

Digital Electronics Project:

By: Keeyan Haghshenas

RUID: 171000841

Parameters:

$$K_p' = 10 \mu\text{A}/\text{V}^2$$

$$K_n' = 35 \mu\text{A}/\text{V}^2$$

$$T_{pd} = 2\text{ns}$$

$$C_L = 4\text{pF}$$

Part 2:

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Parameters
 $K_p' = 10$
 $K_n' = 35$
 $T_{PD} = 2 \text{ ns}$
 $C_L = 4 \text{ pF}$

Part 2:

$T_{LH}: 0V \rightarrow 2.5$

$$V_{DSP(\text{avg})} = \frac{(5-0) + (5-2.5)}{2} = 3.75 \text{ V}$$

$3.75 < 5 - 1$: ohmic

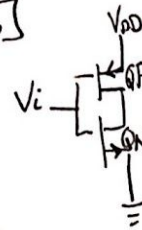
$V_{ASP} = 5 \text{ V}$

$V_{TP} = -1 \text{ V}$

$$I_{DSP} = K_p' (W_p/L_p) [(5-1)3.75 - 3.75^2/2]$$

$$I_{DSP} = K_p' (W_p/L_p) [7.96875]$$

$$I_{DSP(\text{avg})} = \frac{(4 \text{ pF})(2.5)}{2 \text{ ns}}$$



$$\frac{(4 \text{ pF})(2.5)}{2 \text{ ns}} = (10) (W_p/L_p) (7.96875)$$

$$\frac{4 \text{ pF}(2.5)}{2 \text{ ns}(10 \text{ mA/V}^2)(7.96875)} = [W_p/L_p] = [W_p/1] = \boxed{\frac{62.745 \text{ } \mu\text{m}}{L_p=1}}$$

$T_{HL} 5V \rightarrow 2.5V$

$$V_{DSN(\text{avg})} = \frac{(5-0) + (5-2.5)}{2} = 3.75 \text{ V}$$

$$I_{DSN(\text{avg})} = K_n' (W_n/L_n) [(5-1)3.75 - (3.75^2/2)] = K_n' (W_n/L_n) 7.96875$$

$$I_{DSN(\text{avg})} = \frac{(4 \text{ pF})(2.5)}{2 \text{ ns}} = K_n' (W_n/L_n) 7.96875$$

Answers:

$$\frac{W_p}{L_p} = \frac{62.745}{1}$$

$$\frac{W_n}{L_n} = \frac{17.927}{1}$$

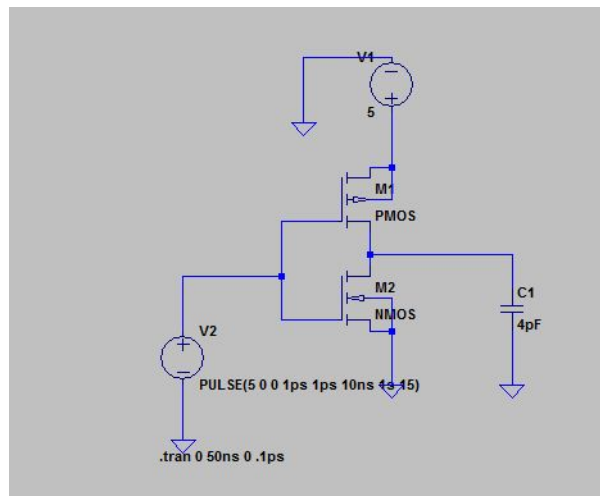
$$\frac{(4 \text{ pF})(2.5)}{2 \text{ ns}(35 \text{ mA/V}^2)(7.96875)} = [W_n/L_n] \rightarrow \left[\frac{W_n}{1} \right] = \boxed{\frac{17.927 \text{ } \mu\text{m}}{L_n=1}}$$



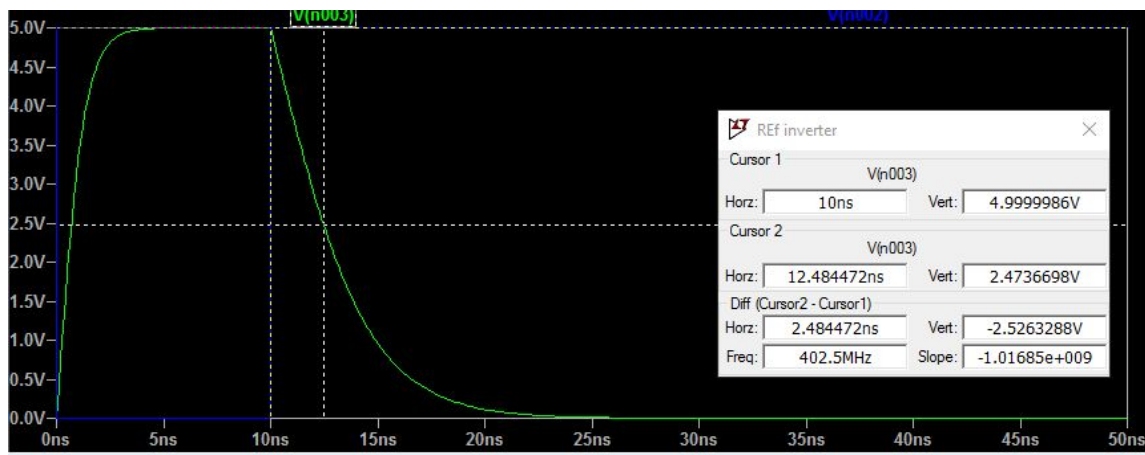
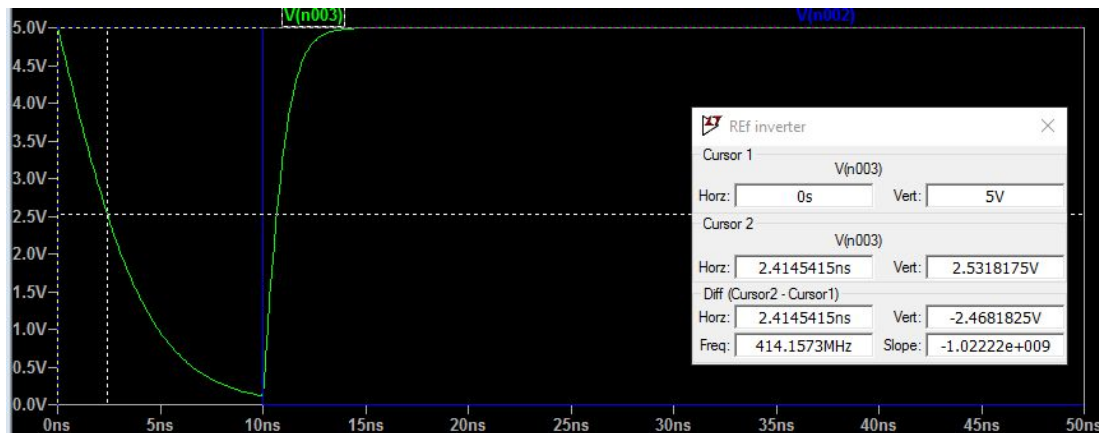
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Part 3:

Circuit:



Rise and Fall Times:



$$T_{PD} = (T_{PDLH} + T_{PDHL}) / 2 = ((2.48ns + 2.41ns)) / 2 \approx 2.40ns$$

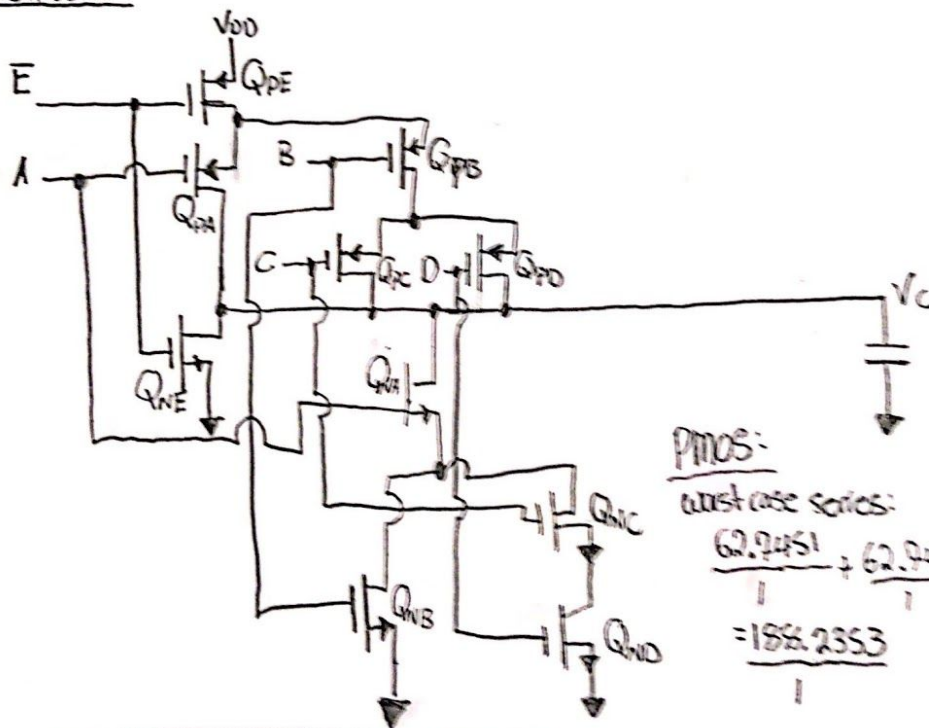
Comparing this value of T_{PD} with the 2ns we can see that they fall within a reasonable margin of error.

Part 4:

Part 4:

$$\begin{aligned}
 Y &= [A(B+CD)+E] \\
 &= (A(B+CD))'E' \\
 &= (A' + (B+CD)')E' \\
 &= (A' + B'(CD)')E' \\
 &= (A' + B'(C'+D'))E' \\
 \boxed{Y &= (A' + B'[C+D])E'}
 \end{aligned}$$

Circuit:



PMOS:

worst case series:

$$\begin{aligned}
 &\frac{62.9451}{1} + \frac{62.9451}{1} + \frac{62.9451}{1} \\
 &= \frac{188.2353}{1}
 \end{aligned}$$

so:

$$\begin{aligned}
 Q_{PE} &= Q_{PB} = Q_{PC} = Q_{PD} = \frac{188.2353}{1} \\
 Q_{PA} &= \frac{188.2353}{2}
 \end{aligned}$$



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Nmos:

$$\frac{17.927}{1} + \frac{17.927}{1} + \frac{17.927}{1} = \frac{53.781}{1}$$

$$Q_{NA} = Q_{NC} = Q_{ND} = \frac{53.781}{1}$$

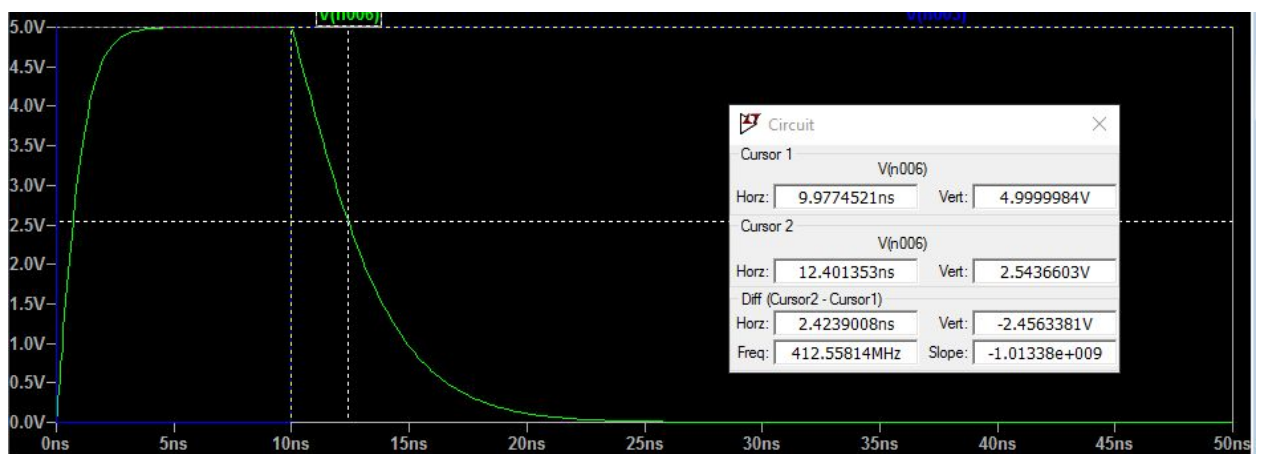
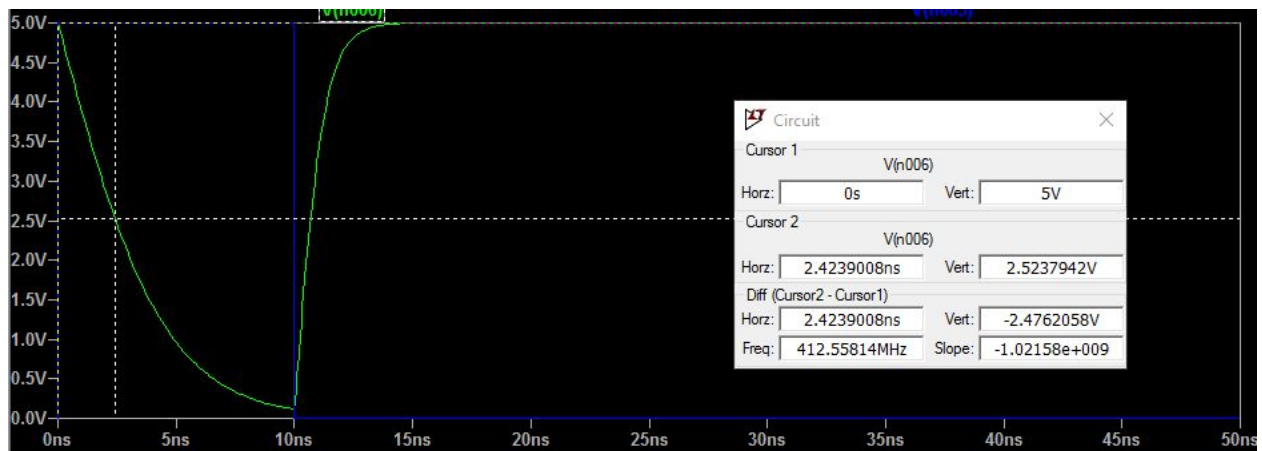
$$Q_{NB} = \frac{53.781}{2}$$

$$Q_{NE} = \frac{53.781}{3}$$



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Rise and Fall Times:



$$T_{PD} = (T_{PDLH} + T_{PDHL}) / 2 = ((2.40 + 2.40) / 2) = 2.40ns$$

Comparing this value of T_{PD} with the 2ns we can see that they fall within a reasonable margin of error.

Part 6:

Part 6: Minimum Area Design:

Qn Worst case:
$$\frac{W_N}{L_N} = \frac{17.927}{1} \rightarrow \frac{17.927}{1} + \frac{17.927}{1} = \frac{17.927}{2}$$

all Q's are going to $\frac{17.927}{1}$

$$T_{PDHL1} = \frac{\frac{17.927}{1}}{\frac{17.927}{2}} (T_{PHL}) = 2(2ns) = \boxed{4ns}$$

Qp worst case:

$$\frac{W_P}{L_P} = \frac{17.927}{1} + \frac{17.927}{1} = \frac{17.927}{2}$$

$$T_{PDHL1} = \left[\frac{62.7451}{1} \right] \cdot T_{PDHL} = 7(2ns) = \boxed{14ns}$$

$$T_{PD1} = \frac{14ns + 4ns}{2} = 9ns$$

$$T_{PD} = T_{PD1} / 2ns = 9ns / 2ns = 4.5$$

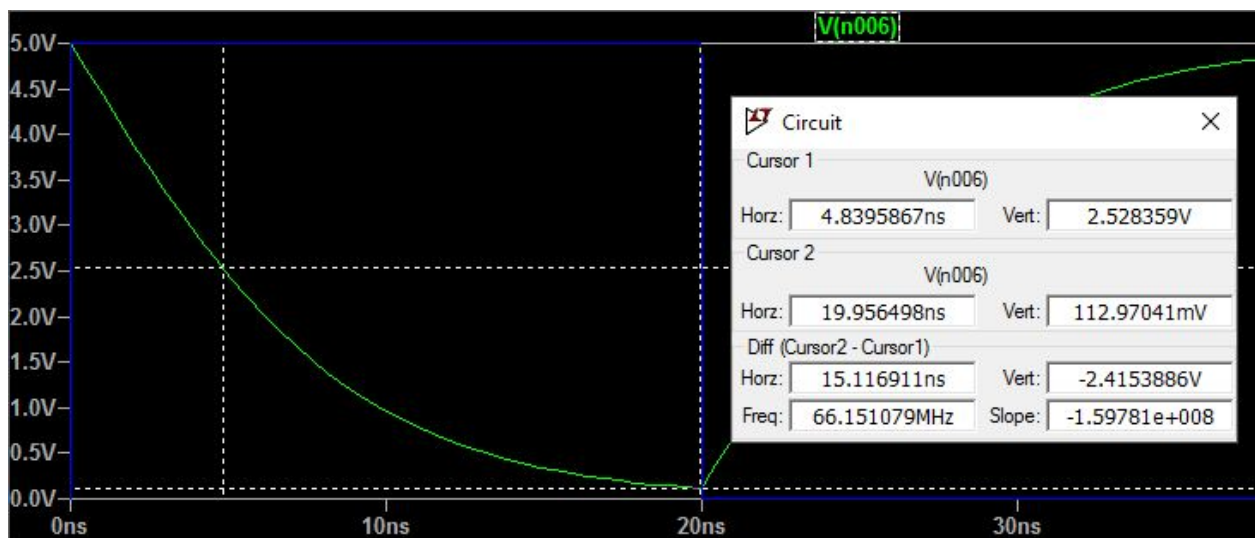
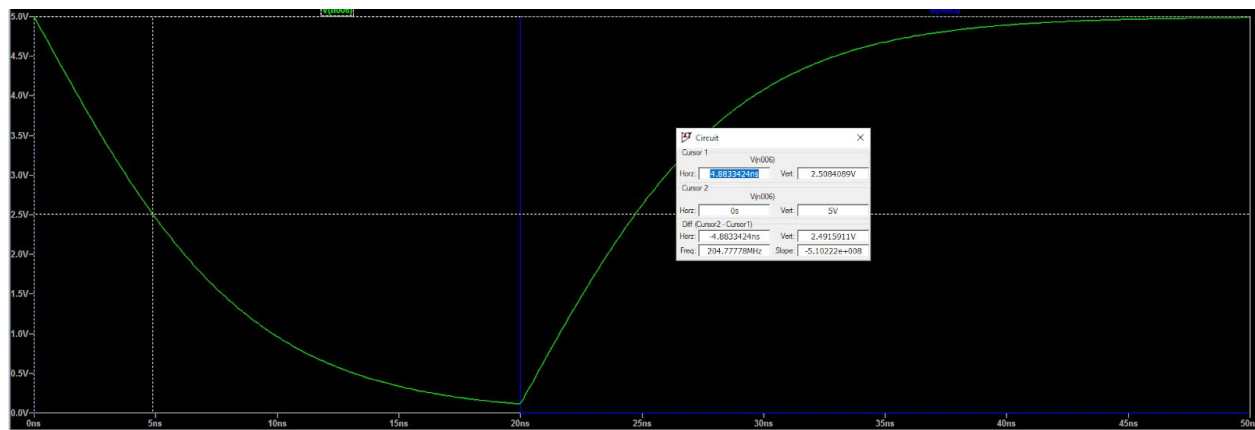
• In min design T_{PD1} is 4.5 times

Slower than original



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WaveForms:



$$T_{PD^*} = (T_{PDLH^*} + T_{PDHL^*}) / 2 = ((15.1ns + 4.80) / 2 \approx 9.5 ns$$

Comparing this value of T_{PD} with the 9ns we can see that they fall within a reasonable margin of error.