

9. I-V relationships in active region: (Low to medium freq.)

$$i_E = i_C + i_B = (1+\beta) i_B$$

$$i_C = \beta \cdot i_B = \alpha \cdot i_E = \left(\frac{\beta}{1+\beta}\right) i_E$$

$$\alpha = \frac{\beta}{1+\beta}$$

$$\beta = \frac{\alpha}{1-\alpha}$$

npn

$$i_C = I_S \cdot e^{\frac{V_{BE}}{V_T}}$$

$$i_E = \frac{i_C}{\alpha} = \frac{I_S \cdot e^{\frac{V_{BE}}{V_T}}}{\alpha}$$

$$i_B = \frac{i_C}{\beta} = \frac{I_S \cdot e^{\frac{V_{BE}}{V_T}}}{\beta}$$

pnp

$$i_C = I_S \cdot e^{\frac{V_{EB}}{V_T}}$$

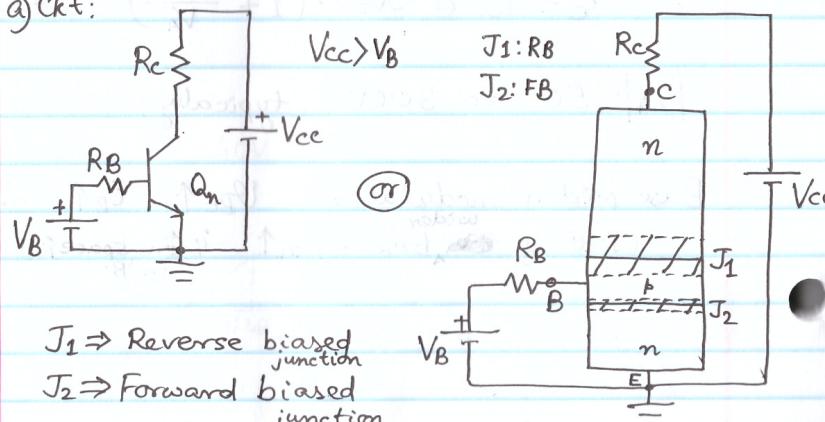
$$i_E = \frac{i_C}{\alpha} = \frac{I_S \cdot e^{\frac{V_{EB}}{V_T}}}{\alpha}$$

$$i_B = \frac{i_C}{\beta} = \frac{I_S \cdot e^{\frac{V_{EB}}{V_T}}}{\beta}$$

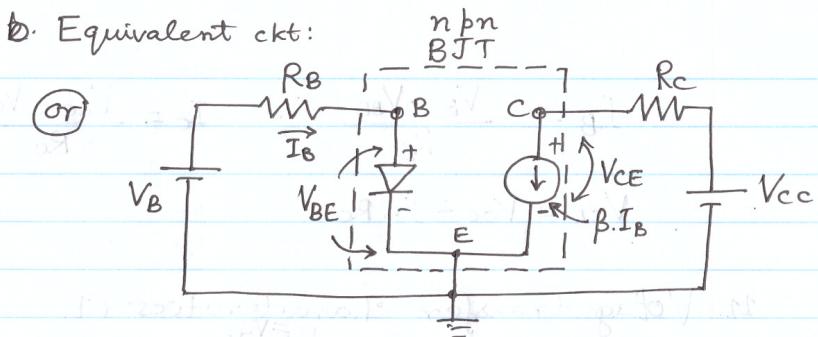
(without early effect).

10. Active region in common-emitter configuration:

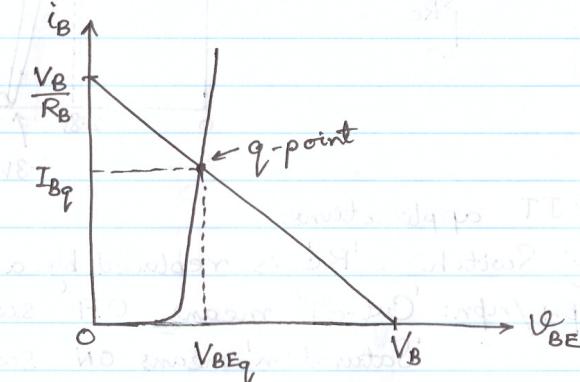
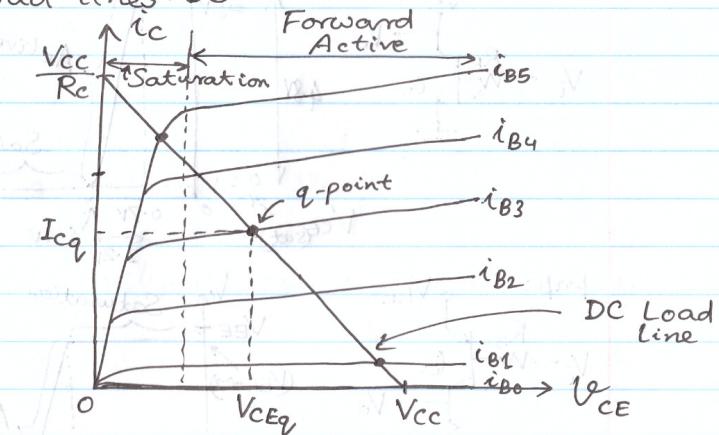
a) Ckt:



b. Equivalent ckt:



c. Load lines: DC



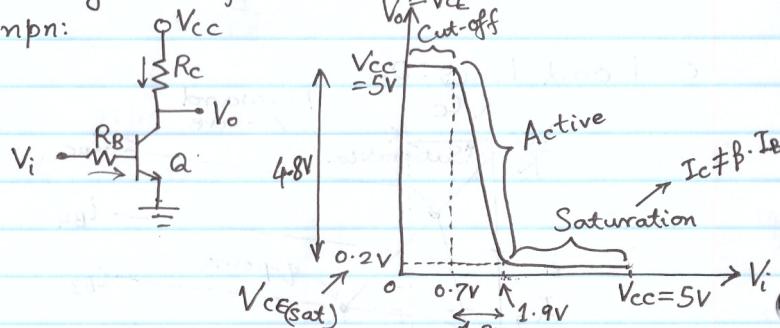
$$I_B = \frac{V_B - V_{BE}}{R_B}$$

$$I_C = \frac{V_{CC} - V_{CE}}{R_C}$$

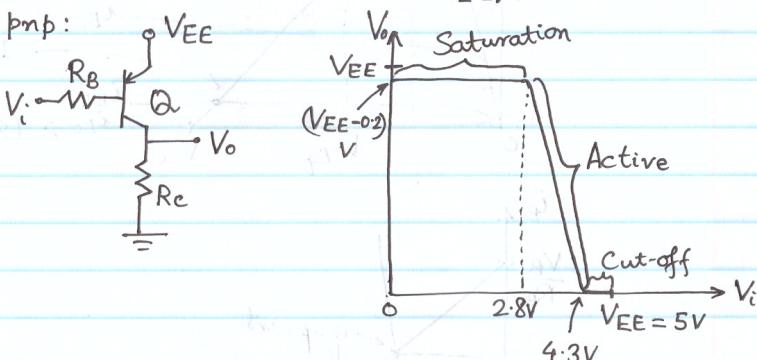
$$V_{CE} = V_{CC} - I_C \cdot R_C$$

### 11. Voltage transfer characteristics: CE

npn:



pnp:

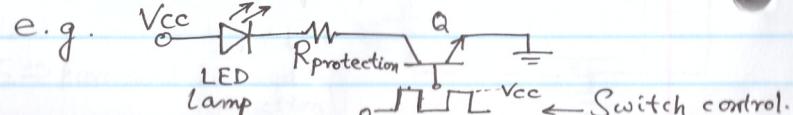


### 12. BJT applications:

a) Switch : 'Rc' is replaced by a load (e.g. an LED)

pnp/npn: 'Cut-off' means OFF switch 'Q'

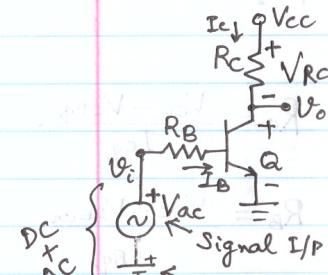
'Saturation' means ON switch 'Q'



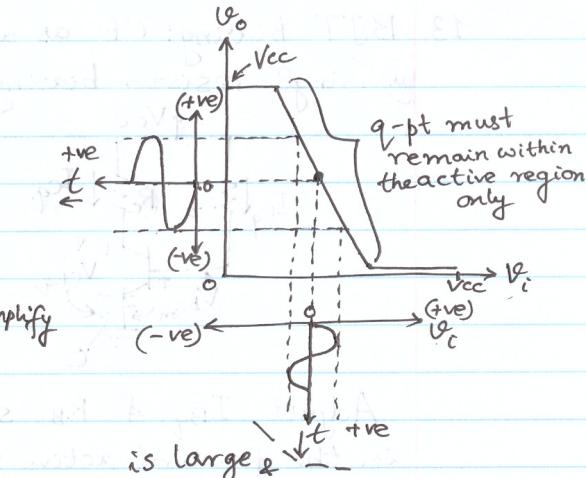
Normalized '0'

V-amplifier  $\rightarrow$  Low/med.freq

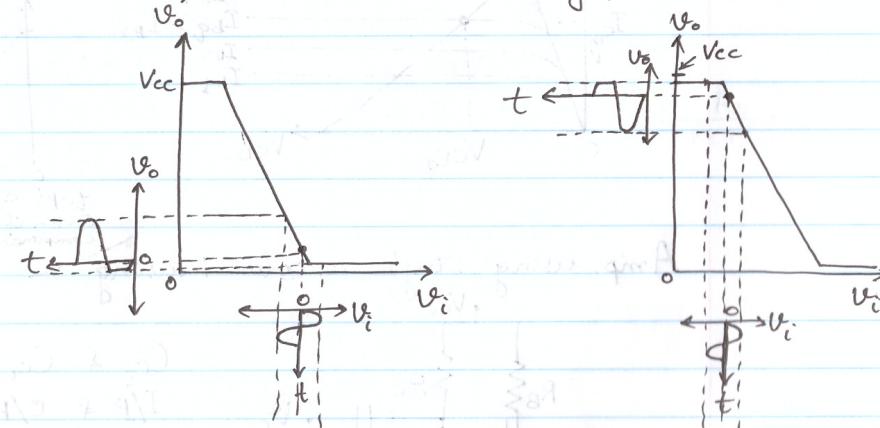
### b. Amplifier: CE



DC { Signal I/P to amplify  
AC { Biassing (q-pt.)  
Vdc { Active reg.



For any instance, if  $V_i$  forces the transistor Q to operate outside the active region (to either cut-off or saturation), a clipped output voltage  $(V_o)$  will appear.



Gain (Voltage) :  $A_v = \frac{\Delta V_o}{\Delta V_i}$

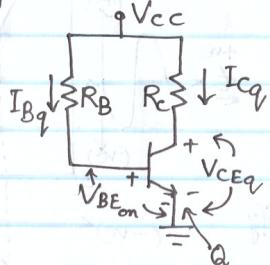
$$A_v = \frac{\Delta V_o}{\Delta V_i}$$

Y-axis: collector current

proportional to collector current

### 13. BJT biasing: CE as an amplifier (amp.)

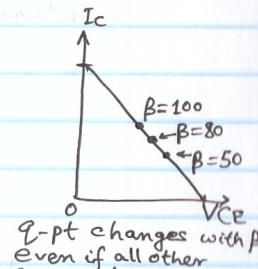
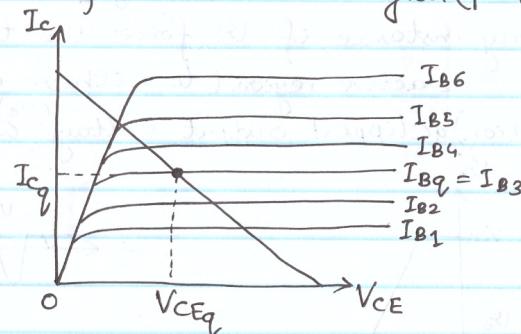
#### a) Single resistor biasing:



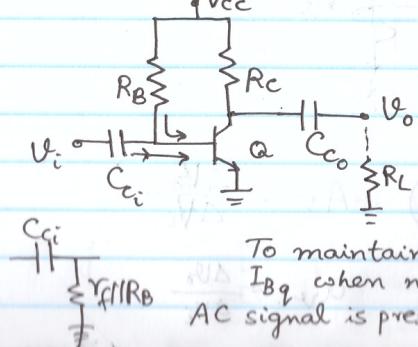
$$R_c = \frac{V_{cc} - V_{ceq}}{I_{cq}}$$

$$R_B = \frac{V_{cc} - V_{beon}}{I_{Bq}}$$

Adjust  $I_{Bq}$  &  $R_B$  such that the q-pt is located in the forward active region (preferably at the middle)



Amp. using Single resistor biasing



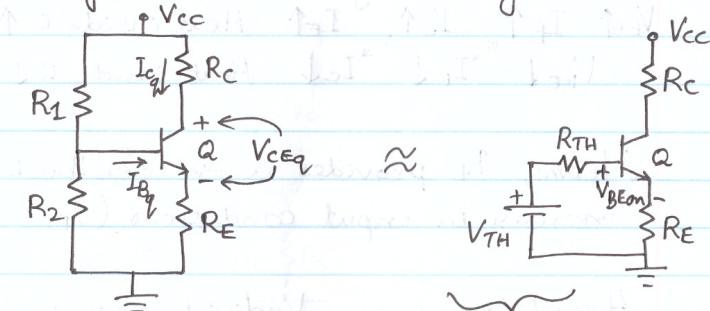
$C_{ci}$  &  $C_{co}$  are I/P & O/P

coupling capacitors  
(eliminates DC offsets at I/P & O/P)

To maintain  $I_{Bq}$  when no AC signal is present

Drawback: Bias instability due to temperature change

#### b) Voltage/resistor divider biasing:



Thevenin's equivalent  
base driving ckt.

Advantage: Improved bias stability due to temp. change. Ratiometric connection of  $R_1$  &  $R_2$  reduces the change in  $V_{TH}$  &  $R_{TH}$ , which helps in improving bias stability with temp. variation.  
 $\therefore \beta \gg 1$

$$R_{TH} = R_1 // R_2 \approx 0.1(1+\beta) R_E$$

$$V_{TH} = I_{Bq}.R_{TH} + V_{BEon} + I_{Eq}.R_E \approx \frac{R_2}{R_1 + R_2} \cdot V_{cc}$$

$$I_{Eq} = (1+\beta) I_{Bq}$$

$$I_{Bq} = \frac{V_{TH} - V_{BEon}}{R_{TH} + (1+\beta) R_E}$$

$$I_{cq} = \beta \cdot I_{Bq} \approx \frac{V_{TH} - V_{BEon}}{R_E}$$

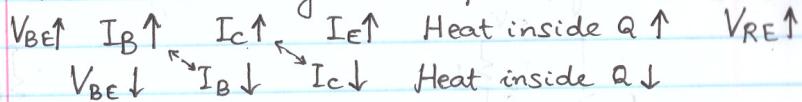
$$V_{ceq} = V_{cc} - I_{cq}.R_c - I_{Eq}.R_E$$

&  $V_{cc}$

Adjust  $R_1$  &  $R_2$ , such that the q-pt lies at the middle of forward active region.

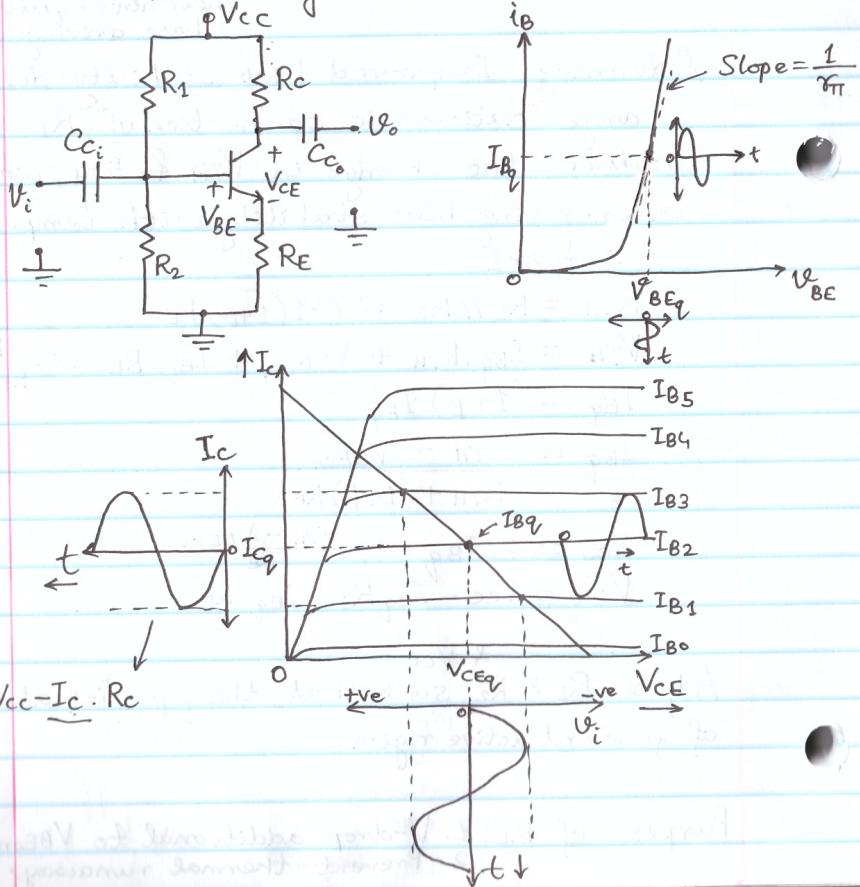
Purpose of  $R_E$ : 1. V-drop additional to  $V_{BEon}$  in base ckt.  
2. Prevent thermal runaway.

Thermal runaway: & its prevention.  $V_{RE}$  f/b



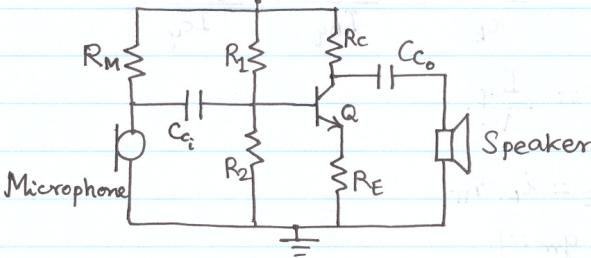
Means,  $R_E$  provides a -ve feedback with increase in input conditions ( $I_B$  &  $V_{BE}$ )

Amplifier using V-divider bias:

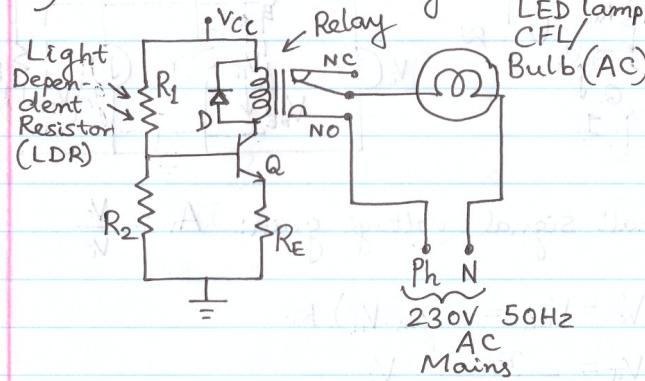


14. Applications of V-divider bias based CE amplifier:

1) Microphone amplifier:

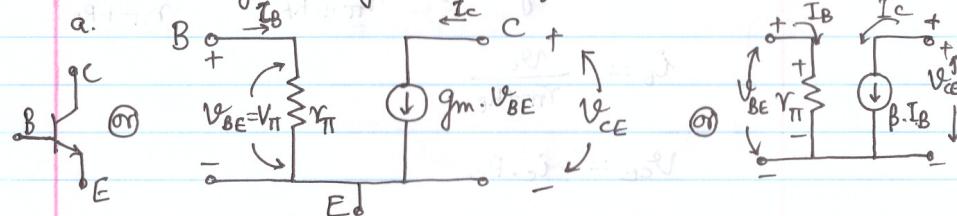


2) Automatic street light controller:



NC: Normally Closed  
NO: Normally Open  
D: Free-wheeling Diode

15. Small signal hybrid- $\pi$  equivalent ckt: CE



$r_{\pi}$  = Diffusion res. (B-E I/P res.)  
 $g_m$  = Transconductance.

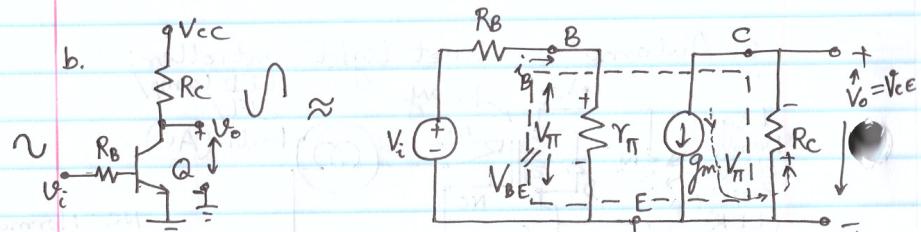
$$i_B = \frac{I_S}{\beta} \cdot e^{\frac{V_{BE}}{V_T}} ; \quad i_C = I_S \cdot e^{\frac{V_{CE}}{V_T}}$$

$$\gamma_{\pi} = \frac{V_{BE}}{i_B} = \frac{V_T}{I_{BQ}} = \frac{\beta \cdot V_T}{I_{CQ}}$$

$$g_m = \frac{I_{CQ}}{V_T}$$

$$V_{BE} = i_B \cdot \gamma_{\pi}$$

$$\gamma_{\pi} \cdot g_m = \beta$$



Small signal voltage gain:  $A_v = \frac{V_o}{V_i}$

$$V_o = V_{CE} = -(g_m \cdot V_{\pi}) \cdot R_c$$

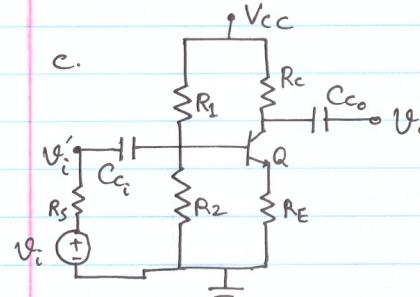
$$V_{\pi} = \frac{\gamma_{\pi}}{\gamma_{\pi} + R_B} \cdot V_i$$

$$\therefore A_v = -(g_m \cdot R_c) \cdot \frac{\gamma_{\pi}}{\gamma_{\pi} + R_B} = -\frac{\beta \cdot R_c}{\gamma_{\pi} + R_B}$$

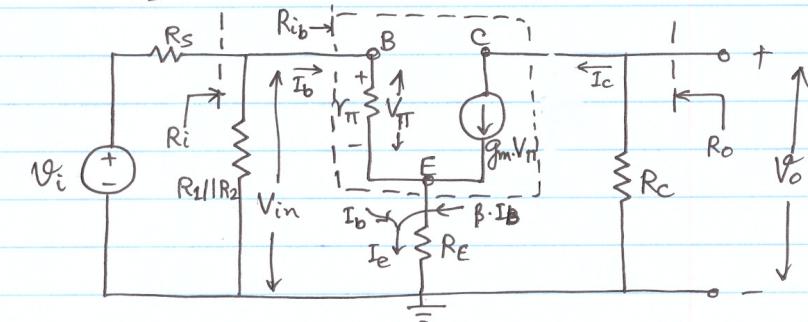
$$i_B = \frac{V_i}{\gamma_{\pi} + R_B}$$

$$V_{CE} = -i_C \cdot R_c$$

Note: Consider 'R<sub>o</sub> || R<sub>c</sub>' if R<sub>o</sub> is connected in parallel to 'g<sub>m</sub>V<sub>\pi</sub>' I-source.



AC small signal  
hybrid- $\pi$  model



$$V_o = -(\beta \cdot I_b) R_c = -I_c \cdot R_c$$

$$V_{in} = I_b \cdot \gamma_{\pi} + (I_b + \beta \cdot I_b) R_E$$

$$R_{ib} = \frac{V_{in}}{I_b} = \gamma_{\pi} + (1 + \beta) R_E \quad (\text{Resistance Reflection Rule})$$

$$R_i = R_1 // R_2 // R_{ib}$$

$$V_{in} = \frac{R_i}{R_i + R_s} \cdot V_i$$

$$A_v = \frac{V_o}{V_i} = \frac{-(\beta \cdot I_b) R_c}{V_i} = -\beta \cdot R_c \cdot \frac{V_{in}}{R_{ib}} \cdot \frac{1}{R_s}$$

$$= \frac{-\beta \cdot R_c}{\gamma_{\pi} + (1 + \beta) R_E} \left( \frac{R_i}{R_i + R_s} \right)$$

$$\approx \frac{-\beta \cdot R_c}{(1 + \beta) R_E} \approx -\frac{R_c}{R_E} \quad [ \because \beta \gg 1 \text{ & } R_i \gg R_s ]$$