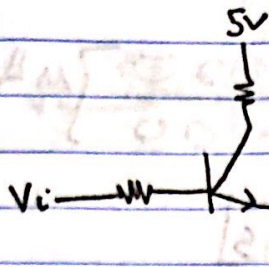


HW2:

1)



Solution: $I_C(\text{sat}) = \frac{V_{CC} - V_{CE}}{R_C}$

$$= \frac{5 - .2}{1000} = 4.8 \text{ mA}$$

$$I_{C(\text{EOS})} = \frac{I_C(\text{sat})}{\beta} = \frac{4.8 \text{ mA}}{100} = 48 \mu\text{A}$$

$$I_{Bf} = \frac{V_i - V_{BE}(\text{sat})}{R_B} = \frac{5 - .7}{5K} = 860 \mu\text{A}$$

$$I_{Br} = \frac{V_{i(\text{REV})} - V_{BE}(\text{sat})}{5K} = \frac{0 - .7}{5K} = -140 \mu\text{A}$$

$$T_s = T_0 \cdot \ln \left[\frac{-140 - 860}{-140 - 48} \right] = \boxed{16.7 \text{ ns} = T_s}$$

2)

a) $I_C = 10/1000 = 10 \text{ mA}$

$$\boxed{I_{B(\text{EOS})} = \frac{I_C}{\beta} = 100 \mu\text{A}}$$

b) $I_{Bf} = \frac{10 - .8}{22K\Omega} = \frac{9.2}{22,000} = \boxed{420 \mu\text{A}}$

c) $I_{Br} = \frac{-.8}{22K\Omega} = \boxed{-36 \mu\text{A}}$

d) $Q_a = T_{BF} I_{B(\text{EOS})} = 20 \text{ ns} \cdot 100 \mu\text{A} = \boxed{2 \text{ pC}}$

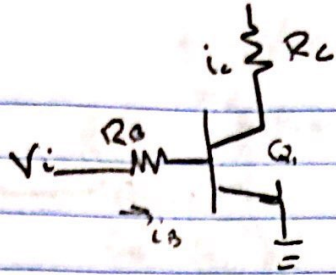
e) $Q_s = T_{BF} (I_{Bf} - I_{B(\text{EOS})}) = 20 (420 - 100) = \boxed{6.4 \text{ pC}}$

$$8) \quad T_s = -T_0 \ln \left[\frac{-36 - 420}{-36 - 100} \right] \mu A$$

$$= \boxed{24.19 ns}$$

$$9) \quad T_s = 20 \ln \left[\frac{-420}{-100} \right] = \boxed{28.70 ns}$$

3)



$$V_b = -5V$$

$$V_c = 5V$$

$$V_e = 0V$$

$$C_j(V_{BE}) = C_{jE0} \left[\frac{V_{0BE} - 0}{V_{0BE} - V_{BE}} \right]^{1/2} \quad V_{BE} = V_b - V_e = -5V$$

$$= [1.5 \times 10^{-12}] \left[\frac{.9 - 0}{.9 + 5} \right]^{1/2} = 5.85 \times 10^{-13} F$$

$$V_{BC} = V_{BE} - V_c = -5 - 5 = -10V$$

$$C_j(V_{BC}) = (0.7 \times 10^{-12}) \left[\frac{.7 - 0}{.7 + 10} \right]^{1/2} = 1.7904 \times 10^{-13} F$$

$$Q_{BE} = C_j(V_{BE}) \cdot V_{BE} = 5.85 \times 10^{-13} \cdot (-5)$$

$$Q_{BC} = C_j(V_{BC}) \cdot V_{BC} = -2.925 pC$$

$$1.7904 \times 10^{-13} \times (-10)$$

$$= -1.7904 pC = Q_{BC}$$

$$4) I_B = \frac{V_i - V_{BE}}{R_B} = \frac{5 - .7}{10k} = .43 mA$$

$$I_B(EOS) = \frac{I_c}{\beta} = \frac{1}{\beta} \cdot \frac{V_{CC} - V_{CE}}{R_c} = \frac{5 - .2}{100 \cdot 1000} = .048 mA$$

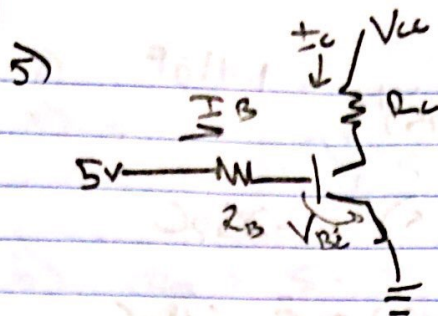
$$C_{jE}(0.7) = 1.5 pF \left(\frac{.9 - 0}{.9 - .7} \right)^{1/2} = 3.18 pF$$

$$C_{jE}(0.5) = .7 pF \left(\frac{.7 - 0}{.7 - .5} \right)^{1/2} = 1.3 pF$$

$$V_{BC} = V_{BE} - V_{CE} = .7 - .2 = .5$$

$$Q_{BE} = 3.18 pF \cdot .7 V = 2.22 pC$$

$$Q_{CE} = 1.3 pF \cdot .5 = 0.65 pC$$



$$V_B - I_B R_B - V_{BE(SAT)} = 0$$

$$5 - I_B R_B - 0.8 = 0$$

$$I_B R_B = 4.2$$

$$V_{CC} - I_C R_C - V_{CE(SAT)} = 0$$

$$10 - (1000) I_C - 0.2 = 0$$

$$I_C = 9.8 \text{ mA}$$

$$N_1 = \frac{\beta_{min}}{\beta} \Rightarrow \beta = \frac{30}{10} = 3$$

$$I_B = \frac{I_C}{\beta} = \frac{9.8 \times 10^{-3}}{3} = 3.267 \text{ mA}$$

$$4.2 = R_B (I_B) \Rightarrow R_B = 1.285 \text{ k}\Omega$$

6) a) $I_B(EOS) = \frac{I_C(sat)}{\beta} - \frac{V_{CC} - V_{CE(SAT)}}{\beta R_C}$

$$= \frac{10 - 0.2}{100 \cdot (470)} = .208 \text{ mA}$$

$$I_{Bf} = \frac{10 - 0.7}{2 \text{ k}\Omega} = 4.65 \text{ mA}$$

$$I_{Br} = \frac{-10 - 0.7}{2 \text{ k}\Omega} = -5.35 \text{ mA}$$

$$T_s = \tau_s \cdot \ln \left[\frac{(-5.35 - 4.65) \text{ mA}}{(-5.35 - .208) \text{ mA}} \right] = 17.62 \text{ ns}$$

storage
time
part 9

b) $I_B^{(EOS)} = .208 \text{ mA}$

$$I_{Bf} = 4.65 \text{ mA}$$

$$I_{Br} = \frac{0 - 0.7}{2 \text{ k}} = -0.35 \text{ mA}$$

$$T_s = 100 \cdot 300 \text{ ps} \cdot \ln \left[\frac{(-.35 - 4.65) \text{ mA}}{(.35 \text{ mA} - .208 \text{ mA})} \right]$$

$$= 65.79 \text{ ns}$$

storage part
time B

a) $C_{je} = 0.45 \text{ pF}$

$$\left(1 + 10 / 75 \right)^{1/2} = 2.31 \text{ pF}$$

$$C_{je} = 2 \cdot 3.7 \text{ pF} / (1 + 20/75)^{1/2} = 1.41 \text{ pF}$$

$$\Delta Q_{BE} = 7.38 \text{ pF} \cdot (-10 - .5) = -25 \text{ pC}$$

$$\Delta Q_{BC} = 1.41 \text{ pF} \cdot (4.5 - .5) = 5.64 \text{ pC}$$

$$I_i = \frac{10 + 10}{2k} = 10 \text{ mA}, \quad I_f = \frac{10 - .5}{2k} = 4.75 \text{ mA}$$

$$I_{AVG} = \frac{(10 + 4.75) \text{ mA}}{2} = 7.375 \text{ mA}$$

$$t_D = \frac{(25 + 5.64) \text{ pC}}{7.375 \text{ mA}} = \boxed{4.1545 \text{ ns}} \quad \leftarrow \text{part A}$$

B)

$$C_{je} = 2 \cdot 4.5 \text{ pF} / (1 + 10/75)^{1/2} = 9 \text{ pF}$$

$$C_{jc} = 2 \cdot 3.7 \text{ pF} / (1 + 20/75)^{1/2} = 1.95 \text{ pF}$$

$$\Delta Q_{BE} = 9 \cdot (-.5) = -4.5 \text{ pC}$$

$$\Delta Q_{BC} = 1.95 \text{ pF} \cdot (4.5 - .5) = 7.8 \text{ pC}$$

$$I_i = \frac{10}{2k} = 5 \text{ mA}, \quad I_f = \frac{10 - .5}{2k} = 4.75 \text{ mA}$$

$$I_{AVG} = \frac{(5 + 4.75) \text{ mA}}{2} = 4.875 \text{ mA}$$

$$t_D = \frac{(4.5 + 7.8) \text{ pC}}{4.875 \text{ mA}} = 2.523 \text{ ns}$$

ANSWERS

$$a) \begin{cases} t_s = 17.62 \text{ ns} \\ t_D = 4.1545 \text{ ns} \end{cases}$$

$$b) \begin{cases} 65.79 \text{ ns} = t_s \\ 2.523 \text{ ns} = t_D \end{cases}$$

→

$$a) \Delta Q = C \Delta V$$

$$10^{-12} (5+5) = \boxed{10 \text{ pC}}$$

$$b) I_B = \frac{5 - .7}{5000} = .86 \text{ mA}$$

$$T = 1/f = 1/5 \cdot 10^6$$

$$I_B \text{ avg} = \int_0^T I_S dt \rightarrow 5 \cdot 10^6 \int_0^{1/5 \cdot 10^6} (.86 \text{ mA}) dt$$

$$5 \cdot 10^6 (.86 \text{ mA}) \frac{1}{5 \cdot 10^6} = \boxed{.86 \text{ mA}}$$

$$c) I_C(\text{sat}) = \frac{V_{CC} - .1}{470}$$

$$I_B(\text{kos}) = \frac{V_{CC} - .1}{470 \cdot 100}$$

$$I_B = \frac{5 - .7}{5000} = .86 \text{ mA}$$

$$I_{BR} = \frac{I_S}{\beta_R} \left[e^{\sqrt{8kT/r_T} - 1} \right] = \boxed{1.45 \times 10^{-12} \left[\frac{I_S}{\beta_R} \right]}$$

$$d) T_S = T_{OFF} - T_{FALL}$$

$$\frac{T}{2} - T_S = \frac{1}{10 \cdot 10^5} - \frac{10}{10^4} = \boxed{90 \text{ ns}}$$

$$e) V_C(10\%) = .5$$

$$V_C(90\%) = 4.5$$

$$FRC = \frac{1}{2} \left[\frac{4.5}{470} + \frac{4.45}{470} \right]$$

$$I = 86 - 5.3 = 80.7 \text{ mA}$$

$$t_f = \frac{C \Delta V}{I} = \frac{(10)(1)}{80.7} = \boxed{495 \text{ ns} = t_f}$$

$$f) \quad T_f = 2.2T = 2.2R_c(C)$$

$$[0.9 \text{ V}] = (2 + 2) = 2.2(51k)(10 \text{ pF}) = [110 \text{ ns}]$$

$$A_{mid} = \frac{V_o - V_i}{V_i} = \frac{V_o}{V_i} - 1 = \frac{V_o}{V_i} - 1$$

8)

$$a) V_{OL} = V_{CE(sat)} = 0.2V$$

$$V_{IL} = V_{BE} = 0.7V$$

$$\boxed{V_{OH} = V_{CC} = 5V}$$

$$b) V_{IH} = V_{BE} + R_B I_B$$

$$I_B = B (V_{CC} - V_{IL}) / R_C$$

$$I_B = 43 \mu A$$

$$\boxed{V_{IH} = 1.56V}$$

$$c) I_B = (V_i - V_{BE}) / R_B$$

$$I_B = 215 \mu A$$

$$\text{forced } B = I_C(sat) / I_B = 1.8 / .215 = \boxed{7.37}$$

$$d) V_{OH} = V_{IH} \cdot \beta = 5 \cdot \beta = \boxed{40V}$$