Linear Least Squares Filling square of sum of residuals $R^2 = \sum_{i} (y_i - y_{fit})^2$ in linear case $R^2 = \sum_{i} (y_i - (x_i + \beta))^2$ yields y_{fit} Maximum Likelihood Estimation L(x1, x2...xN) = [f(x: | param) likelihood function to obtain best param we maximize likelihood function of sparam = 0 or sparam = 0 In case of linear fit: $\mathcal{L} = \prod e^{-\chi^2/20^2} \text{ where } \chi_i^2 = (y_i - (\alpha x_i + \beta))^2$ $\ln \mathcal{L} = \left[\frac{\chi^2}{20^2} + \frac{1}{20^2} \right] = \frac{1}{20^2} \left[\frac{\chi^2}{20^2} + \frac{1}{20^2} + \frac{1}{20^2} \right] = \frac{1}{20^2} \left[\frac{\chi^2}{20^2} + \frac{1}{20^2} + \frac{1}{20^2} \right] = \frac{1}{20^2} \left[\frac{\chi^2}{20^2} + \frac{1}{20^2} + \frac{1}{20^2} \right] = \frac{1}{20^2} \left[\frac{\chi^2}{20^2} + \frac{1}{20^2} + \frac{1}{20^2} + \frac{1}{20^2} \right] = \frac{1}{20^2} \left[\frac{\chi^2}{20^2} + \frac{1}{20^2} + \frac{1}$ $\frac{\partial \ln(2)}{\partial \beta} = 0$ $-\frac{1}{2}(2) \stackrel{?}{\sim} (y_i - (\alpha x_i + \beta))(-1) = 0$ den(Z) =0 - = (2) = (yi - (0xi+B))(-xi)=0 $\xi \left(y_i - \left(x_i + \beta\right)\right) = 0$ Zyi- ~ Zxi-NB=0

multiphy eg I bu N teg 2 by Exi

N Zyixi - NXZxi2-NBZXi=O ZxiZyi-XZxiZxi-NBZxi=O $N \leq (x_i y_i) - N \propto \leq (x_i)^2 = \leq x_i \leq y_i - \alpha (\leq x_i)^2$ $\propto (\leq x_i)^2 - N \propto \leq (x_i)^2 = \leq x_i \leq y_i - N \leq x_i y_i$ $\alpha = \frac{\sum x_i \sum y_i - N \sum (x_i y_i)}{(\sum x_i)^2 - N \sum (x_i y_i)^2}$ divide topo bottom by N^2

for eg 2

Uncertainty on parameters

can analytically solve for linear least squares case.

$$\sigma_{\mathcal{K}} = \sqrt{\frac{1}{(n-2)}(R^2)} \qquad \sigma_{\mathcal{B}} = \sqrt{\frac{1}{n-2}} \frac{R^2}{(n+\frac{\chi^2}{\Sigma(x;\chi)^2})}$$

more generally MIE parameter uncertainties can be measured through determining the covariance matrix, which is the inverse of the Hessian matrix

$$H = \begin{pmatrix} \frac{\partial^2 u(\mathcal{L})}{\partial \alpha^2} & \frac{\partial^2 u(\mathcal{L})}{\partial \alpha \beta} \\ \frac{\partial^2 u(\mathcal{L})}{\partial \beta} & \frac{\partial^2 u(\mathcal{L})}{\partial \beta^2} \end{pmatrix} C = H^{-1}$$

Bayesian

"likelihood" ~ Z(DIM)

"posterior"

Prob of model

given data

V I data probability "
essentially normalization