

HW 4

21 April 2020 06:25 PM

① a) Inverting amplifier

$$\frac{V_{in} - V_i^-}{R_1} = \frac{V_i^- - V_{out}}{R_2}$$

$$\Rightarrow \boxed{\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1}} \quad V_i^- = 0$$

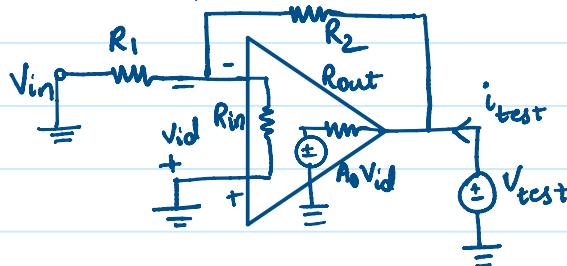
Non-Inverting amplifier

$$\frac{V_{out} - V_i^-}{R_2} = \frac{V_i^-}{R_1} \quad | V_i^- = V_i^+ = V_{in}$$

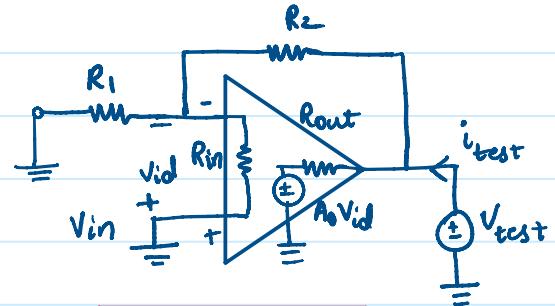
$$\boxed{\frac{V_{out}}{V_{in}} = V_{in} \left(\frac{1}{R_2} + \frac{1}{R_1} \right)}$$

$$\boxed{\frac{V_{out}}{V_{in}} = 1 + \frac{R_2}{R_1}}$$

Closed loop Output resistance

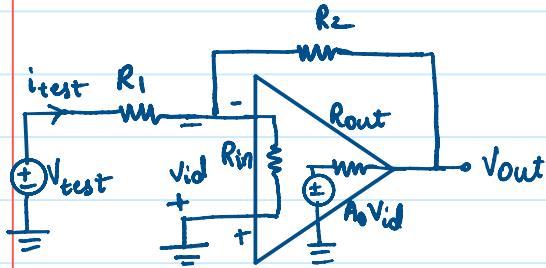


$$R_{out-CL} = \frac{V_{out}}{i_{test}} = R_{out} \parallel (R_1 + R_2) \approx R_{out}$$



$$R_{out-CL} = R_{out}$$

Closed loop input resistance



$$i_{test} = \frac{V_{test} - V_i^-}{R_1} \quad V_i^- = 0$$

$$\Rightarrow \boxed{R_{in-CL} = R_1}$$

NO current flows through the '+' terminal of an ideal Op-amp

$$i_{test} = 0$$

$$\Rightarrow \boxed{R_{in-CL} = \infty}$$

Problem 1 (Contd.)

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b) Inverting Op-amp

1. Gain

$$\frac{V_{in} + V_{id}}{R_1} = -\frac{V_{id} - V_o}{R_2}$$

$$V_{id} = \frac{V_o}{A_o}$$

$$\frac{\left(V_{in} + \frac{V_o}{A_o}\right)}{R_1} = \frac{\left(-\frac{V_o}{A_o} - V_o\right)}{R_2} \Rightarrow \frac{V_{in}}{R_1} = -V_o \left[\frac{1}{R_2} + \frac{1}{A_o R_2} + \frac{1}{A_o R_1} \right]$$

$$\frac{V_o}{V_i} = -\frac{1}{R_1} \cdot \frac{1}{R_2 \left[1 + \frac{1}{A_o} + \frac{R_2}{A_o R_1} \right]}$$

$$A_{CL} = -\frac{R_2}{R_1} \left(1 + \frac{1}{A_o \beta} \right)$$

$$\beta = \frac{R_L}{R_1 + R_2}$$

$$A_{CL} = -\frac{R_2}{R_1} \frac{A_o \beta}{1 + A_o \beta}$$

2. Output resistance

$$R_{out-CL} = \frac{V_{test}}{i_{test}} \Rightarrow i_{test} = i_o + i_f$$

$$i_o = \frac{V_{test} - A_o V_{id}}{R_{out}} \quad \& \quad i_f = \frac{V_{test}}{R_1 + R_2}$$

$$V_{id} = -V_i \quad \& \quad V_i = \beta V_{test}$$

$$i_{test} = \frac{V_{test} + A_o \beta V_{test}}{R_{out}} + \frac{V_{test}}{R_1 + R_2}$$

$$\frac{V_{test}}{i_{test}} = \left(\frac{R_{out}}{1 + A_o \beta} \right) \parallel (R_1 + R_2)$$

$$R_{out-CL} \approx \left(\frac{R_{out}}{1 + A_o \beta} \right)$$

Problem 1 (Contd.)

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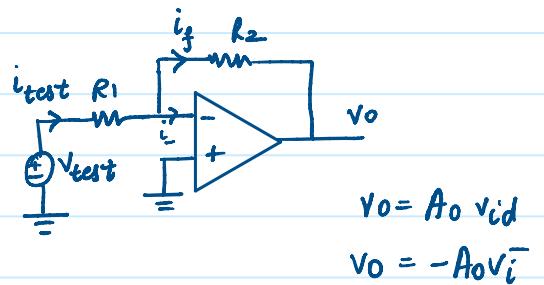
3. Input Resistance

$$\frac{V_{test}}{i_{test}} = \frac{i_{test} R_1 + V_i^-}{i_{test}} \quad \text{--- (1)}$$

$$i_{test} = i_- + i_f = \frac{V_i^-}{R_{in}} + \frac{V_i^- + A_o V_i^-}{R_2}$$

$$\frac{V_i^-}{i_{test}} = \frac{1}{R_{in}} + \frac{1 + A_o}{R_2}$$

from (1), $R_{in-CL} = R_1 + \left(R_{in} \parallel \frac{R_2}{1 + A_o} \right)$



Non-inverting amplifier

1. Gain

$$V_o = A_o (V_i^+ - V_i^-)$$

$$V_o = A_o (V_{in} - \beta V_o)$$

$$V_o (1 + A_o \beta) = A_o V_{in}$$

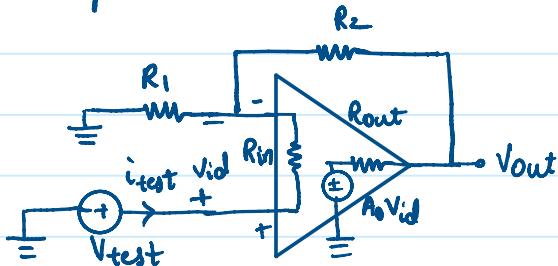
$$A_{CL} = \frac{V_o}{V_{in}} = \frac{A_o}{1 + A_o \beta}$$

$$\beta = \frac{R_1}{R_1 + R_2}$$

2. Output resistance same as inverting case

$$R_{out-CL} = \frac{R_{out}}{1 + A_o \beta} \parallel (R_1 + R_2)$$

3. Input resistance



Problem 1 (Contd.)

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$$\bar{V_i} = \beta V_o$$

$$\bar{V_i} = \beta (A_0 V_{id}) = \beta A_0 (V_{test} - \bar{V_i})$$

$$\bar{V_i} (1 + A_0 \beta) = A_0 \beta V_{test}$$

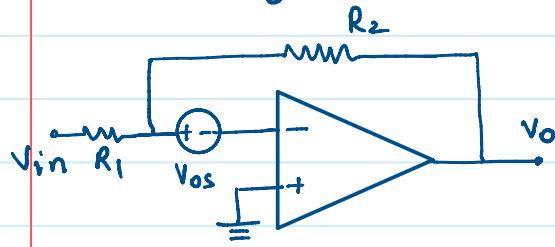
$$\bar{V_i} = \frac{A_0 \beta}{1 + A_0 \beta} V_{test}$$

$$R_{in-CL} = \frac{V_{test}}{i_{test}} = \frac{V_{test}}{V_{test} - \left[\frac{A_0 \beta}{1 + A_0 \beta} \right] V_{test}} R_{in} = R_{in} (1 + A_0 \beta)$$

$$R_{in-CL} = R_{in} (1 + A_0 \beta)$$

c)

Inverting Op-amp:



$$\frac{V_{in} - V_{os}}{R_1} = \frac{V_{os} - V_0}{R_2}$$

$$\frac{V_0}{R_2} = \frac{V_{os}}{R_2} \left[\frac{1}{R_2} + \frac{1}{R_1} \right] - \frac{V_{in}}{R_1}$$

$$V_0 = -\frac{R_2}{R_1} V_{in} + \left(1 + \frac{R_2}{R_1} \right) V_{os}$$

$$R_1 = 1k\Omega, R_2 = 10k\Omega, V_{os} = 0.1V, V_{in} = 0V$$

$$V_0 = 1.1V$$

Simulated value $V_0 = 1.09998V$

Problem 1 (Contd.)

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Non-inverting Op-amp

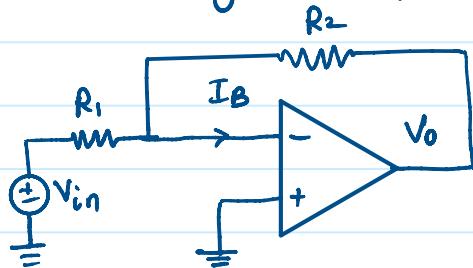
$$V_{os} + V_{in} = V_o \frac{R_1}{R_1 + R_2} \Rightarrow V_o = \left(1 + \frac{R_2}{R_1}\right) V_{in} + \left(1 + \frac{R_2}{R_1}\right) V_{os}$$

$$R_1 = 1k\Omega, R_2 = 10k\Omega, V_{os} = 0.1V, V_{in} = 0V$$

$$\text{Simulated value} = 1.0999V$$

(d)

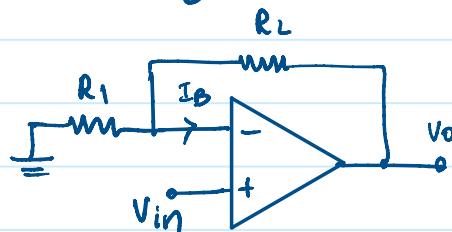
Inverting Op-amp



$$\frac{V_{in}}{R_1} + \frac{V_o}{R_2} = I_B$$

$$V_o = -\frac{R_2}{R_1} V_{in} + R_2 I_B$$

Non-inverting Op-amp



$$\frac{V_o - V_i}{R_2} + \frac{0 - V_i}{R_1} = I_B$$

$$\frac{V_o - V_{in}}{R_2} = I_B + \frac{V_{in}}{R_1}$$

$$V_o = \left(1 + \frac{R_2}{R_1}\right) V_{in} + R_2 I_B$$

Problem 2

03 May 2020 12:30 AM

② a) $V_i^+ = V_i^- = 0 \Rightarrow \frac{V_{out} - 0}{i_{in}} = R \parallel C$

$$\frac{\frac{R}{SC}}{R + \frac{1}{SC}} = \frac{R}{1 + sRC}$$
$$\Rightarrow \frac{V_{out}}{i_{in}} = \frac{R}{1 + sRC}$$

b) Taking inverse laplace transform

$$V_{out}(t) = \frac{R}{RC} e^{-\frac{t}{RC}} \cdot i(t) \quad | \quad i(t) = i_{max} @ t = t_{on}$$

$$V_{out}(t_{on}) = \frac{i_{max}}{C} e^{-\frac{t_{on}}{RC}}$$

Bonus:

$$i_{max} = 10 \mu A \quad 0.1\% \text{ error} \quad t_{settle} = 7RC$$

$$\Rightarrow t_{on} = 7RC$$

$$V_{out} \leq 2.5V \Rightarrow \frac{i_{max}}{C} \leq 2.5V \Rightarrow C \geq \frac{10 \mu}{2.5} \Rightarrow C \geq 4 \mu F$$

Select $C = 5 \mu F$, $t_{on} = 1ms$

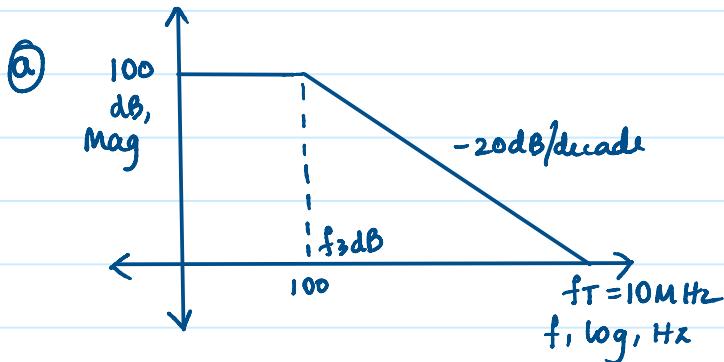
$$R = \frac{1m}{7 \times 5 \mu} = 28.57 \Omega$$

Problem 3

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$$③ A_0 = 100 \text{ dB} \quad f_T = 10 \text{ MHz}, R_1 = R_2 = R_3 = R_4 = 10 \text{ k}\Omega$$

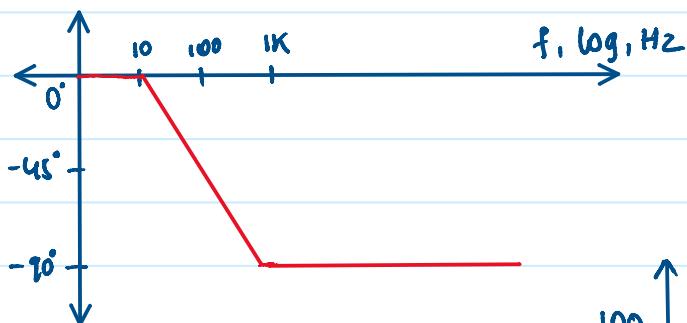
$$V_{out} = -\frac{R_4}{R_3} V_{in} + \left(1 + \frac{R_4}{R_3}\right) \left(\frac{R_L}{R_1 + R_2}\right) V_{ip} \quad ①$$



$$A_0 = 10^{\frac{100-20}{20}} = 10^5 \text{ V/V}$$

$$f_T = 10 \text{ MHz}$$

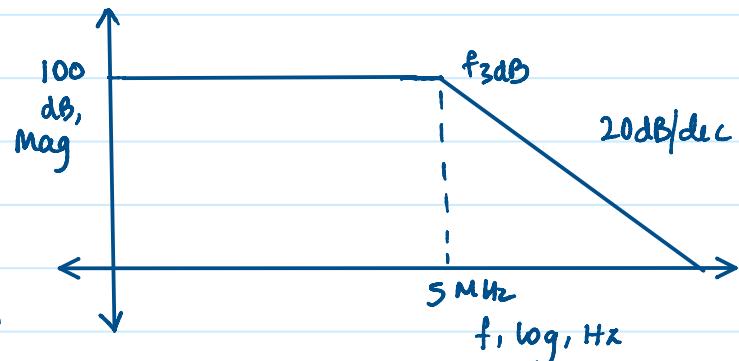
$$f_{3dB} = \frac{10}{10^5} = 100 \text{ Hz}$$



from ①

$$V_{out} = -V_{in} + V_{ip}$$

$$\Rightarrow \frac{V_{out}}{V_{ip} - V_{in}} = 1 \text{ V/V} = 0 \text{ dB}$$



$$f_{3dB, CL} = (1 + \beta A_0) f_{3dB, OL}$$

$$= [1 + 0.5(10^5)] (100)$$

$$f_{3dB, CL} = 5 \text{ MHz}$$



Problem 3 (Contd.)

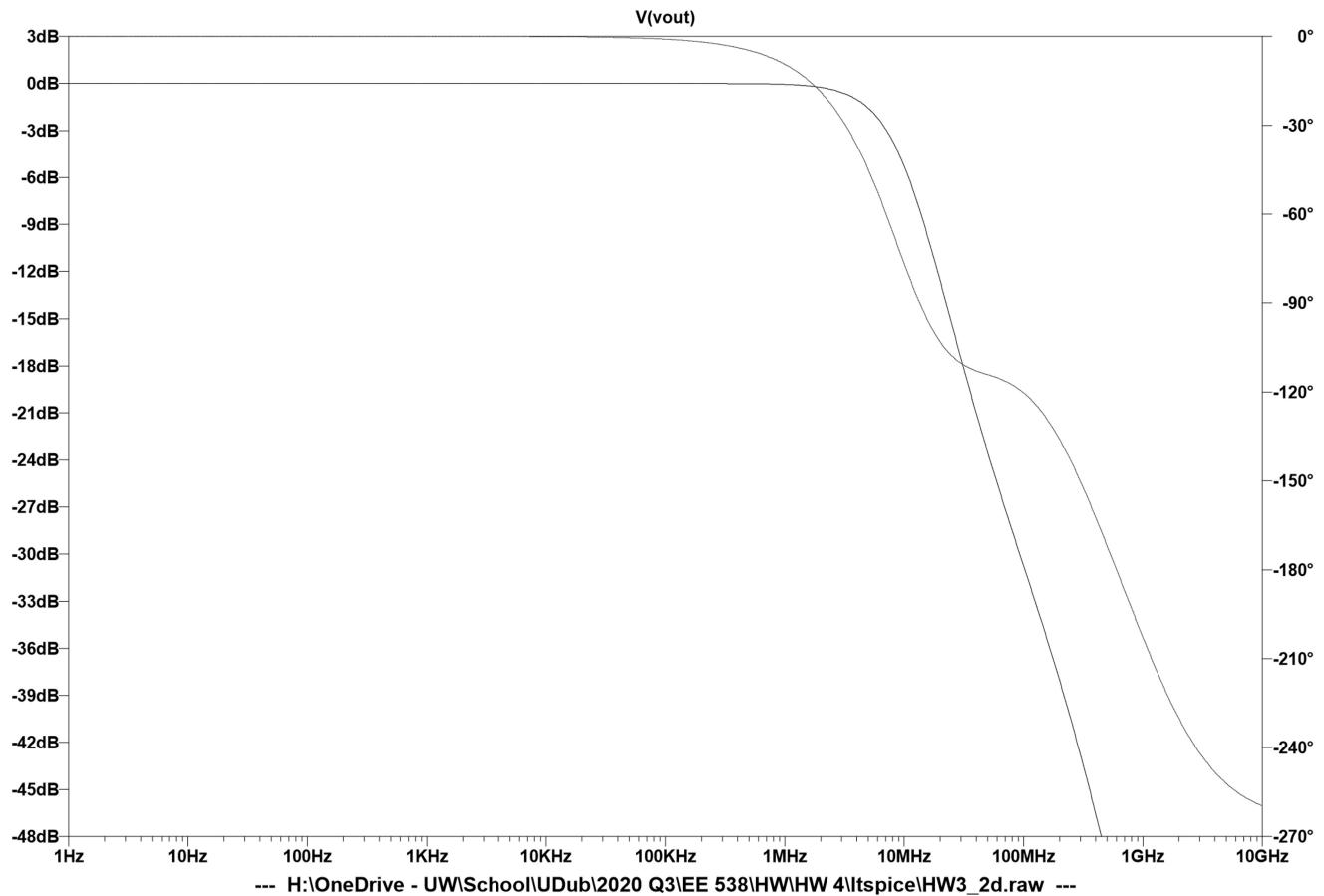
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c) For ideal Opamp

$$\textcircled{1} \quad V_{\text{in}}: \quad R_{\text{in}} = R_3 = 10\text{ k}\Omega$$

$$\textcircled{2} \quad V_{\text{ip}}: \quad R_{\text{in}} = R_1 + R_2 = 20\text{ k}\Omega$$

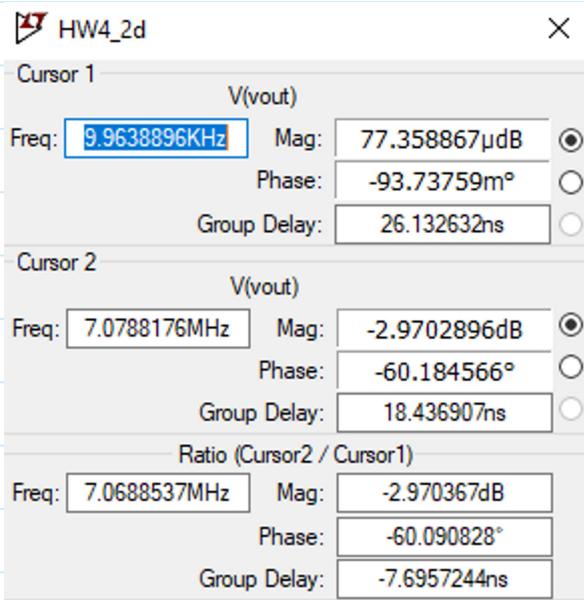
d) AD8691



$$\text{Gain} = 77.35 \mu\text{dB} \approx 0\text{dB}$$
$$f_{3\text{dB}} = 7.07\text{ MHz}$$

Problem 3 (Contd.)

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--- Transfer Function ---

```
Transfer_function:      -1          transfer
vim#Input_impedance: 10000        impedance
output_impedance_at_V(vout): 0.00186035  impedance
```

* H:\OneDrive - UW\School\UDub\2020 Q3\EE 538\HW\HW 4\ltspice\HW4_2d.asc

--- Transfer Function ---

```
Transfer_function:      1.00002    transfer
vip#Input_impedance: 20000        impedance
output_impedance_at_V(vout): 0.00186035  impedance
```

Vim, Input impedance = 10 kΩ

Vip, Input impedance = 20 kΩ