

Calculus Made Easy

Beautiful Ideas Presented Simply

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Aug 2025 / Free Learner's School Conversations

Outline

Calculus
Made Easy

SPT, MG,
KM

Introduc-
tion

1 Introduction

Introducing Calculus Made Easy

Thompson's Treatise for Beginners

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Made Easy

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Introduc-
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- These Slides Are Based on **Silvanus Thompson's Book, Calculus Made Easy**, Which Introduces Calculus Simply.
- After Quite Some Deliberation, [KM] Chose This Book To Introduce Calculus to Rujuta, A High Schooler.
 - Great **Martin Gardner's Thoughtful Recommendation** Provided The Biggest Stimulus.
- We Also Go on '**Excursions**' Outside The Book.
- Each Chapter Is A Separate Slide-deck To Keep Its Size Manageable.
- It Is Supposed To Be Your "**Ready Reckoner**".
 - We're All Forgetful. Wouldn't It Be Nice If This Helps You in College or Beyond in **Bringing It All Back**?
- New Words Are Introduced Slowly And Carefully, But "**Thought Experiments**" Are Often Introduced.
 - Let's **Not Be Afraid to Take the Leap of Guided Imagination**.

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Assumptions

Because A Slide-deck Is Not as Fun as A Fairy Tale!

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- We Wish Mathematics Were Fun to Thinking People Who Enjoy Fairy Tales, Rap Music, or Memes.
 - Sadly, It Isn't!
- However, This Slide-deck Isn't So Great to Make It So!
- We Therefore Expect That:
 - You Want to Explore Calculus of Your Own Accord.
 - You Can Follow Logical (Deductive, Inductive) Arguments.
 - You've Heard of Natural, Rational, Irrational, Real, Complex Numbers.
 - You Understand How a Number Such as $\sqrt{2}$ Differs from a Number Such as 1.737465, 7, or $2 + 3i$.
 - You Understand The Language of School Algebra, And Can Solve Some 'Equations'. Learning Calculus before Algebra Isn't Helpful!
 - You Have Heard of 'Functions', And Know Some of Them (e.g. Polynomial, Rational, Logarithmic, Exponential, and Trigonometric).

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Have Fun!