

LOA

(1)

- Macro programming
Computer has got internal bus (ib).

Registers $\rightarrow A, B, C, D, PC, (S, T)$ $\xrightarrow{\text{Program Counter}}$

We can put data from register to internal bus and vice-versa. \leftarrow carrying out arithmetic operations

ALU - Arithmetic Logic Unit

S & t are special registers

S and t can take value of ib
but ib cannot

Gates

and (\cdot) , or (+)

$$5a + 7b \geq 3$$

$$a=1 \text{ or } b=1$$

$$8a + 3b \geq 10$$

$$8a + 3b \geq 5$$

$$3a + 7b + 2c \geq 8$$

$$7a + 4b + 3c \geq 6$$

$$7a + 4b + 3c + 2d \geq 26$$

$$3a + 7b + 2c + 2d \geq 8$$

$$7a + 4b + 3c + 2d + 2e \geq 26$$

not (')

$$5a - 7b \geq -4 \quad a=1 \text{ or } a=0 \text{ and } b=0 \quad a+b'$$

$$7a + 4b - 3c + 2d \geq 23 \quad d=1 \text{ and } (a+b.c') \\ 7a + 4b - 3c \geq 3 \quad d \cdot (a+b.c')$$

$$\begin{aligned} & \cdot a+b' \cdot c \text{ write inequality} \\ & \rightarrow 2a+c-b \geq 0 \\ & \cdot a \cdot b + c \cdot d \\ & ab + cd \geq 1 \\ & (a+b) \quad a \cdot b \\ & a \cdot b \\ & b \cdot (a+c) \\ & a+b \cdot c \\ & d \cdot (a+b \cdot c) \\ & d + b \cdot (a+c) \\ & e = 0 \quad d \cdot (a+b \cdot c) \quad \text{or} \quad e = 1 \\ & d \cdot (a+b \cdot c) + e \cdot (a+b+d) \\ & (K+K')g = K+g \end{aligned}$$

$$abcd > pqqr$$

$$a=1 \text{ and } p=0 \rightarrow a \cdot p'$$

$$a=1 \text{ and } p=1 , \\ a=0 \text{ and } p=0$$

$$(a \cdot p + a' \cdot p') \cdot b \cdot q' + a \cdot p' \rightarrow ab > pq$$

$$ab > pq \rightarrow a > p \text{ or } a = p \text{ and } b > q$$

$$ab > pq \rightarrow a > p \text{ or } a = p \text{ and } b > q, \\ a \cdot p' + (a+p') \cdot b \cdot q'$$

$a >= p$ when $a < p$ is false

$$(a' \cdot p)' = a + p'$$

$$abc > pqqr$$

$$ab > pq \text{ or } \begin{array}{l} ab = pq \text{ and } c > r \\ a = p \text{ and } b = q \end{array}$$

$$\left\{ \begin{array}{l} a \cdot p' + (a+p') \cdot b \cdot q' + (a \cdot p + a' \cdot p) \cdot (b' \cdot q' + b \cdot q) \cdot c \cdot r' \\ a \cdot p' + (a+p') \cdot [b \cdot q' + \cancel{a \cdot b \cdot q'} + (b' \cdot q' + b \cdot q') \cdot c \cdot r'] \end{array} \right.$$

$ab >= pq$ when $ab < pq$ is false

$$(p \cdot a' + (p+a') \cdot q \cdot b')'$$

$$= (a+p') \cdot (b+q' + p' \cdot \cancel{q}) \cdot c \cdot r'$$

$$\left. \begin{array}{l} a \cdot p' + (a+p') \cdot [(b+q' + p') \cdot c \cdot r' + b \cdot q'] \\ = a \cdot p' + (a+p') \cdot [(b+q') \cdot c \cdot r' + b \cdot q'] \end{array} \right\}$$

$$\left. \begin{array}{l} (a > p) \text{ or } (a = p) \text{ and } bc > qr \\ a \cdot p' + (a+p') \cdot [b \cdot q' + (b+q') \cdot c \cdot r'] \end{array} \right\}$$

$$a \cdot p' + (a+p') \cdot [b \cdot q' + (b+q') \cdot c \cdot r']$$

* Combinational circuits

$P = (x \text{ and } y) \text{ on } z'$ output p
 input $= x, y, z$
 \hookrightarrow This is combinational circuit
 $\langle xyz \rangle = \langle 000, 010, 100, 110, 111 \rangle \rightarrow \text{true}$

$P = (x \text{ or } z') \text{ and } (y \text{ or } z) \rightarrow 110, 111, 101, 010$

$q = x \cdot z' + y \cdot z$ input x, y, z output q
 $\rightarrow 011, 100, 110, 111$

$q = q \cdot z' + y \cdot z$ input y, z output q

$$yz = 11, q = 1$$

$$yz = 00 \quad \text{retain}$$

$$yz = 01, q = 0 \quad (q \cdot 0 + 0 \cdot 1)$$

$$yz = 10 \quad \text{retain}$$

yz is made 11 output is 1.

Now yz is changed to 10 output remains 1.

$$\text{new } q = (\text{old } q) \cdot z' + y \cdot z$$

yz is made 01, output = 0

Fault

and: $x \cdot y$ $xy^{00 \rightarrow 0}$ $xy^{01 \rightarrow 0}$ $xy^{10 \rightarrow 0}$ $xy^{11 \rightarrow 1}$

Input stuck at 0

Let $x=0, y=1$ input is given.

$x=0, y=0$ input is going to circuit.

How to detect whether and gate has stuck at 0 on y?
give $x=1, y=1$ if output is zero, then system has got a fault.

Why not $x=1, y=0$ not??

Input does not change due to fault.

Why not $x=0, y=1$?

Fault will make it $x=0, y=0$

Output is same $xy=00, xy=01$ are both zero output.

or: + $x+y$

fault \rightarrow stuck at 0 on y

How to detect?

$xy = 01$

$x \oplus y$:

fault \rightarrow stuck at 0 on y

How to detect?

y should be 1, x can be anything

(x1)
↓

complementation fault

'and' couple fault at y.

gate $xy = 11, xy = 10$

'or' \rightarrow 01, 00
gate

($x \oplus 1$) \rightarrow 00, 01, 11, 10

Microprocessor Style Address Machine

MR: memory read $b \leftarrow [a]$
 MW: memory write $[a] \leftarrow b$

a + memory address register
 b + memory buffer register
 c \rightarrow PC

Print(2*4) print(4*7) print(3*5)

{ code

$\begin{bmatrix} 2*4 \end{bmatrix}$

$ib \leftarrow 4$
 $sc \leftarrow ib$
 $ib \leftarrow 7$
 $t \leftarrow ib$

$ib \leftarrow sc+t$
 print(ib)

$\boxed{[78] \leftarrow ib}$

$\begin{bmatrix} 3*5 \end{bmatrix}$

$ib \leftarrow [78]$ \rightarrow print(ib)

$\left\{ \begin{array}{l} b \leftarrow ib \\ ib \leftarrow 78 \\ a \leftarrow ib \\ MW \end{array} \right.$

$\left\{ \begin{array}{l} ib \leftarrow 78 \\ a \leftarrow ib \\ MR \\ ib \leftarrow b \end{array} \right.$

0: $ib \leftarrow 12$
 1: print(ib)
 2: $ib \leftarrow 10$
 3: ~~print(ib)~~ $pc \leftarrow ib$
 4: $ib \leftarrow 34$
 5: print(ib)
 6: $ib \leftarrow 47$
 7: print(ib)
 8: $ib \leftarrow 82$
 9: print(ib)
 10: $ib \leftarrow 56$
 11: print(ib)
 12: $ib \leftarrow 91$
 13: print(ib)
 Output + 12, 56, 91

'a' and 'b' can be used as normal register
 but 'c' cannot.

$c \leftarrow ib$
 $pc \leftarrow ib$

} are same

$ib \leftarrow pc$ is valid

(5)

Write ^ expression true for
boolean

$$xy = 10 \text{ only } x \cdot y'$$

$$xy = 00 \text{ and } xy = 11$$

$$xy + x'y' \text{ or } (x'y + xy')'$$

$$\left\{ \begin{array}{l} xy \\ x'y' \end{array} \right. \neq x'y + y$$

$xy + x'y' + \text{sum of product}$

$(x+y') \cdot (x'+y) \rightarrow \text{Product of sum}$

sum of product $\rightarrow 010 \text{ and } 110$

$$x'yz' + xyz' = yz'$$

Proof
 $a+a'b = a+b$

$$a+a'b = (a+a') \cdot (a+b) \\ = a+b$$

$$x \cdot (x'+b) = x \cdot x' + x \cdot b$$

$$x + (x \cdot b) = (x+x')(x+b)$$

$$x'yz' + xyz$$

$$\left\{ \begin{array}{l} 010, 110, 111 \\ yz' + xyz \\ y(z' + xz) \\ yz' + xy \end{array} \right.$$

$a+b-c$ and $a-c+b$ are different

$$a: \{P, q, y\}$$

$$b: \{q, r\}$$

$$c: \{P, r\}$$

$$a+b: \{P, q, r\}$$

$$a+b-c: \{q, y\}$$

$$a-c: \{q\}$$

$$a-c+b: \{q, r\}$$

$$a-b = a \cdot b'$$

c: true for $xy = 00 \text{ and } 10$

~~for $x=0, y=1$~~

d:

$$xy = 00 \text{ and } 01$$

$$x'y' + x'y + z'$$

b: true for $xy = 00 \text{ and } 01$

$$x'y + xy'$$

(6)

Binary 5 \rightarrow 101
~~9~~ \rightarrow 1001

Let us assume there are 5 bits
 then 5 \rightarrow 00101
 9 \rightarrow 01001

2's complement for negative numbers (signed numbers)

Positive number is represented as it.

For negative number, bit by bit complementation is done and one is added.

$$+5 = 00101$$

$$-5 = 11011 = 11010 + 1$$

$$\cdot (11011)' = 00100 + 1 = 00101$$

$$+9 = 01001$$

$$-9 = 10010 + 1 = 10111$$

Add ~~-5~~ and +9

$$\begin{array}{r} -5 = 11011 \\ +9 \quad 01001 \\ \hline \textcircled{1}00100 \end{array}$$

remove carry $00100 = +4$

+9 and +9 added

$$\begin{array}{r} 01001 \\ 01001 \\ \hline 10010 \\ (10010)' + 1 \\ = 01101 + 1 \\ = 01110 \end{array}$$

Add -9 and +5

$$\begin{array}{r} 10111 \\ 00101 \\ \hline \textcircled{0}11100 \end{array}$$

11100 \rightarrow is a negative no.

$$(11100)' + 1 = 00011 + 1 = 00100$$

Add -9 and -5

$$\begin{array}{r} 11011 \\ 101011 \\ \hline 110010 \end{array}$$

negative number

$$\begin{array}{r} -5 \text{ and } -5 \\ 11000 \\ 11000 \\ \hline 11000 \\ 01111 + 1 \\ = 10000 \end{array}$$

$$\begin{array}{r} +8 \text{ and } +8 \\ 01000 \\ 01000 \\ \hline 10000 \\ 01111 + 1 \\ = 10000 \end{array}$$

$$(10010)' + 1 = 01101 + 1 = 01110$$

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Every instruction is in 4 digits

- abcd means $[ab] = [cd]$
5423 means in memory 54 but the content of 23.
 - let memory 45 has 389. Memory 82 has 21345
2745 now^{memory} 27 has 389.
 - 9045 now memory 90 has 45 [not 389]
 - '(90)' - is a working in a immediate mode.
'(0 to 89)' → in normal mode
 - Write a program to store 72 in memory 56
9072, 5690
 - What will 8856 will do?
 $[88] = [56] = 314$
 $[93] = 746$
 - 156 is stored in memory 42?
 9078
 8890
 8990
 4293
 - 240 in 59?
 9080
 8990
 8890
 8893
 5993 } is wrong!
 - 8893 → $[88] = [88] + [89]$ is infinite
- abcd means $[ab] = [cd]$
 Following are exceptions -

 - 90cd means $[90] = [cd]$
~~not $[cd] \neq [90]$~~
 - 93 memory will store $[88] + [89]$

let $[88] = 243$
 $[89] = 432$
 $[56] = 314$
 $9356 \rightarrow [93] = 675$
 it will always store $[88] + [89]$

 - 91 cd means print $[cd]$
 - 97cd means $[97] = cd$ and goto instruction cd
 - 94 memory will store $[88] - [89]$
 - 98cd means $[98] = cd$ and goto instruction cd if $[94] >= 0$

Vector processing

$$x = 12, y = 4, z = \frac{x+y}{16}$$

In vector process -

$$p = [12, 14, 62, 1]$$

$$q = [4, 11, 5, 4]$$

$$n = p + q = [16, 45, 67, 12] \text{ in unit time}$$

$$t = 3:2:12 = [3, 5, 7, 9, 11]$$

will not cross \uparrow 12 (will be included if present)

$$m = p * q = [48, 374, 260, 36] \text{ in unit time}$$

K is matrix

$$\begin{matrix} 2 & 4 & 6 & 7 \\ 8 & 3 & 5 & 9 \\ 7 & 2 & 5 & 4 \end{matrix}$$

$$p = K[2, 3] = 5$$

$\uparrow \uparrow$
element in 2nd row and 3rd column

$$K[2, :] \rightarrow \text{second row} = [8, 3, 5, 9]$$

$$K[:, 3] \rightarrow \begin{matrix} 6 \\ 5 \\ 5 \end{matrix} = [6, 5, 5]^T$$

$$A = B + C$$

$$B \& C \rightarrow 3 \times 4$$

for $i = 1:1:3$

$$A[i, :] = B[i, :] + C[i, :]$$

for $i = 1:1:4$

$$A[:, i] = B[:, i] + C[:, i]$$

$$[p, q] = \text{size}(b)$$

$O(\min(m, n))$
time complexity
otherwise order $O(mn)$

$b(m,n) \cdot c(n,r)$ multiply

To get final matrix $O(m \times n \times r)$

$a(i,j)$

$s = 0$

for $k=1:1:n$

$s = s + b(i,k) * c(k,j)$

To get first row, we need $O(n \times r)$

To get some element of final matrix $c_{i,j}$ in ordinary.
In vector also n .

To get first row in ordinary $\rightarrow n \times r$
and in vector -----.

Matrix b

$$\begin{bmatrix} 6 & 2 & 3 \\ 1 & 7 & 5 \end{bmatrix}$$

Matrix c

$$\begin{bmatrix} 3 & 2 & 5 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 2 & 7 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 3 & 8 & 4 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 6 & 2 & 3 \end{bmatrix} \cdot \begin{bmatrix} 3 & 5 & 3 \end{bmatrix} = \begin{bmatrix} 18 & 10 & 9 \end{bmatrix}$$

$$\begin{bmatrix} 6 & 2 & 3 \end{bmatrix} \cdot \begin{bmatrix} 2 & 2 & 8 \end{bmatrix} = \begin{bmatrix} 12 & 4 & 24 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 7 & 4 \end{bmatrix} \cdot \begin{bmatrix} 3 & 0 & 14 & 12 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 5 & 2 \end{bmatrix} = \begin{bmatrix} 6 & 10 & 6 \end{bmatrix}$$

Above took \approx time

make following matrix

$$18 \quad 10 \quad 9$$

$$12 \quad 4 \quad 24$$

$$30 \quad 14 \quad 12$$

$$6 \quad 10 \quad 6$$

Add columns $n-1$ times $O(n+2)$

$$\begin{bmatrix} 37 \\ 40 \\ 56 \\ 22 \end{bmatrix}$$

$$\text{Time} = O((n-1) + r)$$

$$\text{Total time} = O(m \times (n+r-1))$$

(9)

Tree Interconnection Scheme

Add 4 7 5 9

(4 \oplus 7) ⁱⁿ
add
these numbers

(11 \oplus 5)

(Like Binary Tree,
reduce time to
 $O(\log n)$)

② It takes 2 unit time.

There are many computers. Every computer has two inputs one output. Every computer has two variables x & y .

input-left and input-right

4 is input-left of c2

7 is input-right of c2

$x = \text{input-left}$ $y = \text{input-right}$

$$z = x + y$$

Output z.

+ following is program
of addition of n numbers

Interconnection scheme

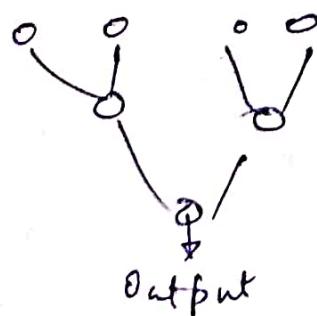
Computer k input-left is connected with computer
2k output.

computer k input-right is connected with computer
2k+1 output.

computer k sends its output to computer (k/2).

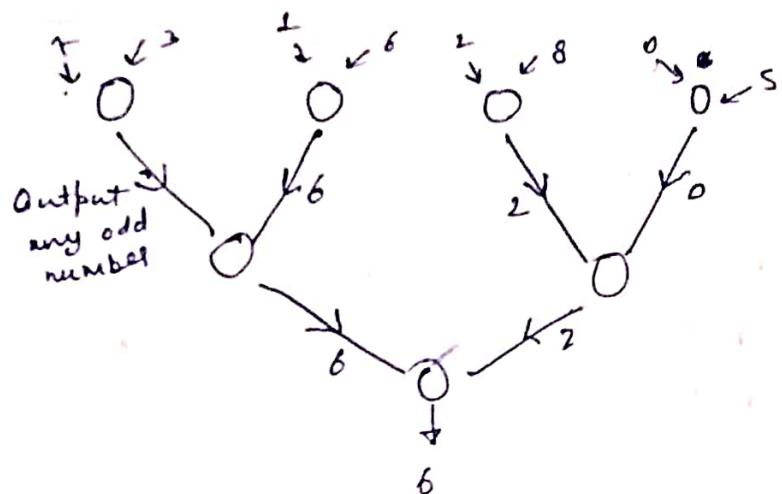
k is even \rightarrow left

k is odd \rightarrow right



- Write program to find first even numbers

$$7 \ 3 \ 1 \ 6 \ 2 \ 8 \ 0 \ 5 \rightarrow (6)$$



$$x = \text{input} - \text{ref t} \quad , \quad y = \text{input} - \text{right}$$

if (n is even) , $z = z$

If $(-i)$ is odd \Rightarrow and If y is even, $\Rightarrow z = y$

else $z = \text{any odd number}$

If t is even then $m=t$ else $m=$ any odd.

\hat{A} can be reduced to

$$m = t$$

- Linear one way interconnection

Initial $y=0$

Let only one computer.
Following is done many times
 $x = \text{input}$

$x = \text{input}$

if $x < y$ $x \leftarrow y$

output - y

$$y = x$$

first input from right

input 6, 3, 5, 4, 2

first time

$$x = 2 \quad y = 0$$

echo false
output 0

4 = 2

$x=4$, $y=2$

out put &

$$x = 5 \quad y = 4$$

Output 4

$$\underline{y = 5}$$

$$y = 5, x = 3$$

• 5

$$\frac{d}{dt} y = 5$$

(10)

```
#include <stdio.h>
main()
{ int a,b;
scanf ("%f", &a);
b = . . . - - - - - ;
printf ("%d %d", a,b);
}
```

input 32.4.

Method to store float numbers

$$12 = 1100$$

0.4 in float form

↓

$$0.4 \times 2 = 0.8$$

$$\begin{array}{r} 0.01001100110 \\ \times 2 \\ \hline 0.001001100110 \end{array}$$

$$0.8 \times 2 = 1.6$$

$$1.6 \times 2 = 1.2$$

$$1.2 \times 2 = 0.4$$

$$0110$$

$$12.4 = 1100.0110011001100110 \dots$$

32 bits to store float number

1st bit is sign bits

s < 8 exponent bits > < 23 mantissa bits >

s=0 → positive

s=1 for negative

± abcd... w * 2^n

exponent is 128+n

mantissa is abcd... w

$$5.25 = 101.01 = 10.101 * 2^1$$

$$.25 = 0.01 = 10.00 * 2^{-3}$$

exponent is 2^1 is $128+1=129$ exponent is $128-2=126$

$$5.25 = 0<129><01\underset{in 8 bits}{0}00000\dots>$$

$$129 = 10000001$$

$$5.25 = 01000000 \quad 1010\underset{in 23 bits}{0}00000000000$$

0.25

$$0<011111010><000\dots\dots>$$

Always mantissa has 2 digits
~~1101110 * 2^13~~ 1101110 * 2^13
~~exponent = 13~~

~~breakdown~~

0 < 10000011 < 1011110

{ while writing mantissa
~~0.01110~~
 is ignored and 1011110
 mantissa will have 2 digits

① 0000001 0, 00100 00000000 00000000 0

$$11.001 * 2^{-8} = 1100.1$$

-12.5

int a,

$$\frac{5.25}{256 \times 256} \quad p = a / 256 \quad q = a \% 256$$

{ int a, *k; float b; int p, q;

b = 5.25; K = 6 b; a = *k;

a = a / 256; q = a % 256;

$$p = 64 \\ q = 168$$

p = a / 256; q = a % 256

printf ("%d %.d", p, q);

}

b = 01000000 10101000 00000000 00000000

b = 01000000 00010000 - - - - -

Multiplexer and Decoder(D)

(selector) \rightarrow method to design memory

$\Rightarrow S(12, 45, 67, 89, 56, 78; 3) \rightarrow$ output 89

① ② ③ ④

$$\alpha = S(\alpha, 45; k)$$

[; 8 \rightarrow error]

o in place
of 3 \rightarrow 12

$$K = S(12, 45, 67, 89, 56, 78; 3)$$

$$K = 89$$

$$\alpha = S(\alpha, 45; K) \text{ What it does?}$$

if $K=0$, ~~selects~~ a unchanged

$$K=1, \alpha = 45$$

$$3125 \rightarrow m[3] \leftarrow m[25]$$

S: selector takes multiple input single output

D: Decoder takes single input and output many numbers
Exactly one number is 1 and others are zero.

$$D(3) \rightarrow 0, 0, 0, 1, 0, 0, 0, 0, 0, \dots$$

$$D(0) \rightarrow 1, 0, 0, 0, \dots$$

abcd does $m[ab] \leftarrow m[cd]$

$$u = S(m[00]; [01], \dots, m[99]; cd)$$

$$k_i = D(ab)$$

$$m_i = S(m_i, u; k_i) \text{ for all } i$$

1247 is given

u is contents of memory \neq

$$u = m[47]$$

$$D(12) \rightarrow k_0 = 0, k_1 = 1, k_{12} = 1, k_{30}, \dots, k_{99} = 0$$

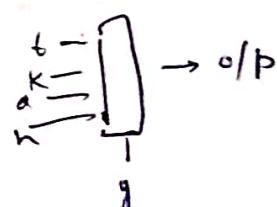
$$m[0] = S(m[0], m[47]; 0) \text{ unchanged}$$

upto $m[11]$

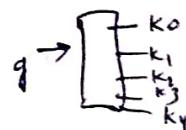
$$m[12] = S(m[12], m[47]; 1) \rightarrow \text{changed}$$

$m[12] = m[47]$

$$S(t, k, d, h, y)$$



$$D(k)$$



Following is exception -

abcd does $w[ab] = w[cd]$

exception 90 cd does $w[90] = cd$

$$\left(\begin{array}{l} w[i] = s(w[i], u; k_i) \text{ for all } i \text{ and } i \neq 90 \\ w[90] = s(w[80], cd; k_{90}) \end{array} \right)$$

ab93 is $w[ab] = w[aa] + w[89]$

ab94

$$\left(\begin{array}{l} u = s(w[aa], w[89], \dots, w[92], w[aa] + w[89], w[aa] - w[93]; cd) \end{array} \right)$$

$$w[94] = s(w[aa] - w[93]; 0)$$

94cd will not modify $w[94]$

88cd will modify $w[94]$

97cd does $w[97] = cd$

98cd does $w[97] = cd$ if $w[94] \geq 0$

$$w[97] = s(w[97], cd; \underbrace{\begin{cases} k_{97} \\ k_{98} \\ (w[94] \geq 0) \end{cases}}_{\rightarrow \text{and}})$$

Architecture of Parallel Computing

Interconnection of computer (Linear one way scheme)

initial, x_0

$y = \text{input}$

if $x > y \quad x \leftarrow y$

output x

$x = y$

computer send output to its left computer

output $\min(x, y)$

$x = \max(x, y)$

let only one computer input 3, 2, 8, 1, 5

$(x_0, y) 3, 2, 8, 1, 5$, infinite

$(x_0, y_3) 2, 8, 1, 5$

{leftmost}

$0 [x_0, y_3] 2, 8, 1, 5$

~~$0 [x_3, y] 2, 8, 1, 5$~~

$(x_3, y_2) 8, 1, 5$

$2 [x_3, y] 8, 1, 5$

----- output - 0 2 3 1 5 8

$n+1$

{leftmost}

$(x_3, y) 8, 1, 5$

$(x_3, y_8) 1, 5$

$3 [x_0, y_8) 1, 5$

$3 [x_8, y) 1, 5$

$(x_8, y_1), 5$

$1 [x_8, y], 5$

$(x_8, y_5), i$

$5 [x_8, y], i$

(x_8, y_i)

$8 [x_i, y] -----$

array $a[1] \dots a[n]$ is given

for ($i=1, i \leq n-1, i++$)

if ($a[i] > a[i+1]$) $a[i] \leftrightarrow a[i+1]$

put biggest element to last

$a[0] = 0$ & $a[n+1] \rightarrow \text{infinite}$

above procedure is

followed from $i=0$ to $n-1$.

let two computers

$[x_0, y] 0 [x_0, y] 3, 2, 8, 1, 5, i, i$

$[x_0, y_0] 0 [x_0, y_3] 2, 8, 1, 5, i, i'$

$0 [x_0, y] 0 [x_3, y] 2, 8, 1, 5, i, i$

$[x_0, y_0] 0 [x_3, y_2] 2, 8, 1, 5, i, i$

$0 [x_0, y] 2 [x_3, y] 8, 1, 5, i, i$

$[x_0, y_2] 0 [x_3, y_8] 1, 5, i, i$

$0 [x_2, y] 3 [x_8, y] 1, 5, i, i$

$[x_2, y_2] (x_8, y_1) \rightarrow 5, 6, 7$

$2[x_3, y_3] (x_8, y_1) \rightarrow 5, 6, 7$

$[x_3, y_3] (x_8, y_5) \rightarrow 1, 2$

$1[x_3, y_3] (x_8, y_5) \rightarrow 1, 2$

$[x_3, y_5] (x_8, y_1) \rightarrow 1, 2$

$3[x_5, y_5] (x_8, y_1) \rightarrow 1, 2$

$[x_5, y_5] (x_1, y_1) \rightarrow 1, 2$

$5[x_8, y_5] (x_1, y_1) \rightarrow 1, 2$

$[x_8, y_1] (x_1, y_1) \rightarrow 1, 2$

$8[x_1, y_1] (x_1, y_1) \rightarrow 1, 2$

$[x_1, y_1] (x_1, y_1) \rightarrow 1, 2$

How many computers are needed to sort?

1, 5, 2, 3, 4, 6, 9, 7, 8 only 2.

9, 1, 2, 3, 4, 5, 6, 7, 8 only 1

2, 3, 4, 5, 6, 7, 8, 9, 1 8

Total time = $\mathcal{O}(n-1)$

sorting n numbers,

$n-1$ computers
is needed

$n-1$ are really
needed when
they are in
reverse
order and
all distinct

Linear interconnection: many computers connected
in linear order

4 6 2 8 5 1 9 \rightarrow 5 computers

- What is $a + a'$? Not always 1

Let $a=1$ from time $t=0$ to $t=55$
 $t=55$ onwards a is 0.
 $a+a'=a+p \quad p=a'$

p is 0 from time $t=0$ to $t=55$

$t=55$ onward p is 1.

When delay of 3 units in not gate,

p is 0, time $t=0$ to $t=58$

$p=1 \quad t=58$ onwards

During $t=55$ to 58 , a and p are both zero. Hence
 $q=a+a'$ is 0.



not specifically this
because delay in or gate
because of transistors take time
to activate.

correct

if delay in or gate of 10 unit, then $t=65$ to 68 is zero.
 $t=65$ to 68 and not gate delay, then output is 0. \rightarrow wrong

$a: 1 \rightarrow 0$ is problematic $a+a'$. From $t=0$ output is 1.

$a \cdot b' + b$ is optimize as $b+a'$. It is not correct.

Owing to delay in not, and, or gates
not so important

Let $b=0$ from $t=0$ to 70 . Let $a=1$ always
delay not 7. delay or 10.

when output is 0 during $t > 50$

→ never 0 during $t > 50$

before $t=70$ only

$b=1 \quad t=70 - 130$ let $b=0 \quad t > 130$

when output is 0 or gate delay 20
 $a \cdot b' + b$
 $p=b', q=a \cdot b, r=q+p \cdot b$

$t = 10.0$ on watch

upto 130 p is 1.

130 onwards p = 0 $\therefore t \geq 130$

p = 0 upto 139 $\Rightarrow p = 135 \dots 139$

upto 147 q is 0 $\therefore q = 1 \quad t \geq 147$

During $t = 130 \dots 147$ both p and q are 0

So, $t = 130 \dots 169 \Rightarrow r$ is 0

$$p = x.z + y.z'$$

delay (and of x.z) = 10

delay (and of y.z') = 8

delay (not) = 4

delay (or) = 0

let $t < 50$, z is 0 let $t > 50$ z is 1

let x and y are 1 always

During what time interval wrong output

come $\Rightarrow 62 \dots 70$ - output is 0

(should be 1)

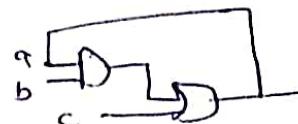
$$q = x.z + y.z' + x.y = x.z + y.z'$$

During q wrong output \Rightarrow never

p is optimized may give wrong output

$$K = a \cdot b + c$$

$$a = a \cdot b + c$$



b and c are inputs. Output is a.

$$b=0, c=1 \quad a=1$$

$$b=1, c=1 \quad a=1$$

$$b=0, c=0 \quad a=0$$

$$b=1, c=0 \quad a=\text{retained} / \text{no change}$$

$$a = a \cdot b + c \cdot b' \rightarrow \text{another expression?} \quad [\text{product of sum form}]$$

b = 1 retain

$$b=0, c=1 \rightarrow 1, a=c$$

$$b=0, c=0 \rightarrow 0$$

$$a \cdot b + c \cdot b' = a \cdot b + c \rightarrow [a=0, b=1, c=1] \text{ is difference between two expressions}$$

$$a = a \cdot b + c \cdot b'$$

{b=1, with options}

$$b=0 \Rightarrow a=c \rightarrow \text{general input}$$

~~b=1~~ then retain

controlled
input

$$a = K(c, b)$$

$$d = d \cdot b' + a \cdot b \quad \text{input } a, b \text{ output } d \quad d = L(a, d)$$

$$b=0, d=\text{retain}$$

$$b=1, d=a$$

$b = 0$, retain

$b = 1$, $d = \text{not yet set}$
 $b = 0$, a is retained
 $b = 0$, retain $b = 1$ retain

$b = 0$ $c = 0$ $a = 0$ $d = d$ retain

$b = 0$ $c = 1$ $a = 1$ $d = d$ retain

$b = 1$ $c = 0$ $a = \text{retained}$ $d = a$

since a is retained hence d is retained

$d \neq a$ previously, then
d is not retained.

$b = 1$ $c = 1$ $a = \text{retained}$ $d = a$

Initially, $b = 0, c = 0, a = 0, d = 0$,

$b = 0, c = 1, a = 0, d = 0$

$b = 1, c = 1, a = \text{retain} = 1, d = 1$

$b = 1, c = 0, a = 1, d = 1$

$b = 0, c = 0, a = 0, d = 1 = 1$

$b = 0, c = 1, a = 1, d = 1 = 1$

$b = 0, c = 0, a = 0, d = 1$

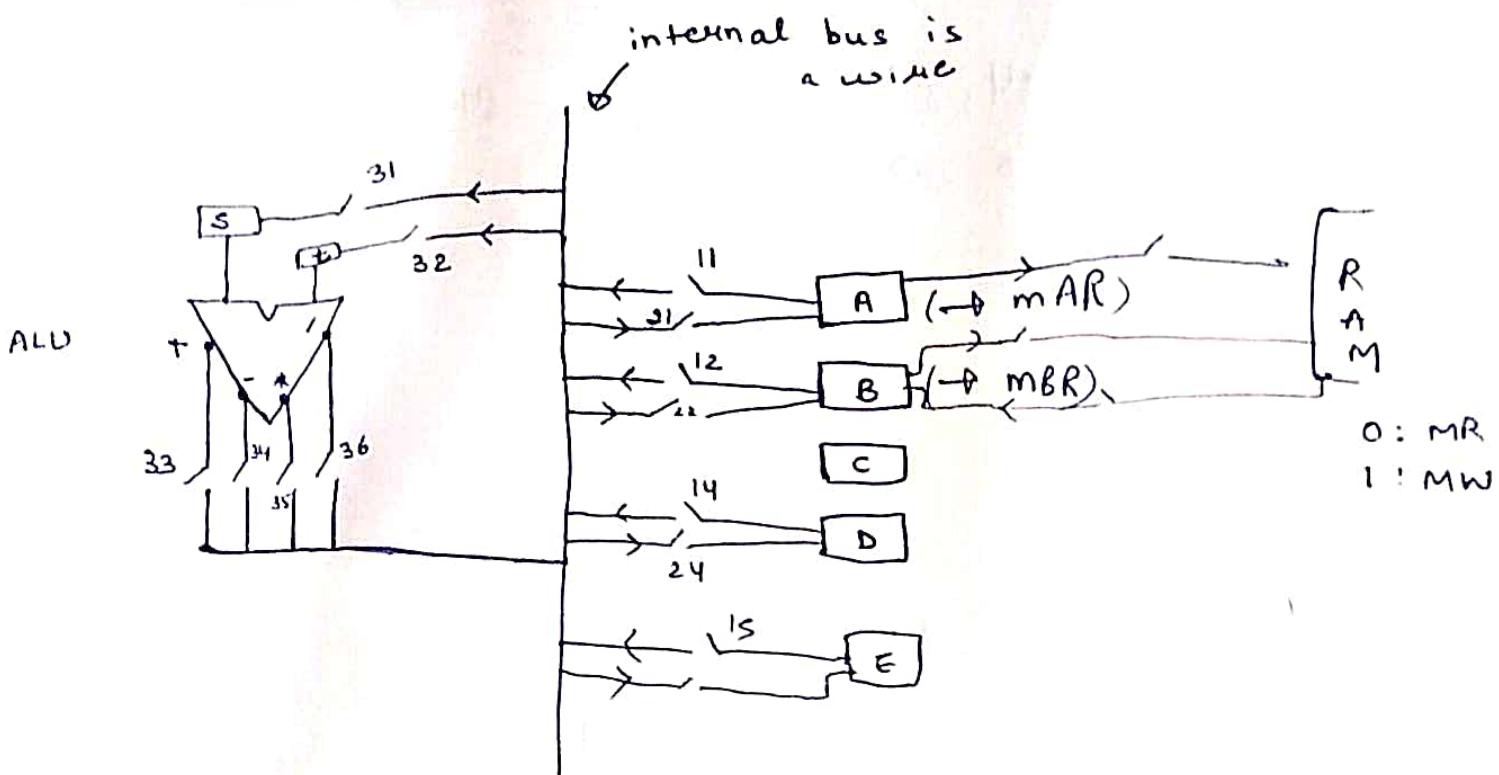
$b = 1, c = 0, a = 0, d = 0$

When output d changes

When c changes but b unchanged then no change in output

When b changes but c unchanged

$b: 1 \rightarrow 0$ no change $\rightarrow b: 0 \rightarrow 1$ $d = c$



how we can perform $a+b = a+t+b$
this operation?

11, 12, 31, 33 → wrong

- 11 and 12 cannot be closed together (data conflict)

close 11, 31
open 11, 31 }
close 12, 32
open 12, 32 }
close 33, 24 }

close 11: ib<--a
close 31: s<--ib
open 11, 31
close 12: ib<--b
close 32: t<--ib
open 12, 32
close 33: ib<--st
close 24: d<--ib

swapping without using (csd)

$a \leftrightarrow b$ let $a=79$ $b=83$
close 11
close 31, 32 ~~swapping~~
open 11, 31, 32 $s=79$ $t=83$

close 12, 21 $a=83$
open 21

close 34, 32 $t=0$
open ~~34~~ 32

open 32

close 22

$b=79$

BCD Numbers

Binary
 $0101 + 0110 = 1011$ carry = 0 Binary
 $0101 + 0110 = 0001$ carry = 1 BCD

Binary numbers →

$$abcd + efg = pqrs \text{ carry } y$$

$$s = d \cdot n' + n' \cdot d$$

$$t_0 = d \cdot h$$

$$r = c_1' \cdot (c_1' g + g' c) + c_1 \cdot [(c_1' g + g' c)']$$

$$(c_1' g + g' c)$$

$$\text{add}(cd, gh) \text{ condition of carry } \rightarrow \cancel{\text{carry}} \quad c \cdot g + ((+g) \cdot u)$$

let $abcd + egh$ is pqrs and carry y in binary

How to convert it in BCD ijkl and carry z.

$$1000 + 1001 = 0001 \text{ cy} = 1 \text{ Binary}$$

$$1000 + 1001 = 0111 \text{ cy} = 1 \text{ BCD}$$

$$- - - - - - - -$$

$$0010 + 0011 = 0101 \text{ cy} = 0 \text{ Binary}$$

$$0010 + 0011 = 0101 \text{ cy} = 0 \text{ BCD}$$

$$- - - - - - - -$$

1010 : A

$$1000 + 0101 = 1101 \text{ cy} = 0 \text{ Binary}$$

1011 : B

$$1000 + 0101 = 0011 \text{ cy} = 1 \text{ BCD}$$

1100 : C

$$- - - - - - - -$$

1101 : D

$$1000 + 0101 = 1101 \text{ cy} = 1 \text{ BCD}$$

1110 : E

$$1000 + 0101 = 0011 \text{ cy} = 1 \text{ BCD}$$

1111 : F

$$5 + 7 = 12, \text{ cy} = 0 \text{ in binary}$$

in BCD ~~12~~, cy = 1

$$8 + 9 = 17, \text{ cy} = 1 \text{ in binary}$$

in BCD 0~~17~~11, cy = 1

$$5 + 3 = 8, \text{ cy} = 0 \text{ in binary}$$

no change

$$pqrs \geq 10$$

$p \geq 1$, among q and r any should be one

$$pqrs - 1010 = ijkl$$

$$l = s$$

$$k = r'$$

$$j = qr + r'q'$$

$$i = \bullet(\text{carry})' \quad | \quad i = 0$$

under condition
when $pqrs \geq 10$ or
 $i = 0$

2-D interconnection one-way

→ 2-D one-way interconnection

p	q	r
s	t	u
v	w	x
y	z	m
.	.	q

F
3
P

→ Linear 2-way
 a b c d e { a can send to b and
 b can send to c }

→ Linear 1-way : (use used it for sorting)

2-D one way interconnection scheme
 (use will used this for matrix multiplication)

Matrix A

1 2 3

4 5 6

Matrix B

7

8

9

Normally it will take 6 multiplications,

Now every computer has x and y, x for A and y for B

--- time $t = 0$ ---

$$\begin{pmatrix} P \\ Q \end{pmatrix} \begin{matrix} 1, 2, 3 \\ 4, 5, 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

--- time $t = 1$ --- 921.611

$$\begin{pmatrix} P \\ Q \end{pmatrix} \begin{matrix} 1, 2, 3 \\ 4, 5, 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$Q = 7 * 4 = 28$$

--- time $t = 2$ --- 922.621, 911.611

~~$\begin{pmatrix} P \\ Q \end{pmatrix} \begin{matrix} 1, 2, 3 \\ 4, 5, 6 \\ 7 \\ 8 \\ 9 \end{matrix}$~~

~~$\begin{pmatrix} P \\ Q \end{pmatrix} \begin{matrix} 1, 2, 3 \\ 4, 5, 6 \\ 7 \\ 8 \\ 9 \end{matrix}$~~

$$P = 1 * 7$$

$$Q = 28 + 5 * 8 = 68$$

--- time $t = 3$ --- 912.621

923.631

$$\begin{pmatrix} P \\ Q \end{pmatrix} \begin{matrix} 1, 2, 3 \\ 4, 5, 6 \\ 7 \\ 8 \\ 9 \end{matrix}$$

$$\begin{aligned} P &= 7 + 2 * 8 = 23 \\ Q &= 68 + 6 * 9 = 122 \end{aligned}$$

$$\begin{array}{l}
 \text{time for } A = 4 \\
 (\text{P } 39) \\
 (\text{Q }) \\
 \text{P} = 23 + 3 * 9 = 50
 \end{array}$$

$$\underline{\text{Total time} = 4}$$

Now much time will be taken
 and $A = (23, 57)$
 $B = (57, 1)$

$$\begin{array}{r}
 23 \\
 57 + 23 - 1 = 79 \\
 \hline
 \end{array}$$

(Example)

Matrix A

7, 8, 9

1, 2, 3

4, 5, 6

Matrix B

7

8

9

at $t = 0$

$$\begin{array}{c}
 \left(\begin{array}{c} m \\ p \\ q \end{array} \right) = \begin{array}{c} 7, 8, 9 \\ 1, 2, 3 \\ 4, 5, 6 \end{array} \\
 \left(\begin{array}{c} 7 \\ 8 \\ 9 \end{array} \right)
 \end{array}$$

$\left\{ \begin{array}{l} \text{It will have} \\ \text{to traverse through} \\ \text{one more} \\ \text{computer} \end{array} \right\}$

$$\underline{\text{So time taken} = 3 + 3 - 1 = 5}$$

Now Matrix A, and Matrix B

$$\begin{pmatrix} 1 & 2 & 3 \end{pmatrix}$$

$$\begin{pmatrix} 4 & 5 \\ 6 & 7 \\ 8 & 9 \end{pmatrix}$$

$$02 = P * S$$

$$8 \ 9$$

$$t=0$$

$$(P) (Q) \begin{pmatrix} 1 & 2 & 3 \end{pmatrix}$$

$$\begin{pmatrix} 4 \\ 5 \\ 6 \end{pmatrix}$$

$$\begin{pmatrix} 5 \\ 7 \\ 9 \end{pmatrix}$$

$$Q = 1 \times 5 = 5$$

$$t=1$$

$$(PQ) (Q) \begin{pmatrix} 2 & 3 \end{pmatrix}$$

$$\begin{pmatrix} 4 \\ 5 \\ 6 \end{pmatrix}$$

$$\begin{pmatrix} 7 \\ 9 \end{pmatrix}$$

$$Q = 1 \times 5 = 5$$

$$t=2$$

$$(P^2 Q) (Q) \begin{pmatrix} 3 \\ 9 \end{pmatrix}$$

$$\begin{pmatrix} 6 \end{pmatrix}$$

$$P = 1 \times 4 = 4$$

$$Q = 5 + 2 \times 7 = 19$$

$$t=3$$

$$(P^2 Q) (P) (Q) \begin{pmatrix} 3 & 9 \end{pmatrix}$$

$$\begin{pmatrix} 6 \end{pmatrix}$$

$$P = 4 + 2 \times 5 = 14$$

$$Q = 5 + 2 \times 9 = 26$$

$$t=4$$

$$(P^3 Q) (Q)$$

$$P = 14 + 3 \times 6 = 32$$

A : 1, 32

B : 32, 79

→ At time $t=1$ what is done? $a_{1,1} * b_{1,79}$ → At $t=2$, what is done? $a_{1,1} * b_{1,78}$ $a_{1,2} * b_{2,79}$ → What is done at last $t=?$ $a_{1,32} * b_{32,1}$

Name Matrix A

2 3

4 5

Matrix B

6 7

8 9

2, 3

4, 5

--- $t=0$ $(P) (Q)$ $(R) (S)$ $\frac{6}{8} +$

9

--- $t=1, a_{21}, b_{12}$ $(P) (Q)$ $(R) (S)$

6 9

8

$$S = 4 \times 7 \\ = 28$$

--- $t=2$ $(P) (Q)$ $(R) (S)$

8

a₂₁, b₁₁b₂₂, a₂₂a₂₁, b₁₂

$$g = 2 \times 7 = 14$$

$$g = 4 \times 6 = 24$$

$$S = 28 + 5 \times 9$$

=

--- --- --- --- $t = 3$, $A_{11} \cdot b_{11}$
 $(P_{26})(Q_{39})$ $A_{22} \cdot b_{21}$
 $(S_{58})(S_{P})$ $A_{12} \cdot b_{22}$

$$P = 2 * 6$$

$$Q = 3 * 9 + 64$$

$$S = 5 * 8 + 24$$

--- --- $t = 4$ --- $A_{12} \cdot b_{21}$

$$(P_{38})(Q_{2})$$

$$P = 12 + 3 \times 8$$

$$A = (30, 33), B = (33, 28)$$

when will $C[10, 12]$ start

$$(50 - 10 + 1) + (78 - 12)$$

~~Time reg above~~

~~Time~~ for multiplying $A(m, n)$
 $B(1, s)$

~~Time reg:~~ $m + s + n - 2$

Pipeline Architecture

Instruction is done in 4 stages.

- Instruction Fetch (IF)
- Fetch Operand (FO)
- Compute (CP)
- Store Result (SR)

Let

initial values of a, b, c, d are $a = 23 \quad b = 67 \quad c = 82 \quad d = 45$

$$c = a + d \quad [IF: 0, 10) \quad [FO: 10, 20) \quad [R = S + T : 20, 30) \quad [C = R, 30, 40)$$

$$S = a = 23 \quad T = d = 45 \quad R = 68$$

$$K = c + 10$$

$$[IF: 10, 20) \quad [S = C = 82 \quad T = 10, 20, 30) \quad [30-40, R = S + T) \quad [K = R, 40, 50)$$

$$= 92$$

Time	0 - 10	10 - 20	20 - 30	30 - 40	40 - 50	50 - 60	60 - 70
$c = a + d$	IF	$S = 23$ $T = 45$	$R = 68$	$C = R$			

$$C = c + 10$$

$$IF \quad S = 82 \quad R = 92 \quad C = R$$

$$K = c + 2$$

$$IF \quad S = C = 82 \quad R = 84 \quad K = R$$

$$U = c + 6$$

$$IF \quad S = C = 68 \quad R = 73 \quad U = R$$

$$V = c + 3$$

$$IF \quad S = C = 92 \quad R = 95$$

↓

$$V = R$$

$$j = 80$$

$$IF \quad j = 80$$

$$K = b$$

$$IF \quad S = b$$

$$K = B7$$

$$\text{print}(K)$$

$$IF$$

$$S = K$$

$$\text{print}(k)$$

84 will be printed

$a = 23$

$b = 67$

$c = 82$

$d = 45$

$e = 26$

$f = 71$

K: print(a) IF

print(b) IF

print(c) IF

goto K [$pc \neq 0$] IF $PC = 0$

print(d) IF

print(e)

print(f)

O/P $\rightarrow 23\ 67\ 82\ 45\ 23\ 67\ 82\ 45 - \sim$

- $0+0 = 0 \quad y=0$
- $0+1 = 1 \quad y=0$
- $1+1 = 1 \quad y=1$

- In, $a+b$ condition for carry = $a \cdot b$
Total time is $\Rightarrow 1$ unit

- $ab+cd$ condition for carry = ~~ac~~ $ac + (a+c) \cdot bd$

Time 1 $\Rightarrow u=a \cdot c; v=a+c; w=b \cdot d$

Time 2 $\Rightarrow z=v \cdot w$

Time 3 $\Rightarrow u+z$

Total time is 3 unit.

- $gab+hcd$ condition for carry.

$$gh + (g+h) \cdot ac + (g+h) \cdot (a+c) \cdot bd$$

$$\Rightarrow gh + (g+h) \cdot (ac + (a+c) \cdot bd)$$

Total time is 5 unit.

15 $gh; g+h; ac; (a+c); bd$

$(a+c) \cdot bd$

$u = ac + (a+c) \cdot bd$

$v = (g+h) \cdot u$

$gh + v$

→ 5 unit Time

- Ripple Carry Adder -

add, $abc\bar{def} + pq\bar{rst}u$
let carry of $\bar{def} + \bar{rst}u = z$.
then final carry = $a \cdot p + z \cdot (a+p)$

$$t(n) = t(n-1) + 2$$

carry of $abc\bar{def} + pq\bar{rst}u$
 \Rightarrow let x is carry in $\bar{def} + \bar{rst}u$; y is carry in $abc + pqr$.
and $\text{then } z = (a+p) \cdot (b+q) \cdot (c+r)$

let ABC are computers in parallel

then we find - ~~$x+y \cdot z$~~ $y \oplus x \cdot z$

$$\text{In this } t(n) = t(n/2) + 2$$

carry of $abc\bar{def} + pq\bar{rst}u$ is true when \swarrow no carry | \nwarrow

$$1) abc + pq\bar{r} \Rightarrow cy = 1$$

$$2) \bar{def} + \bar{rst}u \Rightarrow cy = 1$$

or

$$abc + pq\bar{r} = 111$$

abcd is Binary Coded Decimal. 0 to 9

1010, 1011, 1100, 1101, 1110, 1111 are not possible

How to increment a BCD number?

input 0101 o/p 0110

input 1011 o/p Not possible

A BCD number abcd is incremented. Type condition
for carry ad (when $abcd = 9$) [a, b'c', d]

Binary number pqrs is a binary number.

In this 1 is added. Condition for carry pqrs

uvhm is increment of BCD abcd. Carry is t.

$$t = a \cdot d$$

$$m = d'$$

$$h = \text{if } abcd = 9 \text{ then } (d \cdot c' + c \cdot d') \text{ if } abcd \neq 9$$

$$v = (cd \text{ xor } b) \cdot (a' + d') \text{ or } (cd \text{ xor } b)$$

$$u = (bcd \text{ xor } a) \cdot (a' + d')$$

$$= bcd + d' \cdot a$$

Binary pqrs and 1 is added let xyzw is obtained and carry is q.

$$q = f \cdot q \cdot H.S$$

$$w = s'$$

$$z = s \cdot q' + s' \cdot r = \text{xor}(s, q)$$

$$y = n \cdot s \cdot q' + (q \cdot s)' \cdot q' = n \cdot s \text{ xor } q$$

$$x = q \cdot r \cdot s \cdot p' + (q \cdot r \cdot s)' \cdot p = q \cdot r \cdot s \text{ xor } p$$

Binary number abcd $\leq 7 \rightarrow a'$
 BCD abcd $\leq 7 \rightarrow a' \text{ (same)}$

Binary number abcd $> 7 \rightarrow a + bcd$
 BCD abcd $> 7 \rightarrow a + bcd \text{ (same)}$

$\left\{ \begin{array}{l} \text{Input } x, y \text{ o/p } z \\ z \text{ is } 1 \text{ when } x=1 \text{ and } y=0 \text{ or } x=0 \text{ and } y=1 \\ z = x \text{ xor } y = x'y + x'y' \end{array} \right.$

Input p, q o/p r
 $r=1$ when $p=1$ and $q=0$
 or $p=0$ and $q=1$

input $p, q = 11$ not possible

$$r = p+q$$

Take $p, q = 11$ as $o/p = 1$

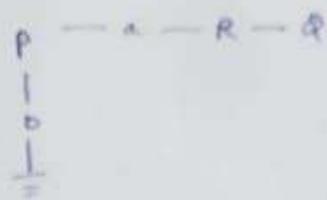
$$p' \cdot q + p \cdot q' + p \cdot q = (p' \cdot q')' = p+q \quad y$$

$$\cdot a+b$$

Between P and Q put switch a

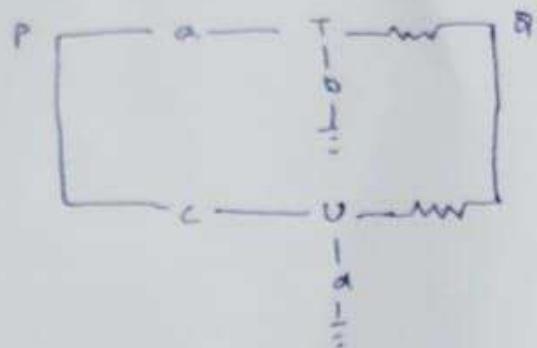
$$\times \quad \times \quad \times \quad a \quad a \quad b$$

$$\cdot a.b'$$



$$\cdot c.d' + a.b'$$

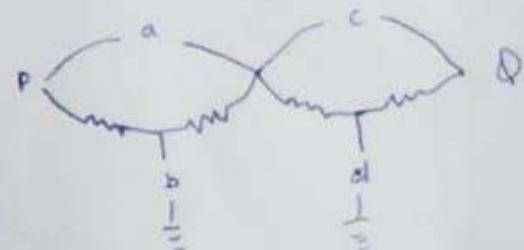
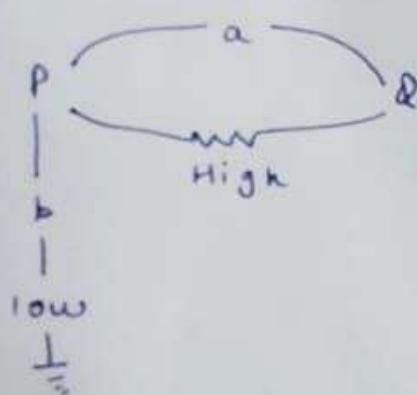
This is wrong why?



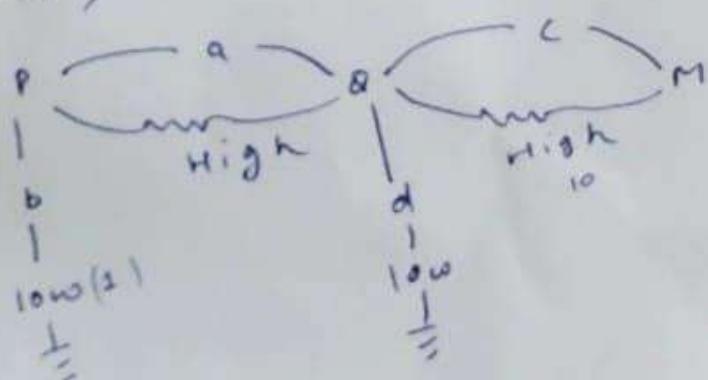
In this case, it will fail

$ab \text{ 11}$	$cd \text{ 10}$
$ab \text{ 10}$	$cd \text{ 11}$

$$\cdot a+b'$$



$$\cdot (c+d').(a+b')$$



$a=1, b=1$ reach Q
 $c=0, d=0$ Pa Q ROM

has more resistance

Pb1 earth has less resistance

And $(x, y) = x \cdot y$ $x * y$ y is 0 or 1.
 Or $(x, y) = x + y$ add x and y atleast one of x or y is 0
 (23)

$$z = C \cdot b + A \cdot b'$$

$$\begin{array}{ll} b=0, & a=\text{retain} \\ b=1, & a=c \end{array}$$

There are two inputs % one of them is control input (b)
 and one is general input (c)

Edge Triggered flip flop + o/p change only when control input change

b : control input 0, then o/p does not change even when input changes

when control input 1, then o/p is same as general input

$$c = 89, b = 0 \quad \text{o/p } g: \text{garbage}$$

$$c = 67, b = 0 \quad \text{o/p same } g$$

$$c = 67, b = 1 \quad \text{o/p } 67$$

$$c = 82, b = 1 \quad \text{o/p } 82$$

$$c = 82, b = 0 \quad \text{o/p } 82$$

$$c = 56, b = 0 \quad \text{o/p } 82$$

$$c = 92, b = 0 \quad \text{o/p } 82$$

$$z = C \cdot b + A \cdot b'$$

$$d = A \cdot b' + D \cdot b$$

$$c = 89, b = 0 \quad a = g \quad d = g \text{ (same)}$$

$$c = 67, b = 0 \quad a = g \text{ (same)} \quad d = g \text{ (same)}$$

$$c = 67, b = 1 \quad a = 67 \quad d = g \text{ (same)}$$

$$c = 82, b = 1 \quad a = 82 \quad d = g$$

$$c = 82, b = 0 \quad a = 82 \quad d = 82$$

$$c = 56, b = 0 \quad a = 82 \quad d = 82$$

$$c = 92, b = 0 \quad a = 82 \quad d = 82$$

$$c = 92, b = 1 \quad a = 92 \quad d = 82$$

Decoder and Encoder

(24)

Decoder

D(a, b) it has many outputs (binary)

a: enable binary

b: address general

a = 0 all outputs are zero

a = 1 then exactly one output is 1.

D(1, 011) → 00010000

D(0, any) → 00000000

D(1, 110) → 000000010

$$pqnsuvwxyz = D_3(a, bcd) \text{ or } D_8$$

Design D₃ using D₂'s

$$uvwxyz = D_2(a'b', cd)$$

$$pqns = D_2(a'b', cd)$$

$$D_3(a, bcd) = D_2(a \cdot b', cd) \quad D_2(a \cdot b', cd)$$

Encoder

Has multiple input.

Atmost one input is 1.

output address of non-zero input

E₈(00100000) → 1,010

E₈(00000000) → 0, any

E₈(pqnsuvwxyz) → a, bcd

E₈(00100100) → non-permitted input

E₄(0010) → 1,10

$$x, yz = E_4(pqns)$$

$$e, gh = E_4(tuvwxyz)$$

$$\begin{aligned} a &= x + e \\ bcd &= x \cdot (0yz) + e \cdot (1gh) \end{aligned}$$



SHOT ON REDMI 7
AI DUAL CAMERA

$bcd = E7(pqrstu)$ Atmost one input is 1.

Previously p was at location zero but now at location 1, output bcd

if o/p is 000 if all inputs are 0.

$$E7(0010000) = 011$$

$$E3(000) = 00$$

$$E3(010) = 10$$

E7 using E3

$$E3(pqr)$$

$$\{E3(pqr)A\} \quad E3(stu)$$

$$(pqr \{ E3(stu))$$

→ Pipeline Architecture : Instruction bypass -

let $a = 12, b = 17, c = 13, d = 51$

$$a = b + c \quad 0 - 40 \quad a = 30$$

$$d = a + 9 \quad 10 - 50 \quad d = 21 / 39$$

$$e = a + 15 \quad 20 - 60 \quad e = 27 / 45$$

$$f = a + 19 \quad 30 - 70 \quad f = 31 / 49$$

$$g = a + 20 \quad 40 - 80 \quad g = 50$$

$$\text{print}(d) \quad 50 - 80$$

$$\text{print}(e) \quad 60 - 90$$

$$\text{print}(f) \quad 70 - 100$$

$$\text{print}(g) \quad 80 - 110$$

Now the question is when $a = 30$ is successful

We are sure $a = 30$ after $t = 40$, but before that we cannot be sure where it occurs.

Let some architectures have 1 instruction bypass
Output = 21 45 49 50

2 instruction bypass

Output = 21 27 49 50

3 instruction bypass

" = 21 27 31 50

1-instruction bypass

if $\text{print}(g)$ → garbage,

" (b) → 49

" (e) → 45

" (d) → 21

0101
1010 1011

0110
1011 1010

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Negative number Multiplication

A number in 4 bits. $-8 \dots +7$

$$+5 = 0101 \quad -5 = (0101)' + 1 = 1010 + 1 = 1011$$

The product of two numbers in 8 bits

$$(+5) * (+7) = +35 = 001000011$$

$$(-5) * (+7) = (1011) * (0111)$$

$$\begin{array}{r} 11 \times 7 \\ = 77 \end{array}$$

$$< 0100011001$$

So our microprocessor may interpret as

But we do not want this behaviour

$$+5 * 7 = -35 \text{ what is expected answer}$$

$$35 = 00100011$$

$$(-35) = (00100011)' + 1 = 11011100 + 1 \\ = 11011101$$

How to multiply & negative numbers?

Subtract the Counterpart negative number from first four bits of output

$$-5 * 7 = 100(1011) * (0111) \\ = 01001101$$

last four bits will

Now subtracting,

$$\begin{array}{r} 01001101 \\ 0111 \cancel{0000} \\ \hline 11011101 \end{array}$$

we do it
is'

NOTE $-x = 2^n - x$

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Subtracting binary

$$\begin{array}{r} 0100 \\ - 0111 \\ \hline 1101 \end{array} \quad \left. \begin{array}{r} 435 \\ 287 \\ \hline 148 \end{array} \right\} \text{similar} \quad \begin{array}{r} 287 \\ - 435 \\ \hline 852 \end{array}$$

we just take the carry and forget about it.

$$+ 6 \rightarrow 0110, - 6 \Rightarrow 1001 + 1 \\ = 1010$$

$$- 6 * 4 = (1010) * (0100) = 10 * 4 \\ = 40 \\ = 00101000$$

$$\begin{array}{r} 00101000 \\ 0100 \\ \hline 11101000 \end{array}$$

NOTE $-x = 2^n - x$
where x is in binary representation
and n is no. of bits for representation

$$\rightarrow 11101000 \\ = -[00010111 + 1] = -00011000 \\ = -24$$

$$\begin{aligned}
 (-6) * (-5) &= (1010) * (1011) \\
 &= 101110 \\
 &= 01101110
 \end{aligned}$$

~~01101110
1011
1010
1101
1010
0111~~

$$\begin{array}{r}
 01101110 \\
 -1011 \\
 \hline
 10111110 \\
 -1010 \\
 \hline
 0001110 \\
 \hline
 = (30)
 \end{array}$$

(Subtracting
-5 from
first 4
bits)

(Subtracting
-6 from first)
4 bits

abcd * pqrst if ~~ab~~ a.p = 1 then
both are negative then we can treat them
as positive but designing this type
of circuitry with many if's is not
easy.

Send Mail ~~not~~ related to

- 1) Why above ~~false~~ multiplication logic is correct?
- 2) Logic for division?

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Multiplication of two 2 digit numbers with a 4 digit number

Let a number in 2 base 10 digits.

$$0 \dots 99 \quad -50 \dots +49$$

Now a negative number is represented \rightarrow by adding 100.

$$\text{What if } -35 \rightarrow -35 + 100 = 65$$

$$40 * -20 = 40 * 80 = 3200$$

$$\begin{array}{r} 3200 \\ -40 \\ \hline 9200 \\ -800 \\ \hline \end{array}$$

0 to 49 are +ve
50 to 99 are -ve

$$\text{How to multiply } 40 * 70 = 2800$$

\rightarrow Let 0 to 80 are positive \rightarrow (0 to 9000 are positive)
Then 0 to 2800 is correct

\rightarrow Now, if 0 to 60 are positive

$$\begin{array}{r} 2800 \\ -40 \\ \hline 8800 \\ -800 \\ \hline -1200 \end{array}$$

this means
in 4 digits
(0 to 6000 are positive)

\rightarrow (0 to 3000 are positive)

\rightarrow Now if let 0 to 30 are positive

$$\begin{array}{r} 2800 \\ -40 \\ \hline 8800 \\ -7000 \\ \hline -1800 \end{array}$$

Checking continuity

$$40 \rightarrow -60$$

$$(730) \rightarrow$$

$$-30$$

$$70 \rightarrow$$

$$(730) \rightarrow$$

$$-30$$

$$(-60)(-30) = 1800$$

So, Rage need not to be 50-50

(In currency we take rage (for positive and negative) to be 50-50 because we determine sign by MSB, but that is not necessary)

(we can divide rage any way we want and answer will depend upon that :)

→ There are three possible ~~other~~ answers for $40 * 70$ depending upon how rage is divided

→ both positive, one negative, both negative

How $(1800)_{40}$ is done for different rage?

* Notation : $[a, b, c, d; T]$ means
 $az + by + cz + dw \geq T$
 a, b, c, d are numbers and x, y, z, w are
boolean variables 0/1
 $[5, 7, 9, 20; 25] \rightarrow 5x + 7y + 9z + 20w \geq 25$
 $w(x+y+z)$

$$[5, 7, 9, 15; 17] \rightarrow w(x+y+z) + w'xyz = w(x+y+z) + xyz$$

What type of boolean expressions can be represented by it

Let $[12, 56, 34, 78, 53; 143]$ be $P(x, y, z, w, u)$

Let $[12, 56, 34, 78, 53, 113]$ be $Q(x, y, z, w, u)$

$$P \rightarrow Q$$

If P is true, then Q is true

Only following type can be represented

$X.Q + P$ where $P \rightarrow Q$ [P and Q are expression without w]

$$w.(z+xy) + z(x+y)$$

Design for $z(x+y)$ and $z+xy$ and here $z(xy) \rightarrow zxy$

$$[2, 4, 10, 11] \quad [2, 4, 10, 6]$$

$$[5, 7, 20, 22] \quad [5, 7, 20, 12]$$

$$w.(z+xy) + z(x+y) = [5, 7, 20, 10, 22]$$

$$\text{z} \leftarrow 12$$

$$z + x'y$$

$$[-2, 9, 10, 8]$$



SHOT ON REDMI 7
AI DUAL CAMERA

SR and JK flip flop

Let input a, b output are p, q

$$p = a + q'$$

$$q = b + p'$$

$$ab = 01 \quad pq = 01$$

$$ab = 10 \quad pq = 10$$

$$ab = 11 \quad pq = 11 \quad [\text{input } 11 \text{ never}]$$

$$ab = 00 \quad pq = \text{retains both}$$

JK flip flop

Input u, v
output is p, q

$$a = u \cdot q$$

$$b = \cdot \cancel{p} \cdot v \cdot p$$

Then SR flip flop

$$uv = 01, \text{ initial } pq = 01$$

$$\begin{array}{l} a=0 \\ b=0 \end{array} \quad \text{then retain as } 01$$

$$uv = 01 \quad \text{initial } pq = 10$$

$$\begin{array}{l} a=0 \\ b=1 \end{array} \quad \text{then } 01$$

$$uv = 01 \quad \text{then } pq = 01 \quad \text{by either way}$$

$$uv = 00 \quad pq = \text{retain}$$

$uv = 10$ is similar to $uv = 01$

$$uv = 11 \quad \text{initial } pq = 01$$

$$\begin{array}{l} ab = \phi 1 \\ ab = \phi 0 \end{array}, \quad \begin{array}{l} \phi 0 \\ \phi 1 \end{array}$$

p, q is complemented

add (0,0) = no carry (n)

add (1,1) = carry (c)

add (0,1) = n

Let a and b be digits.

add (0a, 0b) = n (N) [0,0]

add (1a, 1b) = c (c) [1,1]

add (1a, 0b) = undecided (U) [0,1]

[1,0] will be
used
later

{ add (p, q) }

add (abcd, efg) How to determine carry status.

abcd efg & ij are 0/1.

Let xyzw be N, c or U.

Let add (ai, ej) = x

add (bi, f) = y

add (ci, g) = z

add (di, h) = w

$$x|y|z|w = (x|y)|(z|w)$$

Let p, q, r, s be N, c, U

p|r = c if p is c

p|q = N if p is N

p|q = q if p is f0)U

How to find of add (abcd, efg)

add (abi, ej) = p

add (cdi, ghj) = q

carry status

add (ai, bi) = [a·b, a+b]

Now p|q

• $A \circ B \circ D \dots \circ Y$ are states.

0, 1, 2, 3 are inputs

let initial state is A.

let input string is 02013

$A \circ B \circ E \circ G \circ 1 \circ A \circ 3 \circ G$

Automata $(A \circ B) (A \circ \tau) (B \circ C) (B \circ E) (B \circ E) (C \circ D) (C \circ F) (E \circ B)$
 $(E \circ G) (D \circ A) (E \circ Y)$

let input 0231

$A \circ B \circ E \circ 3 \circ E \circ Y$

let input 013

$A \circ B \circ C \circ 3 \circ F \rightarrow$ not correct

$A \circ B \circ D / (\text{not } C) 3 \cancel{\circ} F$

• $(A \circ B) (B \circ C) (C \circ B) (B \circ Y) (C \circ W)$

0 1 2

$A \circ B \circ 1 / (\text{toggle } B \circ C) 3 / (\text{toggle } Y \circ W)$

\cancel{F}
wrong

$A \circ B \circ 1 / (\text{toggle } B \circ C) 3 / (Y \text{ or } W \text{ uncertain})$

If $B \circ Y$ is not there then after 3 (B or W uncertain)

$(A \circ S)$

• $(P \circ Q)^P (Q \circ R)^T (T \circ U)^S (S \circ V)^U$

$(Q \circ T)$

Input $\rightarrow 03$ initial P

$P \circ Q \circ 3 \circ (Q \circ R)$

$P \circ Q \circ 3 \circ U$

$(Q \circ T) [S / T] 3 \circ U$

- $(A_0 B) (B_1 C) (B_0 \cancel{E}) (B_3 G) (C_2 D) (E_0 H)$
- $\vdots (A_0 S) (B_1 C) (B_3 G) (C_2 D) (D_3 H) (H_3 K)$
- $(A_0 B) (B_1 C) (B_3 G) (G_2 H) (H_2 J) (J_2 K) (B_2 L)$

012

$A_0 B_1 C_2 C \rightarrow$ wrong

1:01 → 2:10

012 is for 0102 or 0132

$A_0 B_1 C_0 C_2 C$ or $A_0 B_1 C_3 C_2 C$
 $\{ A_0 B_3 G_2 (H \text{ is toggle}) \}$

x+y

{ $x + ny = 01$ is given}

$ny = 01 \rightarrow 10$ how to transit?

01 to 10 should be via 11

$$n \cdot y + z \cdot y' + u \cdot z \quad \text{optimize it}$$

$$= ny + z \cdot y'$$

$\{ nyz + ny'zy \}$

Difference ???

• $S(a, b, c, d; p, q)$

$$p, q = 00 \quad o/p : a$$

$$p, q = 01$$

$$p, q = 10$$

$$p, q = 11$$

$S(a, b, c, d; y, y')$ will output what?

{a and d will never be outputted} \Rightarrow not always correct

when delay then 'a' 'd' can be output

$$\begin{array}{c} a \\ \downarrow \\ y_0 \\ b \\ \downarrow \\ 1 \end{array} \quad \begin{array}{c} d \\ \downarrow \\ y \\ \downarrow \\ 0 \end{array}$$

a and d can be outputted for short time.

$Z = S(a, z, z, d; p, q)$

$$p=0 \quad q=1 \quad \text{retain}$$

$$a=56 \quad d=67 \quad pq = 11, \quad Z = 67$$

$$a=56 \quad d=67 \quad pq = 01, \quad Z = 67$$

$$a=56 \quad d=89 \quad pq = 01, \quad Z = 67$$

$$a=56 \quad d=89 \quad pq = 00, \quad Z = 56$$

$$a=56 \quad d=89 \quad pq = 01, \quad Z = 56 \quad \{ \}$$

$Z = S(a, z, z, d; y, y')$

$$a=56 \quad d=67 \quad \{ p \} \quad y=1, \quad Z = 8 \quad \text{stable}$$

$$a=\cancel{56} \quad d=67 \quad y=0, \quad Z = 56 \quad \left(\begin{array}{l} \text{due to} \\ \text{delay} \end{array} \right) \text{ or same } \left(\begin{array}{l} \text{no} \\ \text{delay} \end{array} \right)$$

$$a=74 \quad d=67 \quad y=0, \quad Z = 56$$

$$a=74 \quad d=67 \quad y=1, \quad Z = 67 \rightarrow \text{stable}$$

delay of S is 10 sec \rightarrow shift output

delay of not is 2 sec \rightarrow duration

$$a = 56 \quad d = 67 \quad y = 1 \quad o/b \quad g = 81$$

$$\text{At } t = 50 \quad y = 0$$

during $t = 50 - 52$ both y and $y' = 0$

during $50 - 62$ z is 56.

$$t = 52 - 60 \quad y = 0 \quad y' = 1 \quad \text{hence } z = \text{aetain}(t-10)$$

during 62 onwards $\rightarrow z$ is 81 again

$$62 - 70 \quad z = 81$$

$$70 - 72 \quad z = 56$$

$$72 - 80 \quad z = 81$$

$$u = S(a, b; w)$$

$$w = 0 \quad u = a \quad w = 1 \quad u = b$$

Delay in S is 10

$$a = 34 \quad b = 67$$

$$w: 0 \rightarrow 1, \text{ at } t = 50$$

at $t = 60$, u changed from 34 to 67

$$2: 34 \rightarrow 55 \text{ at } t = 47$$

$$\text{at } t = 50 \quad w: 0 \rightarrow 1$$

$$v = S(d, v; k)$$

$$d = 81 \rightarrow 25 \text{ at } t = 47$$

$$k = 0$$

what is o/b v ?

$$k = 0 \rightarrow 1 \text{ at } t = 50$$

$$0.57, v = 81$$

$$t > 57, v \text{ is } 25$$

Meeting in "General"

59:21

Leave

GS

pawan Krishna Nai... Vishal Prakash San... Pradyumna ... +54 GS

Meeting chat

"General"

Join

sir can we convert whole c program using this circuit ?

Rapeti Tridev 12:55 Sir semi-colon

Pradyumna Peddula 12:55 semicolon

Gaurav Jain 12:55 sir semicolon

Sagnik Sahana 12:55 semicolon

Gaurav Jain 12:55 3,39
6,3
8,1
12,4
6,4
2,3

Type a new message

Gaurav Jain replied to a conversation you're in COA / General

*c - Notepad

```
y=S(a,b,c,d,p+q,p-q,p*q,p/q;v)
k[i]=Decoder(u)
a=S(a,y;k[0]) b=S(b,y;k[1]) d=S(d,v;k[3])
p=S(p,y;k[6]) q=S(q,y*k[7]+v*k[8];k[7]+k[8])
c=S(c+1,v;k[2])<--delete it
c=S(c+1,v;k[2]+k[4]).(p>a)+k[5].(p>a))
when k[12] is 1 then y is printed.

Write a program to print 47,47,47,47,..... infinite times
3,47 d=47
12,3 print(d)
2,1 c=1

print 20,21,22,23,24,..... infinite

3,19
6,3 p=19
8,1 q=1
12,4 print(p+q)=20
6,4 p=p+q
2,3

print 40,41,42,43,,44,45,
```

When K[12] is 1 then y is printed.

File Edit Format View Help

120% Windows (CRLF) UTF-8

29°C ENG 10-11-2021

12:55

27°C Smoke ENG 10-11-2021

- Let a, b, c, d, e be digits. Base 10.

$$5a + 7b \rightarrow \text{carry} = 1$$

$$3a + 4b \rightarrow \text{carry} = 0$$

$$3a + 6b \rightarrow a+b \geq 10 \text{ then carry } 1 \text{ (undecided)}$$

otherwise carry 0

Sum if $a+b=9$ then undecided

When two numbers are added and only their first digits are known then 3 possibilities

carry 0, carry 1, carry undecided

- Let 3 numbers are added.

Only first digits are known.

What are possible carries?

Sum of first digits let k

$k: 0 \dots 7$ carry 0

$k: 8, 9$ carry 0/1

$k: 10 \dots 17$ carry 1

$k: 18, 19$ carry 1/2

$k: 20 \dots 27$ carry 2

Access 8

Numbers are -8 to +7

Representation in 4 bits abcd

Every no. is represented by adding 8.

+3 is 11 \rightarrow 1011

-5 is 3 \rightarrow 0011

0101 \rightarrow $5 - 8 = -3$

+7 is 15 \rightarrow 1111

-7 is 1 \rightarrow 0001

-8 is 0 \rightarrow 0000

How to add? Normal addition ^{in shifts} MSB is carry.

Add +3 and -5

$$\begin{array}{r} 1011 \\ 0011 \\ \hline 01110 \end{array}$$

Normal add $0110 - 1000 = -2$

carry is transferred
to MSB

Add +3 and +7

$$\begin{array}{r} 1011 \\ 1111 \\ \hline 11010 \end{array}$$

+3 and +2

$$\begin{array}{r} 1011 \\ 1010 \\ \hline 10101 \end{array}$$

$1101 - 1000 = 0101$

* Normal addition. Let p₇ n₇ s₇. Ans = p₇ s₇

Multiply +5 and +7

$$+5 = 1101 \leftarrow 13$$

$$+7 = 1111 \leftarrow 15$$

expect +35 normal multiplication = 195

10100011 is expected

normal: 11000011

Multiply +5 and -3

output in access 128

$$+5 \text{ is } 1101$$

$$-3 \text{ is } 0101$$

$$\begin{array}{r} \text{normal multi = 65} \\ = 01000001 \end{array}$$

$$-15 + 128 = 113 = 01110001\cancel{000}$$

Multiplication Rule,

abcd is sign magnitude

+ = 0 a: is sign bd:magnitude

- = 1

+5 is 0101

-5 is 1101

+7 is 0111

-7 is 1111

pqrs is 2's complement

uvwxyz is access 8

express them in terms of each other.