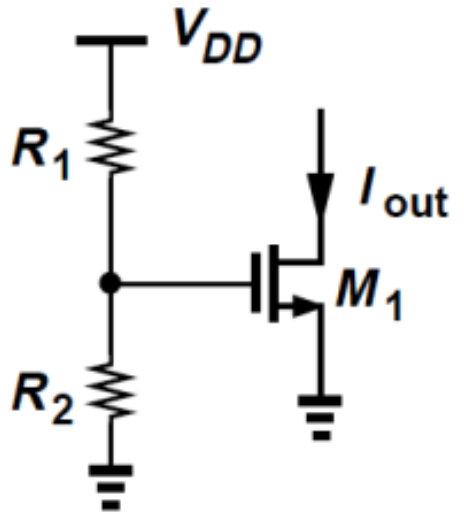
EE 332: Devices and Circuits II

Lecture 5: Current Mirrors

Prof. Sajjad Moazeni
smoazeni@uw.edu
Autumn 2022

Basic Current Source

Ideal Current Source: ?

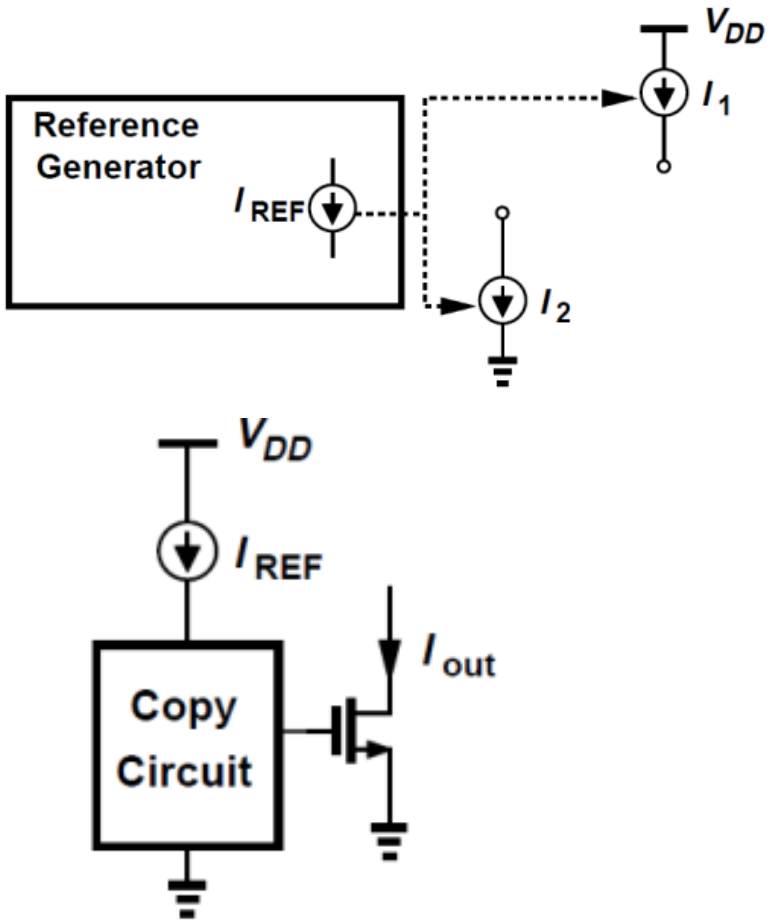


- Assuming M1 is in saturation, we can write

$$I_{out} \approx \frac{1}{2}\mu_n C_{ox}\frac{W}{L}\left(\frac{R_2}{R_1+R_2}V_{DD}-V_{TH}\right)^2$$

- The threshold voltage may vary by 50 to 100 mV from wafer to wafer
- Both μn and V_{TH} exhibit temperature dependence
- We must seek other methods of biasing MOS current sources.

Copying currents (Current Mirroring)



- Use of a reference to generate various currents.
- Two identical MOS devices that have equal V_{GS} and operate in saturation carry equal currents
  - Can change the ratio with W/L
- Distributed "Ref" can be eventually in either Voltage or Current domain.
  - What are the Pros/Cons of each?

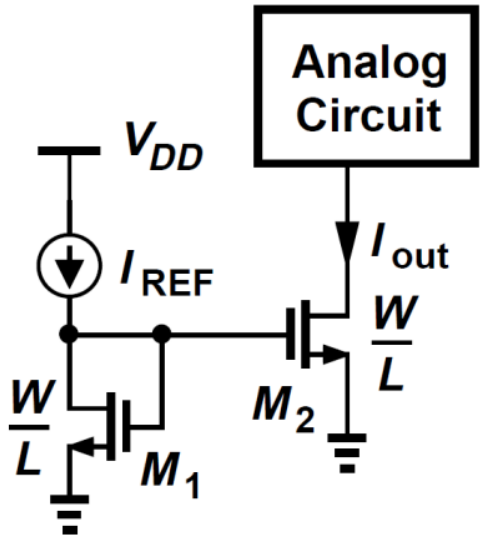
Basic Current Mirror

- Neglecting channel-length modulation (CLM), we can write

$$I_{REF} = \frac{1}{2}\mu_n C_{ox}\left(\frac{W}{L}\right)_1 (V_{GS} - V_{TH})^2$$

$$I_{out} = \frac{1}{2}\mu_n C_{ox}\left(\frac{W}{L}\right)_2 (V_{GS} - V_{TH})^2$$

$$I_{out} = \frac{(W/L)_2}{(W/L)_1} I_{REF}$$



- Allows precise copying of the current with no dependence on process and temperature
- How would Channel-Length Modulation will impact this result?

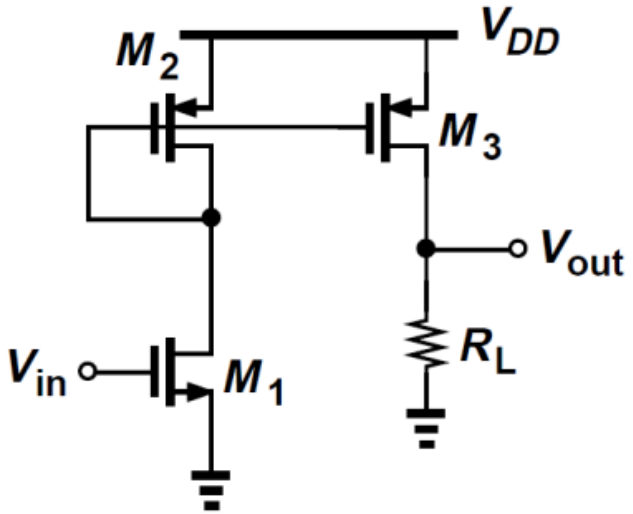
Example

- Calculate the small-signal voltage gain of the circuit shown in Figure.

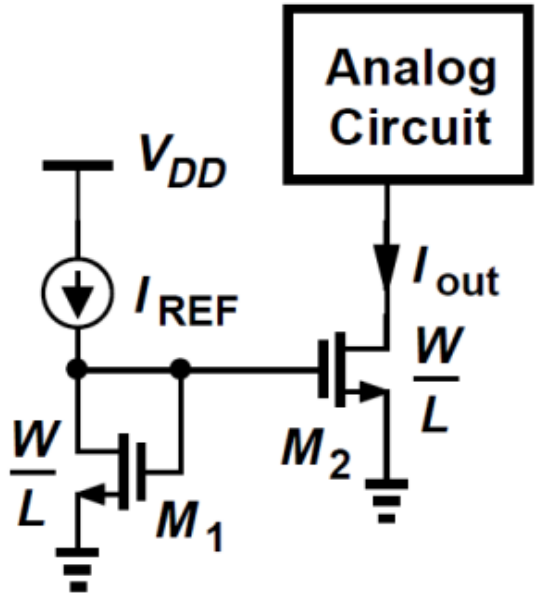
$$I_{D2} = I_{D1}$$

$$I_{D3} = I_{D2}(W/L)_3/(W/L)_2$$

- A_v = ?



Cascode Current Mirrors



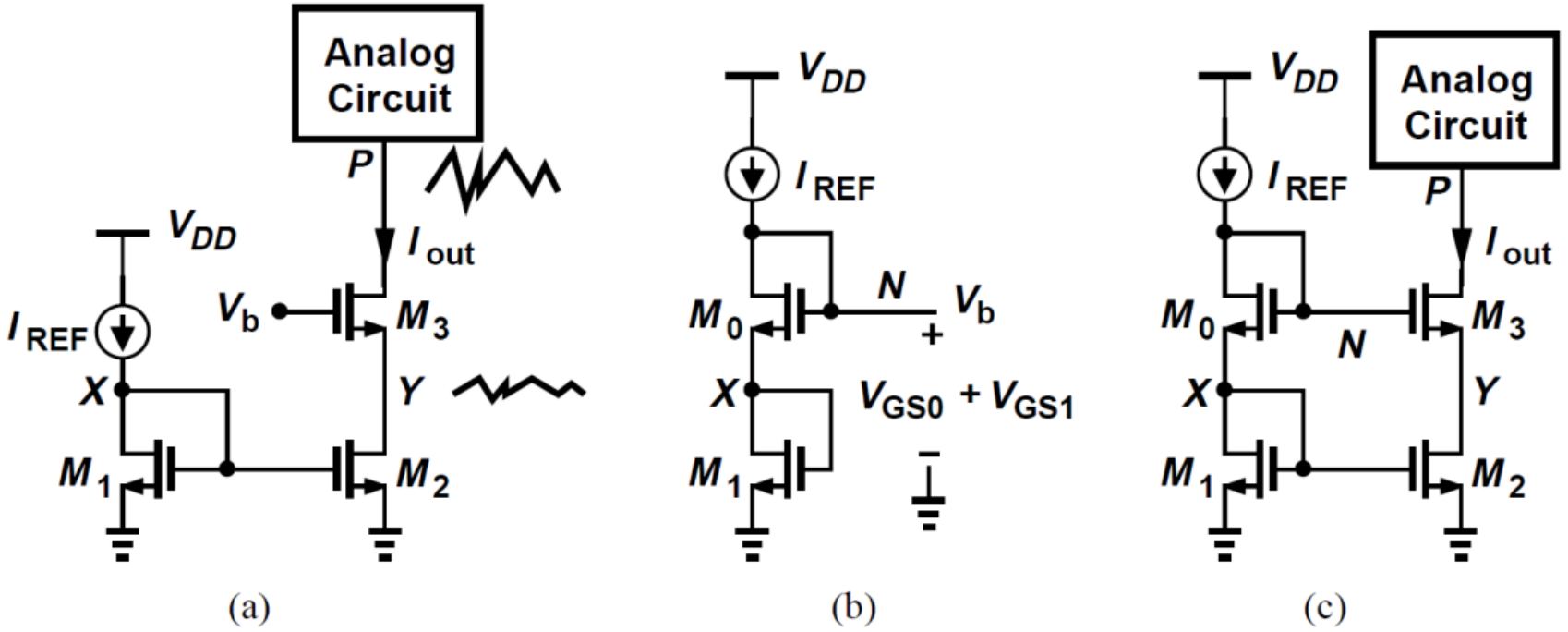
$$I_{D1} = \frac{1}{2}\mu_n C_{ox}\left(\frac{W}{L}\right)_1 (V_{GS} - V_{TH})^2(1 + \lambda V_{DS1})$$

$$I_{D2} = \frac{1}{2}\mu_n C_{ox}\left(\frac{W}{L}\right)_2 (V_{GS} - V_{TH})^2(1 + \lambda V_{DS2})$$

$$\frac{I_{D2}}{I_{D1}} = \frac{(W/L)_2}{(W/L)_1} \cdot \frac{1 + \lambda V_{DS2}}{1 + \lambda V_{DS1}}$$

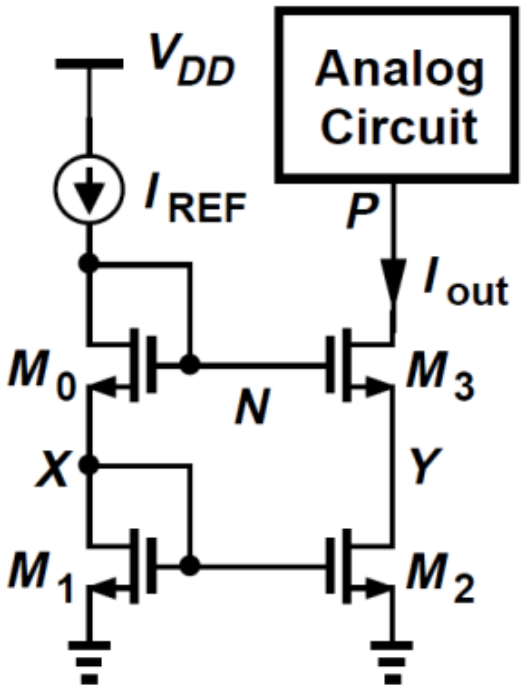
- While $V_{DS1} = V_{GS1} = V_{GS2}$, V_{DS2} may not equal V_{GS2}
- We can (a) force V_{DS2} to be equal to V_{DS1}, or (b) force V_{DS1} to be equal to V_{DS2}.

First Approach



- A cascode device can shield a current source, thereby reducing the voltage variations across it.
- But, how do we ensure that $V_{DS2} = V_{DS1}$?
- We must generate V_b such that $V_b - V_{GS3} = V_{DS1} (= V_{GS1})$

Example

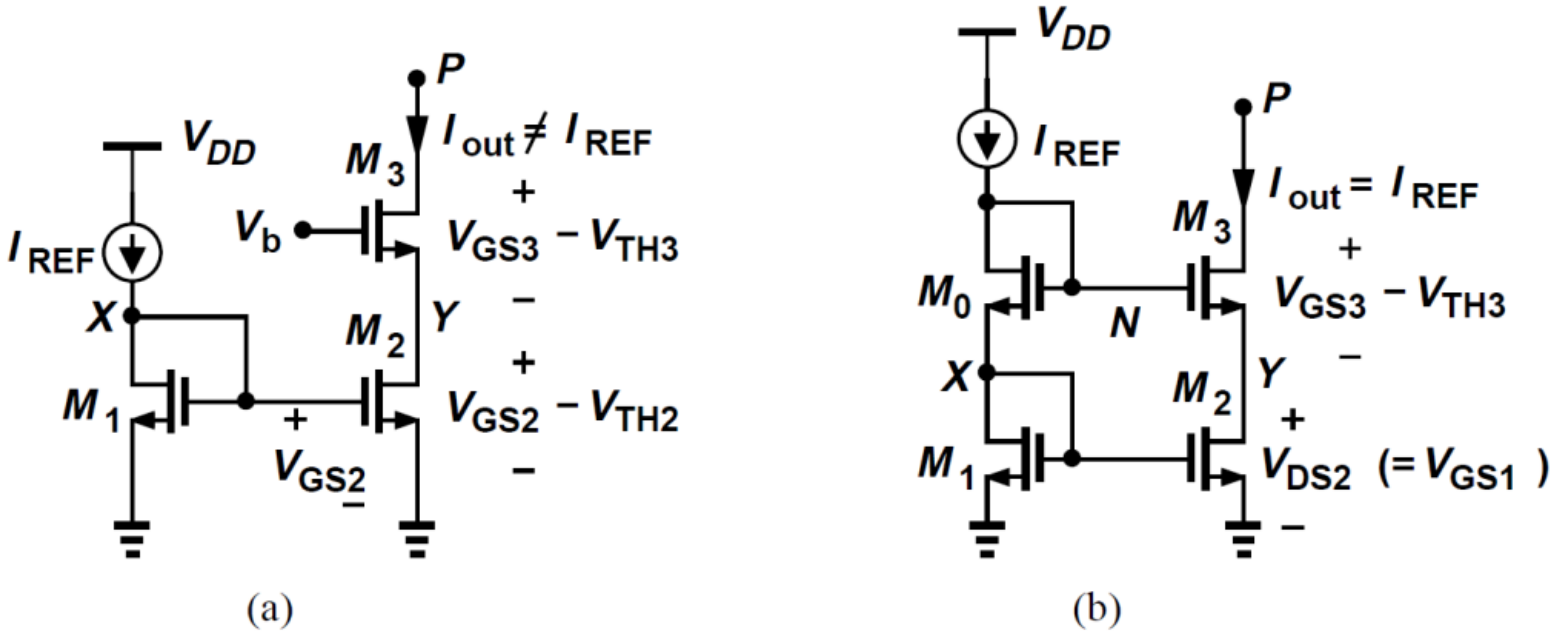


- the minimum allowable voltage at node P is equal to

$$V_N - V_{TH} = V_{GS0} + V_{GS1} - V_{TH}$$
$$= (V_{GS0} - V_{TH}) + (V_{GS1} - V_{TH}) + V_{TH}$$

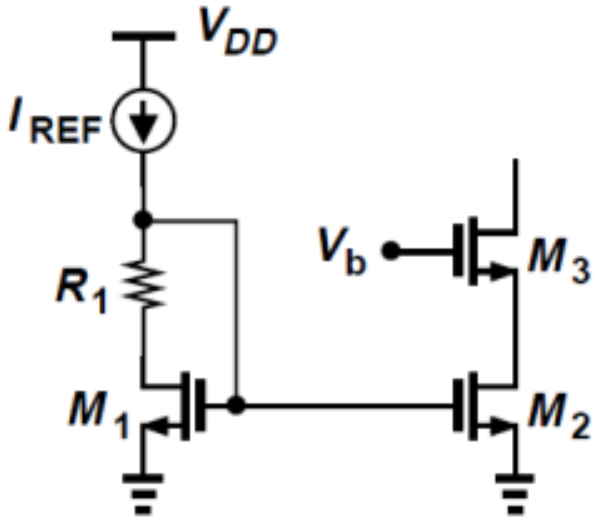
- The cascode mirror “wastes” one threshold voltage in the headroom.
- Because $V_{DS2} = V_{GS2}$, whereas V_{DS2} could be as low as $V_{GS2}-V_{TH}$ while maintaining M2 in saturation.

Approach summary



- In Fig(a), V_b is chosen to allow the lowest possible value of V_P but the output current does not accurately track I_{REF}.
- In Fig(b), a higher accuracy is achieved, but the minimum level at P is higher by one threshold voltage.

Second Approach



- Consider the branch shown in Fig. 5.16(b)
- As a candidate and write $V_b = V_{GS5} + R_6 I_6$.

$$R_1 I_{REF} \approx V_{TH1}$$

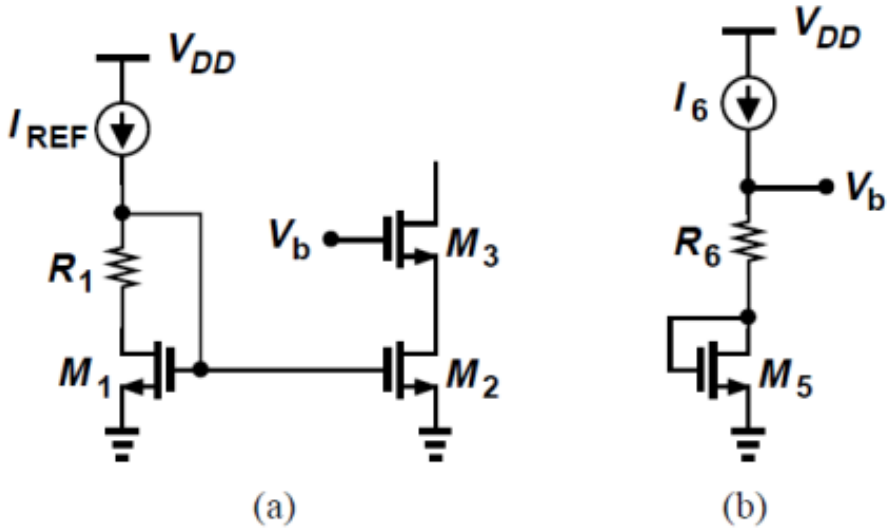
$$V_b = V_{GS3} + (V_{GS1} - V_{TH1})$$

- Thus, from a small-signal point of view, the combination is close to a diode-connected device.
- But …

(1) It may be difficult to guarantee that $R_1 I_{REF} \approx V_{TH1}$

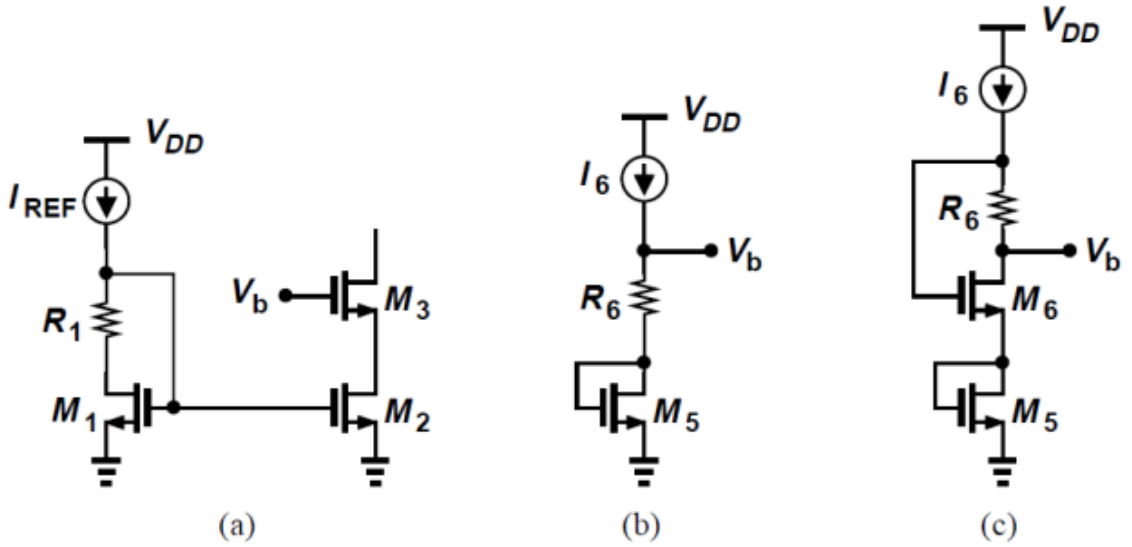
(2) The generation of V_b is not straightforward.

Generate Vb



- Consider the branch shown in Fig(b) as a candidate and write $V_b = V_{GS5} + R_6 I_6$.
- Choose I_6 and $(W/L)_5$ such that: $V_{GS5} = V_{GS3}$
- However, the condition $R_6 I_6 = V_{GS1} - V_{TH1} = V_{GS1} - R_1 I_{REF}$ is hard to meet.
  - This condition translates to: $R_6 I_6 + R_1 I_{REF} = V_{GS1}$

Generate Vb



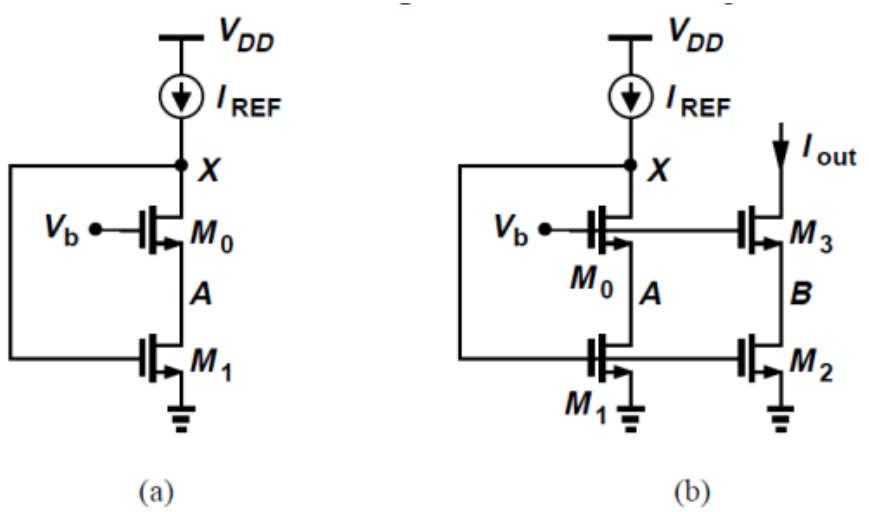
$$V_{GS5} = V_{GS3}$$

$$V_{GS6} - R_6 I_6 = V_{GS1} - V_{TH1}$$

$$= V_{GS1} - R_1 I_{REF}$$

- It is now possible to ensure that V_{GS6} and V_{GS1} track each other.
- For example, we may simply choose $I_6 = I_{REF}$, $R_6 = R_1$, and $(W/L)_6 = (W/L)_1$

Another circuit topology



- In this case

$$V_{DS1} = V_b - V_{GS0}$$

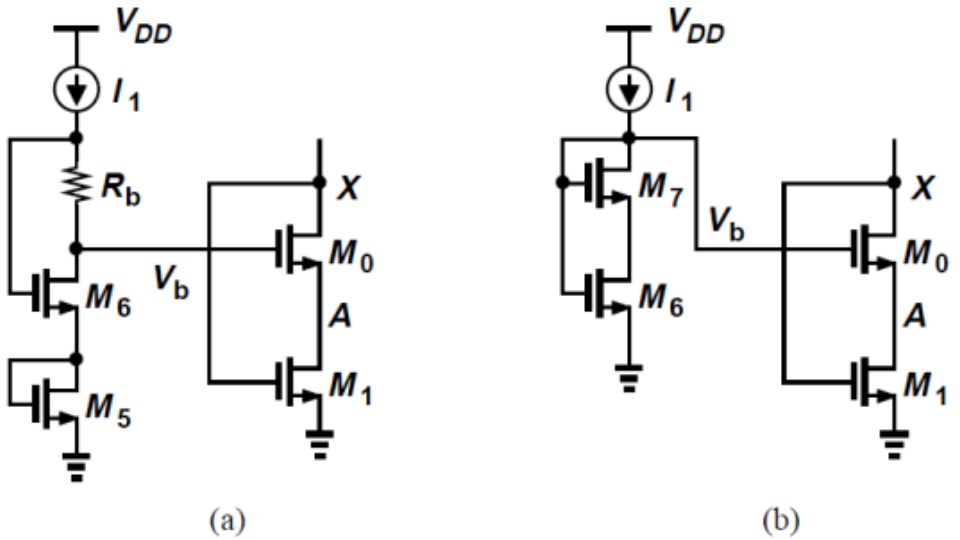
- Must have $V_b - V_{TH0} \leq V_X \ (= V_{GS1})$ for M0 to be saturated and $V_{GS1} - V_{TH1} \leq V_A \ (= V_b - V_{GS0})$ for M1 to be saturated.
- A solution exists if $V_{GS0} + (V_{GS1} - V_{TH1}) \leq V_b \leq V_{GS1} + V_{TH0}$
- We must therefore size M_0 to ensure its overdrive is well below V_{TH1}.

How to generate V_b

- In figure (a):
  - Need $V_b = V_{GS0} + (V_{GS1} - V_{TH1})$
- So we need to …

$$V_{GS5} \approx V_{GS0}$$

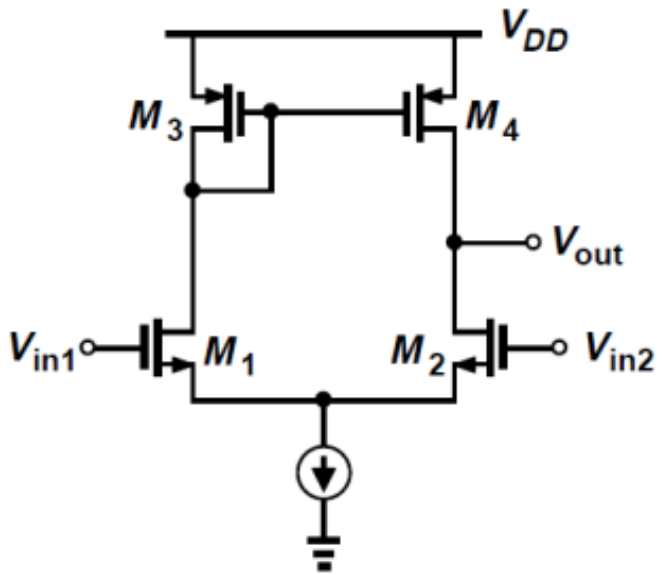
$$V_{DS6} = V_{GS6} - R_b I_1 \approx V_{GS1} - V_{TH1}$$



- Some inaccuracy nevertheless arises because M_5 does not suffer from body effect whereas M_0 does.
- Also, the magnitude of $R_6 x I_1$ is not well-controlled.
- A simpler alternative is shown in Fig (b)

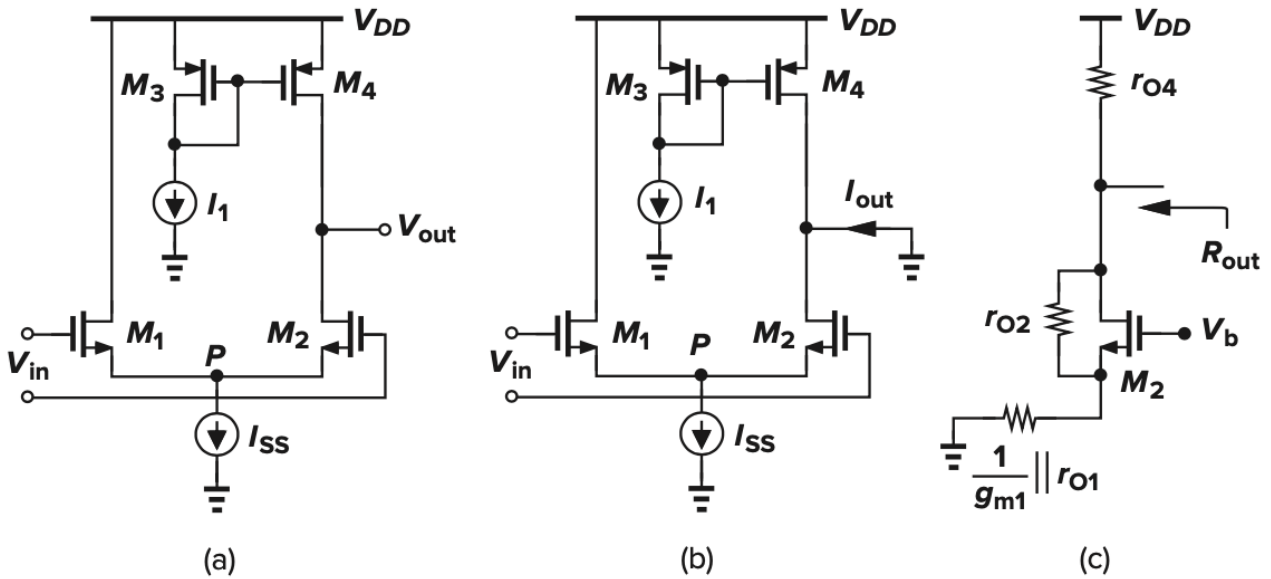
Practical Current Distribution

Active Current Mirrors



- A five-transistor “operational transconductance amplifier” (OTA).
- Note that the output is single-ended, hence the circuit is sometimes used to convert differential signals to a single-ended output.

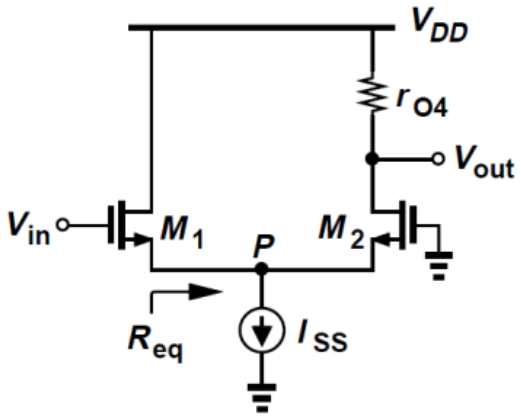
Diff Pair + Active Mirror Load

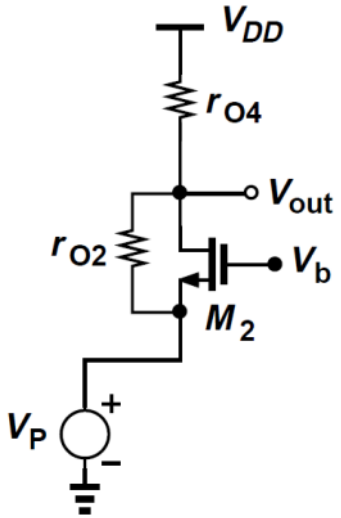


- We may simply discard one output of a differential pair as shown above
- What is the small-signal gain?

$$|A_v| = \frac{g_{m1}}{2}[(2r_{O2}) \| r_{O4}]$$

Second Approach





- We calculate Vp /Vin and Vout/Vp

$$\frac{V_P}{V_{in}} = \frac{R_{eq}||r_{O1}}{R_{eq}||r_{O1} + \frac{1}{g_{m1}}} \qquad R_{eq} = \frac{r_{O2} + r_{O4}}{1 + g_{m2}r_{O2}}$$

$$\frac{V_P}{V_{in}} = \frac{g_{m1}r_{O1}(r_{O2} + r_{O4})}{(1 + g_{m1}r_{O1})(r_{O2} + r_{O4}) + (1 + g_{m2}r_{O2})r_{O1}}$$

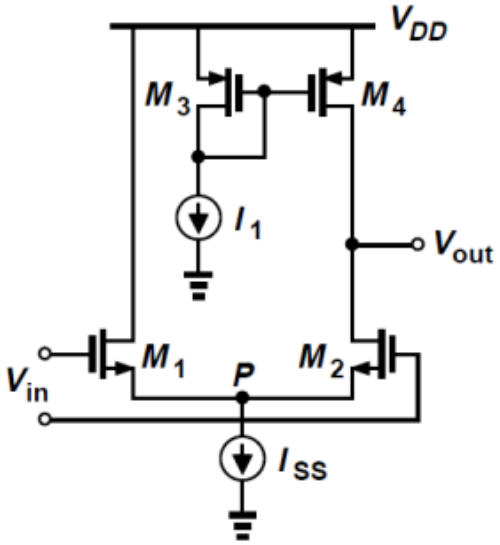
- Calculate Vout/Vp

$$\frac{V_{out}}{V_P} = \frac{(1 + g_{m2}r_{O2})r_{O4}}{r_{O2} + r_{O4}}$$

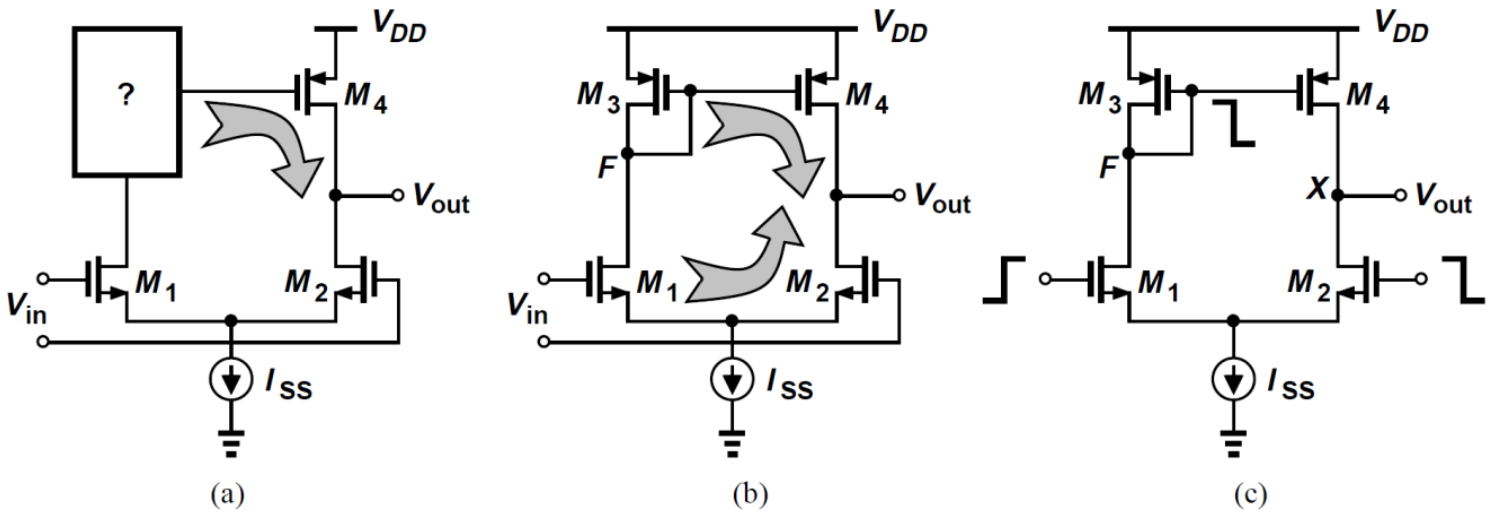
$$\frac{V_{out}}{V_{in}} = \frac{g_{m2}r_{O2}r_{O4}}{2r_{O2} + r_{O4}}$$

$$= \frac{g_{m2}}{2}[(2r_{O2})\|r_{O4}]$$

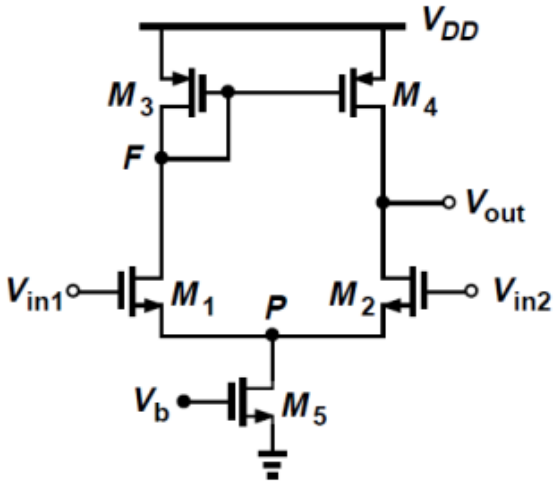
Differential Pair with Active Load



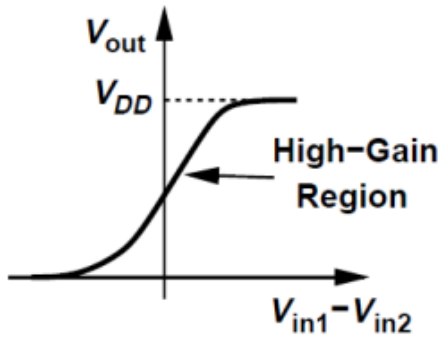
- The small-signal drain current of M1 is “wasted.”
- It is desirable to utilize this current with proper polarity at the output.
- This can be accomplished by the five-transistor OTA, M3 enhances the gain.
- The five-transistor OTA is also called a differential pair with active load.



Large-Signal Analysis



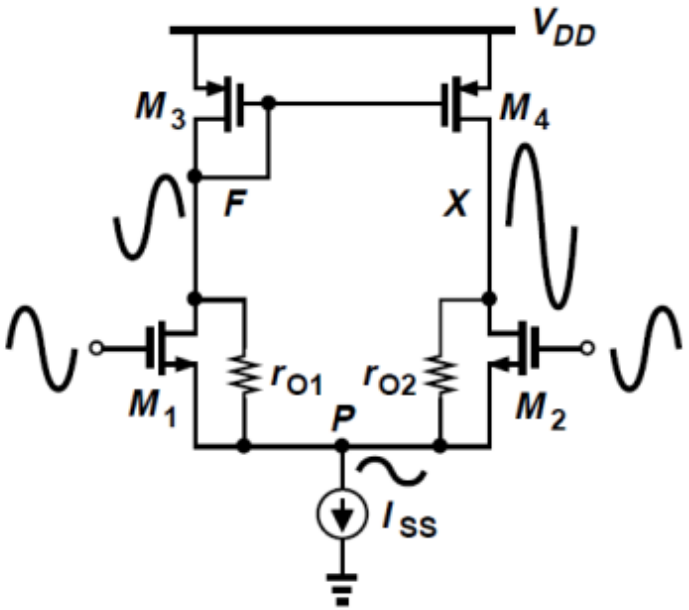
(a)



(b)

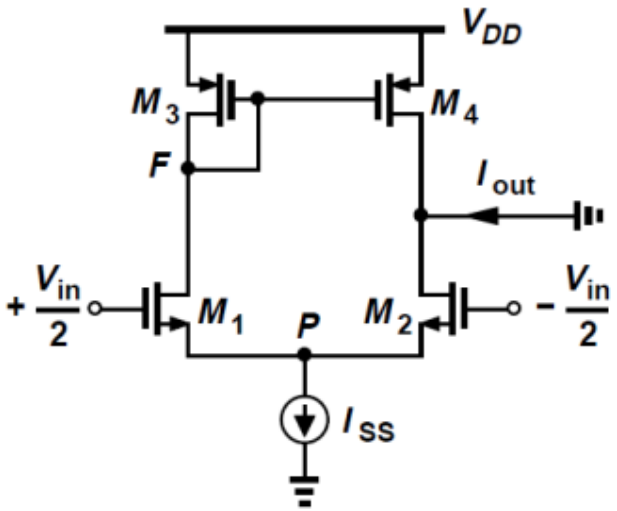
- If V_{in1} is much more negative than V_{in2}, V_{out} = 0.
- As V_{in1} approaches V_{in2}, the output voltage then depends on the difference between I_{D4} and I_{D2}. For a small difference between V_{in1} and V_{in2}, both M2 and M4 are saturated, providing a high gain.
- As V_{in1} becomes more positive than V_{in2}, allowing V_{out} to rise and eventually driving M4 into the triode region .

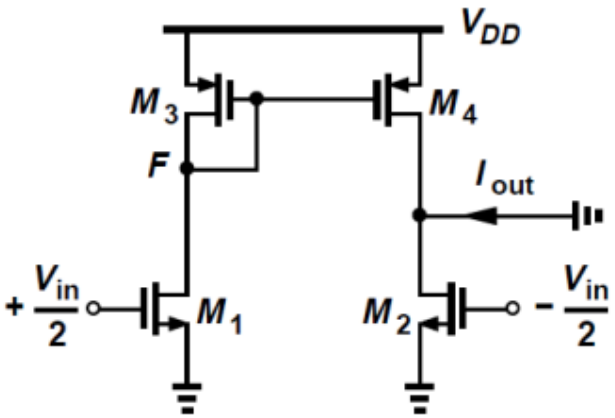
Small-Signal Analysis



- With small differential inputs, the voltage swings at nodes F and X are vastly different.
- The effects of V_F and V_X at node P (through r_{O1} and r_{O2}, respectively) do not cancel each other and this node cannot be considered a virtual ground.

Approximate Analysis





- Node P can be approximated by a virtual ground.

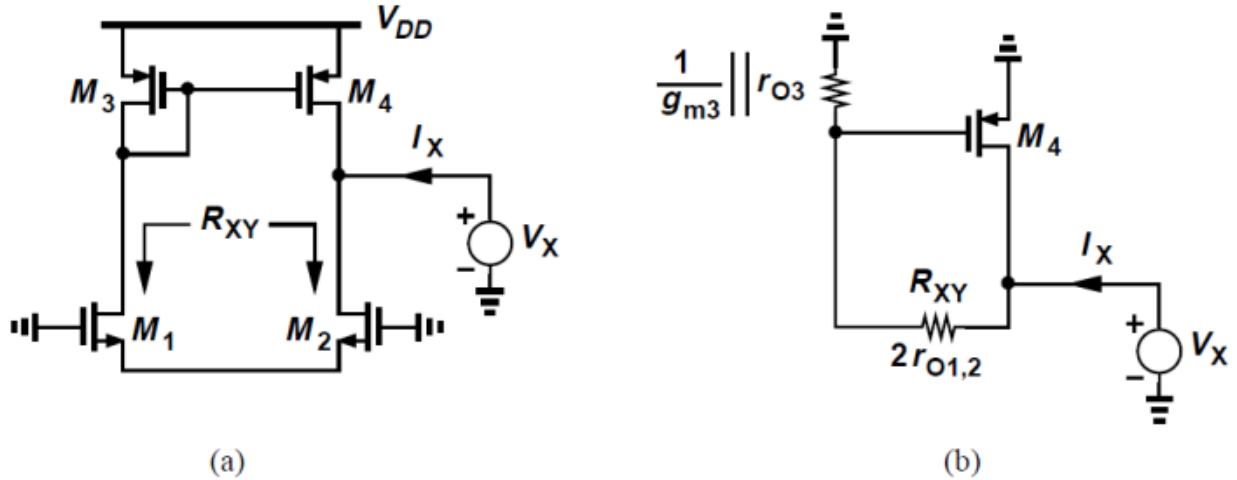
$$I_{D1} = |I_{D3}| = |I_{D4}| = g_{m1,2}V_{in}/2$$

$$I_{D2} = -g_{m1,2}V_{in}/2$$

$$I_{out} = -g_{m1,2}V_{in}$$

$$|G_m| = g_{m1,2}$$

Calculation of R_{out}



- Any current flowing intoM1 must flow out of M2, and the role of the two transistors can be represented by a resistor $R_{XY} = 2r_{O1,2}$
- The current drawn from V_X by R_{XY} is mirrored byM3 ontoM4 with unity gain.

$$I_X = \frac{V_X}{2r_{O1,2} + \frac{1}{g_{m3}} || r_{O3}} \left[1 + \left(\frac{1}{g_{m3}} || r_{O3}\right) g_{m4}\right] + \frac{V_X}{r_{O4}}$$

- For $2r_{O1,2} \gg (1/g_{m3}) \| r_{O3}$

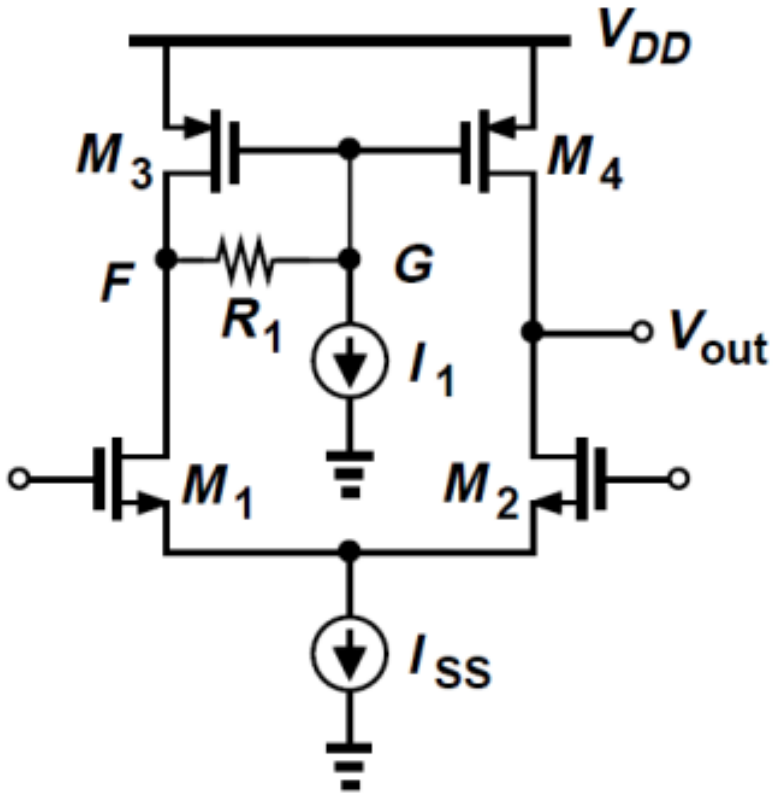
$$R_{out} \approx r_{O2} \| r_{O4}$$

Headroom Issues

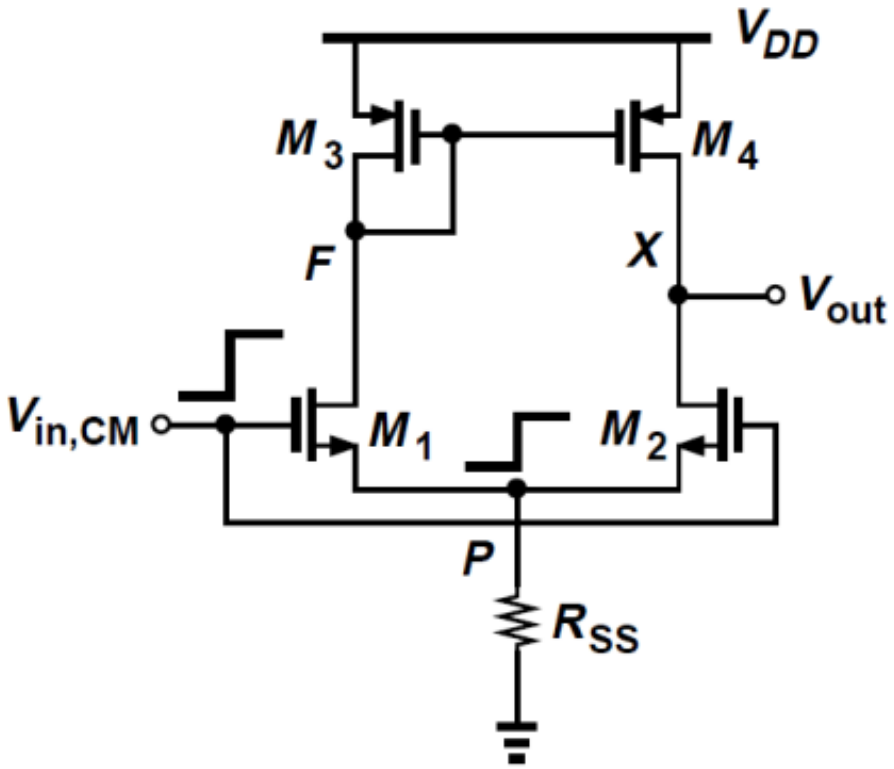
- The five-transistor OTA does not easily lend itself to low-voltage operation.
- The value of I_1 must be much less than Iss/2 and
- Insert a resistor in series with the gate and draw a constant current from it.

$$R_1 I_1 \leq V_{TH3}$$

- Now V_F can be larger than V_G



Common-Mode Properties

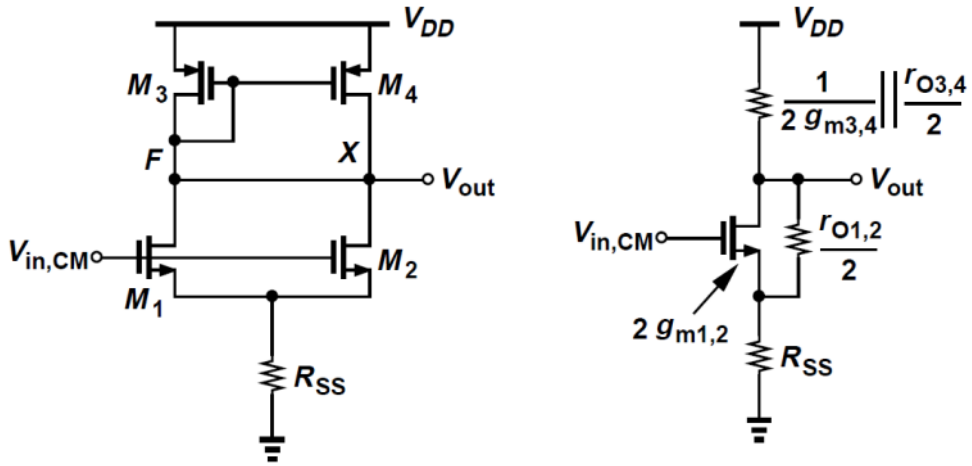


$$A_{CM} = \frac{\Delta V_{out}}{\Delta V_{in,CM}}$$

$$A_{CM} \approx \frac{-\frac{1}{2g_{m3,4}} \left\| \frac{r_{O3,4}}{2} \right.}{\frac{1}{2g_{m1,2}} + R_{SS}}$$

$$= \frac{-1}{1 + 2g_{m1,2}R_{SS}} \frac{g_{m1,2}}{g_{m3,4}}$$

CMRR



(a) (b)

(a) Simplified circuit of Fig. 5.37, (b) equivalent circuit of (a).

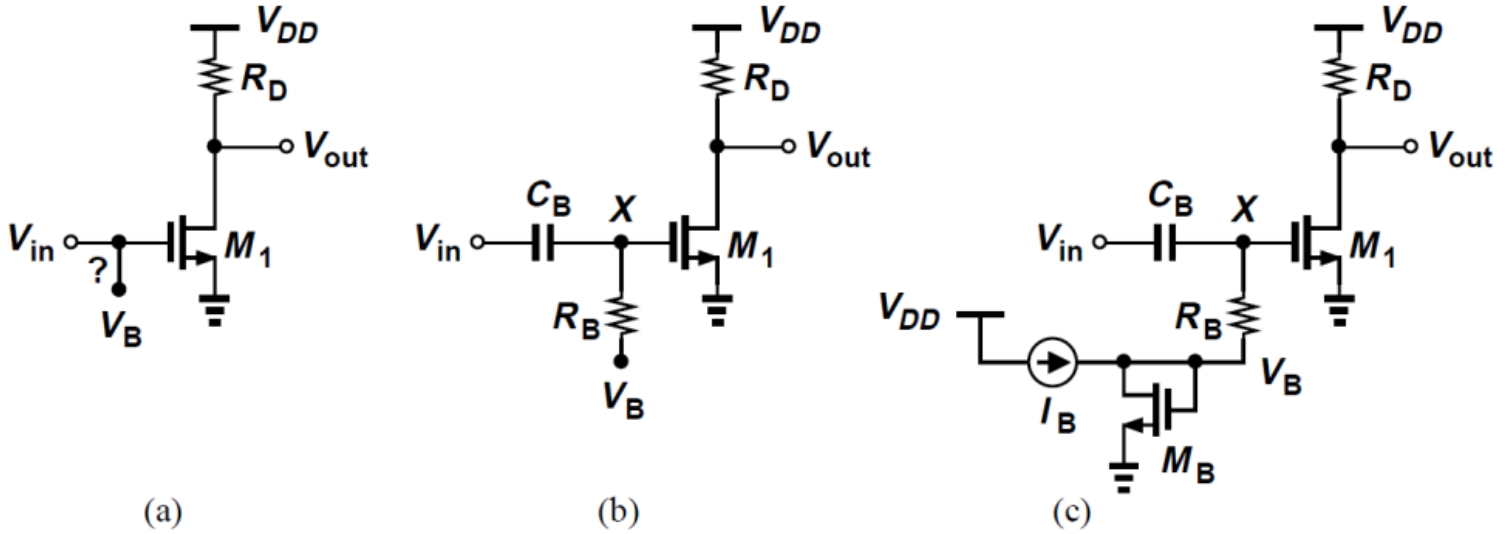
$$\text{CMRR} = \left| \frac{A_{DM}}{A_{CM}} \right|$$

$$= g_{m1,2}(r_{O1,2} \| r_{O3,4}) \frac{g_{m3,4}(1 + 2g_{m1,2}R_{SS})}{g_{m1,2}}$$

$$= (1 + 2g_{m1,2}R_{SS}) g_{m3,4}(r_{O1,2} \| r_{O3,4})$$

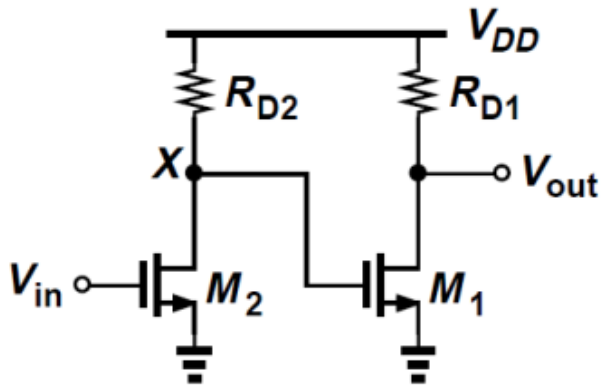
- Even with perfect symmetry, the output signal is corrupted by input CM variations.

Biasing Techniques



- Simple CS Stage
  - How do we ensure that V_B does not "fight" Vin?
- Couple V_{in} capacitively and establish a high impedance for V_B.
- Node X in Fig (b) must have a dc path to a voltage.
- The bias voltage must be generated by a diode-connected device
- Typically select I_B about one-tenth to one-fifth of I_{D1} so as to minimize the power.

Direct Coupling



Direct coupling between two stages.

- Possible to remove the input coupling capacitor and provide the bias voltage from the preceding stage?
- The bias conditions of M1 are influenced by those of M2.
- The PVT variations are amplified.
- One can employ direct coupling between two stages if each has a low gain.