

## Lecture # 5 10/8/2021

- HW 1 due Monday 11:59 pm PT.

Last time

-> General procedure to compute S.S. values in a converter

↳ Using balance eqns.

Today

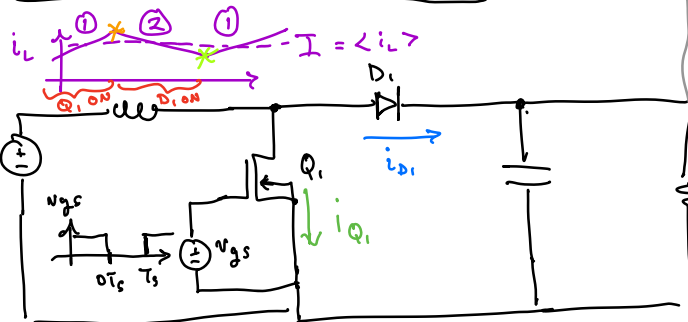
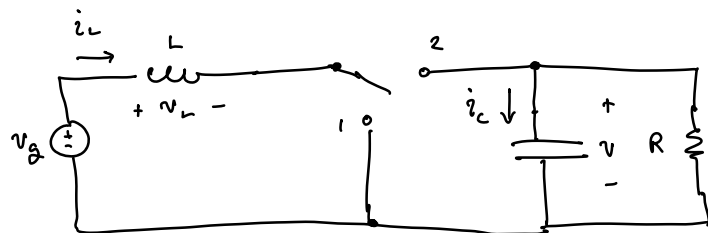
↳ Finish last set of blank pages

↳ Switch realization

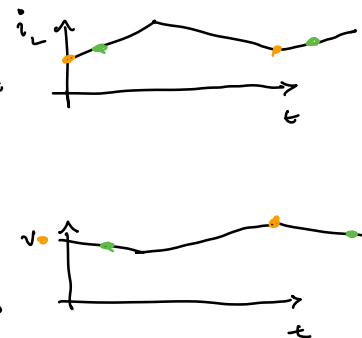
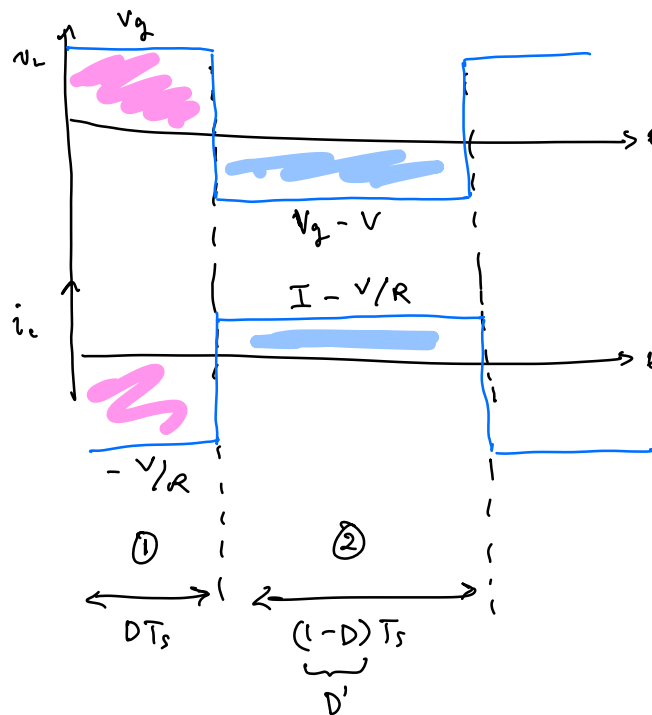
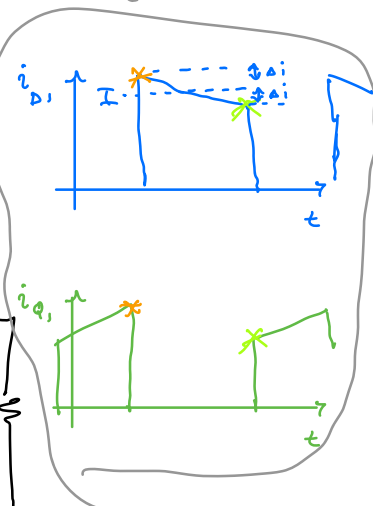
Tip

↳ HW doesn't require a sim., but you can simulate it anyway.

# Boost Example



discontinuous currents



## Lecture #6 10 / 11 / 2021

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Last time

- SS ckt analysis via balance eqns

Today

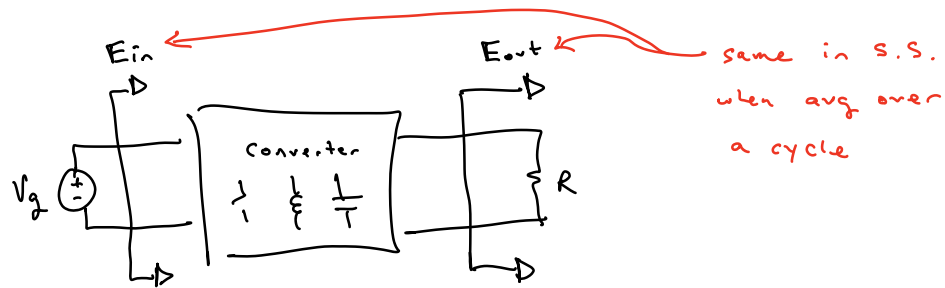
- Cuk converter example w/ balance eqns } Finish Ch2

Next time (maybe today)

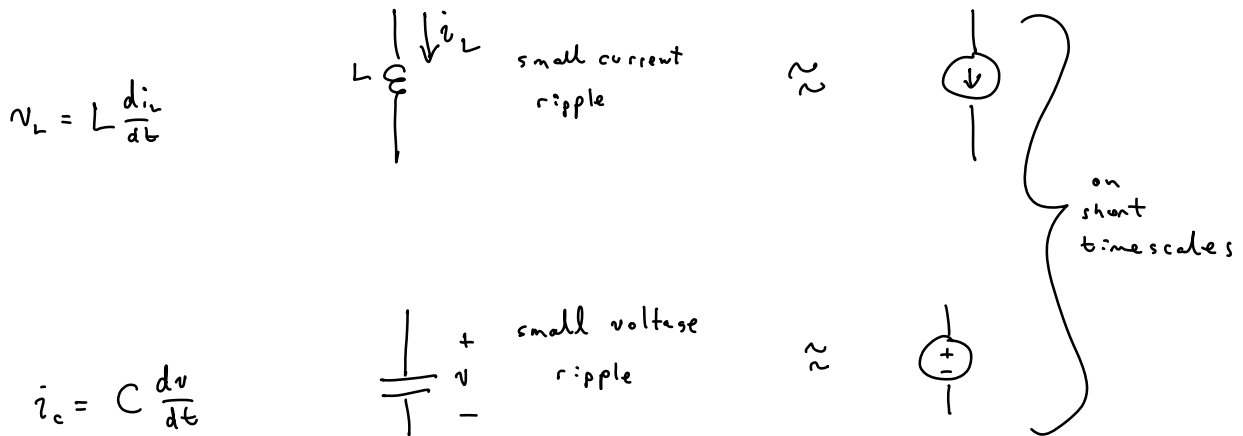
- Start Ch3 (SS balance eqns w/ non ideal ckt elements)

Logistics

- HW 1 deadline extended to Weds noon.



Cap & Inductor Behavior



- Computing Ripple Amplitude

• For L in boost

generally  $\frac{di_L}{dt} = \frac{v_L}{L}$

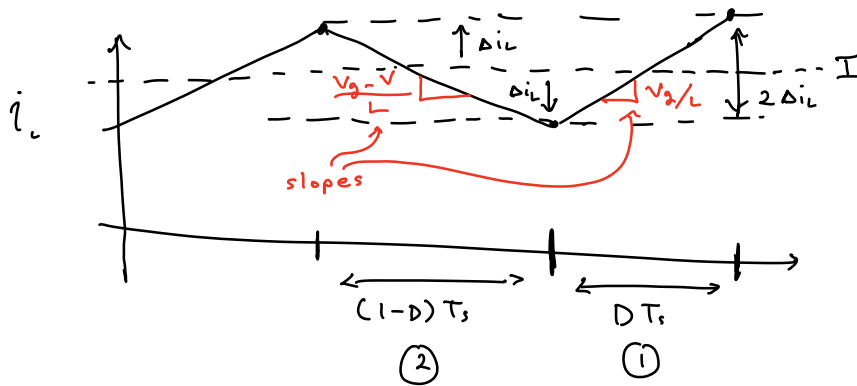
①  $\frac{v_L}{L}$

②  $\frac{(V_g - V)}{L}$

use linear approximation ... rewrite derivative

①  $\frac{2 \Delta i_L}{\Delta t_0} = \frac{2 \Delta i_L}{DT_s} = \left| \frac{V_g}{L} \right| \Rightarrow \Delta i_L = \frac{DT_s V_g}{2L}$

②  $\frac{2 \Delta i_L}{\Delta t_{\text{②}}} = \frac{2 \Delta i_L}{(\underbrace{1-D}_{D'}) T_s} = \left| \frac{V_g - V}{L} \right|$



... similar story for cap

• For C

$$\frac{dv}{dt} = \frac{i_c}{C} \begin{cases} \text{①} & -\frac{V/R}{C} \\ \text{②} & \frac{I - V/R}{C} \end{cases}$$

use approx for derivative

$$\frac{2\Delta V}{\Delta t_1} = \frac{2\Delta V}{DT_s} = \left| \frac{-V/R}{C} \right|$$

$$\text{OR} \quad \frac{2\Delta V}{\Delta t_2} = \frac{2\Delta V}{(1-D)T_s} = \left| \frac{I - V/R}{C} \right| \quad \text{solve either to get } \Delta V$$

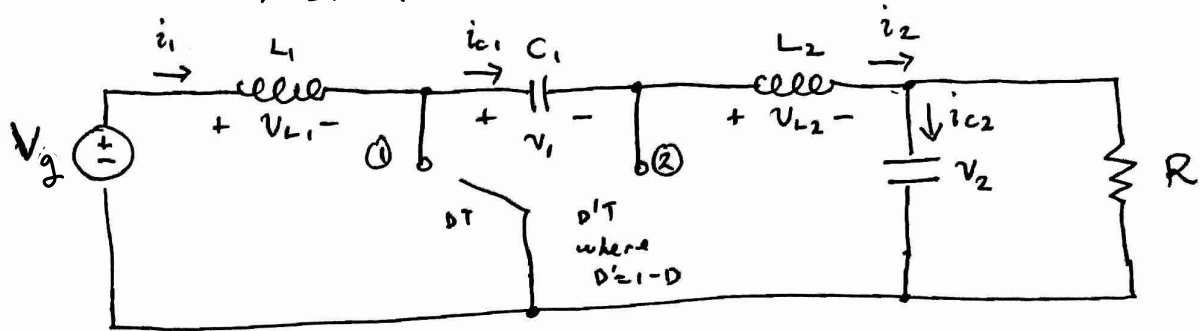
— Discontinuous waveforms through switches

• Look @ boost again

middlebrook was Cuk's advisor @ Caltech

## - Cuk Converter Example

→ D. Maksimovic's advisor @ Caltech



Objective :

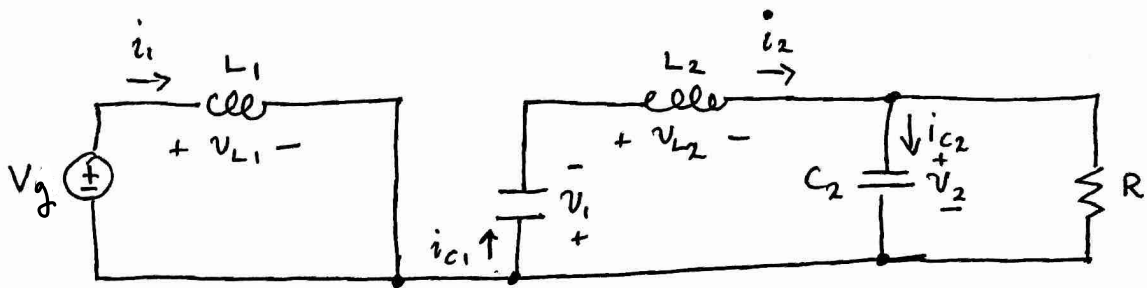
Solve for  $V_{ss}$ , inductor currents & cap voltages  
(dc component of)

Approach

→ 1) Compute balance eqns

2) Do a bunch of algebra

- Cuk: State # 1



$$v_{L1} = V_g$$

$$v_{L2} = -v_1 - v_2$$

$$i_{C1} = i_2$$

$$i_{C2} = i_2 - \frac{v_2}{R}$$

→  
small  
ripple  
approx  
"SRA"

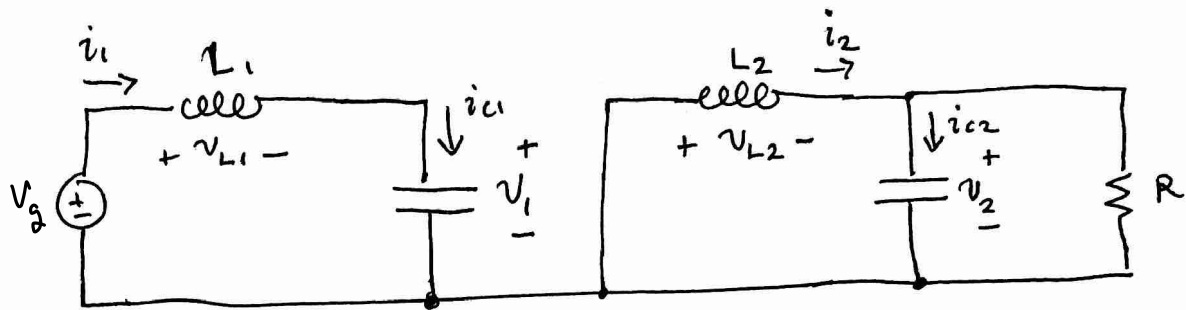
$$v_{L1} = V_g$$

$$v_{L2} = -V_1 - V_2$$

$$i_{C1} = I_2$$

$$i_{C2} = I_2 - \frac{V_2}{R}$$

• Cuk State #2



$$v_{L1} = V_g - v_1$$

$$v_{L2} = -v_2$$

$$i_{c1} = i_1$$

$$i_{c2} = i_2 - \frac{v_2}{R}$$

SRA

→

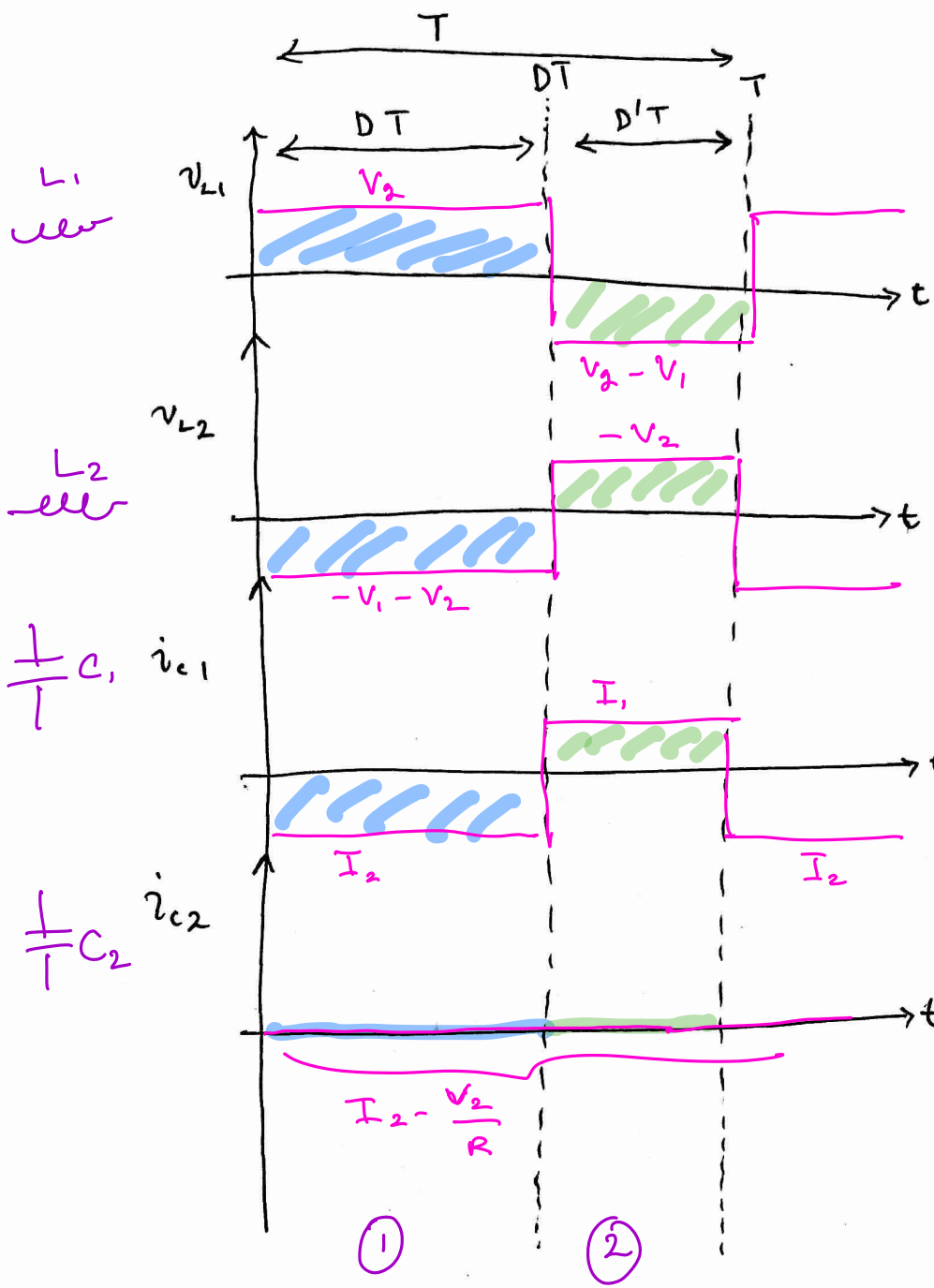
$$v_{L1} = V_g - V_1$$

$$v_{L2} = -V_2$$

$$i_{c1} = I_1$$

$$i_{c2} = I_2 - \frac{V_2}{R}$$





Balance eqns: Set avg to zero.

$$\langle v_{L1} \rangle = D V_2 + D'(V_2 - V_1) = 0$$

$$\langle v_{L2} \rangle = D(-V_1 - V_2) + D'(-V_2) = 0$$

$$\langle i_{c1} \rangle = D I_2 + D' I_1 = 0$$

$$\langle i_{c2} \rangle = I_2 - \frac{V_2}{R} = 0$$

Take stock:

Unknowns:  $I_1, I_2, V_1, V_2$   
 # of equations = 4

can do a bunch of algebra to solve for  $I_1, I_2, V_1, V_2$

- Recap of some basic converters

