

Heat transfer

Equation of heat conduction

In Cartesian co-ordinates,

$$\nabla^2 T + \frac{\dot{q}}{k} = \frac{1}{\alpha} \frac{dT}{dt}$$

where,

∇ = Laplace operator

\dot{q} = Heat generation per unit volume

α = Thermal diffusivity

- *Steady state condition:* $\nabla^2 T + \frac{\dot{q}}{k} = 0$ - Poisson equation
- *No heat sources:* $\dot{q} = 0$ - Diffusion equation
- *No heat source and steady state:* $\dot{q} = 0$ and $\frac{dT}{dt} = 0$ - Laplace equation

In cylindrical co-ordinates,

$$\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial T}{\partial r} \right) + \frac{\dot{q}}{k} = \frac{1}{\alpha} \frac{dT}{dt}$$

In spherical co-ordinates,

$$\frac{\partial^2 T}{\partial r^2} + \frac{2}{r} \frac{\partial T}{\partial r} + \frac{1}{r^2 \sin \psi} \frac{\partial}{\partial \psi} \left(\sin \psi \frac{\partial T}{\partial \psi} \right) + \frac{1}{r^2 \sin \psi} \frac{\partial}{\partial \phi} \left(\frac{\partial^2 T}{\partial \phi} \right) + \frac{\dot{q}}{k} = \frac{1}{\alpha} \frac{dT}{dt}$$

If temperature variation is only in radial direction, then for steady state conditions with no heat generations, conduction equation becomes,

$$\frac{\partial^2 T}{\partial r^2} + \frac{2}{r} \frac{\partial T}{\partial r} = 0 \Rightarrow \frac{\partial}{\partial r} \left(r^2 \frac{\partial T}{\partial r} \right) = 0$$

Boiling

Nucleate boiling: $q_s = \mu_l h_{fg} (g \sigma^{-1} (\rho_l - \rho_v))^{\frac{1}{2}} \left(\left(\frac{C_{pl}}{C_{sg}} \right) \frac{\Delta T_e}{h_{fg} Pr^{1.7}} \right)^3$

Critical heat flux / Burnout point / Boiling crisis: $q_s = 0.18 h_{fg} (g \sigma (\rho_l - \rho_v) \rho_v^2)^{\frac{1}{4}}$