

①

COA

- Internal Bus \Rightarrow ib
- a, b, c, \dots are general registers
- ALU - Arithmetic Logical Unit - performs arithmetic op.
 - uses special registers - " s " and " t "

1) How $a = 4$ will be executed.

~~$ib \leftarrow 4$~~ $ib \leftarrow 4$
 ~~$a \leftarrow ib$~~ $a \leftarrow ib$

2) How $a = a + 1$ will be executed

$ib \leftarrow a$
 $s \leftarrow ib$
 $ib \leftarrow 1$
 $t \leftarrow ib$
 $ib \leftarrow s + t$
 $a \leftarrow ib$

3) Printing the value of a ?

$ib \leftarrow a$
print(ib)

* PC: Program Counter - stores the line number which has to be executed next.

Hence PC is incremented regularly

2

* When 0th instruction is executed, it got incremented to 1 in background automatically

4) $a = 4$ print 5, 6, 7, 8, ...

do {

$a = a + 1;$

print(a);

} while(1);

10 Architecture

~~Architecture~~ program

0: $ib \leftarrow 4$

1: $a \leftarrow ib$

2: $ib \leftarrow a$

3: $s \leftarrow ib$

4: $ib \leftarrow 1$

5: $t \leftarrow ib$

6: $ib \leftarrow s + t$

7: $a \leftarrow ib$

8: $ib \leftarrow a$

9: print(ib)

10: $ib \leftarrow 2$

11: $PC \leftarrow ib$

→ Program Counter

Efficient Version -

0: $ib \leftarrow 4$

1: $s \leftarrow ib$

2: $ib \leftarrow 1$

3: $t \leftarrow ib$

4: $ib \leftarrow s + t$

5: print(ib)

6: $s \leftarrow ib$

7: $ib \leftarrow 4$

8: $PC \leftarrow ib$

$a, b, c \equiv$ general registers

$s, t \equiv$ arithmetic registers

→ only s, t can be used for ALU operations

From s and t , value cannot be read, can only be written.

Hence $ib \leftarrow s$ (not allowed)

$s \leftarrow ib$ (allowed)

$ib \leftarrow s + t$ (allowed)

(3)

- Program to print 5, 6, 8, 11, 15, 20, ...

Diagram showing the sequence of numbers and their differences:

5, 6, 8, 11, 15, 20, ...

Differences: +1, +2, +3, +4, +5

```
5 a = 5
  b = 0
  do {
    a = a + b
    Print(a)
    b = b + 1
  } while(1)
```

- Code using only 3 counters - a, b and t.

```
15 0: ib ← -5
    1: a ← -ib
    2: ib ← -0
    3: t ← -ib
    4: ib ← -a
    5: b ← -ib
    6: ib ← -b + t
    7: a ← -ib
    8: Print(ib)
    9: ib ← -1
    10: b ← -ib
    11: ib ← -b + t
    12: t ← -ib
    13: ib ← -4
    14: PC ← -ib
```


(4)

→ AND and OR gate

AND - (\cdot)

OR - $(+)$

→ Boolean inequalities - $a, b, c, d \equiv \text{boolean variables}$

i) $5a + 7b \geq 3$ \Rightarrow $a=1$ or $b=1 \Rightarrow a+b$ Ans

ii) $8a + 3b \geq 10 \Rightarrow a=1$ and $b=1 \Rightarrow a \cdot b$

iii) $3a + 7b + 2c \geq 8 \Rightarrow b=1$ and $(a \text{ or } c)=1 \Rightarrow b \cdot (a+c)$

iv) $7a + 4b + 3c \geq 6 \Rightarrow a=1$ or $(b=1 \text{ and } c=1)$
 $\Rightarrow a + b \cdot c$

v) $7a + 4b + 3c + 20d \geq 26 \Rightarrow d=1$ and $(a=1 \text{ or } (b=1 \text{ and } c=1))$
 $\Rightarrow d \cdot (a + b \cdot c)$

vi) $3a + 7b + 2c + 20d \geq 8 \Rightarrow d=1$ or $(b=1 \text{ and } (a=1 \text{ or } c=1))$
 $\Rightarrow d + (b \cdot (a+c))$

vii) $7a + 4b + 3c + 20d + 22e \geq 26$

$\Rightarrow e=1$ and $(d=1 \text{ or } a=1 \text{ or } (b=1 \text{ and } c=1))$

$e=0$ and $(d=1 \text{ or } (a=1 \text{ or } (b=1 \text{ and } c=1)))$

$\Rightarrow e \cdot (d + a + b \cdot c) + d \cdot (a + b \cdot c)$

$\Rightarrow ed + (e+d) \cdot (a + b \cdot c)$

(5)

viii) $5a - 7b \geq -4 \Rightarrow$ Everything other than $a=0$ and $b=1$
 $\Rightarrow (a', b)' \Rightarrow a+b'$

ix) $7a + 4b - 3c + 20d \geq 23$

if $c=0 \Rightarrow 7a + 4b + 20d \geq 23 \Rightarrow d \cdot (a+b) \therefore \Rightarrow c' \cdot d \cdot (a+b)$

if $c=1 \Rightarrow 7a + 4b + 20d \geq 26 \Rightarrow a \cdot d$ (No role of b here)

\therefore Net Answer $\Rightarrow c' \cdot d \cdot (a+b) + c \cdot a \cdot d$
 $\Rightarrow d \cdot (c'(a+b) + (a))$
 $\Rightarrow d \cdot (a + c' \cdot b)$

1— Write inequality for the solⁿ $a + b' \cdot c$

\Rightarrow True when $a=1$ or $(b=0 \text{ and } c=1)$

$10a - 4b + 6c \geq 5$

2— $a \cdot b + c \cdot d$

$a + b + c + d \geq$

$$\underline{a \cdot b + c \cdot d}$$

$$pa + qb + rc + sd > x$$

$$- \quad p + q > x \quad (1)$$

$$r + s > x \quad (2)$$

$$p + r < x \quad (3) \quad p + s < x \quad (5)$$

$$q + s < x \quad (4) \quad q + r < x \quad (6)$$

$$p < x$$

$$q < x$$

$$r < x$$

$$s < x$$

Adding (1) and (2),

$$p + q + r + s > 2x$$

Adding (3) and (4)

$$p + q + r + s < 2x$$

No solⁿ

Similarly we can prove ~~for~~ No solⁿ for.

$$pa + qb + rc + sd \leq x$$

— Boolean variables can take only two values 0, 1.

— $K=0 \Rightarrow K'$; $K=1 \Rightarrow K$

— $101 > 011$; $011011 > 010100$

— For $a > P$, condition $\Rightarrow a=1$ and $P=0 \Rightarrow a.P'$

— For $a = P$, condition $\Rightarrow (a=1$ and $P=1)$ or $(a=0$ and $P=0)$
 $\Rightarrow aP + a'P'$

— $ab > pq \Rightarrow 11 > 10; 11 > 00; 11 > 01;$
 $10 > 01; 10 > 00$
 $01 > 00;$

$(a.b.(P+P'+Q')) + a.b'.P' + a'b.P'Q'$

$\Rightarrow aP' + abQ' + a'bP'Q'$

$\Rightarrow aP' + bQ'(a+a'P')$

2nd Approach - $(a > P) \text{ OR } (a = P \text{ and } (b > q))$

$(a=1; P=0) \text{ OR } ((a=1; P=1; b=1, q=0) \text{ OR } (a=0; P=0; b=1, q=0))$

$\Rightarrow aP' + (aP + a'P').bQ'$

— $a \geq P \Rightarrow (a < P)' \Rightarrow (a'.P)' \Rightarrow \underline{a+P}$
 $(0 < 1) \Rightarrow 1$

— $abc > pqr \Rightarrow (a > P) \text{ OR } (a = P \text{ AND } (b > q))$

SOME PROPS

* $K + K.U \Rightarrow K(K+U) = K+U$

* $K + K.1 \Rightarrow K(1+1) \Rightarrow K$

$$* K.U + K'.U = (K+K').U = U$$

$$* a.b + a.c = a.(b+c)$$

$$* (y+z).(y+w) = y+(z.w)$$

$$* 101 + 011 = 1000$$

$$100 + 101 = 1001$$

$$011 + 010 = 0101$$