# Lecture 13 - Debugging ML Models and Error Analysis | Stanford CS229: Machine Learning (Autumn 2018)-Make Written Notes

**Notebook:** 100-Paper-Notes

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**Author:** mohammad.mohtashim76@gmail.com

#### **Debugging learning algorithms**

#### Motivating example:

- Anti-spam. You carefully choose a small set of 100 words to use as features. (Instead of using all 50000+ words in English.)
- Logistic regression with regularization (Bayesian Logistic regression), implemented with gradient ascent, gets 20% test error, which is unacceptably high.

$$\max_{\theta} \sum_{i=1}^{m} \log p(y^{(i)}|x^{(i)}, \theta) - \lambda ||\theta||^2$$

· What to do next?

#### Fixing the learning algorithm

· Logistic regression (with regularization):

$$\max_{\theta} \sum_{i=1}^{m} \log p(y^{(i)}|x^{(i)}, \theta) - \lambda ||\theta||^2$$

- Common approach: Try improving the algorithm in different ways.
  - Try getting more training examples.
  - Try a smaller set of features.
  - Try a larger set of features.
  - Try changing the features: Email header vs. email body features.
  - Run gradient descent for more iterations.
  - Try Newton's method.
  - Use a different value for λ.
  - Try using an SVM.

## Diagnostic for bias vs. variance

#### Better approach:

- Run diagnostics to figure out what the problem is.
- Fix whatever the problem is.

Logistic regression's test error is 20% (unacceptably high).

Suppose you suspect the problem is either:

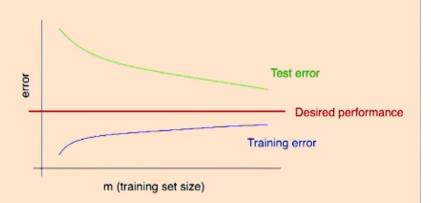
- Overfitting (high variance).
- Too few features to classify spam (high bias).

#### Diagnostic:

- Variance: Training error will be much lower than test error.
- Bias: Training error will also be high.

#### More on bias vs. variance

Typical learning curve for high variance:

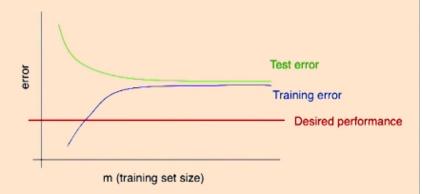


- Test error still decreasing as m increases. Suggests larger training set will help.
- · Large gap between training and test error.

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Typical learning curve for high bias:



- · Even training error is unacceptably high.
- · Small gap between training and test error.

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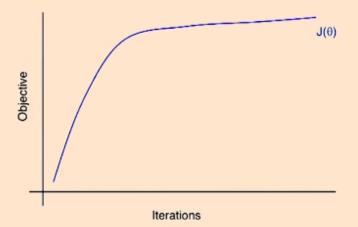
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## **Optimization algorithm diagnostics**

- Bias vs. variance is one common diagnostic.
- For other problems, it's usually up to your own ingenuity to construct your own diagnostics to figure out what's wrong.
- Another example:
  - Logistic regression gets 2% error on spam, and 2% error on non-spam.
    (Unacceptably high error on non-spam.)
  - SVM using a linear kernel gets 10% error on spam, and 0.01% error on nonspam. (Acceptable performance.)
  - But you want to use logistic regression, because of computational efficiency, etc.
- · What to do next?

## More diagnostics

- · Other common questions:
  - Is the algorithm (gradient ascent for logistic regression) converging?



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#### More diagnostics

- · Other common questions:
  - Is the algorithm (gradient ascent for logistic regression) converging?
  - Are you optimizing the right function?
  - I.e., what you care about:

$$a(\theta) = \sum_{i} w^{(i)} 1\{h_{\theta}(x^{(i)}) = y^{(i)}\}$$

(weights w<sup>(i)</sup> higher for non-spam than for spam).

Logistic regression? Correct value for λ?

$$\max_{\theta} J(\theta) = \sum_{i=1}^{m} \log p(y^{(i)}|x^{(i)}, \theta) - \lambda ||\theta||^2$$

- SVM? Correct value for C?

$$\begin{aligned} & \min_{w,b} & ||w||^2 + C \sum_{i=1}^m \xi_i \\ & \text{s.t.} & y^{(i)}(w^T x^{(i)} - b) \geq 1 - \xi_i \end{aligned}$$

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## Diagnostic

An SVM outperforms logistic regression, but you really want to deploy logistic regression for your application.

Let  $\theta_{SVM}$  be the parameters learned by an SVM.

Let  $\theta_{\text{BLR}}$  be the parameters learned by logistic regression. (BLR = Bayesian logistic regression.)

You care about weighted accuracy:

$$a(\theta) = \max_{\theta} \sum_i w^{(i)} \mathbf{1}\{h_{\theta}(x^{(i)}) = y^{(i)}\}$$

 $\theta_{SVM}$  outperforms  $\theta_{BLR}$ . So:

$$a(\theta_{SVM}) > a(\theta_{BLR})$$

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$$a(\theta_{SVM}) > a(\theta_{BLR})$$

BLR tries to maximize 
$$J(\theta) = \sum_{i=1}^m \log p(y^{(i)}|x^{(i)},\theta) - \lambda ||\theta||^2$$

Diagnostic:

$$J(\theta_{SVM}) > J(\theta_{BLR})$$
?

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Very Important-New Insight-Please See it Future Mohtashim

#### Two cases

Case 1: 
$$a(\theta_{\text{SVM}}) > a(\theta_{\text{BLR}})$$
  
 $J(\theta_{\text{SVM}}) > J(\theta_{\text{BLR}})$ 

But BLR was trying to maximize  $J(\theta)$ . This means that  $\theta_{BLR}$  fails to maximize J, and the problem is with the convergence of the algorithm. Problem is with optimization algorithm.

Case 2: 
$$a(\theta_{\text{SVM}}) > a(\theta_{\text{BLR}})$$
  
 $J(\theta_{\text{SVM}}) \leq J(\theta_{\text{BLR}})$ 

This means that BLR succeeded at maximizing  $J(\theta)$ . But the SVM, which does worse on  $J(\theta)$ , actually does better on weighted accuracy  $a(\theta)$ .

This means that  $J(\theta)$  is the wrong function to be maximizing, if you care about  $a(\theta)$ . Problem is with objective function of the maximization problem.

# The Stanford Autonomous Helicopter

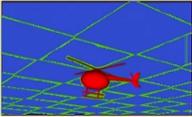
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Payload: 14 pounds Weight: 32 pounds

### Machine learning algorithm





Simulator

- Build a simulator of helicopter.
- 2. Choose a cost function. Say  $J(\theta) = IIx x_{desired}II^2$  (x = helicopter position)
- Run reinforcement learning (RL) algorithm to fly helicopter in simulation, so as to try to minimize cost function:

$$\theta_{RL} = arg min_{\theta} J(\theta)$$

Suppose you do this, and the resulting controller parameters  $\theta_{\text{RL}}$  gives much worse performance than your human pilot. What to do next?

Improve simulator? Modify cost function J? Modify RL algorithm? Stanfo

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#### Debugging an RL algorithm

The controller given by  $\theta_{RL}$  performs poorly.

#### Suppose that:

- The helicopter simulator is accurate.
- 2. The RL algorithm correctly controls the helicopter (in simulation) so as to minimize  $J(\theta)$ .
- Minimizing J(θ) corresponds to correct autonomous flight.

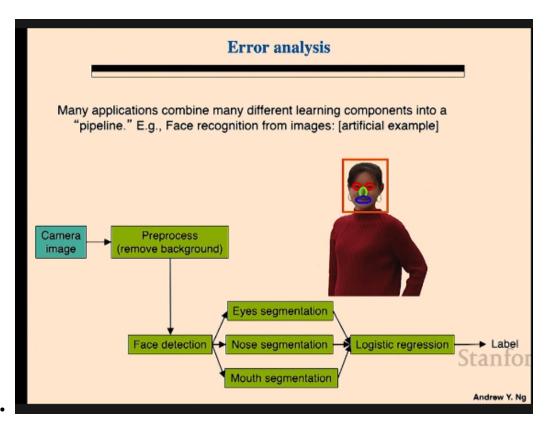
Then: The learned parameters  $\theta_{\text{RL}}$  should fly well on the actual helicopter.

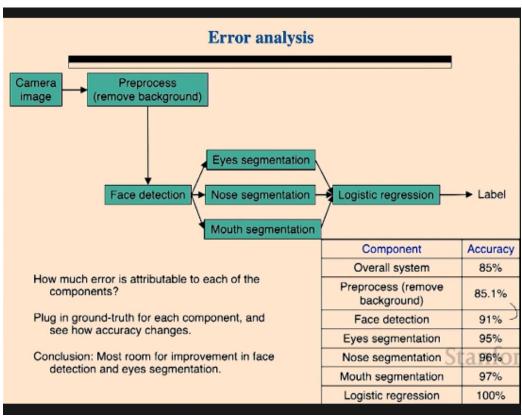
#### Diagnostics:≥

- If θ<sub>RL</sub> flies well in simulation, but not in real life, then the problem is in the simulator. Otherwise:
- 2. Let  $\theta_{\text{human}}$  be the human control policy. If  $J(\theta_{\text{human}}) < J(\theta_{\text{RL}})$ , then the problem is in the reinforcement learning algorithm. (Failing to minimize the cost function J.)
- If J(θ<sub>human</sub>) ≥ J(θ<sub>RL</sub>), then the problem is in the cost function. (Maximizing it doesn't correspond to good autonomous flight.)

Andrew V No

- Remember two things:
  - Bias/Variance Trade-off
  - Analyse whether the problem is in algorithm or objective that you are trying to achieve





## Ablative analysis

Simple logistic regression without any clever features get 94% performance.

Just what accounts for your improvement from 94 to 99.9%?

Ablative analysis: Remove components from your system one at a time, to see how it breaks.

Component	Accuracy
Overall system	99.9%
Spelling correction	99.0
Sender host features	98.9%
Email header features	98.9%
Email text parser features	95%
Javascript parser	94.5%
Features from images	94.0%

[baseline]

Conclusion: The email text parser features account for most of the improvement.

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