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 DLD
 HW 5

HW 5

1) 3 Bit Binary \rightarrow Gray Decoding using mux 151

Data	B ₂	B ₁	B ₀	G ₂	G ₁	G ₀	Decimal to Gray
D ₀	0	0	0	0	0	0	0
D ₁	0	0	1	0	0	1	1
D ₂	0	1	0	0	1	1	3
D ₃	0	1	1	0	1	0	2
D ₄	1	0	0	1	1	0	6
D ₅	1	0	1	1	1	1	7
D ₆	1	1	0	1	0	1	5
D ₇	1	1	1	1	0	0	4

2) 3 Bit Gray \rightarrow Binary Decoding using 151 mux

Gray	B ₂	B ₁	B ₀
G ₂ G ₁ G ₀			
0 0 0	0	0	0
1 0 0	0	0	1
1 1 0	0	1	0
0 1 0	0	1	1
0 1 1	1	0	0
1 1 1	1	0	1
1 0 1	1	1	0
0 0 1	1	1	1

3) 3-Bit Binary \rightarrow Gray decoding using Kmaps & XORs

$G_0 :$

$B_2 \backslash B_1 B_0$	00	01	11	10
0	0	1	1	0
1	1	0	0	1

$G_1 :$

$B_2 \backslash B_1 B_0$	00	01	11	10
0	0	1	0	1
1	0	1	0	1

$G_2 :$

$B_2 \backslash B_1 B_0$	00	01	11	10
0	0	0	1	1
1	0	0	1	1

4) 3-Bit Gray \rightarrow Binary decoding using Kmaps & XORs

$$B_1 = \sum G_2 G_1 G_0 \quad (2, 3, 4, 5)$$

$G_2 \backslash G_1 G_0$	00	01	11	10
0	0	1	0	1
1	0	1	0	1

$$B_1 = G_2 \oplus G_1$$

$$B_2 = \sum G_2 G_1 G_0$$

$G_2 \backslash G_1 G_0$	00	01	11	10
0	0	0	1	1
1	0	0	1	1

$$B_2 = G_2$$

4: Continued:

$$B_0 = \sum_{G_2, G_1, G_0} (1247)$$

σ_2
 σ_1
 σ_0

	σ_2	σ_1	σ_0
0	0	1	0
1	1	0	1

$$B_0 = G_2 \oplus G_1 \oplus G_0$$

5) $A \cdot B = 0$ { $A + B = I$
 \downarrow
 $A = B$

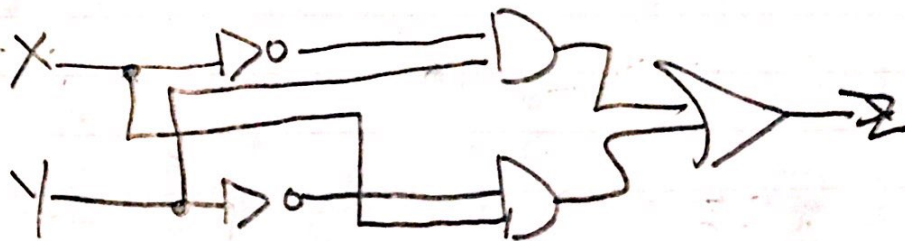
$A \cdot B = 0$ means either A or $B = 0$ or both equal 0
 $A + B = 1$ means 1 input has to be one
 therefore $A = B'$

by the $(A \cdot A = 0 \text{ and } A + A = 0 \text{ rule})$

b) $x \cdot y = 0$ & $x + y = 1$ implies that $x = y$ by the same logic above:

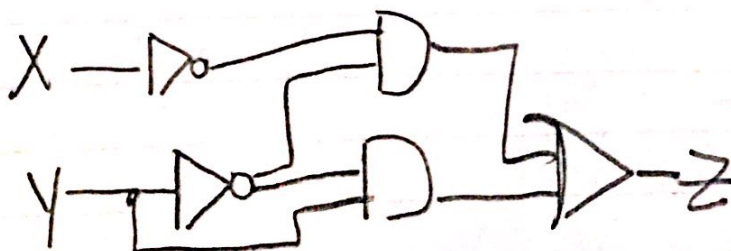
35) $X|Y|Z \quad Z = X'Y + XY'$

X	Y	Z
0	6	6
6	1	1
1	6	1
1	1	0



36) $x|y|z \quad z = x'y' + xy$

X	Y	Z
0	0	1
0	1	0
1	0	0
1	1	1



55) $P = P_2P_1P_0$ $Q = Q_2Q_1Q_0$

Output = 1 ; iff $P < Q$

P_2Q_2	P_1Q_1	P_0Q_0	$P < Q$	$P = Q$	$P > Q$
$P_2 < Q_2$	X	X	0	0	1
$P_2 = Q_2$	$P_1 > Q_1$	X	0	0	1
$P_2 = Q_2$	$P_1 = Q_1$	$P_0 > Q_0$	0	1	0
$P_2 = Q_2$	$P_1 = Q_1$	$P_0 = Q_0$	1	0	0
$P_2 < Q_2$	X	X	1	0	0
$P_2 = Q_2$	$P_1 < Q_1$	X	1	0	0
$P_2 = Q_2$	$P_1 = Q_1$	$P_0 < Q_0$	1	0	0

$$(P < Q)' = P_2'Q_2 + X_2P_1'Q_1 + X_2X_1P_0'Q_0$$

