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024/08/19

### NMOS HW

1) a) NOR GATE

b)  $V_{DD} = 3V$ ,  $V_{DSL} = 5 - V_{DSS}$

$$I_{DSSL\text{SAT}} = I_{DSS\text{OHMIC}} \\ \cdot \frac{W}{L} (2V_{DSS} - V_{DSS}^2/2) \rightarrow V_0 = 1.33V$$

c)  $V_{DSS} = 3V$

$$V_{DSL} = 5V = V_{DSS} \quad 1.5 \times 10^{-3} \quad 2K\Omega$$

$$I_{DSSL\text{SAT}} = I_{DSS\text{OHMIC}} \\ \cdot 4 \times 10^{-3} / 2(4 - V_{DSS})^2 \rightarrow V_0 = .8V$$

d)  $V_{OL} = 1V$

b/c  $V_0 = V_T$

2) a)  $V_{OH} = V_{DD} - V_T = 4V$

b)  $V_{DSS} = 4V$

$$\cdot 2 \times 10^{-8} / 2(4 - V_{DSS})^2 = 1 \times 10^{-3} (3V_{DSS} - V_{DSS}^2/2)$$

$$V_{OL} = V_{DSS} = 0.45V$$

c)  $V_{IL} = V_T = 1V$

$$d) 0.1 \times 10^{-3} \cdot 16 = 1 \times 10^{-3} [V_{DSS} - 1 - 1/2]$$

$$16 = 10 [V_{DSS} - 1.5] \rightarrow V_{DSS} = 3.1V$$

e)  $V_{DSS}(\text{av}) = (4)/2 = 2$ ;  $V_{DSS} = 4V$ ;  $2 < 4 - 3 \rightarrow \text{ohmic}$

$$I_{DS} = 1 [(3)^2 - 4/2] = 4$$

$$V_{DSL}(\text{av}) = 4.6 + 1.4/2 = 3$$

$$I_{DSSL}(\text{av}) = (.2/2) (V_{DSL}(\text{av}) - 1)^2 = 0.4$$

$$I_0 = 4 - .4 = 3.6$$

$$\tau = (20pF + 3.2) / 3.6mA = 17.8nS$$

f)  $R_2 = 1/2 = 5V$

$$V_{OH} = V_{DD} - V_T = 4V$$

$$V_{OL} = 4 / \sqrt{16} = 4/4 = 1V$$

$$V_{IH} = 1.5 + (3)^2 / 16 = 2.4V$$



c)

a)  $V_{DS} = 4.5V$

$V_{GS} = 4.5 - 1 = 3.5V$

$I_{DS} = K/2 (V_{GS} - V_T)^2 = .13 (3.5 - 1.5)^2$

$R = 1V / 1.5mA = 666.6\Omega$

b)  $V_{DS} = 2V$   $V_{GS} = 0.5V$

$V_{GS} = 1.5mA / 1.5mA^2 = 1.1mA / \mu^2$

c)  $V_{DS} = 3V$   $I_{DS} = 2.5\mu A$

$V_{GS} = 3 - (2.5\mu A)^2 \cdot 2.5k\Omega / 2 = 1.5V$

$= 0.5V$

$V_{DS} = 5 - .15A \cdot 1.5k\Omega = 2.75V$

$= 5 - .15^2 \cdot (1.5k\Omega \cdot 1.5k\Omega)$

$= 3.44V$

$1.543 - 1 = 3.443$

$V_{GS} = V_{DS} - V_T$  we can assume

the Q is saturated

d)  $V_{DS} = 2V$

Intercept of graph

$(5 - 12)I_{DS} + 15 = 0$

1	1.5mA
2	1.5mA
3	1.5mA
4	0.5mA



5)

a)  $V_{LNL} = V_{DD} - V_{DSS}$   $V_{GH} = V_{DD} - V_t = 4V = V_{LNL}$

$$3V_{DSS}^2 - 20V_{DSS} + 16 = 0$$

$$V_{OL} = 0.929V$$

b)  $I_{DS} = 1(4 - 0.929)^2 = 9.43mA$

$$6V_{DSS1}^2 - 12(3)V_{DSS1} + 9.43 = 0$$

$$V_{DSS1} = 0.275V$$

$Q_2$

$$6V_{DSS2}^2 - 12(3.725 - 1)V_{DSS2} + 9.43 = 0$$

$$V_{DSS2} = 0.306V$$

$Q_3$

$$6V_{DSS3}^2 - 12(3.491 - 1)V_{DSS3} + 9.43 = 0$$

$$V_{DSS3} = 0.350V$$

6) a)  $V_{GH} = 4V$

b)  $3[2V_{DSS} - 1/2 V_{DSS}^2] = 0(4 - V_{DSS})^2$

$$60V_{DSS} - 15V_{DSS}^2 = (4 - V_{DSS})^2$$

$$4V_{DSS}^2 - 17V_{DSS} - 16 = 0$$

$$V_{DSS} = 0.25V$$

c)  $I_{DNL} = I_{DSS} = 1.4mA$

7) a)  $V_{OH} = 4V$

b)  $6V_{DSS}^2 - 35V_{DSS} + 16 = 0$

$$V_{DSS} = V_{OL} = 0.454V$$

c)

$$I_{DS} = 2/2[3 \cdot 0.454 - 1/2 \cdot 0.454^2] = 1.26mA$$

d)  $V_{DS2} = 6V_{DS} + 126 = 0$

$$V_{DS} = 0.217V$$

e)  $\Delta T = CV/F = 100 \cdot 2.4 / 3.6mA = 67ms$



b)

a)  $5V$

b)  $20V_0 - 25V_0^2 = 5 - V_0$

$V_0 = 0.24$

c)  $V_{IL} = 1V$

d)  $V_{DSS} = 1.7V_0$

$I_{DSS} = V_i - 1 - .5 = V_i - 1.5; V_i = 2.3$

e)  $I_{R17} = 0.5mA$

$V_{DSS(av)} = 2.5V$

$t_{DSS} = [4.25 - 2.5^2 / 2]$   
 $= 6.88mA$

$I_0 = 6.38mA \rightarrow \Delta T = 80 / 6.38mA$

$= 12.5ns$

f)  $V_{IL} = 1 + .2 = 1.2$

$V_{OH} = 4.9V$

$V_{IH} = .8 + 1.6 = 2.4$

$V_{OL} = .82$



a) a) 5V

b)  $V_0^2 - 8V_0 + 18 = 0 \quad V_0 = 0.23V$

c)  $V_{IL} = 1.1V$

d)  $V_{IH} = 1.5 = 0.9$

$V_{IH} = 2.4$

e)  $V_0 = 0.5 \text{ and } 4.5$   
 $\omega = 0.5$

$I_{DNL} = 0.25 \text{ mA ohmic}$

$\Rightarrow 4.5 I_{DNL} = 0.9 \text{ mA sat}$

$I_{DNL}(\text{avg}) = 0.57 \text{ mA}$

$V_{DSS}(\text{avg}) = 2.5V$

$I_{DSS} = 6.55 \text{ mA}$

$\pm_0 = 6.31 \text{ mA} \rightarrow t_f = 20 \text{ pF} \cdot 4 / 6.31 \text{ mA}$

$\boxed{12.7 \text{ ns}}$

f)  $V_{IL} = 1 + 3(\sqrt{30})$

$= 1 + 0.55 = 1.55V$

$V_{OL} = 5 - (1 - (5/26)^{1/2})$

$V_{OL} = 3/\sqrt{15} = 0.77V$

$V_{IH} = 1 - 2(-3)/\sqrt{15} = 1 + 1.26 = 2.26$

10) a)  $S = 4V$

$V_{TL} \text{ at } S = 4V = 1.69V$

$V_{IL} = V_{TL} = 1.69$

$V_{OH} = V_{DD} - V_{TL} = 3.31V$

$\omega = 5 = 1V$

$V_{TL} = 1.25V$

$V_{OL} = 0.94V$

$V_{IH} = 1.65V$