



Vulnerability Detection - Symbolic Execution

Holistic Software Security

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Why is fuzzing inadequate?

- Generating highly constrained inputs could take long time!

```
void test_me(int x) {  
    if (x == 94389) {  
        ERROR;  
    }  
}
```

Probability of generating input that triggers **ERROR**:

$$1/2^{32} \approx 0.000000023\%$$



Symbolic Execution (SymEx)

- A technique to explore a program systematically:
 - Symbolically execute all the paths in the program.
 - At each path check for possible error conditions.



Symbolic Execution (SymEx)

- Use symbolic values for inputs
- Execute program symbolically on symbolic input values:
 - Collect symbolic path constraints
- Use constraint solver to check if a path is feasible or to generate concrete inputs.
- **Unlike classic static analysis, symbolic execution:**
 - **Enables us to generate concrete inputs.**
 - **Can made to only explore feasible paths (states).**

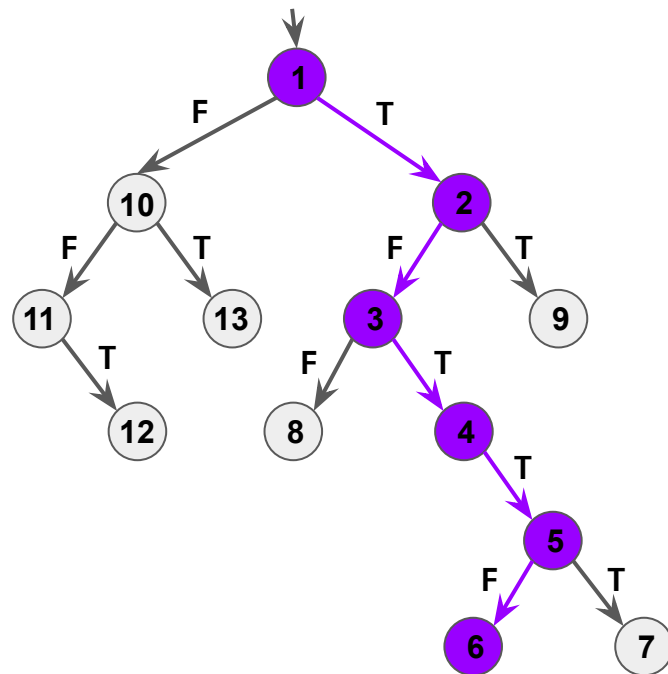


SymEx Impact

We also used KLEE as a bug finding tool, applying it to 452 applications (over 430K total lines of code), where it found 56 serious bugs, including three in COREUTILS that had been missed for over 15 years. Finally, we used KLEE to cross-check purportedly identical BUSYBOX and COREUTILS utilities, finding functional correctness errors and a myriad of inconsistencies.

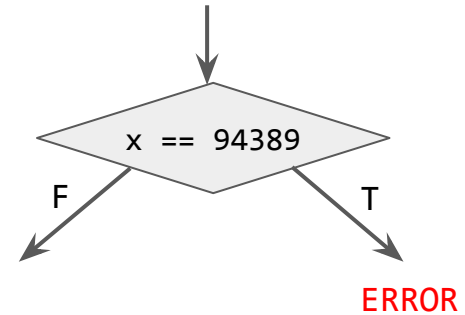
Execution Paths

- A path in the control flow graph (CFG) of a function.
- Edge represents a condition being taken.
- How many paths does a program with loops has?



Execution Paths: Example

```
void test_me(int x) {  
    if (x == 94389) {  
        ERROR;  
    }  
}
```



Symbolic Execution: Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```

Symbolic
State

Path
Condition


Symbolic Execution

Path1

$x = x_0$

$y = y_0$

Symbolic Execution: Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)   
        if (x > y+10)  
            ERROR;  
}
```

Symbolic
State



Path
Condition

Symbolic Execution

Path1

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

Symbolic Execution: Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  Path2  
            ERROR;  
    }  Path1  
}
```

Symbolic
State

Path
Condition

Symbolic Execution

Path1

$x = x_0$
 $y = y_0$
 $z = 2*y_0$


$2*y_0 \neq x_0$

Path2

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

Symbolic Execution: Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  Path2  
            ERROR;  
}
```

Symbolic
State

Path
Condition

Symbolic Execution

Path1

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 \neq x_0$

END

Path2

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

Symbolic Execution: Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
    }  
}
```

Path2 points to the closing brace of the inner if statement.

Path3 points to the ERROR statement.

Symbolic
State

Path
Condition

Symbolic Execution

Path1

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 \neq x_0$

END

Path2

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

$x_0 \leq y_0 + 10$

Path3

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

$x_0 > y_0 + 10$

Symbolic Execution: Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR; ← Path3  
}
```

Symbolic
State

Path
Condition

Symbolic Execution

Path1

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 \neq x_0$

END

Path2

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

$x_0 \leq y_0 + 10$

END

Path3

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

$x_0 > y_0 + 10$

ERROR

Symbolic Execution: Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```

Symbolic
State

Path
Condition

Solve: $(2*y_0 == x_0)$ and $(x_0 > y_0+10)$

Input causing error: $x_0 = 30, y_0 = 15$

Symbolic Execution

Path1

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 != x_0$

END

Path2

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

$x_0 \leq y_0 + 10$

END

Path3

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

$2*y_0 == x_0$

$x_0 > y_0 + 10$

ERROR



Symbolic Execution: Drawbacks

- Loops => Infinite paths.
- Can explore **infeasible** paths.
- Bugs should be converted into asserts.
- Does not scale for real-world programs.

```
void test_me(int x) {  
    // c = product of two  
    // large primes  
    if (pow(2,x) % c == 17) {  
        print("something bad");  
        ERROR;  
    } else  
        print("OK");  
}
```

Symbolic execution will say
both branches are reachable:
False Positive!



Symbolic Execution: Practical problems

- Memory model.

```
// Consider i and j as symbolic  
arr[i]++;  
arr[j] = arr[j] + 1;
```

Which memory cell to update?

- Symbolically sized memory.

```
// Consider i as symbolic  
p = malloc(i*sizeof(int));
```

What should be the size of p?

- External or Library functions.

```
// Consider argv[1] as symbolic  
j = atoi(argv[1]);
```

We do not have source code of library. How should we handle passing arguments?



Dynamic Symbolic Execution (DSE)

- Random testing or fuzzing cannot generate highly constraint inputs.
- Can we use symbolic execution to generate these constrained inputs?
- Also called Concolic execution.



DSE Approach

1. Start with random input values.
2. Keep track of both concrete values and symbolic constraints.
3. Use concrete values to simplify symbolic constraints.

DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 22
y = 7


Symbolic
Execution

symbolic
state

x = x_0
y = y_0

path
condition

DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)   
        if (x > y+10)  
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 22
y = 7
z = 14

Symbolic
Execution

symbolic
state


$x = x_0$
 $y = y_0$
 $z = 2*y_0$

path
condition



DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



Concrete
Execution

concrete
state

x = 22
y = 7
z = 14

Symbolic
Execution

symbolic
state

x = x_θ
y = y_θ
z = $2*y_\theta$

path
condition

$2*y_\theta \neq x_\theta$

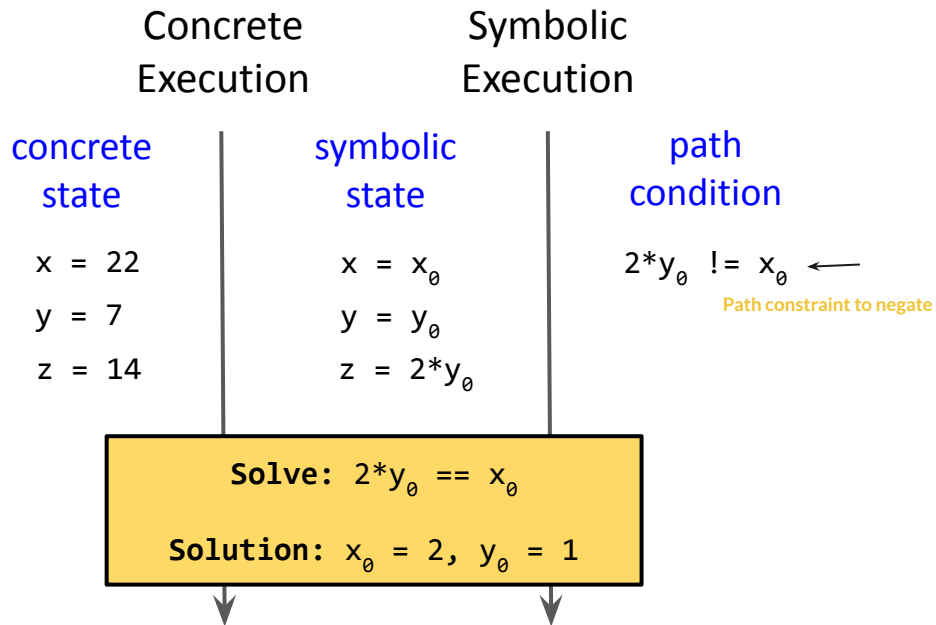



DSE Example

Now to generate new input => **Negate** the path condition and **solve** to get inputs that will make the program execute another path.

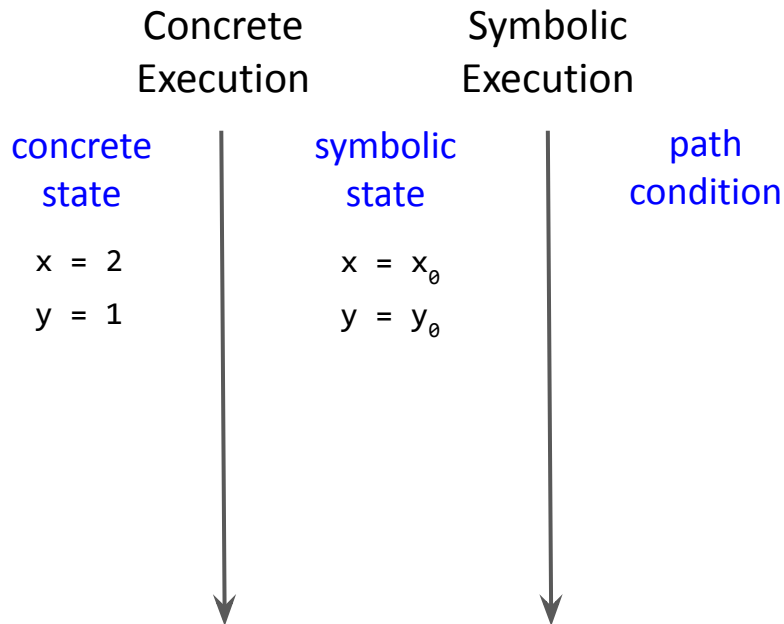
DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```




DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)   
        if (x > y+10)  
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 2
y = 1
z = 2


Symbolic
Execution

symbolic
state

x = x_θ
y = y_θ
z = $2*y_\theta$

path
condition

DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)   
            ERROR;  
}
```

Concrete
Execution

concrete
state

$x = 2$
 $y = 1$
 $z = 2$

Symbolic
Execution

symbolic
state


$x = x_\theta$
 $y = y_\theta$
 $z = 2*y_\theta$

path
condition

$2*y_\theta == x_\theta$

DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



Concrete
Execution

concrete
state

$x = 2$
 $y = 1$
 $z = 2$

Symbolic
Execution

symbolic
state

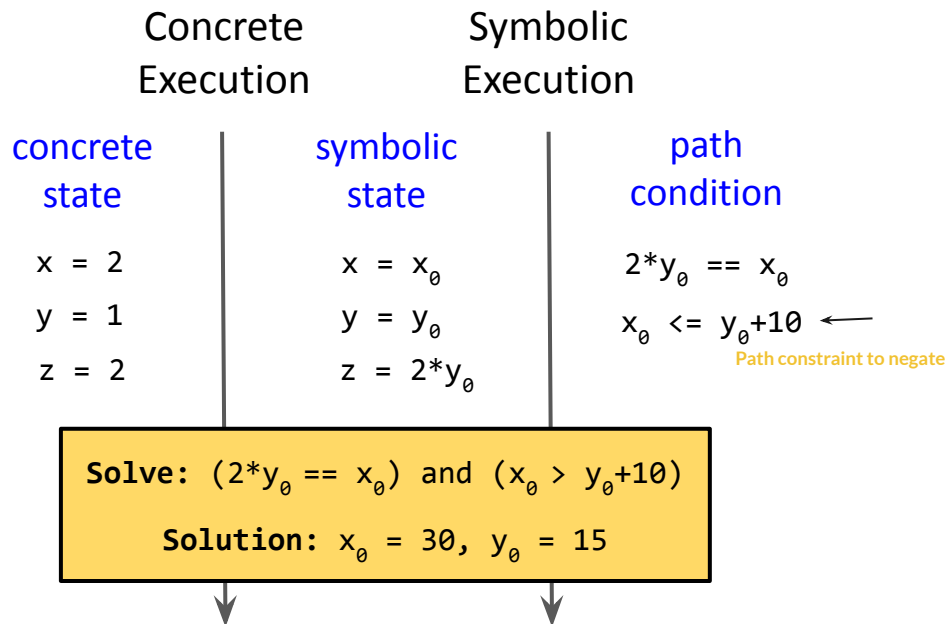

$x = x_\theta$
 $y = y_\theta$
 $z = 2*y_\theta$

path
condition

$2*y_\theta == x_\theta$
 $x_\theta \leq y_\theta + 10$

DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



Concrete
Execution

concrete
state

x = 30
y = 15

Symbolic
Execution


symbolic
state

x = x_0
y = y_0

path
condition



DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)   
        if (x > y+10)  
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 30
y = 15
z = 30

Symbolic
Execution


symbolic
state

x = x_0
y = y_0
z = $2*y_0$

path
condition



DSE Example

```
int foo(int v) {  
    return 2*v;  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)    
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 30
y = 15
z = 30

Symbolic
Execution

symbolic
state

x = x_θ
y = y_θ
z = $2*y_\theta$

path
condition

$2*y_\theta == x_\theta$

DSE Example

```
int foo(int v) {  
    return 2*v;  
}
```

```
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



Concrete
Execution

concrete
state

$x = 30$
 $y = 15$
 $z = 30$

Symbolic
Execution

symbolic
state

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

path
condition

$2*y_0 == x_0$
 $x_0 > y_0 + 10$

DSE Example

```
int foo(int v) {  
    return 2*v;  
}
```

```
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



Concrete
Execution

concrete
state

$x = 30$
 $y = 15$
 $z = 30$

Symbolic
Execution

symbolic
state

$x = x_0$
 $y = y_0$
 $z = 2*y_0$

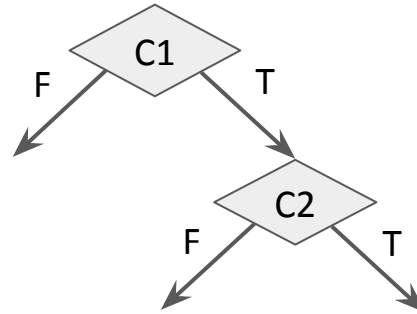
path
condition

$2*y_0 == x_0$
 $x_0 > y_0 + 10$

DSE Constraints

Which of the following constraints DSE might possibly solve in exploring the computation tree shown below:

- | | |
|------------------------------------|---|
| <input type="checkbox"/> $C1$ | <input type="checkbox"/> $C1 \wedge C2$ |
| <input type="checkbox"/> $C2$ | <input type="checkbox"/> $C1 \wedge \neg C2$ |
| <input type="checkbox"/> $\neg C1$ | <input type="checkbox"/> $\neg C1 \wedge C2$ |
| <input type="checkbox"/> $\neg C2$ | <input type="checkbox"/> $\neg C1 \wedge \neg C2$ |



DSE Constraints

Which of the following constraints DSE might possibly solve in exploring the computation tree shown below:



C1



$C1 \wedge C2$



C2



$C1 \wedge \neg C2$



$\neg C1$



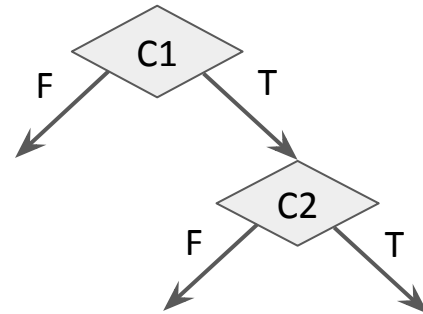
$\neg C1 \wedge C2$



$\neg C2$



$\neg C1 \wedge \neg C2$






Symbolic Execution

path
condition

$$\begin{aligned}x &= x_\theta \\ y &= y_\theta\end{aligned}$$

DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)   
        if (x > y+10)  
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 22
y = 7
z = 601...129

Symbolic
Execution

symbolic
state

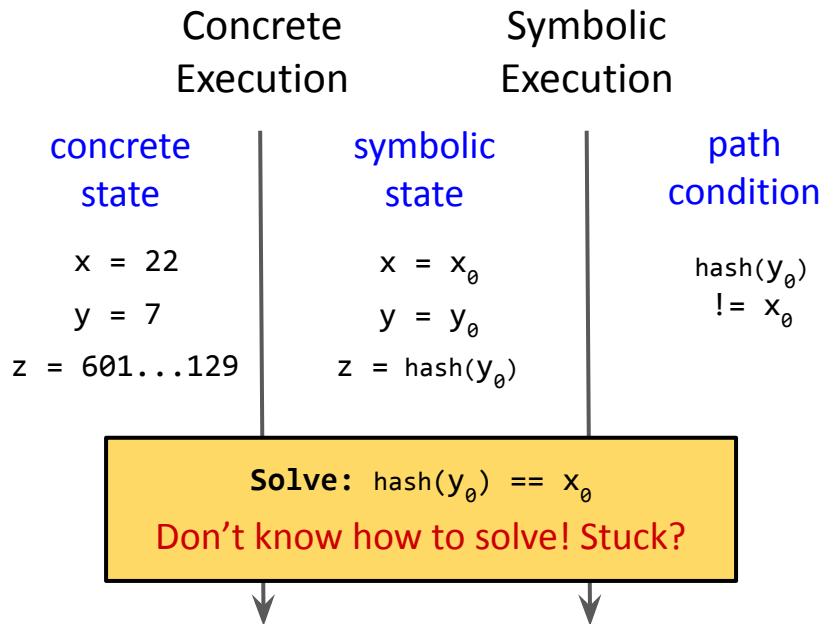

x = x_θ
y = y_θ
z = hash(y_θ)

path
condition



DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}
```

```
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```

ERROR;

Not stuck! Use
concrete state: replace
 y_θ by 7

Concrete
Execution

concrete
state

$x = 22$
 $y = 7$
 $z = 601\dots129$

Symbolic
Execution

symbolic
state

$x = x_\theta$
 $y = y_\theta$
 $z = \text{hash}(y_\theta)$

path
condition

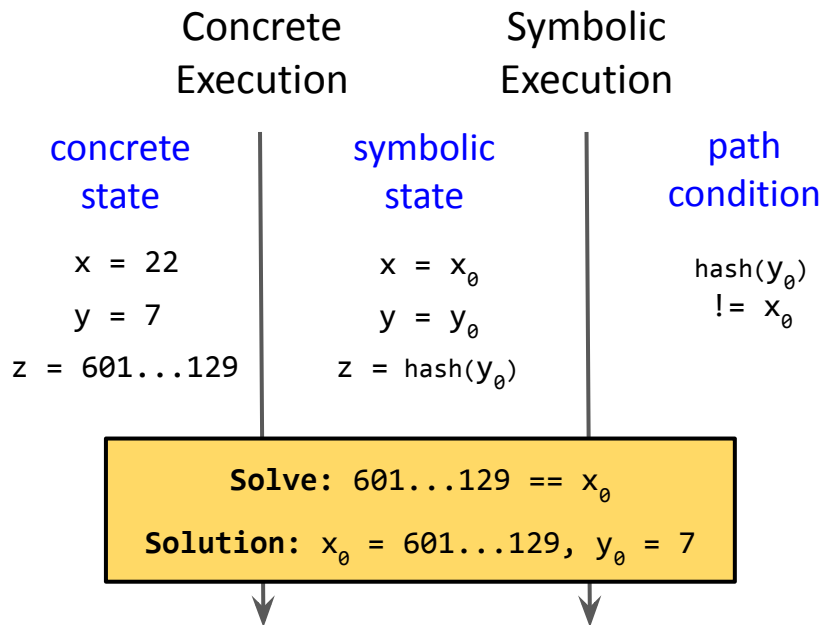

$\text{hash}(y_\theta) \neq x_\theta$

Solve: $\text{hash}(y_\theta) == x_\theta$

Don't know how to solve! Stuck?

DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



Concrete
Execution

concrete
state

$x = 601 \dots 129$
 $y = 7$

Symbolic
Execution


symbolic
state

$x = x_0$
 $y = y_0$

path
condition



DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)   
        if (x > y+10)  
            ERROR;  
}
```

Concrete
Execution

concrete
state

$x = 601 \dots 129$
 $y = 7$
 $z = 601 \dots 129$

Symbolic
Execution


symbolic
state

$x = x_\theta$
 $y = y_\theta$
 $z = \text{hash}(y_\theta)$

path
condition



DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}  
  
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)   
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 601...129
y = 7
z = 601...129

Symbolic
Execution

symbolic
state

x = x_θ
y = y_θ
z = hash(y_θ)

path
condition

hash(y_θ)
== x_θ

DSE Example 2

```
int foo(int v) {  
    return hash(v);  
}
```

```
void test_me(int x, int y) {  
    int z = foo(y);  
    if (z == x)  
        if (x > y+10)  
            ERROR;  
}
```



Concrete
Execution

concrete
state

$x = 601 \dots 129$
 $y = 7$
 $z = 601 \dots 129$

Symbolic
Execution

symbolic
state

$x = x_\theta$
 $y = y_\theta$
 $z = \text{hash}(y_\theta)$

path
condition


$\text{hash}(y_\theta)$
 $= x_\theta$
 $x_\theta > y_\theta + 10$



DSE Example 3

We may not be able to generate inputs for all the paths.

DSE Example 3

```
int foo(int v) {  
    return secure_hash(v);  
}  
  
void test_me(int x, int y) {  
    if (x != y)   
        if (foo(x) == foo(y))  
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 22
y = 7


Symbolic
Execution

symbolic
state

x = x_0
y = y_0

path
condition

DSE Example 3

```
int foo(int v) {  
    return secure_hash(v);  
}  
  
void test_me(int x, int y) {  
    if (x != y)   
        if (foo(x) == foo(y))  
            ERROR;  
}
```

Concrete
Execution

concrete
state

x = 22
y = 7

Symbolic
Execution

symbolic
state

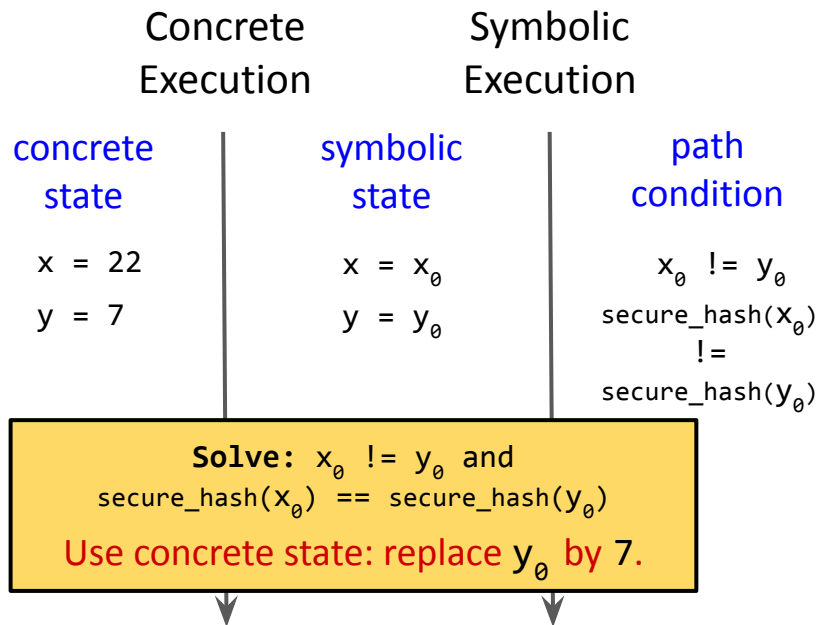
x = x_0
y = y_0

path
condition

$x_0 \neq y_0$

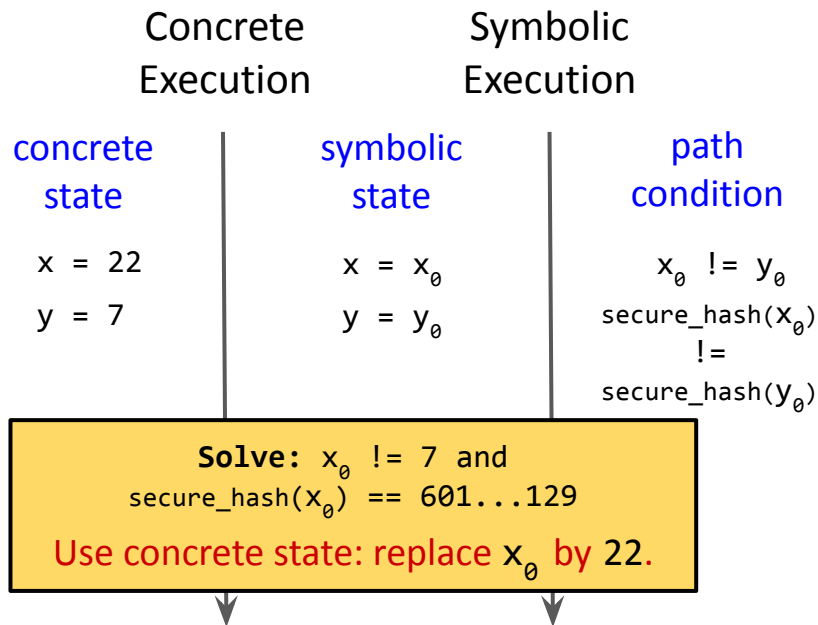
DSE Example 3

```
int foo(int v) {  
    return secure_hash(v);  
}  
  
void test_me(int x, int y) {  
    if (x != y)  
        if (foo(x) == foo(y))  
            ERROR;  
} ←
```



DSE Example 3

```
int foo(int v) {  
    return secure_hash(v);  
}  
  
void test_me(int x, int y) {  
    if (x != y)  
        if (foo(x) == foo(y))  
            ERROR;  
} ←
```



DSE Example 3

```
int foo(int v) {  
    return secure_hash(v);  
}  
  
void test_me(int x, int y) {  
    if (x != y)  
        if (foo(x) == foo(y))  
            ERROR;  
} ←
```

False negative!

Concrete
Execution

concrete
state

$x = 22$
 $y = 7$

Symbolic
Execution

symbolic
state

$x = x_0$
 $y = y_0$

path
condition

$x_0 \neq y_0$
 $\text{secure_hash}(x_0)$
 \neq
 $\text{secure_hash}(y_0)$

Solve: $22 \neq 7$ and
 $438\dots861 == 601\dots129$

Unsatisfiable!



DSE v/s SymEx

- Similar to SymEx, DSE may not terminate.
- Unlike SymEx:
 - DSE has false negatives, i.e., might not be able to execute all paths.
 - DSE will always generate concrete inputs.



SymEx/DSE tools

- KLEE: LLVM (C family of languages)
- PEX: .NET Framework
- JavaPathFinder: Java
- jCUTE: Java
- Jalangi: Javascript
- SAGE and S2E: binaries (x86, ARM, ...)



SymEx based Vulnerability Detection

- **ucklee:** Under constrained symbolic execution.
 - Symbolically execute arbitrary functions.

user input. We evaluate the checkers on over 20,000 functions from BIND, OpenSSL, and the Linux kernel, find 67 bugs, and verify that hundreds of functions are leak free and that thousands of functions do not access uninitialized data.



SymEx based Vulnerability Detection

- SAGE = Scalable Automated Guided Execution
- Found many expensive security bugs in many Microsoft applications (Windows, Office, etc.)
- Used daily in various Microsoft groups, runs continuously in the cloud
- What makes it so useful?
 - Works on large applications => finds bugs across components
 - Focus on input file fuzzing => fully automated
 - Works on x86 binaries => easy to deploy (not dependent upon programming language or build process)
 - Target-Driven Compositional Concolic Testing

SAGE Crashing a media parser!

```
00000000h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000010h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000020h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000030h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000040h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000050h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000060h: 00 00 00 00                                ; ....
```

```
00000000h: 52 49 46 46 00 00 00 00 ** ** 20 00 00 00 00 ; RIFF...***....
00000010h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000020h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000030h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000040h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000050h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000060h: 00 00 00 00                                ; ....
```

```
00000000h: 52 49 46 46 00 00 00 00 00 00 00 00 00 00 00 00 ; RIFF.....
00000010h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000020h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000030h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000040h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000050h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000060h: 00 00 00 00                                ; ....
```

... after a few more iterations:

```
00000000h: 52 49 46 46 3D 00 00 00 ** ** ** 20 00 00 00 00 ; RIFF=...***....
00000010h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000020h: 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 ; .....
00000030h: 00 00 00 00 73 74 72 68 00 00 00 00 76 69 64 73 ; ...strh...vids
00000040h: 00 00 00 00 73 74 72 66 B2 75 76 3A 28 00 00 00 ; ...strf^uv:(...
00000050h: 00 00 00 00 00 00 00 00 00 00 00 00 01 00 00 00 ; .....
00000060h: 00 00 00 00                                ; ....
```



Using SymEx/DSE

- *Blindly using symbolic execution is inefficient and does not scale well for real programs.*
- Lot of massaging happens before using symex on real-programs:
 - <https://adalogics.com/blog/symbolic-execution-with-klee>
- Using symex smartly is an art, Examples:
 - Force symex to execute certain interesting paths:
 - BootStomp: On the Security of Bootloaders in Mobile Devices (USENIX 2017).
 - Try to concolically execute individual functions:
 - Target-Driven Compositional Concolic Testing (FSE 2019).
 - Execute only interesting parts of a program:
 - Chopped Symbolic Execution (ICSE 2018).



SymEx/DSE Trends

- May works use symex/DSE as an auxiliary technique:
 - Driller/Vuzzer: Uses concolic execution to assist fuzzer.
 - Sys: Filter out false positives.
- Applying SymEx to different domains:
 - Symbolic execution of smart contracts.
 - Symbolic execution of RTL code.
- Making SymEx/DSE fast:
 - Qsym: A Practical Concolic Execution Engine Tailored for Hybrid Fuzzing
 - SymCC: Compiling concolic execution engine into the program.
 - Neuro Symbolic Execution: Augmenting symbolic execution with neural nets.



SymEx/DSE Final Remarks!

- Symbolic execution is a powerful technique, which is impractical and cannot work for large real-world programs.
- However, we can be smart and use it opportunistically.