

(1a) Which locations grow both the beans "Catuai" and "Catimor"?

$$\pi_{FL}(\sigma_{BN='Catuai'}(BEAN)) \cap (\pi_{FL}(\sigma_{BN='Catimor'}(BEAN)))$$

(1b) Which people drink a coffee that contains a bean from "Brazil" or from "Peru"?

$$\pi_P(\sigma_{(FL='Brazil' \text{ or } FL='Peru')}(BEAN * HAS_BEAN * DRINKS))$$

(1c) Which countries produce all the beans in the coffee "Breakfast Delight" (or "BD")?

$$R \leftarrow \pi_{FL,BN}(BEAN)$$
$$S \leftarrow \pi_{BN}(\sigma_{C='BD'}(HAS_BEAN))$$

we have two relations R and S with attributes respectively A and B, their division can be defined as : for a better understanding refer- (<https://users.abo.fi/soini/divisionEnglish.pdf>)

where $R \div S = \pi_{A-B}(R) - \pi_{A-B}((\pi_{A-B}(R) \times S) - R)$

in our case which is $= \pi_{FL}(R) - \pi_{FL}((\pi_{FL}(R) \times S) - R)$

(2a) Which locations contribute a bean to a coffee consumed by "Chris"?

$$\{b.FROM_LOCATION \mid BEAN(b) \wedge \exists(h,d) (HAS_BEAN(h) \wedge DRINKS(d) \wedge d.COFFEE=h.COFFEE \wedge h.BEAN_NAME=b.BEAN_NAME \wedge d.PERSON='Chris')\}$$

(2b) Which people don't drink any of the coffees that are consumed by "Chris"?

$$\{d.PERSON \mid DRINKS(d) \wedge \forall(d1)((DRINKS(d1) \wedge d.PERSON=d1.PERSON) \Rightarrow \neg \exists d2(DRINKS(d2) \wedge d2.PERSON='Chris' \wedge d2.COFFEE=d1.COFFEE))\}$$

(2c) Which people drink a set of coffees that together contain all the beans from "Hawaii"?

$$\{d.PERSON \mid DRINKS(d) \wedge \forall(b) ((BEAN(b) \wedge b.FROM_LOCATION = "Hawaii") \Rightarrow \exists(d1,h)(DRINKS(d1) \wedge HAS_BEAN(h) \wedge h.COFFEE=d1.COFFEE \wedge d1.PERSON=d.PERSON \wedge h.BEAN_NAME=b.BEAN_NAME))\}$$