$$\sin A \cos B = \frac{1}{2} \left[ \sin(A - B) + \sin(A + B) \right]$$
  
$$\sin A \sin B = \frac{1}{2} \left[ \sin(A - B) - \cos(A + B) \right]$$
  
$$\cos A \cos B = \frac{1}{2} \left[ \cos(A - B) + \cos(A + B) \right]$$