Assignment 1

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Download all python codes from

https://github.com/keerthi/Matrix-theory/codes

and latex-tikz codes from

https://github.com/keerthi/Matrix-theory

1 Question No. 2.3

Draw $\triangle ABC$ in which $\angle B = 45^{\circ}, \angle C = 45^{\circ}$ and a + b + c = 11

2 EXPLANATION

Given,

$$\angle C = 45^{\circ}, \angle B = 45^{\circ}, \text{ and } a + b + c = 11$$
 (2.0.1)

By using Sin Rule:

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c} \tag{2.0.2}$$

$$\implies b \sin C = c \sin B \tag{2.0.3}$$

$$b\sin 45 = c\sin 45 \tag{2.0.4}$$

$$\implies b = c \tag{2.0.5}$$

$$a\sin B = b\sin A \tag{2.0.6}$$

$$a\sin 45 = b\sin 90 \tag{2.0.7}$$

$$\implies a = \sqrt{2}b$$
 (2.0.8)

Then, AX=B which can be expressed as the matrix equation

$$\begin{pmatrix} 0 & 1 & -1 \\ 1 & -\sqrt{2} & 0 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 11 \end{pmatrix}$$
 (2.0.9)

(2.0.9) by solving, we get values like,

$$\implies a = 26.546;$$
 (2.0.10)

$$\implies b = 18.77;$$
 (2.0.11)

$$\implies c = 18.77$$
 (2.0.12)

The Vertices of $\triangle ABC$ are

$$\mathbf{A} = \begin{pmatrix} 0 \\ c \end{pmatrix} = \begin{pmatrix} 0 \\ 18.7 \end{pmatrix} \tag{2.0.13}$$

$$\mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{2.0.14}$$

$$\mathbf{C} = \begin{pmatrix} a \\ 0 \end{pmatrix} = \begin{pmatrix} 26.5 \\ 0 \end{pmatrix} \tag{2.0.15}$$

Plot the $\triangle ABC$ is as follows:

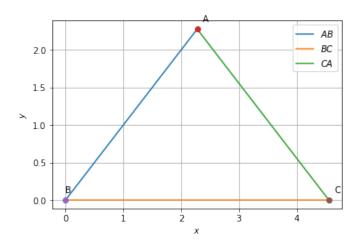


Fig. 0: *△ABC*