1$

test returns "composite"

$n = 237$

$237 - 1 = 2^2 \times 59$, thus $k=2$, $q=59$

$a^q \bmod n = 2^{59} \bmod 237 = 167 \neq 1$

$167 \neq 237 - 1$

$167^2 \bmod 237 = 160 \neq 237 - 1$

test returns "composite"

$n = 239$

$239 - 1 = 2^1 \times 119$.

$2^{119} \bmod 239 = 1$

test returns "inconclusive" ("probably prime")

$n = 241$

$241 - 1 = 2^4 \times 15$

$2^4 \bmod 241 = 16$

$16 \neq 1$ and $16 \neq 241 - 1$

$16^2 \bmod 241 = 256 \bmod 241 = 15$

$15 \neq 241 - 1$

$15^2 \bmod 241 = 225 \bmod 241 = 225$

$225 \neq 241 - 1$

$225^2 \bmod 241 = 15$

$15 \neq 241 - 1$

test returns "inconclusive" ("probably prime")

- b. $M=2$, $e=23$, $n=233 \times 241=56,153$ therefore $p=233$ and $q=241$
 $e = 23 = (10111)_2$

I		4	3	2	1	0
e_i		1	0	1	1	1
D	1	2	4	32	2048	21,811

- c. Compute private key (d, p, q) given public key $(e=23, n=233 \times 241=56,153)$.

Since $n=233 \times 241=56,153$, $p=233$ and $q=241$

$\phi(n) = (p-1)(q-1) = 55,680$

Using Extended Euclidean algorithm, we obtain

$d = 23^{-1} \bmod 55680 = 19,367$

- d. Without CRT: $M = 21,811^{19,367} \bmod 56,153 = 2$

With CRT:

$d_p = d \bmod (p-1)$

$d_q = d \bmod (q-1)$

$d_p = 19367 \bmod 232 = 111$

$d_q = 19367 \bmod 240 = 167$

$C_p = C \bmod p$

$M_p = C_p^{d_p} \bmod p = 141^{111} \bmod 233 = 2$

$C_q = C \bmod q$

$$M_q = C_q^{d_q} \bmod q$$

$$M_q = 121^{167} \bmod 241 = 2$$

$$M = 2.$$

- 9.10** $C = (M^{d_S} \bmod N_S)^{e_R} \bmod N_R = S^{e_R} \bmod N_R$
 where
 $S = M^{d_S} \bmod N_S$.
 $M' = (C^{d_R} \bmod N_R)^{e_S} \bmod N_S = S'^{e_S} \bmod N_S =$
 where
 $S' = C^{d_R} \bmod N_R$.

The scheme does not work correctly if $S \neq S'$. This situation may happen for a significant subset of messages M if $N_S > N_R$. In this case, it might happen that $N_R \leq S < N_S$, and since by definition $S' < N_R$, then $S \neq S'$, and therefore also $M' \neq M$. For all other relations between N_S and N_R , the scheme works correctly (although $N_S = N_R$ is discouraged for security reasons).

In order to resolve the problem both sides can use two pairs of keys, one for encryption and the other for signing, with all signing keys N_{SGN} smaller than the encryption keys N_{ENC} .

- 9.11** 3rd element, because it equals to the 1st squared,
 5th element, because it equals to the product of 1st and 2nd
 7th element, because it equals to the cube of 1st,
 etc.
- 9.12** Refer to Figure 9.5 The private key k is the pair $\{d, n\}$; the public key x is the pair $\{e, n\}$; the plaintext p is M ; and the ciphertext z is C . $M1$ is formed by calculating $d = e^{-1} \bmod \phi(n)$. $M2$ consists of raising M to the power $e \pmod n$. $M3$ consists of raising C to the power $d \pmod n$.
- 9.13** Yes.
- 9.14** This algorithm is discussed in the CESG report mentioned in Chapter 9 [ELLI99], and is known as Cocks algorithm.
- Cocks makes use of the Chinese remainder theorem (see Section 8.4 and Problem 8.10), which says it is possible to reconstruct integers in a certain range from their residues modulo a set of pairwise relatively prime moduli. In particular for relatively prime P and Q , any integer M in the range $0 \leq M < N$ can be the pair of numbers $M \bmod P$ and $M \bmod Q$, and that it is possible to recover M given $M \bmod P$ and $M \bmod Q$. The security lies in the difficulty of finding the prime factors of N .
 - In RSA, a user forms a pair of integers, d and e , such that $de \equiv 1 \bmod ((P-1)(Q-1))$, and then publishes e and N as the public key. Cocks is a special case in which $e = N$.
 - The RSA algorithm has the merit that it is symmetrical; the same process is used both for encryption and decryption, which simplifies the software needed. Also, e can be chosen arbitrarily so that a particularly simple version can be

used for encryption with the public key. In this way, the complex process would be needed only for the recipient.

- d. The private key k is the pair P and Q ; the public key x is N ; the plaintext p is M ; and the ciphertext z is C . $M1$ is formed by multiplying the two parts of k , P and Q , together. $M2$ consists of raising M to the power $N \pmod{N}$. $M3$ is the process described in the problem statement.

- 9.15** 1) Adversary X intercepts message sent by A to B , i.e. $[A, E(PU_b, M), B]$
 2) X sends B $[X, E(PU_b, M), B]$
 3) B acknowledges receipt by sending X $[B, E(PU_x, M), X]$
 4) X decrypts $E(PU_x, M)$ using his secret decryption key, thus getting M

9.16

I	9	8	7	6	5	4	3	2	1	0
B_i	1	0	0	1	0	1	0	1	0	0
C	1	2	4	5	11	23	46	93	186	372
F	5	25	625	937	595	569	453	591	59	1013

- 9.17** First, let us consider the algorithm in Figure 9.8. The binary representation of b is read from left to right (most significant to least significant) to control which operations are performed. In essence, if c is the current value of the exponent after some of the bits have been processed, then if the next bit is 0, the exponent is doubled (simply a left shift of 1 bit) or it is doubled and incremented by 1. Each iteration of the loop uses one of the identities:

$$a^{2c} \pmod{n} = (a^c)^2 \pmod{n} \quad \text{if } b_i = 0$$

$$a^{2c+1} \pmod{n} = a \times (a^c)^2 \pmod{n} \quad \text{if } b_i = 1$$

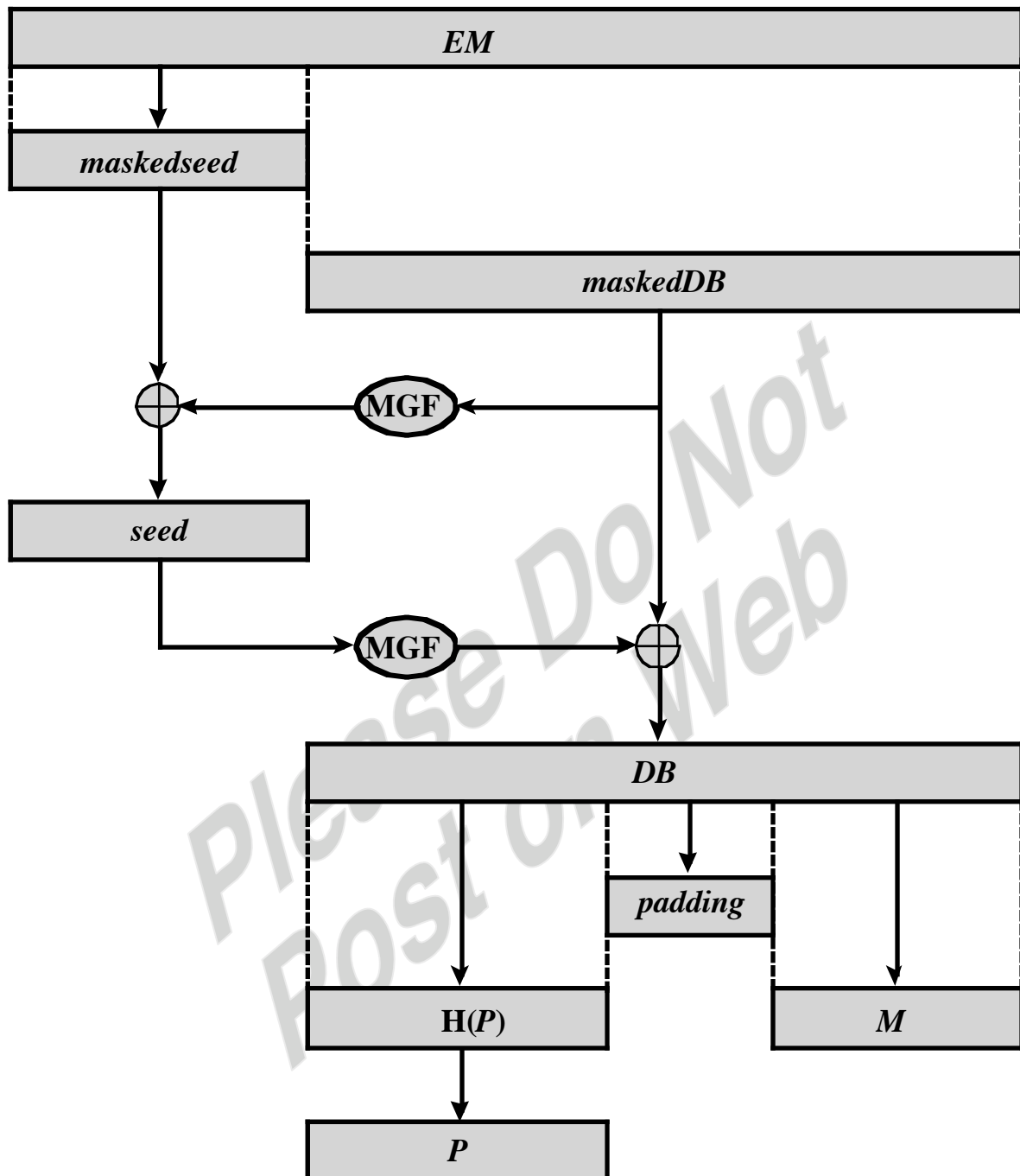
The algorithm preserves the invariant that $d = a^c \pmod{n}$ as it increases c by doublings and incrementations until $c = b$.

Now let us consider the algorithm in the problem, which is adapted from one in [KNUT98, page 462]. This algorithm processes the binary representation of b from right to left (least significant to most significant). In this case, the algorithm preserves the invariant that $a^n = d \times T^E$. At the end, $E = 0$, leaving $a^n = d$.

- 9.18** Note that because $Z = r^e \pmod{n}$, then $r = Z^d \pmod{n}$. Bob computes:

$$tY \pmod{n} = r^{-1}X^d \pmod{n} = r^{-1}Z^d C^d \pmod{n} = C^d \pmod{n} = M$$

9.19



- 9.20 a. By noticing that $x^{i+1} = x^i \times x$, we can avoid a large amount of recomputation for the S terms.

algorithm P2;

```

n, i: integer; x, polyval: real;
a, S, power: array [0..100] of real;
begin
  read(x, n);
  power[0] := 1; read(a[0]); S[0] := a[0];
  for i := 1 upto n do
    begin
      read(a[i]); power[i] := x × power[i - 1];
      S[i] := a[i] × power[i]
    end;
  polyval := 0;
  for i := 0 upto n do polyval := polyval + S[i];
  write ('value at', x, 'is', polyval)
end.

```

- b. The hint, known as Horner's rule, can be written in expanded form for $P(x)$:

$$P(x) = ((\dots (a_n x + a_{n-1})x + a_{n-2})x + \dots + a_1) + a_0$$

We use this to produce the revised algorithm:

algorithm P2;

```

n, i: integer; x, polyval: real;
a: array [0..100] of real;
begin
  read(x, n);
  polyval := 0;
  for i := 0 upto n do
    begin
      read(a[n - i]); polyval := polyval × x + a[n - i]
    end;
  write ('value at', x, 'is', polyval)
end.

```

P3 is a substantial improvement over P2 not only in terms of time but also in terms of storage requirements.

9.21 $90 + 455 + 341 + 132 + 56 + 82 = 1.156 \times 10^3$

- 9.22 a. $w^{-1} \equiv 3 \pmod{20}$; $\mathbf{a} = (7, 1, 15, 10)$; ciphertext = 18.
 b. $w^{-1} \equiv 387 \pmod{491}$; $\mathbf{a} = (203, 118, 33, 269, 250, 9, 112, 361)$; ciphertext = 357.
 c. $w^{-1} \equiv 15 \pmod{53}$; $\mathbf{a} = (39, 32, 11, 22, 37)$; ciphertext = 119.
 d. $w^{-1} \equiv 1025 \pmod{9291}$; $\mathbf{a} = (8022, 6463, 7587, 7986, 65, 8005, 6592, 7274)$; ciphertext = 30869.

9.23 To see this requirement, let us redo the derivation Appendix F, expanding the vectors to show the actual arithmetic.

The sender develops a simple knapsack vector \mathbf{a}' and a corresponding hard knapsack $\mathbf{a} = w\mathbf{a}' \bmod m$. To send a message \mathbf{x} , the sender computes and sends:

$$S = \mathbf{a} \bullet \mathbf{x} = \sum a_i x_i$$

Now, the receiver can easily compute S' and solve for \mathbf{x} :

$$\begin{aligned} S' &= w^{-1}S \bmod m \\ &= w^{-1} \sum a_i x_i \bmod m \\ &= w^{-1} \sum (w a'_i \bmod m) x_i \bmod m \\ &= \sum (w^{-1} w a'_i \bmod m) x_i \\ &= \sum a'_i x_i \bmod m \end{aligned}$$

Each of the x_i has a value of zero or one, so that the maximum value of the summation is $\sum a_i$. If $m > \sum a_i$, then the mod m term has no effect and we have

$$S' = \sum a'_i x_i$$

This can easily be solved for the x_i .

CHAPTER 10 OTHER PUBLIC-KEY CRYPTOSYSTEMS

ANSWERS TO QUESTIONS

- 10.1** Two parties each create a public-key, private-key pair and communicate the public key to the other party. The keys are designed in such a way that both sides can calculate the same unique secret key based on each side's private key and the other side's public key.
- 10.2** An elliptic curve is one that is described by cubic equations, similar to those used for calculating the circumference of an ellipse. In general, cubic equations for elliptic curves take the form

$$y^2 + axy + by = x^3 + cx^2 + dx + e$$

where a, b, c, d , and e are real numbers and x and y take on values in the real numbers

- 10.3** Also called the point at infinity and designated by O . This value serves as the additive identity in elliptic-curve arithmetic.
- 10.4** If three points on an elliptic curve lie on a straight line, their sum is O .

ANSWERS TO PROBLEMS

- 10.1** Users A and B use the Diffie-Hellman key exchange technique with a common prime $q = 71$ and a primitive root $\alpha = 7$.
- a. If user A has private key $X_A = 5$, what is A's public key Y_A ?
 - b. If user B has private key $X_B = 12$, what is B's public key Y_B ?
 - c. What is the shared secret key?
- 10.2** Consider a Diffie-Hellman scheme with a common prime $q = 11$ and a primitive root $\alpha = 2$.
- a. Show that 2 is a primitive root of 11.
 - b. If user A has public key $Y_A = 9$, what is A's private key X_A ?
 - c. If user B has public key $Y_B = 3$, what is the secret key K shared with A?
- 10.3** In the Diffie-Hellman protocol, each participant selects a secret number x and sends the other participant $\alpha^x \bmod q$ for some public number α . What

would happen if the participants sent each other x^α for some public number α instead? Give at least one method Alice and Bob could use to agree on a key. Can Eve break your system without finding the secret numbers? Can Eve find the secret numbers?

- 10.4** This problem illustrates the point that the Diffie-Hellman protocol is not secure without the step where you take the modulus; i.e. the "Indiscrete Log Problem" is not a hard problem! You are Eve, and have captured Alice and Bob and imprisoned them. You overhear the following dialog.
Bob: Oh, let's not bother with the prime in the Diffie-Hellman protocol, it will make things easier.
Alice: Okay, but we still need a base α to raise things to. How about $g = 3$?
Bob: All right, then my result is 27.
Alice: And mine is 243.
 What is Bob's secret X_B and Alice's secret X_A ? What is their secret combined key? (Don't forget to show your work.)
- 10.5** Section 10.1 describes a man-in-the-middle attack on the Diffie-Hellman key exchange protocol in which the adversary generates two public-private key pairs for the attack. Could the same attack be accomplished with one pair? Explain.
- 10.6** a. (49, 57)
 b. $C_2 = 29$
- 10.7** a. For a vertical tangent line, the point of intersection is infinity. Therefore $2Q = O$.
 b. $3Q = 2Q + Q = O + Q = Q$.
- 10.8** We use Equation (10.1), which defines the form of the elliptic curve as $y^2 = x^3 + ax + b$, and Equation (10.2), which says that an elliptic curve over the real numbers defines a group if $4a^3 + 27b^2 \neq 0$.
 a. For $y^2 = x^3 - x$, we have $4(-1)^3 + 27(0) = -4 \neq 0$.
 b. For $y^2 = x^3 + x + 1$, we have $4(1)^3 + 27(1) = 21 \neq 0$.
- 10.9** Yes, since the equation holds true for $x = 4$ and $y = 7$:

$$7^2 = 4^3 - 5(4) + 5$$

$$49 = 64 - 20 + 5 = 49$$
- 10.10** a. First we calculate $R = P + Q$, using Equations (10.3).

$$\Delta = (8.5 - 9.5) / (-2.5 + 3.5) = -1$$

$$x_R = 1 + 3.5 + 2.5 = 7$$

$$y_R = -8.5 - (-3.5 - 7) = 2$$

$$R = (7, 2)$$
 b. For $R = 2P$, we use Equations (10.4), with $a = -36$

$$x_r = [(36.75 - 36) / 19]^2 + 7 \approx 7$$

$$y_r = [(36.75 - 36) / 19](-3.5 - 7) - 9.5 \approx 9.9$$
- 10.11** $(4a^3 + 27b^2) \bmod p = 4(10)^3 + 27(5)^2 \bmod 17 = 4675 \bmod 17 = 0$

This elliptic curve does not satisfy the condition of Equation (10.6) and therefore does not define a group over Z_{17} .

10.12

x	$(x^3 + x + 6) \bmod 11$	square roots mod p?	y
0	6	no	
1	8	no	
2	5	yes	4, 7
3	3	yes	5, 6
4	8	no	
5	4	yes	2, 9
6	8	no	
7	4	yes	2, 9
8	9	yes	3, 8
9	7	no	
10	4	yes	2, 9

10.13 The negative of a point $P = (x_P, y_P)$ is the point $-P = (x_P, -y_P \bmod p)$. Thus $-P = (5, 9)$; $-Q = (3, 0)$; $-R = (0, 11)$

10.14 We follow the rules of addition described in Section 10.3. To compute $2G = (2, 7) + (2, 7)$, we first compute

$$\begin{aligned}\lambda &= (3 \times 2^2 + 1) / (2 \times 7) \bmod 11 \\ &= 13/14 \bmod 11 = 2/3 \bmod 11 = 8\end{aligned}$$

Then we have

$$\begin{aligned}x_3 &= 8^2 - 2 - 2 \bmod 11 = 5 \\ y_3 &= 8(2 - 5) - 7 \bmod 11 = 2 \\ 2G &= (5, 2)\end{aligned}$$

Similarly, $3G = 2G + G$, and so on. The result:

$2G = (5, 2)$	$3G = (8, 3)$	$4G = (10, 2)$	$5G = (3, 6)$
$6G = (7, 9)$	$7G = (7, 2)$	$8G = (3, 5)$	$9G = (10, 9)$
$10G = (8, 8)$	$11G = (5, 9)$	$12G = (2, 4)$	$13G = (2, 7)$

10.15 a. $P_B = n_B \times G = 7 \times (2, 7) = (7, 2)$. This answer is seen in the preceding table.

b. $C_m = \{kG, P_m + kP_B\}$
 $= \{3(2, 7), (10, 9) + 3(7, 2)\} = \{(8, 3), (10, 9) + (3, 5)\} = \{(8, 3), (10, 2)\}$

c. $P_m = (10, 2) - 7(8, 3) = (10, 2) - (3, 5) = (10, 2) + (3, 6) = (10, 9)$

10.16 a. $S + kY_A = M - kx_A G + kx_A G = M$.

b. The imposter gets Alice's public verifying key Y_A and sends Bob M, k , and $S = M - kY_A$ for any k .

10.17 a. $S + kY_A = M - x_A C_1 + kY_A = M - x_A kG + kx_A G = M$.

- b.** Suppose an imposter has an algorithm that takes as input the public G , $Y_A = x_A G$, Bob's $C_1 = kG$, and the message M and returns a valid signature which Bob can verify as $S = M - kY_A$ and Alice can reproduce as $M - x_A C_1$. The imposter intercepts an encoded message $C_m = \{k'G', P_m + k'P_A\}$ from Bob to Alice where $P_A = n_A G'$ is Alice's public key. The imposter gives the algorithm the input $G = G'$, $Y_A = P_A$, $C_1 = k'G'$, $M = P_m + k'P_A$ and the algorithm computes an S which Alice could "verify" as $S = P_m + k'P_A - n_A k'G' = P_m$.
- c.** Speed, likelihood of unintentional error, opportunity for denial of service or traffic analysis.

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CHAPTER 11 CRYPTOGRAPHIC HASH FUNCTIONS

ANSWERS TO QUESTIONS

- 11.1
1. H can be applied to a block of data of any size.
 2. H produces a fixed-length output.
 3. $H(x)$ is relatively easy to compute for any given x , making both hardware and software implementations practical.
 4. For any given value h , it is computationally infeasible to find x such that $H(x) = h$. This is sometimes referred to in the literature as the **one-way** property.
 5. For any given block x , it is computationally infeasible to find $y \neq x$ with $H(y) = H(x)$.
 6. It is computationally infeasible to find any pair (x, y) such that $H(x) = H(y)$.
- 11.2 Property 5 in Question 11.9 defines **weak collision resistance**. Property 6 defines **strong collision resistance**.
- 11.3 A typical hash function uses a compression function as a basic building block, and involves repeated application of the compression function.
- 11.4 In **little-endian format**, the least significant byte of a word is in the low-address byte position. In **big-endian format**, the most significant byte of a word is in the low-address byte position.
- 11.5 Addition modulo 2^{64} or 2^{32} , circular shift, primitive Boolean functions based on AND, OR, NOT, and XOR.

ANSWERS TO PROBLEMS

- 11.1 a. Yes. The XOR function is simply a vertical parity check. If there is an odd number of errors, then there must be at least one column that contains an odd number of errors, and the parity bit for that column will detect the error. Note that the RXOR function also catches all errors caused by an odd number of error bits. Each RXOR bit is a function of a unique "spiral" of bits in the block of data. If there is an odd number of errors, then there must be at least one spiral that contains an odd number of errors, and the parity bit for that spiral will detect the error.
- b. No. The checksum will fail to detect an even number of errors when both the XOR and RXOR functions fail. In order for both to fail, the pattern of error bits must be at intersection points between parity spirals and parity columns such that there is an even number of error bits in each parity column and an even number of error bits in each spiral.

- c. It is too simple to be used as a secure hash function; finding multiple messages with the same hash function would be too easy.

11.2 a. For clarity, we use overbars for complementation. We have:

$$E(\overline{M_i}, \overline{H_{i-1}}) = \overline{E(M_i, H_{i-1})} \oplus \overline{H_{i-1}} = E(M_i, H_{i-1}) \oplus H_{i-1}$$

Therefore, the hash function of message M with initial value I is the same as the hash function for message N with initial value \bar{I} for any given I , where

$$M = M_1 \parallel M_2 \parallel \dots \parallel M_n; \quad N = \bar{M}_1 \parallel M_2 \parallel \dots \parallel M_n$$

- b. The same line of reasoning applies with the M s and H s reversed in the derivation.

- 11.3 a.** It satisfies properties 1 through 3 but not the remaining properties. For example, for property 4, a message consisting of the value h satisfies $H(h) = h$. For property 5, take any message M and add the decimal digit 0 to the sequence; it will have the same hash value.
- b.** It satisfies properties 1 through 3. Property 4 is also satisfied if n is a large composite number, because taking square roots modulo such an integer n is considered to be infeasible. Properties 5 and 6 are not satisfied because $-M$ will have the same value as M .
- c.** 955

- 11.4** If you examine the structure of a single round of DES, you see that the round includes a one-way function, f , and an XOR:

$$R_i = L_{i-1} \oplus f(R_{i-1}, K_i)$$

For DES, the function f is depicted in Figure 3.6. It maps a 32-bit R and a 48-bit K into a 32-bit output. That is, it maps an 80-bit input into a 32-bit output. This is clearly a one-way function. Any hash function that produces a 32-bit output could be used for f . The demonstration in the text that decryption works is still valid for any one-way function f .

- 11.5** The opponent has the two-block message $B1, B2$ and its hash $\text{RSAH}(B1, B2)$. The following attack will work. Choose an arbitrary $C1$ and choose $C2$ such that:

$$C2 = \text{RSA}(C1) \oplus \text{RSA}(B1) \oplus B2$$

then

$$\begin{aligned} \text{RSA}(C1) \oplus C2 &= \text{RSA}(C1) \oplus \text{RSA}(C1) \oplus \text{RSA}(B1) \oplus B2 \\ &= \text{RSA}(B1) \oplus B2 \end{aligned}$$

so

$$\begin{aligned} \text{RSAH}(C1, C2) &= \text{RSA}[\text{RSA}(C1) \oplus C2] = \text{RSA}[\text{RSA}(B1) \oplus B2] \\ &= \text{RSAH}(B1, B2) \end{aligned}$$

- 11.6** The statement is false. Such a function cannot be one-to-one because the number of inputs

to the function is of arbitrary, but the number of unique outputs is 2^n . Thus, there are multiple inputs that map into the same output.

- 11.7** Assume an array of sixteen 64-bit words $W[0], \dots, W[15]$, which will be treated as a circular queue. Define $\text{MASK} = 0000000F$ in hex. Then for round t :

$s = t \wedge \text{MASK};$
 if $(t \geq 16)$ then
 $W[s] = W[s] \oplus \sigma_0(W[(s + 1) \wedge \text{MASK}]) \oplus$
 $W[(s + 9) \wedge \text{MASK}] \oplus \sigma_1(W[(s + 14) \wedge \text{MASK}])$

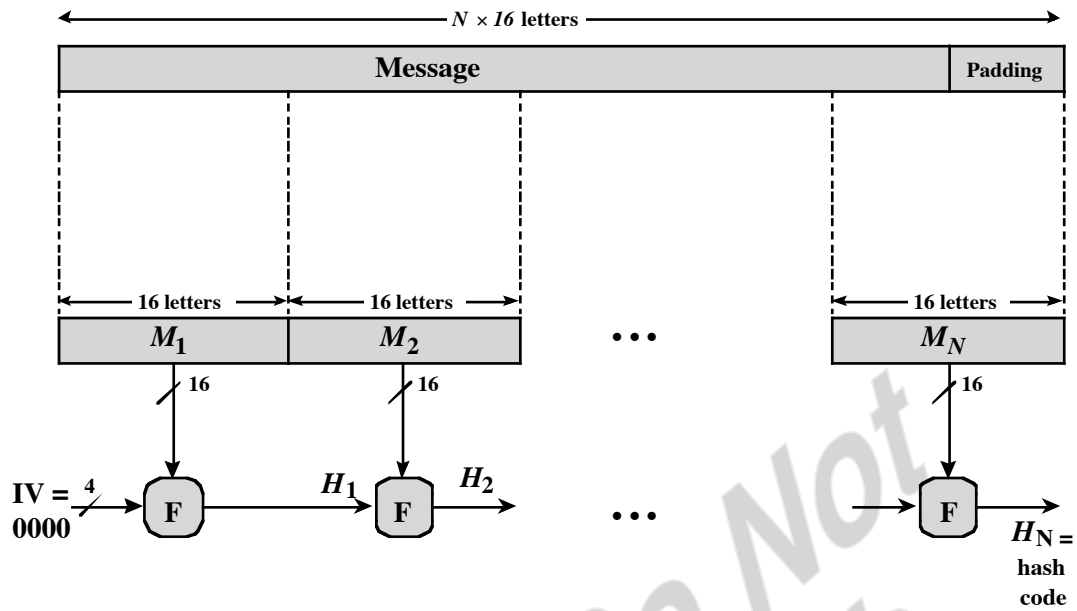
- 11.8** $W_{16} = W_0 \oplus \sigma_0(W_1) \oplus W_9 \oplus \sigma_1(W_{14})$
 $W_{17} = W_1 \oplus \sigma_0(W_2) \oplus W_{10} \oplus \sigma_1(W_{15})$
 $W_{18} = W_2 \oplus \sigma_0(W_3) \oplus W_{11} \oplus \sigma_1(W_{16})$
 $W_{19} = W_3 \oplus \sigma_0(W_4) \oplus W_{12} \oplus \sigma_1(W_{17})$

- 11.9** a. 1 bit
 b. 1024 bits
 c. 1023 bits

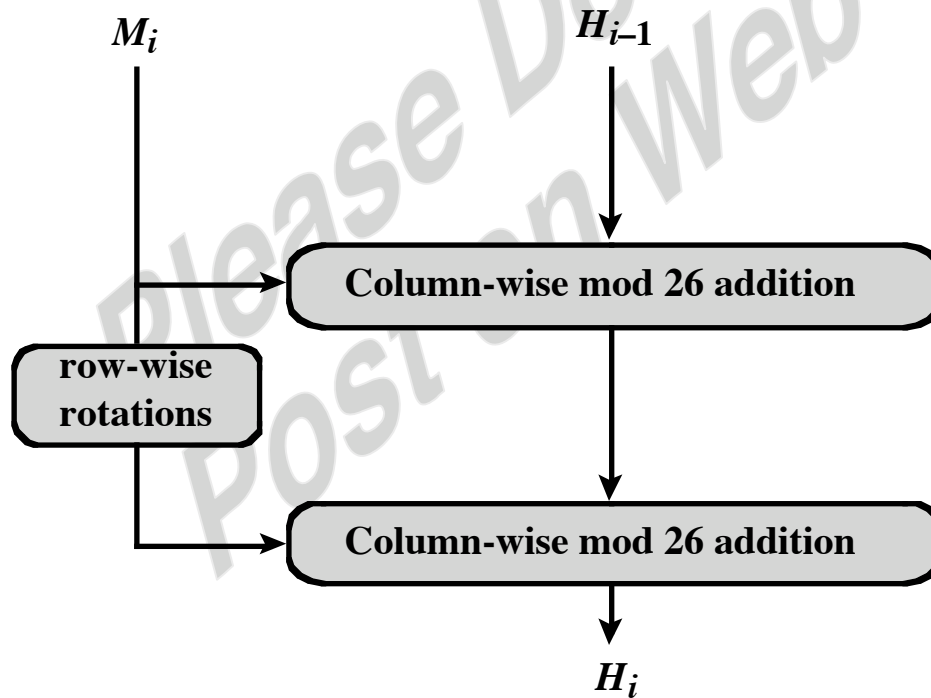
- 11.10** a. 1919
 b. 1920
 c. 1921

- 11.11** a. 1. Interchange x_1 and x_4 ; x_2 and x_3 ; y_1 and y_4 ; and y_2 and y_3 .
 2. Compute $Z = X + Y \bmod 2^{32}$.
 3. Interchange z_1 and z_4 ; and z_2 and z_3 .
 b. You must use the same sort of interchange.

11.12 a. Overall structure:



Compression function F :



b. BFQG

c. Simple algebra is all you need to generate a result:

AYHGDAAAAAAAAAAAAAAAAAAAA
AAAAAAAAAAAAAAAAAAAAAAAAAAAA

11.13 Generator for GF(2⁸) using $x^8 + x^4 + x^3 + x^2 + 1$. Partial results:

Power Representation	Polynomial Representation	Binary Representation	Decimal (Hex) Representation
0	0	00000000	00
$g^0 (= g^{127})$	1	00000001	01
g^1	g	00000010	02
g^2	g^2	00000100	04
g^3	g^3	00001000	08
g^4	g^4	00010000	10
g^5	g^5	00100000	20
g^6	g^6	01000000	40
g^7	g^7	10000000	80
g^8	$g^4 + g^3 + g^2 + 1$	00011101	1D
g^9	$g^5 + g^4 + g^3 + g$	00111010	3A
g^{10}	$g^6 + g^5 + g^4 + g^2$	01110100	74
g^{11}	$g^7 + g^6 + g^5 + g^3$	11101000	E8
g^{12}	$g^7 + g^6 + g^3 + g^2 + 1$	11001101	CD
g^{13}	$g^7 + g^2 + g + 1$	10000111	87
g^{14}	$g^4 + g + 1$	00010011	13

11.14

	00	01	10	11
00	1	B	9	C
01	D	6	F	3
10	E	8	7	4
11	A	2	5	0

E box

	00	01	10	11
00	F	0	D	7
01	B	E	5	A
10	9	2	C	1
11	3	4	8	6

E⁻¹ box

- 11.15**
- For input 00: The output of the first E box is 0001. The output of the first E⁻¹ box is 1111. The input to R is 1110 and the output of R is 0001. The input to the second E box is 0000 and the output is 0001. The input to the second E⁻¹ box is 1110 and the output is 1000. So the final output is 00011000 in binary, which is 18 in hex. This agrees with Table N.2a.
 - For input 55: The output of the first E box is 0110. The output of the first E⁻¹ box is 1110. The input to R is 1000 and the output of R is 0110. The input to the second E box is 0000 and the output is 0001. The input to the second E⁻¹ box is 1000 and the output is 1001. So the final output is 00011001 in binary, which is 19 in hex. This agrees with Table N.2a.

- c. For input 1E: The output of the first E box is 1011. The output of the first E^{-1} box is 1000. The input to R is 0011 and the output of R is 1101. The input to the second E box is 0110 and the output is 1111. The input to the second E^{-1} box is 0101 and the output is 1110. So the final output is 1111110 in binary, which is in hex FE. This agrees with Table N.2a.

- 11.16** Treat the input to the S-box as two 4-bit variables u and v and the output as the 4-bit variables u' and v' . The S-box can be expressed as $(u', v') = S(u, v)$. Using Figure N.5, we can express this as:

$$u' = E[E(u) \oplus r], \quad v' = E^{-1}[E^{-1}(v) \oplus r]$$

where $r = R[E(u) \oplus E^{-1}(v)]$

- 11.17** Consider the encryption $E(H_{i-1}, M_i)$. We could write the last round key as $K_{10} = E(RC, H_{i-1})$; this quantity is XORed onto the cipher state as the last encryption step. Now take a look at the recursion: $H_i = E(H_{i-1}, M_i) \oplus M_i$. Formally applying this construction to the "key encryption line" we get $K'_{10} = E(RC, H_{i-1}) \oplus H_{i-1}$. Using this value as the effective last round key formally creates two interacting lines (as compared to the interacting encryption lines), and results in the Whirlpool scheme, which therefore shows up as the natural choice for the compression function. This explanation is taken from the Whirlpool document.

CHAPTER 12 MESSAGE AUTHENTICATION CODES

ANSWERS TO QUESTIONS

- 12.1 Masquerade:** Insertion of messages into the network from a fraudulent source. This includes the creation of messages by an opponent that are purported to come from an authorized entity. Also included are fraudulent acknowledgments of message receipt or nonreceipt by someone other than the message recipient. **Content modification:** Changes to the contents of a message, including insertion, deletion, transposition, and modification. **Sequence modification:** Any modification to a sequence of messages between parties, including insertion, deletion, and reordering. **Timing modification:** Delay or replay of messages. In a connection-oriented application, an entire session or sequence of messages could be a replay of some previous valid session, or individual messages in the sequence could be delayed or replayed. In a connectionless application, an individual message (e.g., datagram) could be delayed or replayed.
- 12.2** At the lower level, there must be some sort of function that produces an authenticator: a value to be used to authenticate a message. This lower-level function is then used as primitive in a higher-level authentication protocol that enables a receiver to verify the authenticity of a message.
- 12.3** Message encryption, message authentication code, hash function.
- 12.4** Error control code, then encryption.
- 12.5** An authenticator that is a cryptographic function of both the data to be authenticated and a secret key.
- 12.6** A hash function, by itself, does not provide message authentication. A secret key must be used in some fashion with the hash function to produce authentication. A MAC, by definition, uses a secret key to calculate a code used for authentication.
- 12.7** Figures 11.2 and 11.3 illustrate a variety of ways in which a hash code can be used to provide message authentication, as follows. Figure 11.2: **a.** The message plus concatenated hash code is encrypted using symmetric encryption. **b.** Only the hash code is encrypted, using symmetric encryption. **c.** Only the hash code is encrypted, using public-key encryption and using the sender's private key. **d.** If confidentiality as well as a digital signature is desired, then the message plus the public-key-encrypted hash code can be encrypted using a symmetric secret key. Figure 11.3 **a.** This technique uses a hash function but no encryption for message

authentication. The technique assumes that the two communicating parties share a common secret value S . A computes the hash value over the concatenation of M and S and appends the resulting hash value to M . Because B possesses S , it can recompute the hash value to verify. **b.** Confidentiality can be added to the approach of (e) by encrypting the entire message plus the hash code.

12.8 No. Section 12.4 outlines such attacks.

12.9 To replace a given hash function in an HMAC implementation, all that is required is to remove the existing hash function module and drop in the new module.

ANSWERS TO PROBLEMS

12.1 No. If internal error control is used, error propagation in the deciphering operation introduces too many errors for the error control code to correct.

12.2 The CBC mode with an IV of 0 and plaintext blocks D_1, D_2, \dots, D_n and 64-bit CFB mode with $IV = D_1$ and plaintext blocks D_2, D_3, \dots, D_n yield the same result.

12.3 We use the definition from Section 12.6. For a one-block message, the MAC using CBC-MAC is $T = E(K, X)$, where K is the key and X is the message block. Now consider the two-block message in which the first block is X and the second block is $X \oplus T$. Then the MAC is $E(K, [T \oplus (X \oplus T)]) = E(K, X) = T$.

12.4 We use Figure 12.8a but put the XOR with K_1 after the final encryption. For this problem, there are two blocks to process. The output of the encryption of the first message block is $E(K, 0) = \text{CBC}(K, 0) = T_0 \oplus K_1$. This is XORed with the second message block $(T_0 \oplus T_1)$, so that the input to the second encryption is $(T_1 \oplus K_1) = \text{CBC}(K, 1) = E(K, 1)$. So the output of the second encryption is $E(K, [E(K, 1)]) = \text{CBC}(K, [\text{CBC}(K, 1)]) = T_2 \oplus K_1$. After the final XOR with K_1 , we get $\text{VMAC}(K, [0 \parallel (T_0 \oplus T_1)]) = T_2$.

12.5 a. In each case (64 bits, 128 bits) the constant is the binary representation of the irreducible polynomial defined in Section 12.6. The two constants are

$$R_{128} = 0^{120}10000111 \quad \text{and} \quad R_{64} = 0^{59}11011$$

b. Here is the algorithm from the NIST document:

1. Let $L = E(K, 0^b)$.
2. If $\text{MSB}_1(L) = 0$, then $K_1 = L \ll 1$;
Else $K_1 = (L \ll 1) \oplus R_b$;
3. If $\text{MSB}_1(K_1) = 0$, then $K_2 = K_1 \ll 1$;
Else $K_2 = (K_1 \ll 1) \oplus R_b$.

12.6 a. MtE

b. This is basically the E&M approach, but uses one key instead of two.

- 12.7 As was discussed in Chapter 4, multiplication distributes over addition in a field, and for this type of field the XOR operation is the addition operation. Consider a message consisting of two blocks. Then by Figure 12.10a, the GHASH function is

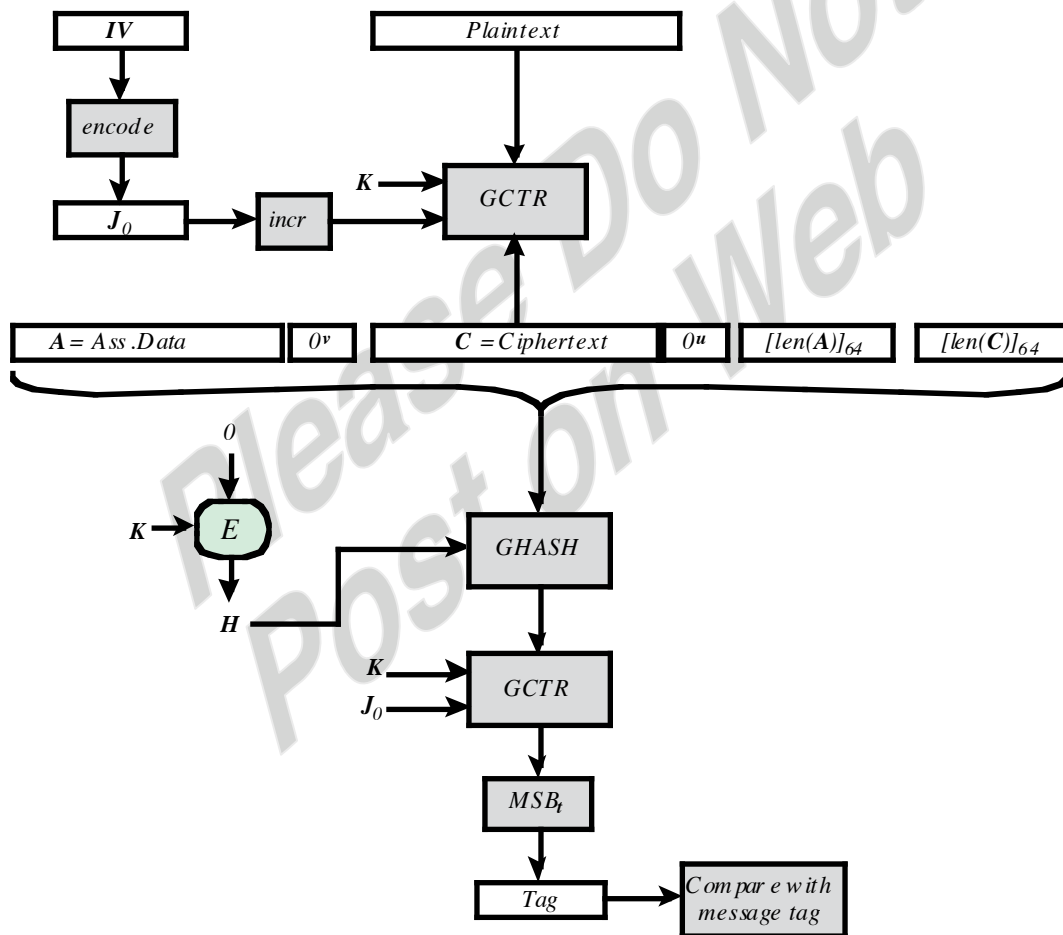
$$(X_1 \cdot H) \oplus X_2 \cdot H)$$

Multiplying through by H, we get the expression

$$(X_1 \cdot H^2) \oplus (X_2 \cdot H)$$

This calculation can be extended through more blocks, up to X_m , to get the expression shown in Problem 12.7.

12.8



- 12.9 a. The following matrix shows the message for each received 2-bit word.

	Word			
Key	00	01	10	11
1	0	1	—	—
2	1	—	0	—
3	—	0	—	1
4	—	—	1	0

- b. The probability that some one can successfully impersonate Alice is 0.5 because only two of the four words are possible as transmitted word under the joint secret key.
- c. An opponent Eve who tries to replace a transmitted message by another one will know that only two keys can possibly have been used, but she doesn't know which one. So, the probability of a successful substitution is also 0.5.

Please Do Not
Post on Web

CHAPTER 13 DIGITAL SIGNATURES

ANSWERS TO QUESTIONS

- 13.1** Suppose that John sends an authenticated message to Mary. The following disputes that could arise: **1.** Mary may forge a different message and claim that it came from John. Mary would simply have to create a message and append an authentication code using the key that John and Mary share. **2.** John can deny sending the message. Because it is possible for Mary to forge a message, there is no way to prove that John did in fact send the message.
- 13.2** **1.** It must be able to verify the author and the date and time of the signature. **2.** It must be able to authenticate the contents at the time of the signature. **3.** The signature must be verifiable by third parties, to resolve disputes.
- 13.3** **1.** The signature must be a bit pattern that depends on the message being signed. **2.** The signature must use some information unique to the sender, to prevent both forgery and denial. **3.** It must be relatively easy to produce the digital signature. **4.** It must be relatively easy to recognize and verify the digital signature. **5.** It must be computationally infeasible to forge a digital signature, either by constructing a new message for an existing digital signature or by constructing a fraudulent digital signature for a given message. **6.** It must be practical to retain a copy of the digital signature in storage.
- 13.4** A **direct digital signature** involves only the communicating parties (source, destination). It is assumed that the destination knows the public key of the source. A digital signature may be formed by encrypting the entire message with the sender's private key or by encrypting a hash code of the message with the sender's private key. An **arbitrated digital signature** operates as follows. Every signed message from a sender X to a receiver Y goes first to an arbiter A, who subjects the message and its signature to a number of tests to check its origin and content. The message is then dated and sent to Y with an indication that it has been verified to the satisfaction of the arbiter.
- 13.5** It is important to perform the signature function first and then an outer confidentiality function. In case of dispute, some third party must view the message and its signature. If the signature is calculated on an encrypted message, then the third party also needs access to the decryption key to read the original message. However, if the signature is the inner operation, then the recipient can store the plaintext message and its signature for later use in dispute resolution.
- 13.6** **1.** The validity of the scheme depends on the security of the sender's private key. If a sender later wishes to deny sending a particular message, the sender can claim that the private key was lost or stolen and that someone else forged his or her

signature. 2. Another threat is that some private key might actually be stolen from X at time T. The opponent can then send a message signed with X's signature and stamped with a time before or equal to T.

ANSWERS TO PROBLEMS

13.1 Instead of two keys e and d we will have THREE keys u , v , and w . They must be selected in such way that $uvw = 1 \pmod{\phi(N)}$. (This can be done e.g. by selecting u and v randomly (but they have to be prime to $\phi(N)$) and then choosing w such that the equation holds.) The key w is made public, while u and v become the first and the second signatory's key respectively. Now the first signatory signs document M by computing $S1 = M^u \pmod N$. The second signatory can verify the signature with the help of his key v and publicly known w , because $S1^{vw} \pmod N$ has to be M . He then 'adds' his signature by computing $S2 = S1^v \pmod N$ (that is $S2 = M^{uv} \pmod N$). Anyone can now verify that $S2$ is really the double signature of M (i.e. that M was signed by both signatories) because $S2^w \pmod N$ is equal to M only if $S2 = M^{uv} \pmod N$.

13.2 A user who produces a signature with $s = 0$ is inadvertently revealing his or her private key x via the relationship:

$$s = 0 = k^{-1}[H(m) + xr] \pmod q$$

$$x = \frac{-H(m)}{r} \pmod q$$

13.3 A user's private key is compromised if k is discovered.

13.4 a. Note that at the start of step 4, $z = b^{2^j m} \pmod w$. The idea underlying this algorithm is that if $(b^m \pmod w) \neq 1$ and $w = 1 + 2^a m$ is prime, the sequence of values

$$b^m \pmod w, \quad b^{2m} \pmod w, \quad b^{4m} \pmod w, \dots$$

will end with 1, and the value just preceding the first appearance of 1 will be $w - 1$. Why? Because, if w is prime, then if we have $z^2 \pmod w = 1$, then we have $z^2 \equiv 1 \pmod w$. And if that is true, then $z = (w - 1)$ or $z = (w + 1)$. We cannot have $z = (w + 1)$, because on the preceding step, z was calculated mod w , so we must have $z = (w - 1)$. On the other hand, if we reach a point where $z = 1$, and z was not equal to $(w - 1)$ on the preceding step, then we know that w is not prime.

b. This algorithm is a simplified version of the Miller-Rabin algorithm. In both cases, a test variable is repeatedly squared and computed modulo the possible prime, and the possible fails if a value of 1 is encountered.

13.5 The signer must be careful to generate the values of k in an unpredictable manner, so that the scheme is not compromised.

- 13.6
- If Algorithm 1 returns the value g , then we see that $g^q = 1 \pmod{p}$. Thus, $\text{ord}(g)$ divides q . Because q is prime, this implies that $\text{ord}(g) \in \{1, q\}$. However, because $g \neq 1$, we have that $\text{ord}(g) \neq 1$, and so it must be that $\text{ord}(g) = q$.
 - If Algorithm 2 returns the value g , then we see that $g^q \equiv (h^{p-1/q})^q \equiv h^{p-1} \equiv 1 \pmod{p}$. Thus, $\text{ord}(g)$ divides q . Because q is prime, this implies that $\text{ord}(g) \in \{1, q\}$. However, because $g \neq 1$, we have that $\text{ord}(g) \neq 1$, and so it must be that $\text{ord}(g) = q$.
 - Algorithm 1 works by choosing elements of Z_p until it finds one of order q . Since q divides $p-1$, Z_p contains exactly $\phi(q) = q-1$ elements of order q . Thus, the probability that $g \in Z_p$ has order q is $(q-1)/(p-1)$. When $p = 40193$ and $q = 157$ this probability is $156/40192$. So, we expect Algorithm 1 to make $40192/156 \approx 258$ loop iterations.
 - No. If p is 1024 bits and q is 160 bits, then we expect Algorithm 1 to require $(q-1)/(p-1) \approx (2^{160})/(2^{1024}) = 2^{-864}$ loop iterations.
 - Algorithm 2 will fail to find a generator in its first loop iteration only if $1 \equiv h^{(p-1)/q} \pmod{p}$. This implies that $\text{ord}(h)$ divides $(p-1)/q$. Thus, the number of bad choices for h is the number of elements of Z_p with order dividing $(p-1)/q$:

$$\sum_{d|(p-1)/q} \phi(d)$$

This sum is equal to $(p-1)/q$. Thus, the desired probability is:

$$1 - \frac{(p-1)/q}{p-1} = 1 - \frac{1}{q} = \frac{q-1}{q} = \frac{156}{157} \approx 0.994$$

- 13.7
- To verify the signature, the user verifies that $(g^Z)^h = g^X \pmod{p}$.
 - To forge the signature of a message, I find its hash h . Then I calculate Y to satisfy $Yh = 1 \pmod{p-1}$. Now $g^{Yh} = g$, so $g^{XYh} = g^X \pmod{p}$. Hence (h, g^{XY}) is a valid signature and the opponent can calculate g^{XY} as $(g^X)^Y$.
- 13.8
- The receiver validates the digital signature by ensuring that the first 56-bit key in the signature will encipher validation parameter $u1$ into $E(k1, u1)$ if the first bit of M is 0, or that it will encipher $U1$ into $E(K1, U1)$ if the first bit of M is 1; the second 56-bit key in the signature will encipher validation parameter $u2$ into $E(k2, u2)$ if the second bit of M is 0, or it will encipher $U2$ into $E(K2, U2)$ if the second bit of M is 1; and so on.
 - Only the sender, who knows the private values of k_i and K_i and who originally creates v_i and V_i from u_i and U_i can disclose a key to the receiver. An opponent would have to discover the value of the secret keys from the plaintext-ciphertext pairs of the public key, which was computationally infeasible at the time that 56-bit keys were considered secure.
 - This is a one-time system, because half of the keys are revealed the first time.
 - A separate key must be included in the signature for each bit of the message resulting in a huge digital signature.

CHAPTER 14 KEY MANAGEMENT AND DISTRIBUTION

ANSWERS TO QUESTIONS

- 14.1 For two parties A and B, key distribution can be achieved in a number of ways, as follows:
1. A can select a key and physically deliver it to B.
 2. A third party can select the key and physically deliver it to A and B.
 3. If A and B have previously and recently used a key, one party can transmit the new key to the other, encrypted using the old key.
 4. If A and B each has an encrypted connection to a third party C, C can deliver a key on the encrypted links to A and B.
- 14.2 A **session key** is a temporary encryption key used between two principals. A **master key** is a long-lasting key that is used between a key distribution center and a principal for the purpose of encoding the transmission of session keys. Typically, the master keys are distributed by noncryptographic means.
- 14.3 A nonce is a value that is used only once, such as a timestamp, a counter, or a random number; the minimum requirement is that it differs with each transaction.
- 14.4 A key distribution center is a system that is authorized to transmit temporary session keys to principals. Each session key is transmitted in encrypted form, using a master key that the key distribution center shares with the target principal.
- 14.5 1. The distribution of public keys. 2. The use of public-key encryption to distribute secret keys
- 14.6 Public announcement. Publicly available directory. Public-key authority. Public-key certificates
- 14.7 1. The authority maintains a directory with a {name, public key} entry for each participant. 2. Each participant registers a public key with the directory authority. Registration would have to be in person or by some form of secure authenticated communication. 3. A participant may replace the existing key with a new one at any time, either because of the desire to replace a public key that has already been used for a large amount of data, or because the corresponding private key has been compromised in some way. 4. Periodically, the authority publishes the entire directory or updates to the directory. For example, a hard-copy version much like a telephone book could be published, or updates could be listed in a widely circulated newspaper. 5. Participants could also access the directory

electronically. For this purpose, secure, authenticated communication from the authority to the participant is mandatory.

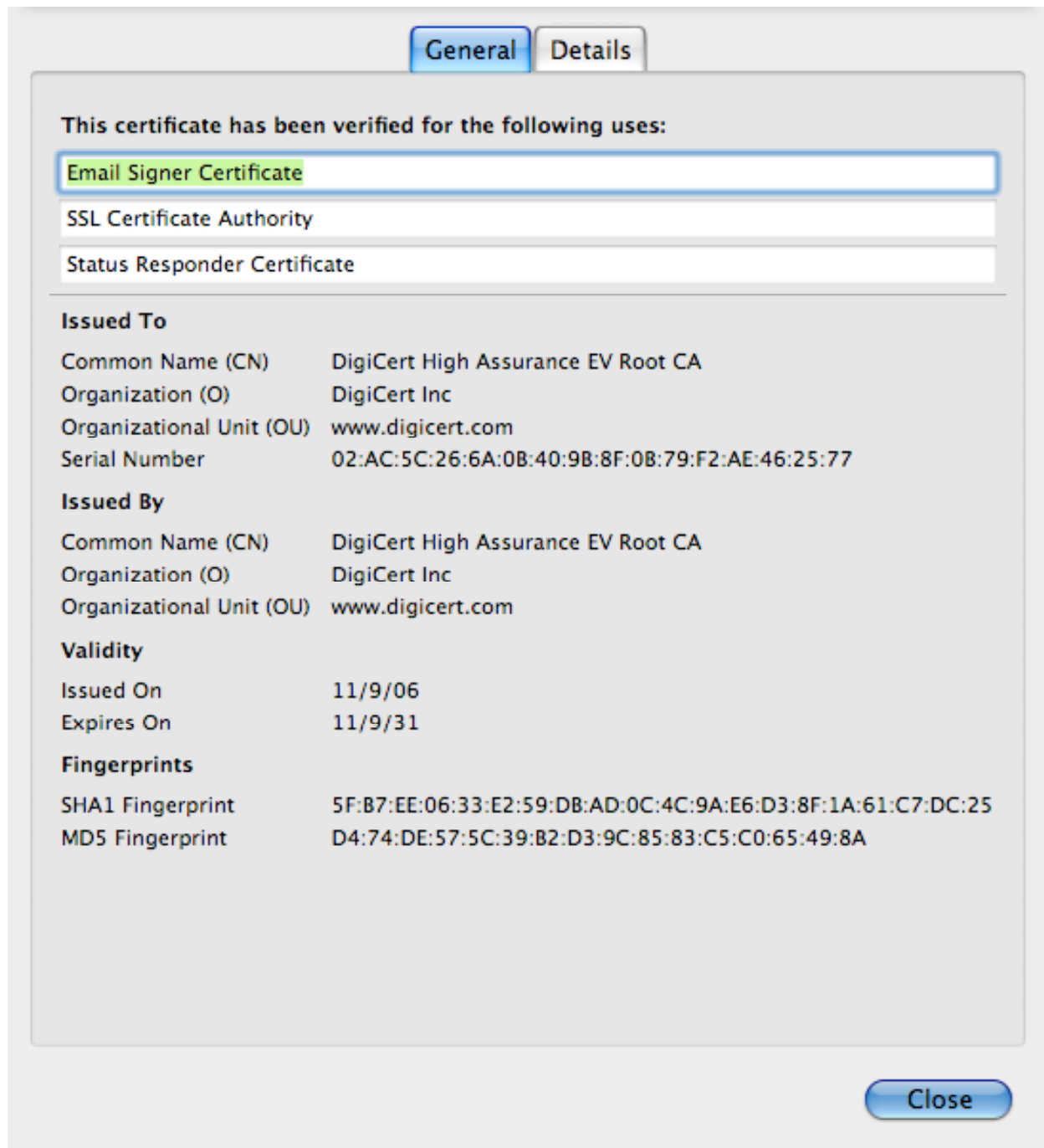
- 14.8** A public-key certificate contains a public key and other information, is created by a certificate authority, and is given to the participant with the matching private key. A participant conveys its key information to another by transmitting its certificate. Other participants can verify that the certificate was created by the authority.
- 14.9** 1. Any participant can read a certificate to determine the name and public key of the certificate's owner. 2. Any participant can verify that the certificate originated from the certificate authority and is not counterfeit. 3. Only the certificate authority can create and update certificates. 4. Any participant can verify the currency of the certificate.
- 14.10** X.509 defines a framework for the provision of authentication services by the X.500 directory to its users. The directory may serve as a repository of public-key certificates. Each certificate contains the public key of a user and is signed with the private key of a trusted certification authority.
- 14.11** A chain of certificates consists of a sequence of certificates created by different certification authorities (CAs) in which each successive certificate is a certificate by one CA that certifies the public key of the next CA in the chain.
- 14.12** The owner of a public-key can issue a certificate revocation list that revokes one or more certificates.

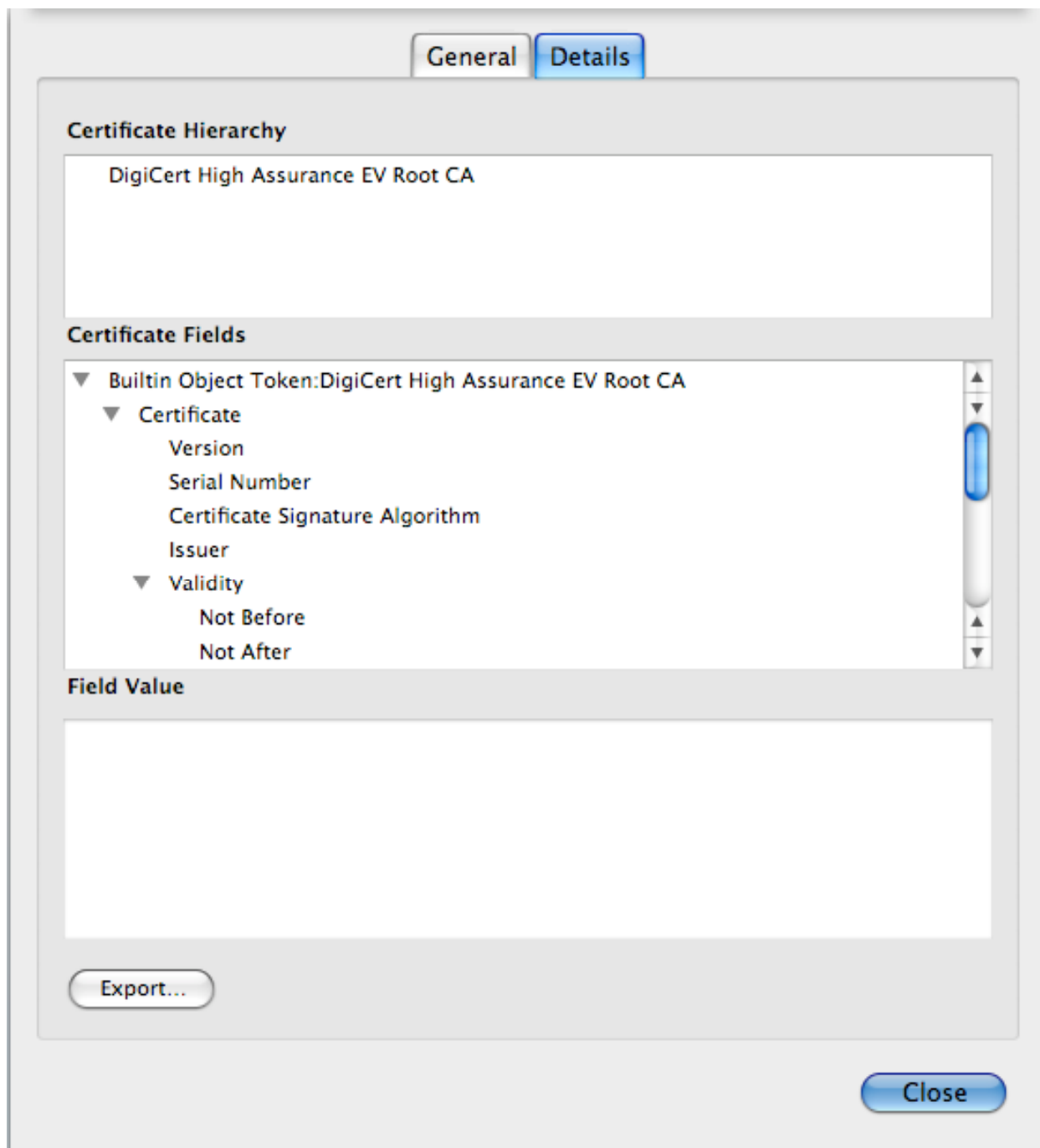
ANSWERS TO PROBLEMS

- 14.1 a.** A sends a connection request to B, with an event marker or nonce (N_a) encrypted with the key that A shares with the KDC. If B is prepared to accept the connection, it sends a request to the KDC for a session key, including A's encrypted nonce plus a nonce generated by B (N_b) and encrypted with the key that B shares with the KDC. The KDC returns two encrypted blocks to B. One block is intended for B and includes the session key, A's identifier, and B's nonce. A similar block is prepared for A and passed from the KDC to B and then to A. A and B have now securely obtained the session key and, because of the nonces, are assured that the other is authentic.
- b.** The proposed scheme appears to provide the same degree of security as that of Figure 14.3. One advantage of the proposed scheme is that the, in the event that B rejects a connection, the overhead of an interaction with the KDC is avoided.
- 14.2 i)** Sending to the server the source name A, the destination name Z (his own), and $E(K_a, R)$, as if A wanted to send him the same message encrypted under the same key R as A did it with B
- ii)** The server will respond by sending $E(K_z, R)$ to A and Z will intercept that
- iii)** because Z knows his key K_z , he can decrypt $E(K_z, R)$, thus getting his hands on R that can be used to decrypt $E(R, M)$ and obtain M.

14.3 Taking the e th root mod n of a ciphertext block will always reveal the plaintext, no matter what the values of e and n are. In general this is a very difficult problem, and indeed is the reason why RSA is secure. The point is that, if e is too small, then taking the normal integer e th root will be the same as taking the e th root mod n , and taking integer e th roots is relatively easy.

14.4 Here is an example of a trusted root CA certificate from Firefox.





- 14.5 When a symmetric key is used to protect stored information, the recipient usage period may start after the beginning of the originator usage period as shown in the figure. For example, information may be encrypted before being stored on a compact disk. At some later time, the key may be distributed in order to decrypt and recover the information.
- 14.6 a. A believes that she shares K'_{AB} with B since her nonce came back in message 2 encrypted with a key known only to B (and A). B believes that he shares K'_{AB} with A since N_A was encrypted with K'_{AB} , which could only be retrieved from message 2 by someone who knows K'_{AB} (and this is known only by A and B). A

believes that K'_{AB} is fresh since it is included in message 2 together with N_A (and hence message 2 must have been constructed after message 1 was sent). B believes (indeed, knows) that K'_{AB} is fresh since he chose it himself.

b. B. We consider the following interleaved runs of the protocol:

1. $A \rightarrow C(B) : A, N_A$
- 1'. $C(B) \rightarrow A : B, N_A$
- 2'. $A \rightarrow C(B) : E(K_{AB}, [N_A, K'_{AB}])$
2. $C(B) \rightarrow A : E(K_{AB}, [N_A, K'_{AB}])$
3. $A \rightarrow C(B) : E(K'_{AB}, N_A)$

C cannot encrypt A's nonce, so he needs to get help with message 2. He therefore starts a new run with A, letting A do the encryption and reflecting the reply back. A will accept the unprimed protocol run and believe that B is present.

c. To prevent the attack, we need to be more explicit in the messages, e.g. by changing message 2 to include the sender and receiver (in this order), i.e. to be $E(K_{AB}, [A, B, N_A, K'_{AB}])$.

14.7 A typical PKI consists of seven core components. These are briefly described below:

1. Digital certificates (public-key certificates, X.509 certificates): A digital certificate is a signed data structure that binds one or more attributes of an entity with its corresponding public key. By being signed by a recognized and trusted authority (i.e. the Certification Authority) a digital certificate provides assurances that a particular public key belongs to a specific entity (and that the entity possesses the corresponding private key).
2. Certification Authority (CA): Certification Authorities are the people, processes and tools that are responsible for the creation, issue and management of public-key certificates that are used within a PKI.
3. Registration Authority (RA): Registration Authorities are the people, processes and tools that are responsible for authenticating the identity of new entities (users or computing devices) that require certificates from CAs. RAs additionally maintain local registration data and initiate renewal or revocation processes for old or redundant certificates. They act as agents of CAs (and in that regard can carry out some of the functions of a CA if required).
4. Certificate repository: A database, or other store, which is accessible to all users of a PKI, within which public-key certificates, certificate revocation information and policy information can be held.
5. PKI client software: Client-side software is required to ensure PKI-entities are able to make use of the key and digital certificate management services of a PKI (e.g. key creation, automatic key update and refreshment).
6. PKI-enabled applications: Software applications must be PKI-enabled before they can be used within a PKI. Typically this involves modifying an application so that it can understand and make use of digital certificates (e.g. to authenticate a remote user and authenticate itself to a remote user).
7. Policy (Certificate Policy and Certification Practice Statement): Certificate Policies and Certification Practice Statements are policy documents that define the

procedures and practices to be employed in the use, administration and management of certificates within a PKI.

14.8 The primary weakness of symmetric encryption algorithms is keeping the single key secure. Known as key management, it poses a number of significant challenges. If a user wants to send an encrypted message to another using symmetric encryption, he must be sure that she has the key to decrypt the message. How should the first user get the key to the second user? He would not want to send it electronically through the Internet, because that would make it vulnerable to eavesdroppers. Nor can he encrypt the key and send it, because the recipient would need some way to decrypt the key. And if he can even get the key securely to the user, how can he be certain that an attacker has not seen the key on that person's computer? Key management is a significant impediment to using symmetric encryption.

14.9 Adding EMK_0 would allow users to generate personal session keys, which could be exchanged, avoiding the necessity of storing a key variable in a user-to-user session.

14.10 Host i has master key KMH_i , with variants $KMH_{i,j}$, $j = 0, 1, 2$.

$KMH_{i,0}$: used to encrypt session key KS

$KMH_{i,1}$: used to encrypt user master keys (at Host i)

$KMH_{i,2}$: used to encrypt cross domain key $KMH(i, j) = KMH(j, i)$
(Host i to Host j)

Host i stores $E[KMH_{i,2}, KMH(i, j)]$ and uses a translation instruction $RFMK'$:

$RFMK'[E[KMH_{i,2}, KMH(i, j)], E(KMH_{i,0}, KS)] \rightarrow E(KMH_{i,j}, K)$

A second translation function $RTMK$ (at Host j)

$RTMK[E[KMH_{j,2}, KMH(j, i)], E(KMH(i, j), KS)] \rightarrow E(KMH_{j,0}, KS)$

which may be deciphered by a user at Host j .

14.11 One solution is to add an instruction similar to $RFMK$ of the form

$KEYGEN[RN, KMT_i, KMT_j]$

which will interpret RN as $E(KMH_0, KS)$ and return both $E(KMH_i, KS)$ and $E(KMH_j, KS)$, which are sent to the terminals i and j , respectively. RN need not be maintained at the host.

CHAPTER 15 USER AUTHENTICATION

ANSWERS TO QUESTIONS

- 15.1 Simple replay:** The opponent simply copies a message and replays it later. **Repetition that can be logged:** An opponent can replay a timestamped message within the valid time window. **Repetition that cannot be detected:** This situation could arise because the original message could have been suppressed and thus did not arrive at its destination; only the replay message arrives. **Backward replay without modification:** This is a replay back to the message sender. This attack is possible if symmetric encryption is used and the sender cannot easily recognize the difference between messages sent and messages received on the basis of content.
- 15.2** 1. Attach a sequence number to each message used in an authentication exchange. A new message is accepted only if its sequence number is in the proper order. 2. Party A accepts a message as fresh only if the message contains a timestamp that, in A's judgment, is close enough to A's knowledge of current time. This approach requires that clocks among the various participants be synchronized. 3. Party A, expecting a fresh message from B, first sends B a nonce (challenge) and requires that the subsequent message (response) received from B contain the correct nonce value.
- 15.3** When a sender's clock is ahead of the intended recipient's clock., an opponent can intercept a message from the sender and replay it later when the timestamp in the message becomes current at the recipient's site. This replay could cause unexpected results.
- 15.4** The problem that Kerberos addresses is this: Assume an open distributed environment in which users at workstations wish to access services on servers distributed throughout the network. We would like for servers to be able to restrict access to authorized users and to be able to authenticate requests for service. In this environment, a workstation cannot be trusted to identify its users correctly to network services.
- 15.5** 1. A user may gain access to a particular workstation and pretend to be another user operating from that workstation. 2. A user may alter the network address of a workstation so that the requests sent from the altered workstation appear to come from the impersonated workstation. 3. A user may eavesdrop on exchanges and use a replay attack to gain entrance to a server or to disrupt operations.
- 15.6** 1. Rely on each individual client workstation to assure the identity of its user or users and rely on each server to enforce a security policy based on user identification (ID). 2. Require that client systems authenticate themselves to

servers, but trust the client system concerning the identity of its user. **3.** Require the user to prove identity for each service invoked. Also require that servers prove their identity to clients.

- 15.7 Secure:** A network eavesdropper should not be able to obtain the necessary information to impersonate a user. More generally, Kerberos should be strong enough that a potential opponent does not find it to be the weak link. **Reliable:** For all services that rely on Kerberos for access control, lack of availability of the Kerberos service means lack of availability of the supported services. Hence, Kerberos should be highly reliable and should employ a distributed server architecture, with one system able to back up another. **Transparent:** Ideally, the user should not be aware that authentication is taking place, beyond the requirement to enter a password. **Scalable:** The system should be capable of supporting large numbers of clients and servers. This suggests a modular, distributed architecture.
- 15.8** A full-service Kerberos environment consists of a Kerberos server, a number of clients, and a number of application servers.
- 15.9** A realm is an environment in which: **1.** The Kerberos server must have the user ID (UID) and hashed password of all participating users in its database. All users are registered with the Kerberos server. **2.** The Kerberos server must share a secret key with each server. All servers are registered with the Kerberos server.
- 15.10** Version 5 overcomes some environmental shortcomings and some technical deficiencies in Version 4.

ANSWERS TO PROBLEMS

- 15.1** It is not so much a protection against an attack as a protection against error. Since N_a is not unique across the network, it is possible for B to mistakenly send message 6 to some other party that would accept N_a .
- 15.2**
- (1) $A \rightarrow B: ID_A \parallel N_a$
 - (2) $B \rightarrow KDC: ID_A \parallel ID_B \parallel N_a \parallel N_b$
 - (3) $KDC \rightarrow B: E(PR_{auth'} [ID_A \parallel PU_a]) \parallel E(PU_b, E(PR_{auth'} [N_a \parallel N_b \parallel K_s \parallel ID_A \parallel ID_B]))$
 - (4) $B \rightarrow A: E(PU_a, E(PR_{auth'} [N_a \parallel N_b \parallel K_s \parallel ID_A \parallel ID_B]))$
 - (5) $A \rightarrow B: E(K_s, N_b)$
- 15.3 a.** An unintentionally postdated message (message with a clock time that is in the future with respect to the recipient's clock) that requests a key is sent by a client. An adversary blocks this request message from reaching the KDC. The client gets no response and thinks that an omission or performance failure has occurred. Later, when the client is off-line, the adversary replays the suppressed message from the same workstation (with the same network address) and establishes a secure connection in the client's name.

- b. An unintentionally postdated message that requests a stock purchase could be suppressed and replayed later, resulting in a stock purchase when the stock price had already changed significantly.

- 15.4 All three really serve the same purpose. The difference is in the vulnerability. In **Usage 1**, an attacker could breach security by inflating N_a and withholding an answer from B for future replay attack, a form of suppress-replay attack. The attacker could attempt to predict a plausible reply in **Usage 2**, but this will not succeed if the nonces are random. In both Usage 1 and 2, the messages work in either direction. That is, if N is sent in either direction, the response is $E[K, N]$. In **Usage 3**, the message is encrypted in both directions; the purpose of function f is to assure that messages 1 and 2 are not identical. Thus, Usage 3 is more secure.
- 15.5 An error in C_1 affects P_1 because the encryption of C_1 is XORed with IV to produce P_1 . Both C_1 and P_1 affect P_2 , which is the XOR of the encryption of C_2 with the XOR of C_1 and P_1 . Beyond that, P_{N-1} is one of the XORed inputs to forming P_N .
- 15.6 Let us consider the case of the interchange of C_1 and C_2 . The argument will be the same for any other adjacent pair of ciphertext blocks. First, if C_1 and C_2 arrive in the proper order:

$$\begin{aligned} P_1 &= E[K, C_1] \oplus IV \\ P_2 &= E[K, C_2] \oplus C_1 \oplus P_1 = E[K, C_2] \oplus C_1 \oplus E[K, C_1] \oplus IV \\ P_3 &= E[K, C_3] \oplus C_2 \oplus P_2 = E[K, C_3] \oplus C_2 \oplus E[K, C_2] \oplus C_1 \oplus E[K, C_1] \oplus IV \end{aligned}$$

Now suppose that C_1 and C_2 arrive in the reverse order. Let us refer to the decrypted blocks as Q_i .

$$\begin{aligned} Q_1 &= E[K, C_2] \oplus IV \\ Q_2 &= E[K, C_1] \oplus C_2 \oplus Q_1 = E[K, C_1] \oplus C_2 \oplus E[K, C_2] \oplus IV \\ Q_3 &= E[K, C_3] \oplus C_1 \oplus Q_2 = E[K, C_3] \oplus C_1 \oplus E[K, C_1] \oplus C_2 \oplus E[K, C_2] \oplus IV \end{aligned}$$

The result is that $Q_1 \neq P_1$; $Q_2 \neq P_2$; but $Q_3 = P_3$. Subsequent blocks are clearly unaffected.

- 15.7 The problem has a simple fix, namely the inclusion of the name of B in the signed information for the third message, so that the third message now reads:

$$A \rightarrow B: \quad A \{r_B, B\}$$

- 15.8 a. This is a means of authenticating A to B. R_1 serves as a challenge, and only A is able to encrypt R_1 so that it can be decrypted with A's public key.
- b. Someone (e.g., C) can use this mechanism to get A to sign a message. Then, C will present this signature to D along with the message, claiming it was sent by A. This is a problem if A uses its public/private key for both authentication, signatures, etc.

- 15.9 a.** This is a means of authenticating A to B. Only A can decrypt the second message, to recover R_2 .
- b.** Someone (e.g. C) can use this mechanism to get A to decrypt a message (i.e., send that message as R_2) that it has eavesdropped from the network (originally sent to A).
- 15.10** It contains the Alice's ID, Bob's name, and timestamp encrypted by the KDC-Bob secret key.
- 15.11** It contains Alice's name encrypted by the KDC-Bob secret key.
- 15.12** It has a nonce (e.g., time stamp) encrypted with the session key.
- 15.13** It contains the session key encrypted by the KDC-Bob secret key.

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CHAPTER 16 TRANSPORT-LEVEL SECURITY

ANSWERS TO QUESTIONS

- 16.1** The advantage of using **IPSec** (Figure 16.1a) is that it is transparent to end users and applications and provides a general-purpose solution. Further, IPSec includes a filtering capability so that only selected traffic need incur the overhead of IPSec processing. The advantage of using **SSL** is that it makes use of the reliability and flow control mechanisms of TCP. The advantage of **application-specific security services** (Figure 16.1c) is that the service can be tailored to the specific needs of a given application.
- 16.2** SSL handshake protocol; SSL change cipher spec protocol; SSL alert protocol; SSL record protocol.
- 16.3** **Connection:** A connection is a transport (in the OSI layering model definition) that provides a suitable type of service. For SSL, such connections are peer-to-peer relationships. The connections are transient. Every connection is associated with one session. **Session:** An SSL session is an association between a client and a server. Sessions are created by the Handshake Protocol. Sessions define a set of cryptographic security parameters, which can be shared among multiple connections. Sessions are used to avoid the expensive negotiation of new security parameters for each connection.
- 16.4** **Session identifier:** An arbitrary byte sequence chosen by the server to identify an active or resumable session state. **Peer certificate:** An X509.v3 certificate of the peer. **Compression method:** The algorithm used to compress data prior to encryption. **Cipher spec:** Specifies the bulk data encryption algorithm (such as null, DES, etc.) and a hash algorithm (such as MD5 or SHA-1) used for MAC calculation. It also defines cryptographic attributes such as the hash_size. **Master secret:** 48-byte secret shared between the client and server. **Is resumable:** A flag indicating whether the session can be used to initiate new connections.
- 16.5** **Server and client random:** Byte sequences that are chosen by the server and client for each connection. **Server write MAC secret:** The secret key used in MAC operations on data sent by the server. **Client write MAC secret:** The secret key used in MAC operations on data sent by the client. **Server write key:** The conventional encryption key for data encrypted by the server and decrypted by the client. **Client write key:** The conventional encryption key for data encrypted by the client and decrypted by the server. **Initialization vectors:** When a block cipher in CBC mode is used, an initialization vector (IV) is maintained for each key. This field is first initialized by the SSL Handshake Protocol. Thereafter the final ciphertext block from each record is preserved for use as the IV with the following record. **Sequence numbers:** Each party maintains separate sequence

numbers for transmitted and received messages for each connection. When a party sends or receives a change cipher spec message, the appropriate sequence number is set to zero. Sequence numbers may not exceed $2^{64} - 1$.

- 16.6 Confidentiality:** The Handshake Protocol defines a shared secret key that is used for conventional encryption of SSL payloads. **Message Integrity:** The Handshake Protocol also defines a shared secret key that is used to form a message authentication code (MAC).
- 16.7** Fragmentation; compression; add MAC; encrypt; append SSL record header.
- 16.8** HTTPS (HTTP over SSL) refers to the combination of HTTP and SSL to implement secure communication between a Web browser and a Web server.
- 16.9** The initial version, SSH1 was focused on providing a secure remote logon facility to replace TELNET and other remote logon schemes that provided no security. SSH also provides a more general client/server capability and can be used for such network functions as file transfer and e-mail.
- 16.10 Transport Layer Protocol:** Provides server authentication, data confidentiality, and data integrity with forward secrecy (i.e., if a key is compromised during one session, the knowledge does not affect the security of earlier sessions). The transport layer may optionally provide compression.
User Authentication Protocol: Authenticates the user to the server.
Connection Protocol: Multiplexes multiple logical communications channels over a single underlying SSH connection.

ANSWERS TO PROBLEMS

- 16.1** The change cipher spec protocol exists to signal transitions in ciphering strategies, and can be sent independent of the complete handshake protocol exchange.
- 16.2** To integrity protect the first set of messages where the cookies and crypto suite information is exchanged. This will prevent a man-in-the-middle attack in step 1 for instance, where someone can suppress the original message and send a weaker set of crypto suites.
- 16.3**
- a. **Brute Force Cryptanalytic Attack:** The conventional encryption algorithms use key lengths ranging from 40 to 168 bits.
 - b. **Known Plaintext Dictionary Attack:** SSL protects against this attack by not really using a 40-bit key, but an effective key of 128 bits. The rest of the key is constructed from data that is disclosed in the Hello messages. As a result the dictionary must be long enough to accommodate 2^{128} entries.
 - c. **Replay Attack:** This is prevented by the use of nonces.
 - d. **Man-in-the-Middle Attack:** This is prevented by the use of public-key certificates to authenticate the correspondents.
 - e. **Password Sniffing:** User data is encrypted.
 - f. **IP Spoofing:** The spoofer must be in possession of the secret key as well as the forged IP address.
 - g. **IP Hijacking:** Again, encryption protects against this attack.

h. SYN Flooding: SSL provides no protection against this attack.

- 16.4** SSL relies on an underlying reliable protocol to assure that bytes are not lost or inserted. There was some discussion of reengineering the future TLS protocol to work over datagram protocols such as UDP, however, most people at a recent TLS meeting felt that this was inappropriate layering (from the SSL FAQ).
- 16.5** This allows for the message to be authenticated before attempting decryption, which may be more efficient.

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CHAPTER 17 WIRELESS NETWORK SECURITY

ANSWERS TO QUESTIONS

- 17.1 Basic service set.
- 17.2 Two or more basic service sets interconnected by a distribution system.
- 17.3 **Association:** Establishes an initial association between a station and an AP. **Authentication:** Used to establish the identity of stations to each other. **Deauthentication:** This service is invoked whenever an existing authentication is to be terminated. **Disassociation:** A notification from either a station or an AP that an existing association is terminated. A station should give this notification before leaving an ESS or shutting down. **Distribution:** used by stations to exchange MAC frames when the frame must traverse the DS to get from a station in one BSS to a station in another BSS. **Integration:** enables transfer of data between a station on an IEEE 802.11 LAN and a station on an integrated IEEE 802.x LAN. **MSDU delivery:** delivery of MAC service data units. **Privacy:** Used to prevent the contents of messages from being read by other than the intended recipient. **Reassociation:** Enables an established association to be transferred from one AP to another, allowing a mobile station to move from one BSS to another.
- 17.4 It may or may not be.
- 17.5 **Mobility** refers to the types of physical transitions that can be made by a mobile node within an 802.11 environment (no transition, movement from one BSS to another within an ESS, movement from one ESS to another). **Association** is a service that allows a mobile node that has made a transition to identify itself to the AP within a BSS so that the node can participate in data exchanges with other mobile nodes.
- 17.6 IEEE 802.11i addresses three main security areas: authentication, key management, and data transfer privacy.
- 17.7 **Discovery:** An AP uses messages called Beacons and Probe Responses to advertise its IEEE 802.11i security policy. The STA uses these to identify an AP for a WLAN with which it wishes to communicate. The STA associates with the AP, which it uses to select the cipher suite and authentication mechanism when the Beacons and Probe Responses present a choice. **Authentication:** During this phase, the STA and AS prove their identities to each other. The AP blocks non-authentication traffic between the STA and AS until the authentication transaction is successful. The AP does not participate in the authentication transaction other than forwarding traffic between the STA and AS.

Key generation and distribution: The AP and the STA perform several operations that cause cryptographic keys to be generated and placed on the AP and the STA. Frames are exchanged between the AP and STA only

Protected data transfer: Frames are exchanged between the STA and the end station through the AP. As denoted by the shading and the encryption module icon, secure data transfer occurs between the STA and the AP only; security is not provided end-to-end.

Connection termination: The AP and STA exchange frames. During this phase, the secure connection is torn down and the connection is restored to the original state.

- 17.8 TKIP is designed to require only software changes to devices that are implemented with the older wireless LAN security approach called Wired Equivalent Privacy (WEP).
- 17.9 An HTML filter translates the HTML content into WML content. It may or may not be collocated with the WAP proxy. The proxy converts the WML to a more compact form known as binary WML and delivers it to the mobile user over a wireless network using the WAP protocol stack.
- 17.10 **Text and image support:** Formatting and layout commands are provided for text and limited image capability. **Deck/card organizational metaphor:** WML documents are subdivided into small, well-defined units of user interaction called *cards*. Users navigate by moving back and forth between cards. A card specifies one or more units of interaction (a menu, a screen of text, or a text-entry field). A WML deck is similar to an HTML page in that it is identified by a Web address (URL) and is the unit of content transmission. **Support for navigation among cards and decks:** WML includes provisions for event handling, which is used for navigation or executing scripts.
- 17.11 **Class 0** provides an unreliable datagram service, which can be used for an unreliable push operation. **Class 1** provides a reliable datagram service, which can be used for a reliable push operation. **Class 2** provides a request/response transaction service and supports the execution of multiple transactions during one WSP session.
- 17.12 **Data integrity:** Ensures that data sent between the client and the gateway are not modified, using message authentication. **Privacy:** Uses encryption to ensure that a third party cannot read the data. **Authentication:** Establishes the authentication of the two parties, using digital certificates. **Denial-of-service protection:** Detects and rejects messages that are replayed or not successfully verified.
- 17.13 The WTLS **Record Protocol** takes user data from the next higher layer (WTP, WTLS Handshake Protocol, WTLS Alert Protocol, WTLS Change Cipher Spec Protocol) and encapsulates these data in a PDU. The **Change Cipher Spec Protocol** consists of a single message, which consists of a single byte with the value 1; the sole purpose of this message is to cause the pending state to be copied into the current state, which updates the cipher suite to be used on this connection. The **Alert Protocol** is used to convey WTLS-related alerts to the peer entity. The **Handshake Protocol** allows the server and client to authenticate each

other and to negotiate encryption and MAC algorithms and cryptographic keys to be used to protect data sent in a WTLS record.

- 17.14 Pairwise keys used for communication between an STA and an AP include the following: A **pre-shared key (PSK)** is a secret key shared by the AP and a STA and installed in some fashion outside the scope of IEEE 802.11i. A **master session key (MSK)**, also known as the AAK, is generated using the IEEE 802.1X protocol during the authentication phase. The **pairwise master key (PMK)** is derived from the master key. The PMK is used to generate the **pairwise transient key (PTK)**, which in fact consists of three keys to be used for communication between an STA and AP after they have been mutually authenticated.

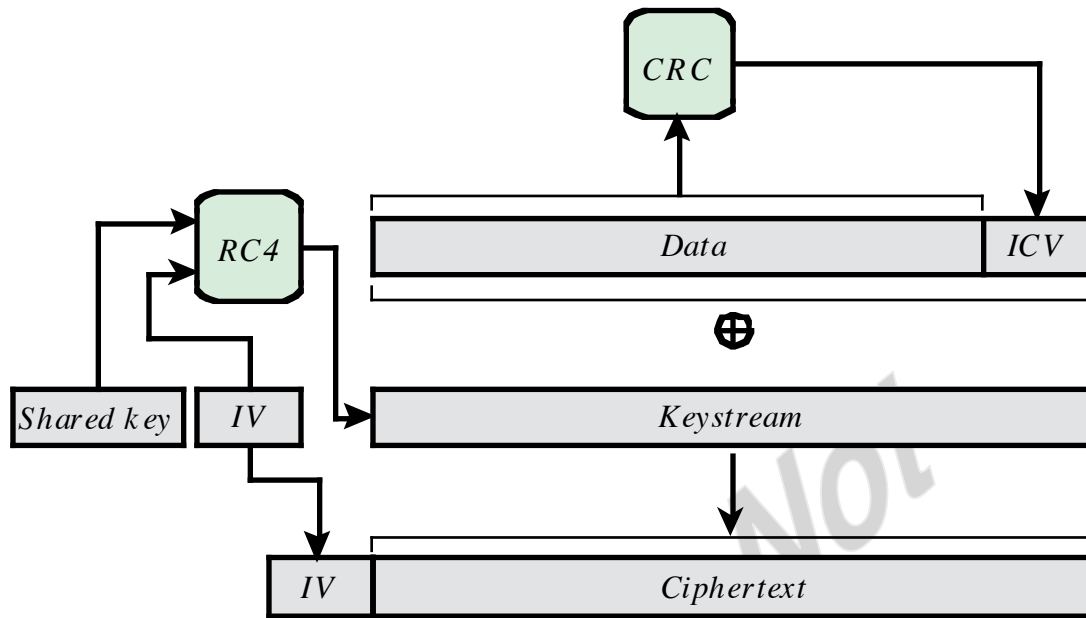
Group keys used for multicast communication include the following: The GMK is a key-generating key used with other inputs to derive the **group temporal key (GTK)**.

- 17.15 The first approach (Figure 17.20a) is to make use of TLS between client and server. Another possible approach is shown in Figure 17.20b. Here we assume that the WAP gateway acts as a simple Internet router. In this case, end-to-end security can be provided at the IP level using IPsec. Yet another, somewhat more complicated, approach has been defined in more specific terms by the WAP forum in specification entitled "WAP Transport Layer End-to-End Security." This approach is illustrated in Figure 17.21

ANSWERS TO PROBLEMS

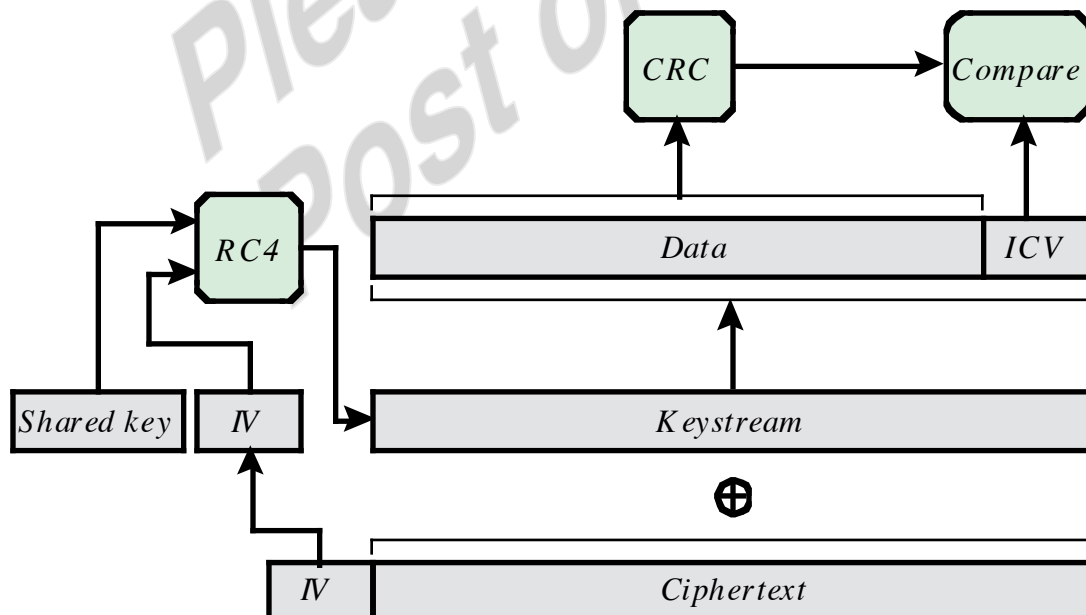
- 17.1
- This scheme is extremely simple and easy to implement. It does protect against very simple attacks using an off-the-shelf Wi-Fi LAN card, and against accidental connection to the wrong network.
 - This scheme depends on all parties behaving honestly. The scheme does not protect against MAC address forgery.
- 17.2
- Because the AP remembers the random number previously sent, it can check whether the result sent back was encrypted with the correct key; the STA must know the key in order to encrypt the random value successfully.
 - This scheme does nothing to prove to the STA that the AP knows the key, so authentication is only one way.
 - If an attacker is eavesdropping, this scheme provides the attacker with a plaintext-ciphertext pair to use in cryptanalysis.

17.3 a.



- b. 1. The IV value, which is received in plaintext, is concatenated with the WEP key shared by transmitter and receiver to form the seed, or key input, to RC4.
2. The ciphertext portion of the received MPDU is decrypted using RC4 to recover the Data block and the ICV.
3. The ICV is computed over the plaintext received Data block and compared to the received plaintext ICV to authenticate the Data block.

c.



17.4 Because WEP works by XORing the data to get the ciphertext, bit flipping survives the encryption process. Flipping a bit in the plaintext always flips the same bit in the ciphertext and vice versa.

17.5 Eve now has blocks of type

$$C_1 = E(K, [IV \oplus S \oplus P_{s,1}])$$

Where $P_{s,1}$ contains an unknown letter of Alice's password. Eve guesses that the unknown letter in the password in the intercepted packet is L. Eve sends the following packet through Alice's channel:

$$P_{r,1} = L \oplus R \oplus S$$

Where r is the sequence number of this packet and R is the concatenated version of r . This results in the following packet:

$$C_1 = E(K, [IV \oplus R \oplus P_{r,1}]) = E(K, [IV \oplus R \oplus L \oplus R \oplus S]) = E(K, [IV \oplus L \oplus S])$$

One can see that because R cancels out in the CBC computation, a correct guess $L = P_{s,1}$ leads to matching ciphertexts. Therefore, the entire password can be recovered by brute force, letter by letter, with a few hundred tests for each letter.

- 17.6** If one inverts a bit position n in the ciphertext, the MAC can be made to match by inverting the bit $(n \bmod 40)$ in the MAC. This can be repeated arbitrary number of times. Thus, when stream ciphers are used, the XOR MAC does not provide any integrity protection.

CHAPTER 18 ELECTRONIC MAIL SECURITY

ANSWERS TO QUESTIONS

- 18.1** Authentication, confidentiality, compression, e-mail compatibility, and segmentation
- 18.2** A detached signature is useful in several contexts. A user may wish to maintain a separate signature log of all messages sent or received. A detached signature of an executable program can detect subsequent virus infection. Finally, detached signatures can be used when more than one party must sign a document, such as a legal contract. Each person's signature is independent and therefore is applied only to the document. Otherwise, signatures would have to be nested, with the second signer signing both the document and the first signature, and so on.
- 18.3** **a.** It is preferable to sign an uncompressed message so that one can store only the uncompressed message together with the signature for future verification. If one signed a compressed document, then it would be necessary either to store a compressed version of the message for later verification or to recompress the message when verification is required. **b.** Even if one were willing to generate dynamically a recompressed message for verification, PGP's compression algorithm presents a difficulty. The algorithm is not deterministic; various implementations of the algorithm achieve different tradeoffs in running speed versus compression ratio and, as a result, produce different compressed forms. However, these different compression algorithms are interoperable because any version of the algorithm can correctly decompress the output of any other version. Applying the hash function and signature after compression would constrain all PGP implementations to the same version of the compression algorithm.
- 18.4** R64 converts a raw 8-bit binary stream to a stream of printable ASCII characters. Each group of three octets of binary data is mapped into four ASCII characters.
- 18.5** When PGP is used, at least part of the block to be transmitted is encrypted. If only the signature service is used, then the message digest is encrypted (with the sender's private key). If the confidentiality service is used, the message plus signature (if present) are encrypted (with a one-time symmetric key). Thus, part or all of the resulting block consists of a stream of arbitrary 8-bit octets. However, many electronic mail systems only permit the use of blocks consisting of ASCII text.
- 18.6** PGP includes a facility for assigning a level of trust to individual signers and to keys.
- 18.7** RFC 5322 defines a format for text messages that are sent using electronic mail.

- 18.8** MIME is an extension to the RFC 822 framework that is intended to address some of the problems and limitations of the use of SMTP (Simple Mail Transfer Protocol) or some other mail transfer protocol and RFC 822 for electronic mail.
- 18.9** S/MIME (Secure/Multipurpose Internet Mail Extension) is a security enhancement to the MIME Internet e-mail format standard, based on technology from RSA Data Security.
- 18.10** DomainKeys Identified Mail (DKIM) is a specification for cryptographically signing e-mail messages, permitting a signing domain to claim responsibility for a message in the mail stream.

ANSWERS TO PROBLEMS

- 18.1** CFB avoids the need to add and strip padding.
- 18.2** This is just another form of the birthday paradox discussed in Appendix 11A. Let us state the problem as one of determining what number of session keys must be generated so that the probability of a duplicate is greater than 0.5. From Equation (11.6) in Appendix 11A, we have the approximation:

$$k = 1.18 \times \sqrt{n}$$

For a 128-bit key, there are 2^{128} possible keys. Therefore

$$k = 1.18 \times \sqrt{2^{128}} = 1.18 \times 2^{64}$$

- 18.3** Again, we are dealing with a birthday-paradox phenomenon. We need to calculate the value for:

$$P(n, k) = \Pr [\text{at least one duplicate in } k \text{ items, with each item able to take on one of } n \text{ equally likely values between 1 and } n]$$

In this case, $k = N$ and $n = 2^{64}$. Using equation (11.5) of Appendix 1A:

$$P(2^{64}, N) = 1 - \frac{2^{64}!}{(2^{64} - N)! 2^{64 \times k}}$$

$$> 1 - e^{-\frac{N \times (N-1)}{2^{65}}}$$

- 18.4 a.** Not at all. The message digest is encrypted with the sender's private key. Therefore, anyone in possession of the public key can decrypt it and recover the entire message digest.
- b.** The probability that a message digest decrypted with the wrong key would have an exact match in the first 16 bits with the original message digest is 2^{-16} .

- 18.5** We trust this owner, but that does not necessarily mean that we can trust that we are in possession of that owner's public key.
- 18.6** In X.509 there is a hierarchy of Certificate Authorities. Another difference is that in X.509 users will only trust Certificate Authorities while in PGP users can trust other users.
- 18.7** DES is unsuitable because of its short key size. Two-key triple DES, which has a key length of 112 bits, is suitable. AES is also suitable.
- 18.8** It certainly provides more security than a monoalphabetic substitution. Because we are treating the plaintext as a string of bits and encrypting 6 bits at a time, we are not encrypting individual characters. Therefore, the frequency information is lost, or at least significantly obscured.

- 18.9 a.** The first step is to convert the characters into 8-bit ASCII with zero parity. Consulting the table in Appendix Q, we have the following correspondence:

```
p  01110000
l  01101100
a  01100001
i  01101001
n  01101110
t  01110100
e  01100101
x  01111000
t  01110100
```

Next, we block these off into groups of 6 bits, show the 6-bit decimal value, and do the encoding.

```
011100 000110 110001 100001 011010 010110 111001 110100
 28      6      49      33      26      22      57      52
  c      G      x      h      a      W      5      0
011001 010111 100001 110100
 25      23      33      52
  Z      X      h      0
```

So the radix-64 encoding is cGxhaW50ZXh0

- b.** All of the characters are "safe", so the quoted-printable encoding is simply plaintext

CHAPTER 19 IP SECURITY

ANSWERS TO QUESTIONS

- 19.1 Secure branch office connectivity over the Internet:** A company can build a secure virtual private network over the Internet or over a public WAN. This enables a business to rely heavily on the Internet and reduce its need for private networks, saving costs and network management overhead. **Secure remote access over the Internet:** An end user whose system is equipped with IP security protocols can make a local call to an Internet service provider (ISP) and gain secure access to a company network. This reduces the cost of toll charges for traveling employees and telecommuters. **Establishing extranet and intranet connectivity with partners:** IPSec can be used to secure communication with other organizations, ensuring authentication and confidentiality and providing a key exchange mechanism. **Enhancing electronic commerce security:** Even though some Web and electronic commerce applications have built-in security protocols, the use of IPSec enhances that security.
- 19.2** Access control; connectionless integrity; data origin authentication; rejection of replayed packets (a form of partial sequence integrity); confidentiality (encryption); and limited traffic flow confidentiality
- 19.3** A security association is uniquely identified by three parameters: **Security Parameters Index (SPI):** A bit string assigned to this SA and having local significance only. The SPI is carried in AH and ESP headers to enable the receiving system to select the SA under which a received packet will be processed. **IP Destination Address:** Currently, only unicast addresses are allowed; this is the address of the destination endpoint of the SA, which may be an end user system or a network system such as a firewall or router. **Security Protocol Identifier:** This indicates whether the association is an AH or ESP security association.
- A security association is normally defined by the following parameters: **Sequence Number Counter:** A 32-bit value used to generate the Sequence Number field in AH or ESP headers, described in Section 19.3 (required for all implementations). **Sequence Counter Overflow:** A flag indicating whether overflow of the Sequence Number Counter should generate an auditable event and prevent further transmission of packets on this SA (required for all implementations). **Anti-Replay Window:** Used to determine whether an inbound AH or ESP packet is a replay, described in Section 19.3 (required for all implementations). **AH Information:** Authentication algorithm, keys, key lifetimes, and related parameters being used with AH (required for AH implementations). **ESP Information:** Encryption and authentication algorithm, keys, initialization values, key lifetimes, and related parameters being used with ESP (required for ESP implementations). **Lifetime of this Security Association:** A time interval or byte count after which an SA must be replaced with a new SA

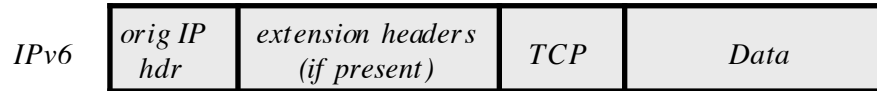
(and new SPI) or terminated, plus an indication of which of these actions should occur (required for all implementations). **IPSec Protocol Mode:** Tunnel, transport, or wildcard (required for all implementations). These modes are discussed later in this section. **Path MTU:** Any observed path maximum transmission unit (maximum size of a packet that can be transmitted without fragmentation) and aging variables (required for all implementations).

- 19.4 Transport mode** provides protection primarily for upper-layer protocols. That is, transport mode protection extends to the payload of an IP packet. **Tunnel mode** provides protection to the entire IP packet.
- 19.5** A replay attack is one in which an attacker obtains a copy of an authenticated packet and later transmits it to the intended destination. The receipt of duplicate, authenticated IP packets may disrupt service in some way or may have some other undesired consequence.
- 19.6** 1. If an encryption algorithm requires the plaintext to be a multiple of some number of bytes (e.g., the multiple of a single block for a block cipher), the Padding field is used to expand the plaintext (consisting of the Payload Data, Padding, Pad Length, and Next Header fields) to the required length. 2. The ESP format requires that the Pad Length and Next Header fields be right aligned within a 32-bit word. Equivalently, the ciphertext must be an integer multiple of 32 bits. The Padding field is used to assure this alignment. 3. Additional padding may be added to provide partial traffic flow confidentiality by concealing the actual length of the payload.
- 19.7 Transport adjacency:** Refers to applying more than one security protocol to the same IP packet, without invoking tunneling. This approach to combining AH and ESP allows for only one level of combination; further nesting yields no added benefit since the processing is performed at one IPSec instance: the (ultimate) destination. **Iterated tunneling:** Refers to the application of multiple layers of security protocols effected through IP tunneling. This approach allows for multiple levels of nesting, since each tunnel can originate or terminate at a different IPSec site along the path.

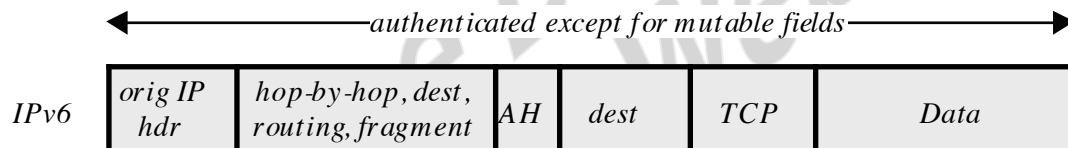
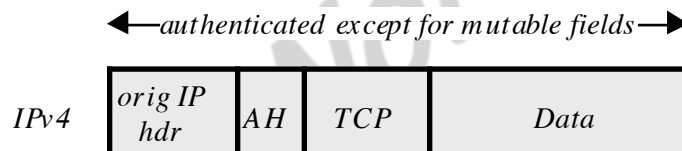
ANSWERS TO PROBLEMS

- 19.1** row 1: Traffic between this host and any other host, both using port 500, and using UDP, bypasses IPsec. This is used for IKE traffic.
row 2: ICMP message to or from any remote address are error messages, and bypass IPsec.
row 3: Traffic between 1.2.3.101 and 1.2.3.0/24 is intranet traffic and must be protected by ESP, with the exception of traffic defined in earlier rows.
row 4: TCP traffic between this host (1.2.3.101) and the server (1.2.4.10) on server port 80 is ESP protected.
row 5: TCP traffic between this host (1.2.3.101) and the server (1.2.4.10) on server port 80 is protected by TLS and so can bypass IPsec.
row 6: Any other traffic between 1.2.3.101 and 1.2.3.0/24 is prohibited and is discarded.
row 7: Any other traffic between 1.2.3.101 goes to the Internet and bypasses IPsec.

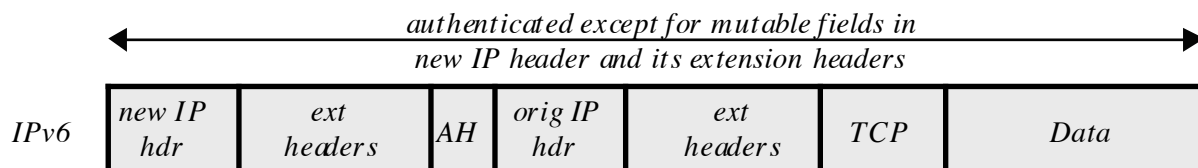
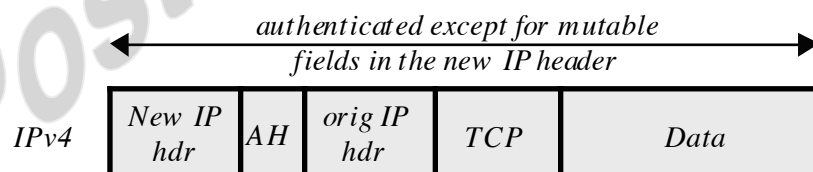
19.2.



(a) Before Applying AH



(b) Transport Mode



(c) Tunnel Mode

19.3 AH provides access control, connectionless integrity, data origin authentication, and rejection of replayed packets. ESP provides all of these plus confidentiality and limited traffic flow confidentiality.

- 19.4 a. Immutable:** Version, Internet Header Length, Total Length, Identification, Protocol (This should be the value for AH.), Source Address, Destination Address (without loose or strict source routing). None of these are changed by routers in transit.
- Mutable but predictable:** Destination Address (with loose or strict source routing). At each intermediate router designated in the source routing list, the Destination Address field is changed to indicate the next designated address. However, the source routing field contains the information needed for doing the MAC calculation.
- Mutable (zeroed prior to ICV calculation):** Type of Service (TOS), Flags, Fragment Offset, Time to Live (TTL), Header Checksum. TOS may be altered by a router to reflect a reduced service. Flags and Fragment offset are altered if an router performs fragmentation. TTL is decreased at each router. The Header Checksum changes if any of these other fields change.
- b. Immutable:** Version, Payload Length, Next Header (This should be the value for AH.), Source Address, Destination Address (without Routing Extension Header)
- Mutable but predictable:** Destination Address (with Routing Extension Header)
- Mutable (zeroed prior to ICV calculation):** Class, Flow Label, Hop Limit
- c. IPv6 options in the Hop-by-Hop and Destination Extension Headers contain a bit that indicates whether the option might change (unpredictably) during transit.**
- Mutable but predictable:** Routing
- Not Applicable:** Fragmentation occurs after outbound IPSec processing and reassembly occur before inbound IPSec processing , so the Fragmentation Extension Header, if it exists, is not seen by IPSec.
- 19.5 a.** The received packet is to the left of the window, so the packet is discarded; this is an auditable event. No change is made to window parameters.
- b.** The received packet falls within the window. If it is new, the MAC is checked. If the packet is authenticated, the corresponding slot in the window is marked. If it is not new, the packet is discarded. In either case, no change is made to window parameters.
- c.** The received packet is to the right of the window and is new, so the MAC is checked. If the packet is authenticated, the window is advanced so that this sequence number is the right edge of the window, and the corresponding slot in the window is marked. In this case, the window now spans from 120 to 540.

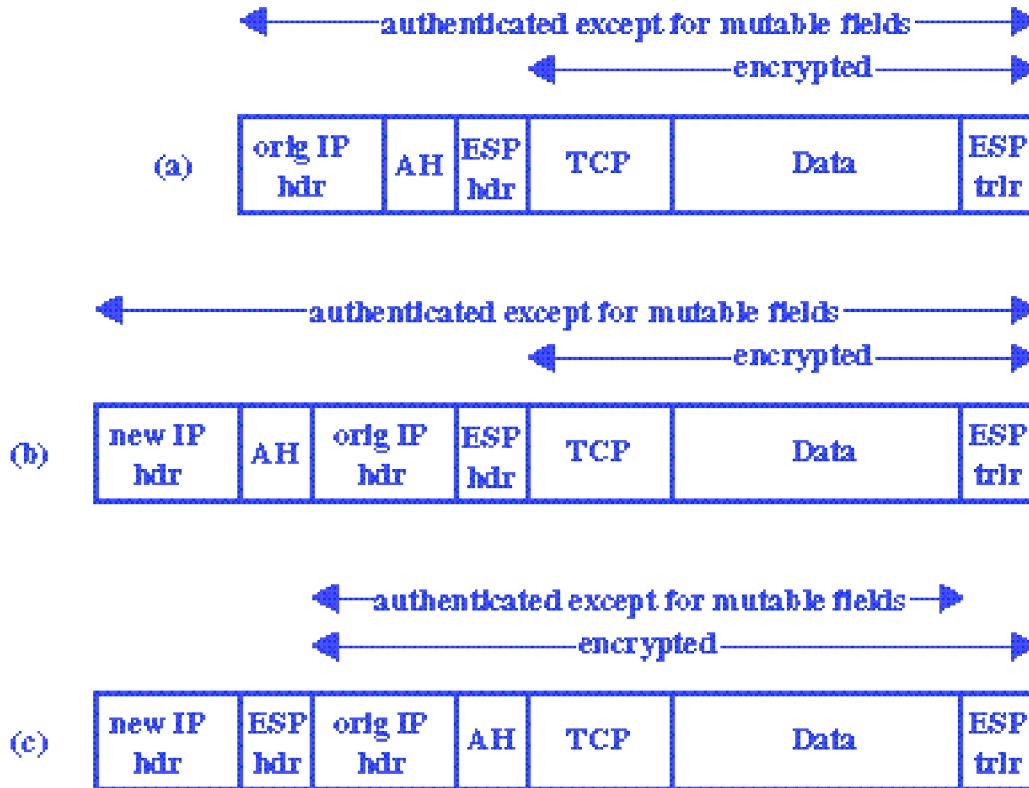
19.6 From RFC 2401

IPv4 Header Fields	Outer Header at Encapsulator	Inner Header at Decapsulator
version	4 (1)	no change
header length	constructed	no change
TOS	copied from inner header (5)	no change
total length	constructed	no change
ID	constructed	no change
Flags	constructed, DF (4)	no change
Fragment offset	constructed	no change
TTL	constructed	decrement (2)
protocol	AH, ESP, routing header	no change
checksum	constructed	no change
source address	constructed (3)	no change
destination address	constructed (3)	no change
options	never copied	no change

IPv6 Header Fields	Outer Header at Encapsulator	Inner Header at Decapsulator
version	6 (1)	no change
class	copied or configured (6)	no change
flow id	copied or configured	no change
length	constructed	no change
next header	AH, ESP, routing header	no change
hop count	constructed (2)	decrement (2)
source address	constructed (3)	no change
dest address	constructed (3)	no change
extension headers	never copied	no change

1. The IP version in the encapsulating header can be different from the value in the inner header.
2. The TTL in the inner header is decremented by the encapsulator prior to forwarding and by the decapsulator if it forwards the packet.
3. src and dest addresses depend on the SA, which is used to determine the dest address, which in turn determines which src address (net interface) is used to forward the packet.
4. configuration determines whether to copy from the inner header (IPv4 only), clear or set the DF.
5. If Inner Hdr is IPv4, copy the TOS. If Inner Hdr is IPv6, map the Class to TOS.
6. If Inner Hdr is IPv6, copy the Class. If Inner Hdr IPv4, map the TOS to Class.

19.7 We show the results for IPv4; IPv6 is similar.



19.8 This order of processing facilitates rapid detection and rejection of replayed or bogus packets by the receiver, prior to decrypting the packet, hence potentially reducing the impact of denial of service attacks. It also allows for the possibility of parallel processing of packets at the receiver, i.e., decryption can take place in parallel with authentication.

19.9 The Initial Exchanges and the CREATE_CHILD_SA Exchange

19.10 It is an addition to the IP layer.

CHAPTER 20 INTRUDERS

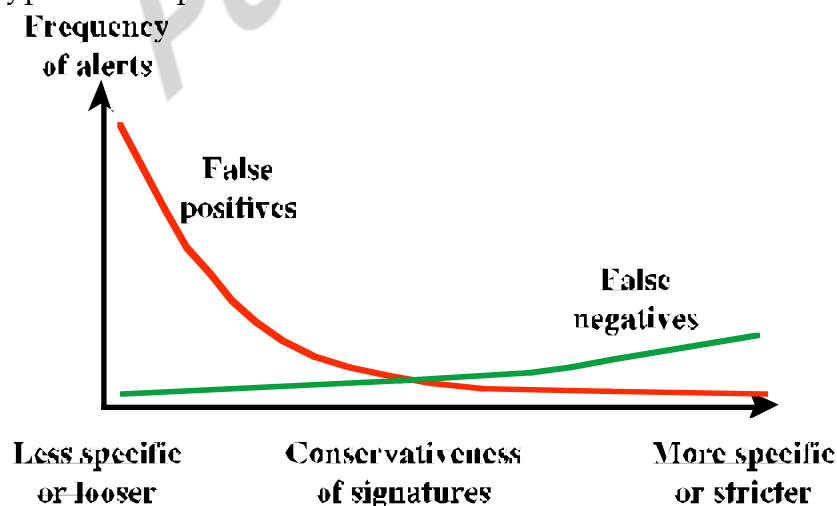
ANSWERS TO QUESTIONS

- 20.1 Masquerader:** An individual who is not authorized to use the computer and who penetrates a system's access controls to exploit a legitimate user's account. **Misfeasor:** A legitimate user who accesses data, programs, or resources for which such access is not authorized, or who is authorized for such access but misuses his or her privileges. **Clandestine user:** An individual who seizes supervisory control of the system and uses this control to evade auditing and access controls or to suppress audit collection.
- 20.2 One-way encryption:** The system stores only an encrypted form of the user's password. When the user presents a password, the system encrypts that password and compares it with the stored value. In practice, the system usually performs a one-way transformation (not reversible) in which the password is used to generate a key for the encryption function and in which a fixed-length output is produced. **Access control:** Access to the password file is limited to one or a very few accounts.
- 20.3** 1. If an intrusion is detected quickly enough, the intruder can be identified and ejected from the system before any damage is done or any data are compromised. Even if the detection is not sufficiently timely to preempt the intruder, the sooner that the intrusion is detected, the less the amount of damage and the more quickly that recovery can be achieved. 2. An effective intrusion detection system can serve as a deterrent, so acting to prevent intrusions. 3. Intrusion detection enables the collection of information about intrusion techniques that can be used to strengthen the intrusion prevention facility.
- 20.4 Statistical anomaly detection** involves the collection of data relating to the behavior of legitimate users over a period of time. Then statistical tests are applied to observed behavior to determine with a high level of confidence whether that behavior is not legitimate user behavior. **Rule-Based Detection** involves an attempt to define a set of rules that can be used to decide that a given behavior is that of an intruder.
- 20.5 Counter:** A nonnegative integer that may be incremented but not decremented until it is reset by management action. Typically, a count of certain event types is kept over a particular period of time. **Gauge:** A nonnegative integer that may be incremented or decremented. Typically, a gauge is used to measure the current value of some entity. **Interval timer:** The length of time between two related events. **Resource utilization:** Quantity of resources consumed during a specified period.

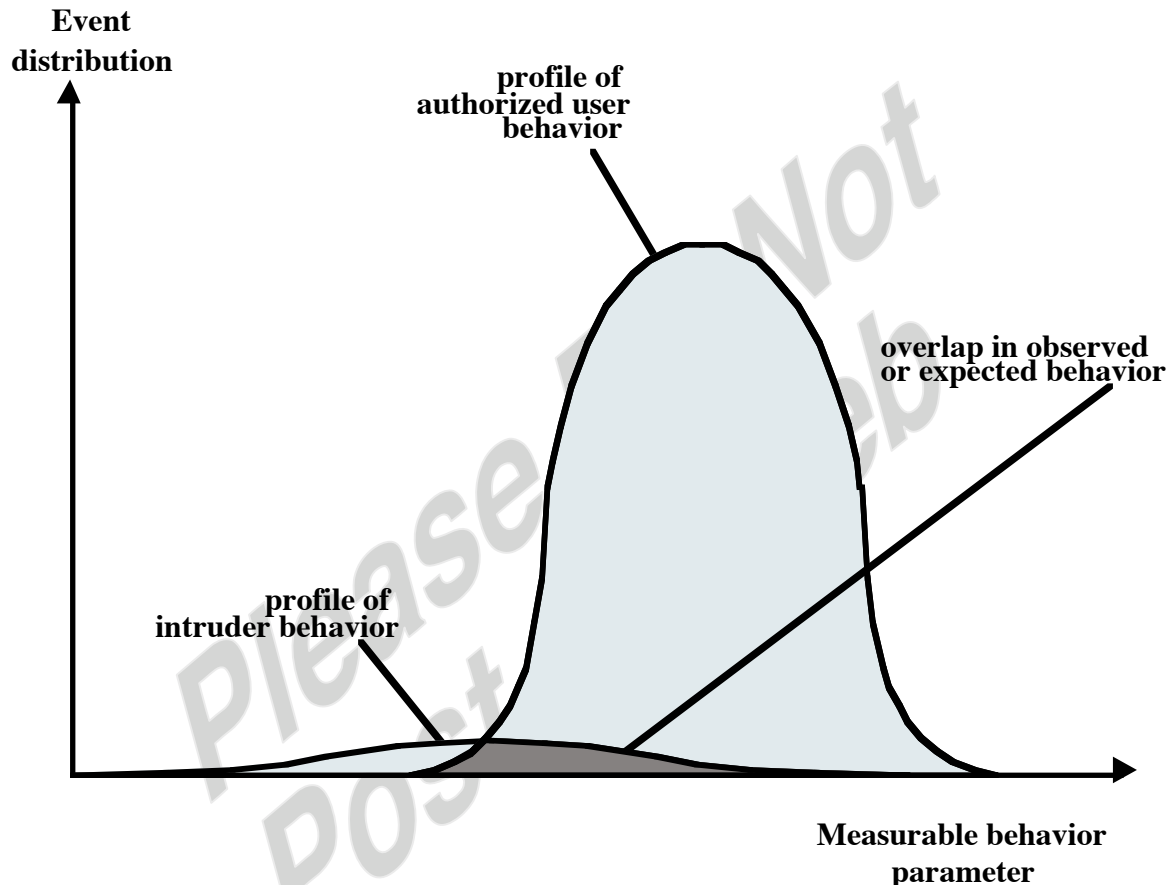
- 20.6 With **rule-based anomaly detection**, historical audit records are analyzed to identify usage patterns and to generate automatically rules that describe those patterns. Rules may represent past behavior patterns of users, programs, privileges, time slots, terminals, and so on. Current behavior is then observed, and each transaction is matched against the set of rules to determine if it conforms to any historically observed pattern of behavior. **Rule-based penetration identification** uses rules for identifying known penetrations or penetrations that would exploit known weaknesses. Rules can also be defined that identify suspicious behavior, even when the behavior is within the bounds of established patterns of usage. Typically, the rules used in these systems are specific to the machine and operating system. Also, such rules are generated by "experts" rather than by means of an automated analysis of audit records.
- 20.7 Honeypots are decoy systems that are designed to lure a potential attacker away from critical systems.
- 20.8 The salt is combined with the password at the input to the one-way encryption routine.
- 20.9 **User education:** Users can be told the importance of using hard-to-guess passwords and can be provided with guidelines for selecting strong passwords. **Computer-generated passwords:** Users are provided passwords generated by a computer algorithm. **Reactive password checking:** the system periodically runs its own password cracker to find guessable passwords. The system cancels any passwords that are guessed and notifies the user. **Proactive password checking:** a user is allowed to select his or her own password. However, at the time of selection, the system checks to see if the password is allowable and, if not, rejects it.

ANSWERS TO PROBLEMS

- 20.1 This is a typical example:



- 20.2 a. The graph below doesn't look like a correct probability distribution and is instead labeled as *event distribution*. The point here is that even if you have nice, mostly non-overlapping probability distributions for distinguishing intruders and authorized users like Figure 20.1, the problem is for most systems we hope the actual numbers of intruders is dwarfed by the number of authorized users. This means that the long tail of the authorized user's distribution that overlaps with the intruder's distribution would generate lots of false positives (relative to the number of real intruders detected) even if it is only a few percent of the authorized users.



- b. A randomly selected event that in the overlap region is (roughly) 95% likely to be an authorized user, even though the region covers 50% of the intruder's probability distribution.
- 20.3 A file integrity checking tool such as tripwire can be very useful in identifying changed files or directories on a system, particularly when those change should not have occurred. However most computer systems are not static, and significant numbers of files do change constantly. Hence it is necessary to configure tripwire with a list of files and directories to monitor, since otherwise reports to the administrator would be filled with lists of files that are changing as a matter of normal operation of the system. It is not too difficult to monitor a small list of critical system programs, daemons and configuration files. Doing this means attempts to alter these files will likely be detected. However the large areas of the system not being monitored means an attacker changing or adding files in these areas will not be detected. The more of the system that is to be monitored, the more care is needed to identify only files not expected to change. Even then, it is likely that user's home areas, and other shared document areas, cannot be

monitored, since they are likely to be creating and changing files in there regularly. As well, there needs to be a process to manage the update of monitored files (as a result of installing patches, upgrades, new services, configuration changes etc). This process has to verify that the changed files are correct, and then update the cryptographic checksums of these files. Lastly the database of cryptographic checksums must be protected from any attempt by an attacker to corrupt it, ideally by locating on read-only media (except when controlled updates are occurring).

20.4 Let WB equal the event {witness reports Blue cab}. Then:

$$\begin{aligned}\Pr[\text{Blue}/\text{WB}] &= \frac{\Pr[\text{WB}/\text{Blue}]\Pr[\text{Blue}]}{\Pr[\text{WB}/\text{Blue}]\Pr[\text{Blue}] + \Pr[\text{WB}/\text{Green}]\Pr[\text{Green}]} \\ &= \frac{(0.8)(0.15)}{(0.8)(0.15) + (0.2)(0.85)} = 0.41\end{aligned}$$

This example, or something similar, is referred to as "the juror's fallacy."

- 20.5**
- a. If this is a license plate number, that is easily guessable.
 - b. suitable
 - c. easily guessable
 - d. easily guessable
 - e. easily guessable
 - f. suitable
 - g. very unsuitable
 - h. This is bigbird in reverse; not suitable.

20.6 The number of possible character strings of length 8 using a 36-character alphabet is $36^8 \approx 2^{41}$. However, only 2^{15} of them need be looked at, because that is the number of possible outputs of the random number generator. This scheme is discussed in [MORR79].

- 20.7**
- a. $T = \frac{26^4}{2}$ seconds = 63.5 hours
 - b. Expect 13 tries for each digit. $T = 13 \times 4 = 52$ seconds.

- 20.8**
- a. $p = r^k$
 - b. $p = \frac{r^k - r^p}{r^{k+p}}$
 - c. $p = r^p$

- 20.9**
- a. $T = (21 \times 5 \times 21)^2 = 4,862,025$
 - b. $p = 1/T \approx 2 \times 10^{-7}$

20.10 There are $95^{10} \approx 6 \times 10^{19}$ possible passwords. The time required is:

$$\frac{6 \times 10^{19} \text{ passwords}}{6.4 \times 10^6 \text{ passwords / second}} = 9.4 \times 10^{12} \text{ seconds}$$

$$= 300,000 \text{ years}$$

- 20.11 a.** Since PU_a and PR_a are inverses, the value PR_a can be checked to validate that P_a was correctly supplied: Simply take some arbitrary block X and verify that $X = D(PR_a, E[PU_a, X])$.
- b.** Since the file `/etc/publickey` is publicly readable, an attacker can guess P (say P') and compute $PR_{a'} = D(P', E[P, PR_a])$. now he can choose an arbitrary block Y and check to see if $Y = D(PR_{a'}, E[PU_{a'}, Y])$. If so, it is highly probable that $P' = P$. Additional blocks can be used to verify the equality.
- 20.12** Yes.
- 20.13** Without the salt, the attacker can guess a password and encrypt it. If ANY of the users on a system use that password, then there will be a match. With the salt, the attacker must guess a password and then encrypt it once for each user, using the particular salt for each user.
- 20.14** It depends on the size of the user population, not the size of the salt, since the attacker presumably has access to the salt for each user. The benefit of larger salts is that the larger the salt, the less likely it is that two users will have the same salt. If multiple users have the same salt, then the attacker can do one encryption per password guess to test all of those users.
- 20.15 a.** If there is only one hash function ($k = 1$), which produces one of N possible hash values, and there is only one word in the dictionary, then the probability that an arbitrary bit b_i is set to 1 is just $1/N$. If there are k hash functions, let us assume for simplicity that they produce k distinct hash functions for a given word. This assumption only introduces a small margin of error. Then, the probability that an arbitrary bit b_i is set to 1 is k/N . Therefore, the probability that b_i is equal to 0 is $1 - k/N$. The probability that a bit is left unset after D dictionary words are processed is just the probability that each of the D transformations set other bits:

$$\Pr[b_i = 0] = \left(1 - \frac{k}{N}\right)^D$$

- This can also be interpreted as the expected fraction of bits that are equal to 0.
- b.** A word not in the dictionary will be falsely accepted if all k bits tested are equal to 1. Now, from part (a), we can say that the expected fraction of bits in the hash table that are equal to one is $1 - \phi$. The probability that a random word will be mapped by a single hash function onto a bit that is already set is the probability that the bit generated by the hash function is in the set of bits equal to one, which is just $1 - \phi$. Therefore, the probability that the k hash functions applied to the word will produce k bits all of which are in the set of bits equal to one is $(1 - \phi)^k$.

c. We use the approximation $(1 - x) \approx e^{-x}$.

- 20.16** The system enciphers files with a master system key KM, which is stored in some secure fashion. When User i attempts to read file F, the header of F is decrypted using KM and User i's read privilege is checked. If the user has read access, the file is decrypted using KM and the reencrypted using User i's key for transmission to User i. Write is handled in a similar fashion.

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CHAPTER 21 MALICIOUS SOFTWARE

ANSWERS TO QUESTIONS

- 21.1 A virus may use compression so that the infected program is exactly the same length as an uninfected version.
- 21.2 A portion of the virus, generally called a *mutation engine*, creates a random encryption key to encrypt the remainder of the virus. The key is stored with the virus, and the mutation engine itself is altered. When an infected program is invoked, the virus uses the stored random key to decrypt the virus. When the virus replicates, a different random key is selected.
- 21.3 A dormant phase, a propagation phase, a triggering phase, and an execution phase
- 21.4 A digital immune system provides a general-purpose emulation and virus-detection system. The objective is to provide rapid response time so that viruses can be stamped out almost as soon as they are introduced. When a new virus enters an organization, the immune system automatically captures it, analyzes it, adds detection and shielding for it, removes it, and passes information about that virus to systems running a general antivirus program so that it can be detected before it is allowed to run elsewhere.
- 21.5 Behavior-blocking software integrates with the operating system of a host computer and monitors program behavior in real-time for malicious actions. The behavior blocking software then blocks potentially malicious actions before they have a chance to affect the system.
- 21.6 1. Search for other systems to infect by examining host tables or similar repositories of remote system addresses. 2. Establish a connection with a remote system. 3. Copy itself to the remote system and cause the copy to be run.
- 21.7 **Signature-based worm scan filtering:** This type of approach generates a worm signature, which is then used to prevent worm scans from entering/leaving a network/host. Typically, this approach involves identifying suspicious flows and generating a worm signature. This approach is vulnerable to the use of polymorphic worms: Either the detection software misses the worm or, if it is sufficiently sophisticated to deal with polymorphic worms, the scheme may take a long time to react. [NEWS05] is an example of this approach.
Filter-based worm containment: This approach is similar to class A but focuses on worm content rather than a scan signature. The filter checks a message to determine if it contains worm code. An example is Vigilante [COST05], which relies on collaborative worm detection at end hosts. This approach can be quite effective but requires efficient detection algorithms and rapid alert dissemination.

Payload-classification-based worm containment: These network-based techniques examine packets to see if they contain a worm. Various anomaly detection techniques can be used, but care is needed to avoid high levels of false positives or negatives. An example of this approach is reported in [CHIN05], which looks for exploit code in network flows. This approach does not generate signatures based on byte patterns but rather looks for control and data flow structures that suggest an exploit.

Threshold random walk (TRW) scan detection: TRW exploits randomness in picking destinations to connect to as a way of detecting if a scanner is in operation [JUNG04]. TRW is suitable for deployment in high-speed, low-cost network devices. It is effective against the common behavior seen in worm scans.

Rate limiting: This class limits the rate of scanlike traffic from an infected host. Various strategies can be used, including limiting the number of new machines a host can connect to in a window of time, detecting a high connection failure rate, and limiting the number of unique IP addresses a host can scan in a window of time. [CHEN04] is an example. This class of countermeasures may introduce longer delays for normal traffic. This class is also not suited for slow, stealthy worms that spread slowly to avoid detection based on activity level.

Rate halting: This approach immediately blocks outgoing traffic when a threshold is exceeded either in outgoing connection rate or diversity of connection attempts [JHI07]. The approach must include measures to quickly unblock mistakenly blocked hosts in a transparent way. Rate halting can integrate with a signature- or filter-based approach so that once a signature or filter is generated, every blocked host can be unblocked. Rate halting appears to offer a very effective countermeasure. As with rate limiting, rate-halting techniques are not suitable for slow, stealthy worms.

- 21.8 A denial of service (DoS) attack is an attempt to prevent legitimate users of a service from using that service. When this attack comes from a single host or network node, then it is simply referred to as a DoS attack. A more serious threat is posed by a DDoS attack. In a DDoS attack, an attacker is able to recruit a number of hosts throughout the Internet to simultaneously or in a coordinated fashion launch an attack upon the target.

ANSWERS TO PROBLEMS

- 21.1 The program will loop indefinitely once all of the executable files in the system are infected.
- 21.2 D is supposed to examine a program P and return TRUE if P is a computer virus and FALSE if it is not. But CV calls D. If D says that CV is a virus, then CV will not infect an executable. But if D says that CV is not a virus, it infects an executable. D always returns the wrong answer.
- 21.3 a. When the program is executed, it produces the following output:
`begin print (); end.`
The program was probably intended to produce, upon execution, an exact listing of the original program text. Clearly, it fails.
- b. This works. Basically, it is a three-step process: (1) declare a character string that corresponds to the main body of the program; (2) print each character of

the defined string individually; (3) print the value of the array as a defined character string.

- c. The problem shows a self-replicating program, the type of functionality used in a virus.

21.4 Logic bomb.

21.5 Backdoor.

21.6 The original code has been altered to disrupt the signature without affecting the semantics of the code. The ineffective instructions in the metamorphic code are the second, third, fifth, sixth, and eighth.

21.7 a. The following is from Spafford, E. "The Internet Worm Program: An Analysis." Purdue Technical Report CSD-TR-823

Common choices for passwords usually include fantasy characters, but this list contains none of the likely choices \ (e.g., ``hobbit," ``dwarf," ``gandalf," ``skywalker," ``conan"\). Names of relatives and friends are often used, and we see women's names like ``jessica," ``caroline," and ``edwina," but no instance of the common names ``jennifer" or ``kathy." Further, there are almost no men's names such as ``thomas" or either of ``stephen" or ``steven" \ (or ``eugene"! \). Additionally, none of these have the initial letters capitalized, although that is often how they are used in passwords. Also of interest, there are no obscene words in this dictionary, yet many reports of concerted password cracking experiments have revealed that there are a significant number of users who use such words \ (or phrases \) as passwords. The list contains at least one incorrect spelling: ``commrades" instead of ``comrades"; I also believe that ``markus" is a misspelling of ``marcus." Some of the words do not appear in standard dictionaries and are non-English names: ``jixian," ``vasant," ``puneet," etc. There are also some unusual words in this list that I would not expect to be considered common: ``anthropogenic," ``imbroglio," ``umesh," ``rochester," ``fungible," ``cerulean," etc.

b. Again, from Spafford:

I imagine that this list was derived from some data gathering with a limited set of passwords, probably in some known \ (to the author \) computing environment. That is, some dictionary-based or brute-force attack was used to crack a selection of a few hundred passwords taken from a small set of machines. Other approaches to gathering passwords could also have been used \ 320 Ethernet monitors, Trojan Horse login programs, etc. However they may have been cracked, the ones that were broken would then have been added to this dictionary. Interestingly enough, many of these words are not in the standard on-line dictionary \ (in /usr/dict/words \). As such, these words are useful as a supplement to the main dictionary-based attack the worm used as strategy #4, but I would suspect them to be of limited use before that time.

21.8 One approach is to send out false alerts. This would cause alerted systems to shut down traffic incorrectly. If the spoofed alerts come from an external (to the network) source, the firewall can filter them. Also, authentication schemes can prevent the attack. Alternatively, the attacker can first compromise an internal host and then forge an alert. If an authentication scheme is used, this attack can only succeed if the spoofer has access to keys. This creates a higher hurdle for the

attacker. Another approach: if an attacker is aware of the use of PWC, the worm could be designed to try to thwart the timing analysis of the PWC agents. This appears to be very difficult because you have multiple cooperating agents and if the worm is to propagate in a reasonable time, sooner or later, worm propagation attempts must be made.

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CHAPTER 22 FIREWALLS

ANSWERS TO QUESTIONS

- 22.1** 1. All traffic from inside to outside, and vice versa, must pass through the firewall. This is achieved by physically blocking all access to the local network except via the firewall. Various configurations are possible, as explained later in this section. 2. Only authorized traffic, as defined by the local security policy, will be allowed to pass. Various types of firewalls are used, which implement various types of security policies, as explained later in this section. 3. The firewall itself is immune to penetration. This implies that use of a trusted system with a secure operating system.
- 22.2** **Service control:** Determines the types of Internet services that can be accessed, inbound or outbound. The firewall may filter traffic on the basis of IP address and TCP port number; may provide proxy software that receives and interprets each service request before passing it on; or may host the server software itself, such as a Web or mail service. **Direction control:** Determines the direction in which particular service requests may be initiated and allowed to flow through the firewall. **User control:** Controls access to a service according to which user is attempting to access it. This feature is typically applied to users inside the firewall perimeter (local users). It may also be applied to incoming traffic from external users; the latter requires some form of secure authentication technology, such as is provided in IPSec. **Behavior control:** Controls how particular services are used. For example, the firewall may filter e-mail to eliminate spam, or it may enable external access to only a portion of the information on a local Web server.
- 22.3** **Source IP address:** The IP address of the system that originated the IP packet. **Destination IP address:** The IP address of the system the IP packet is trying to reach. **Source and destination transport-level address:** The transport level (e.g., TCP or UDP) port number, which defines applications such as SNMP or TELNET. **IP protocol field:** Defines the transport protocol. **Interface:** For a router with three or more ports, which interface of the router the packet came from or which interface of the router the packet is destined for.
- 22.4** 1. Because packet filter firewalls do not examine upper-layer data, they cannot prevent attacks that employ application-specific vulnerabilities or functions. For example, a packet filter firewall cannot block specific application commands; if a packet filter firewall allows a given application, all functions available within that application will be permitted. 2. Because of the limited information available to the firewall, the logging functionality present in packet filter firewalls is limited. Packet filter logs normally contain the same information used to make access control decisions (source address, destination address, and traffic type). 3. Most packet filter firewalls do not support advanced user authentication schemes. Once

again, this limitation is mostly due to the lack of upper-layer functionality by the firewall. 4. They are generally vulnerable to attacks and exploits that take advantage of problems within the TCP/IP specification and protocol stack, such as *network layer address spoofing*. Many packet filter firewalls cannot detect a network packet in which the OSI Layer 3 addressing information has been altered. Spoofing attacks are generally employed by intruders to bypass the security controls implemented in a firewall platform. 5. Finally, due to the small number of variables used in access control decisions, packet filter firewalls are susceptible to security breaches caused by improper configurations. In other words, it is easy to accidentally configure a packet filter firewall to allow traffic types, sources, and destinations that should be denied based on an organization's information security policy.

- 22.5 A traditional packet filter** makes filtering decisions on an individual packet basis and does not take into consideration any higher layer context. A **stateful inspection packet filter** tightens up the rules for TCP traffic by creating a directory of outbound TCP connections, as shown in Table 22.2. There is an entry for each currently established connection. The packet filter will now allow incoming traffic to high-numbered ports only for those packets that fit the profile of one of the entries in this directory
- 22.6** An application-level gateway, also called a proxy server, acts as a relay of application-level traffic.
- 22.7** A circuit-level gateway does not permit an end-to-end TCP connection; rather, the gateway sets up two TCP connections, one between itself and a TCP user on an inner host and one between itself and a TCP user on an outside host. Once the two connections are established, the gateway typically relays TCP segments from one connection to the other without examining the contents. The security function consists of determining which connections will be allowed.
- 22.8 Packet filtering firewall:** Applies a set of rules to each incoming and outgoing IP packet and then forwards or discards the packet.
Stateful inspection firewall: Tightens up the rules for TCP traffic by creating a directory of outbound TCP connections, as shown in Table 22.2. There is an entry for each currently established connection. The packet filter will now allow incoming traffic to high-numbered ports only for those packets that fit the profile of one of the entries in this directory.
Application proxy firewall: Acts as a relay of application-level traffic (Figure 22.1d). The user contacts the gateway using a TCP/IP application, such as Telnet or FTP, and the gateway asks the user for the name of the remote host to be accessed. When the user responds and provides a valid user ID and authentication information, the gateway contacts the application on the remote host and relays TCP segments containing the application data between the two endpoints. If the gateway does not implement the proxy code for a specific application, the service is not supported and cannot be forwarded across the firewall. Further, the gateway can be configured to support only specific features of an application that the network administrator considers acceptable while denying all other features
Circuit-level proxy firewall: As with an application gateway, a circuit-level gateway does not permit an end-to-end TCP connection; rather, the gateway sets up two TCP connections, one between itself and a TCP user on an inner host and

one between itself and a TCP user on an outside host. Once the two connections are established, the gateway typically relays TCP segments from one connection to the other without examining the contents. The security function consists of determining which connections will be allowed.

- 22.9**
- The bastion host hardware platform executes a secure version of its operating system, making it a hardened system.
 - Only the services that the network administrator considers essential are installed on the bastion host. These could include proxy applications for DNS, FTP, HTTP, and SMTP.
 - The bastion host may require additional authentication before a user is allowed access to the proxy services. In addition, each proxy service may require its own authentication before granting user access.
 - Each proxy is configured to support only a subset of the standard application's command set.
 - Each proxy is configured to allow access only to specific host systems. This means that the limited command / feature set may be applied only to a subset of systems on the protected network.
 - Each proxy maintains detailed audit information by logging all traffic, each connection, and the duration of each connection. The audit log is an essential tool for discovering and terminating intruder attacks.
 - Each proxy module is a very small software package specifically designed for network security. Because of its relative simplicity, it is easier to check such modules for security flaws. For example, a typical UNIX mail application may contain over 20,000 lines of code, while a mail proxy may contain fewer than 1000.
 - Each proxy is independent of other proxies on the bastion host. If there is a problem with the operation of any proxy, or if a future vulnerability is discovered, it can be uninstalled without affecting the operation of the other proxy applications. Also, if the user population requires support for a new service, the network administrator can easily install the required proxy on the bastion host.
 - A proxy generally performs no disk access other than to read its initial configuration file. Hence, the portions of the file system containing executable code can be made read only. This makes it difficult for an intruder to install Trojan horse sniffers or other dangerous files on the bastion host.
 - Each proxy runs as a nonprivileged user in a private and secured directory on the bastion host.
- 22.10**
- Filtering rules can be tailored to the host environment. Specific corporate security policies for servers can be implemented, with different filters for servers used for different application.
 - Protection is provided independent of topology. Thus both internal and external attacks must pass through the firewall.
 - Used in conjunction with stand-alone firewalls, the host-based firewall provides an additional layer of protection. A new type of server can be added to the network, with its own firewall, without the necessity of altering the network firewall configuration.
- 22.11** Between internal and external firewalls are one or more networked devices in a region referred to as a DMZ (demilitarized zone) network. Systems that are externally accessible but need some protections are usually located on DMZ networks. Typically, the systems in the DMZ require or foster external

connectivity, such as a corporate Web site, an e-mail server, or a DNS (domain name system) server.

- 22.12** An **external firewall** is placed at the edge of a local or enterprise network, just inside the boundary router that connects to the Internet or some wide area network (WAN). One or more **internal firewalls** protect the bulk of the enterprise network.

ANSWERS TO PROBLEMS

- 22.1** It will be impossible for the destination host to complete reassembly of the packet if the first fragment is missing, and therefore the entire packet will be discarded by the destination after a time-out.
- 22.2** When a TCP packet is fragmented so as to force interesting header fields out of the zero-offset fragment, there must exist a fragment with FO equal to 1. If a packet with FO = 1 is seen, conversely, it could indicate the presence, in the fragment set, of a zero-offset fragment with a transport header length of eight octets. Discarding this one-offset fragment will block reassembly at the receiving host and be as effective as the direct method described above.
- 22.3** If the router's filtering module enforces a minimum fragment offset for fragments that have non-zero offsets, it can prevent overlaps in filter parameter regions of the transport headers.
- 22.4**
1. Allow return TCP Connections to internal subnet.
 2. Prevent Firewall system itself from directly connecting to anything.
 3. Prevent External users from directly accessing the Firewall system.
 4. Internal Users can access External servers,
 5. Allow External Users to send email in.
 6. Allow External Users to access WWW server.
 7. Everything not previously allowed is explicitly denied.
- 22.5**
- a. Rules A and B allow inbound SMTP connections (incoming email)
Rules C and D allow outbound SMTP connections (outgoing email)
Rule E is the default rule that applies if the other rules do not apply.
 - b. Packet 1: Permit (A); Packet 2: Permit (B); Packet 3: Permit (C)
Packet 4: Permit (D)
 - c. The attack could succeed because in the original filter set, rules B and D allow all connections where both ends are using ports above 1023.
- 22.6**
- a. A source port is added to the rule set.
 - b. Packet 1: Permit (A); Packet 2: Permit (B); Packet 3: Permit (C)
Packet 4: Permit (D); Packet 5: Deny (E); Packet 6: Deny (E)
- 22.7**
- a. Packet 7 is admitted under rule D. Packet 8 is admitted under rule C.
 - b. Add a column called ACK Set, with the following values for each rule: A = Yes; B = Yes; C = Any; D = Yes; E = Any

- 22.8** A requirement like "all external Web traffic must flow via the organization's Web proxy." is easier stated than implemented. This is because identifying what actually constitutes "web traffic" is highly problematical. Although the standard port for HTTP web servers is port 80, servers are found on a large number of other ports (including servers belonging to large, well-known and widely used organizations). This means it is very difficult to block direct access to all possible web servers just using port filters. Whilst it is easy enough to configure web browser programs to always use a proxy, this will not stop direct access by other programs. It also means that the proxy server must have access to a very large number of external ports, since otherwise access to some servers would be limited. As well as HTTP access, other protocols are used on the web. All of these should also be directed via the proxy in order to implement the desired policy. But this may impact the operation of other programs using these protocols. In particular, the HTTPS protocol is used for secure web access that encrypts all traffic flowing between the client and the server. Since the traffic is encrypted, it means the proxy cannot inspect its contents in order to apply malware, SPAM or other desired filtering. Whilst there are some mechanisms for terminating the encrypted connections at the proxy, they have limitations and require the use of suitable browsers and proxy servers.
- 22.9** A possible requirement to manage information leakage requires all external e-mail to be given a sensitivity tag (or classification) in its subject and for external e-mail to have the lowest sensitivity tag. At its simplest a policy can just require user's to always include such a tag in email messages. Alternatively with suitable email agent programs it may be possible to enforce the prompting for and inclusion of such a tag on message creation. Then, when external email is being relayed through the firewall, the mail relay server must check that the correct tag value is present in the Subject header, and refuse to forward the email outside the organization if not, and notify the user of its rejection.

22.10 Suitable packet filter rulesets FOR the "External Firewall" and the "Internal Firewall" respectively, to satisfy the stated "informal firewall policy", could be:

action	src	port	dest	port	flags	comment
permit	DMZ mail gateway	any	any	SMTP (25)		header sanitize
permit	any	any	DMZ mail gateway	SMTP (25)		content filtered
permit	any	any	DMZ mail gateway	POP3S (995)		user auth
permit	DMZ web proxy	any	any	HTTP/S (80,443)		content filtered, user auth
permit	DMZ DNS server	DNS (53)	any	DNS (53)		TCP & UDP
permit	any	DNS (53)	DMZ DNS server	DNS (53)		TCP & UDP
permit	any	any	any DMZ server	any	established	return traffic flow
deny	any	any	any	any		block all else

action	src	port	dest	port	flags	comment
permit	any internal	any	DMZ mail gateway	SMTP (25)		
permit	any internal	any	DMZ mail gateway	POP3/S (110,995)		user auth
permit	any internal	any	DMZ web proxy	HTTP/S (80,443)		content filtered, user auth
permit	any internal	DNS (53)	DMZ DNS server	DNS (53)		UDP lookup
permit	DMZ DNS server	DNS (53)	any internal	DNS (53)		UDP lookup
permit	any internal	any	any DMZ server	SSH (22)		user auth on server
permit	mgmt user hosts	any	any DMZ server	SNMP (161)		
permit	any DMZ server	any	mgmt user hosts	SNMP TRAP (162)		
permit	any DMZ server	any	any internal	any	established	return traffic flow
deny	any	any	any	any		block all else

CHAPTER 23 LEGAL AND ETHICAL ASPECTS

ANSWERS TO QUESTIONS

- 23.1** • **Computers as targets:** This form of crime targets a computer system, to acquire information stored on that computer system, to control the target system without authorization or payment (theft of service), or to alter the integrity of data or interfere with the availability of the computer or server. Using the terminology of Chapter 1, this form of crime involves an attack on data integrity, system integrity, data confidentiality, privacy, or availability.
- **Computers as storage devices:** Computers can be used to further unlawful activity by using a computer or a computer device as a passive storage medium. For example, the computer can be used to store stolen password lists, credit card or calling card numbers, proprietary corporate information, pornographic image files, or "warez" (pirated commercial software).
 - **Computers as communications tools:** Many of the crimes falling within this category are simply traditional crimes that are committed online. Examples include the illegal sale of prescription drugs, controlled substances, alcohol, and guns; fraud; gambling; and child pornography.
- 23.2** • **Real property:** Land and things permanently attached to the land, such as trees, buildings, and stationary mobile homes.
- **Personal property:** Personal effects, moveable property and goods, such as cars, bank accounts, wages, securities, a small business, furniture, insurance policies, jewelry, patents, pets, and season baseball tickets.
 - **Intellectual property:** Any intangible asset that consists of human knowledge and ideas. Examples include software, data, novels, sound recordings, the design of a new type of mousetrap, or a cure for a disease.
- 23.3** • **Copyrights:** Copyright law protects the tangible or fixed expression of an idea, not the idea itself.
- **Trademarks:** A trademark is a word, name, symbol, or device that is used in trade with goods to indicate the source of the goods and to distinguish them from the goods of others.
 - **Patents:** A patent for an invention is the grant of a property right to the inventor.
- 23.4** (1) The proposed work is original. (2) The creator has put this original idea into a concrete form, such as hard copy (paper), software, or multimedia form.
- 23.5** • **Reproduction right:** Lets the owner make copies of a work
- **Modification right:** Also known as the derivative-works right, concerns modifying a work to create a new or derivative work
 - **Distribution right:** Lets the owner publicly sell, rent, lease, or lend copies of the work.

- Public-performance right: Applies mainly to live performances
- Public-display right: Lets the owner publicly show a copy of the work directly or by means of a film, slide, or television image

23.6 The DMCA, signed into law in 1998, is designed to implement World Intellectual Property Organization (WIPO) treaties, signed in 1996. In essence, DMCA strengthens the protection of copyrighted materials in digital format.

23.7 Digital Rights Management (DRM) refers to systems and procedures that ensure that holders of digital rights are clearly identified and receive the stipulated payment for their works.

- 23.8**
- Content provider: Holds the digital rights of the content and wants to protect these rights. Examples are a music record label and a movie studio.
 - Distributor: Provides distribution channels, such as an online shop or a Web retailer. For example, an online distributor receives the digital content from the content provider and creates a Web catalog presenting the content and rights metadata for the content promotion.
 - Consumer: Uses the system to access the digital content by retrieving downloadable or streaming content through the distribution channel and then paying for the digital license. The player/ viewer application used by the consumer takes charge of initiating license request to the clearinghouse and enforcing the content usage rights.
 - Clearinghouse: Handles the financial transaction for issuing the digital license to the consumer and pays royalty fees to the content provider and distribution fees to the distributor accordingly. The clearinghouse is also responsible for logging license consumptions for every consumer.

- 23.9**
- Notice: Organizations must notify individuals what personal information they are collecting, the uses of that information, and what choices the individual may have.
 - Consent: Individuals must be able to choose whether and how their personal information is used by, or disclosed to, third parties. They have the right not to have any sensitive information collected or used without express permission, including race, religion, health, union membership, beliefs, and sex life.
 - Consistency: Organizations may use personal information only in accordance with the terms of the notice given the data subject and any choices with respect to its use exercised by the subject.
 - Access: Individuals must have the right and ability to access their information and correct, modify, or delete any portion of it.
 - Security: Organizations must provide adequate security, using technical and other means, to protect the integrity and confidentiality of personal information.
 - Onward transfer: Third parties receiving personal information must provide the same level of privacy protection as the organization from whom the information is obtained.
 - Enforcement: The Directive grants a private right of action to data subjects when organizations do not follow the law. In addition, each EU member has a regulatory enforcement agency concerned with privacy rights enforcement.

23.10 1. A code can serve two inspirational functions: as a positive stimulus for ethical conduct on the part of the professional, and to instill confidence in the

customer or user of an IS product or service. However, a code that stops at just providing inspirational language is likely to be vague and open to an abundance of interpretations.

2. A code can be educational. It informs professionals about what should be their commitment to undertake a certain level of quality of work and their responsibility for the well being of users of their product and the public, to the extent the product may affect nonusers. The code also serves to educate managers on their responsibility to encourage and support employee ethical behavior and on their own ethical responsibilities.
3. A code provides a measure of support for a professional whose decision to act ethically in a situation may create conflict with an employer or customer.
4. A code can be a means of deterrence and discipline. A professional society can use a code as a justification for revoking membership or even a professional license. An employee can use a code as a basis for a disciplinary action.
5. A code can enhance the profession's public image, if it is seen to be widely honored.

ANSWERS TO PROBLEMS

23.1 Article 2 Illegal access: This is a general threat the could fall into any of the three categories, depending on what use is made of the access.

Article 3 Illegal interception: Computer as target, attack on data confidentiality.

Article 4 Data interference: Computer as target, attack on data integrity.

Article 5 System interference: Computer as target, various attack types.

Article 6 Misuse of devices: Primarily computer as communications tool.

Article 7 Computer-related forgery: Computer as target, data integrity or privacy.

Article 8 Computer-related fraud: Computer as communications tool

Article 9 Offenses related to child pornography: Computer as communications tool.

Article 10 Infringements of copyright and related rights: Computer as communications tool.

Article 11 Attempt and aiding or abetting: Computer as communications tool.

23.2 Theft of intellectual property: Computer as target, attack on data confidentiality.

Theft of other (proprietary) info including customer records, financial records, etc.: Computer as target, attack on privacy.

Denial of service attacks: Computer as target, attack on availability.

Virus, worms or other malicious code: This is a general threat the could fall into any of the three categories, depending on what use is made of the attack.

Fraud (credit card fraud, etc.): Computer as communications tool.

Identity theft of customer: Computer as communications tool.

Illegal generation of spam e-mail. Computer as communications tool.

Phishing: Computer as target, attack on privacy.

Unauthorized access to/use of information, systems or networks: This is a general threat the could fall into any of the three categories, depending on what use is made of the attack.

Sabotage: deliberate disruption, deletion, or destruction of information, systems, or networks: Computer as target, attack on availability.

Extortion: Computer as communications tool.

Web site defacement: Computer as target, attack on data integrity.

Zombie machines on organization's network/bots/use of network by BotNets: Computer as communications tool.

Intentional exposure of private or sensitive information: Computer as target, attack on privacy.

Spyware (not including adware): Computer as communications tool.

- 23.3 There is no simple answer to this problem, as it depends on which survey is reviewed, given that the details do change from year to year and region to region. Any answer should note significant changes in the types of crime reported, and differences between the survey results and those shown in Table 23.2.
- 23.4 There is no single answer to this problem. However a web search on 'DeCSS' should be done. Two key current sites are the [Gallery of CSS Descramblers at CMU](#) and the [Wikipedia DeCSS page](#) which both provide many details and further links on the case. Given the very large number of items in the [Gallery of CSS Descramblers](#) it is fair to conclude that the MPAA failed to suppressing details of the DeCSS descrambling algorithm.
- 23.5 If a person purchases a track from the iTunes store, protected by Apple's FairPlay DRM, by an EMI artist, then the DRM component roles shown in Figure 23.3 in this case are: Content Provider is EMI, Distributor and Clearinghouse are both handled by the iTunes Store, and the Consumer is the person purchasing the track.
- 23.6 EU calls out the need for notice. This proactive measure is worthwhile. OECD mentions collection limitation, not explicitly called out in the EU list. Again, a worthwhile principle.
- 23.7 There is no simple answer to this problem, as it depends on the relevant organization's Privacy Policy. However any answer should consider all the principles listed in section 23.3, and should also refer to any relevant privacy legislation that applies to the chosen organization.
- 23.8 In this scenario, the administrator has very likely broken the law (though it depends on the jurisdiction applying), and breached company policy (provided they actually had one), even if for potentially altruistic reasons. The actions likely violated several of the potential ethical dilemmas listed in Table 23.3 including employee monitoring (in checking their passwords), hacking (in accessing the password files from other sections), and even internal privacy (knowing other user's passwords gives access to their data that you otherwise do not have authorization for). You might defend yourself by arguing that as a systems administrator you were authorized to access the password file. Unfortunately you are not the administrator for the section whose password file was cracked, and it will be difficult to argue that you had authority to do so. You would also have to argue that you had no intent to use that data to break any law, that your motives were not malicious and that they were in the interests of the organization and its employees. You might support these arguments by referring to item 2.5 (analysis of risks) in the ACM code, and item 7 (correct errors) in the IEEE code. The counter argument is that you failed to obey for example item 2.8 (authorized access) in the ACM code. Clearly the outcome would have been more satisfactory if the

administrator had raised the issue of password security with senior management, and been granted permission to conduct the survey of current password security in a manner consistent with the law and company policy.

23.9 Assume appropriate section and subsection numbering for AITP.

	ACM	IEEE	AITP
dignity and worth of people	1.2	8, 9	—
personal integrity	Section 2	2, 3, 4	2.1, 3.6
responsibility for work	Section 2	1	1.3
confidentiality of information	1.7, 1.8	—	3.1, 4.5
public safety, health, and welfare	1.1, 1.2	1	3.3
participation in professional societies	—	—	—
knowledge about technology related to social power.	2.7	5	4.8

- 23.10** a. EC1.2, EC2.2, and EC4.1 seem designed more to protect ACM's reputation than to focus on the professionals ethical responsibility and so can reasonably be excluded. EC 2.3 and EC 3.1 are not explicit in the 1997 Code and perhaps should be. They are covered implicitly however.
- b. In a number of areas, the 1997 Code is more detailed and more explicit, which provides better guidance to the professional. For example, the 1997 Code includes references to being aware of the legal responsibilities of professionals and managerial obligations.
- 23.11** a. I.3 refers to adequate compensation; this does not seem to be on target for an ethics code. II.b refers to disseminating information. Even though this is qualified with respect to legal and proprietary restraints, it seems better not to include this in the Code. II.e seems designed more for IEEE's benefit than the individual's. Section III, on responsibilities to employers and clients, is not explicit in the 2006 Code and perhaps should be.
- b. Nothing new in the 2006 Code not covered in the older Code.
- 23.12** a. ACM Code. The Software Engineering Code (SEC) specifically calls out responsibilities to client and employer. Perhaps ACM Code should as well. In general SEC is more detailed; this has the benefit of covering more ground in more detail but the disadvantage of discouraging professionals from reading the whole code.
- b. IEEE Code. SEC specifically calls out responsibilities to client and employer. SEC specifically addresses confidentiality. Both should probably be addressed in IEEE code.
- c. AITP Code. SEC refers to the quality of the products of the professional. AITP does not specifically call this out.