

Lecture # 8, 10/18/2021

Last time

- S.S. Analysis w nonideal ckt elements (Ch 3)

→ continue today

Today

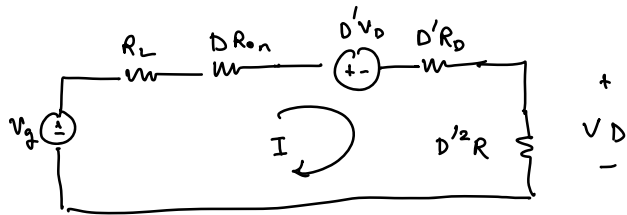
- Realistic η curves from ckt nonidealities
- Might start Ch 4

Tips

- Don't be a calculator monkey! Algebra is more imp. Learn to do math symbolically.
- Pros use computers w/ symbolic formulas

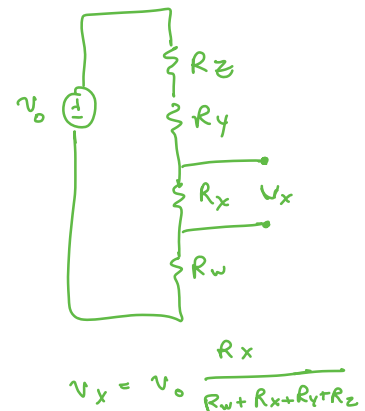
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- Boost example contd.

Push load R to LHS



Easy to find I

$$I = \frac{V_g - V_o D'}{R_L + D R_{on} + D' R_o + D'^2 R}$$



$$V_x = V_o \frac{R_x}{R_w + R_x + R_y + R_z}$$

V_o is easy to get w/ divider formula

$$D'V = (V_g - D'V_D) \frac{D'^2 R}{R_L + D R_{on} + D' R_D + D'^2 R}$$

look @ output/input ratio

$$\frac{V}{V_g} = \frac{1}{D'} \left(1 - \frac{D' V_D}{V_g} \right) \left(\frac{1}{1 + \frac{R_L + D R_{on} + D' R_D}{D'^2 R}} \right) \quad (1)$$

• Efficiency?

$$P_{in} = \quad \neq \quad P_{out} =$$

$$\eta = \frac{P_{out}}{P_{in}} = \quad = \quad = \quad \neq \text{rearrange (1)}$$

=

How to get high $\eta \rightarrow 1$?

pick $\gg \Rightarrow$ supply V_g much higher than diode drop

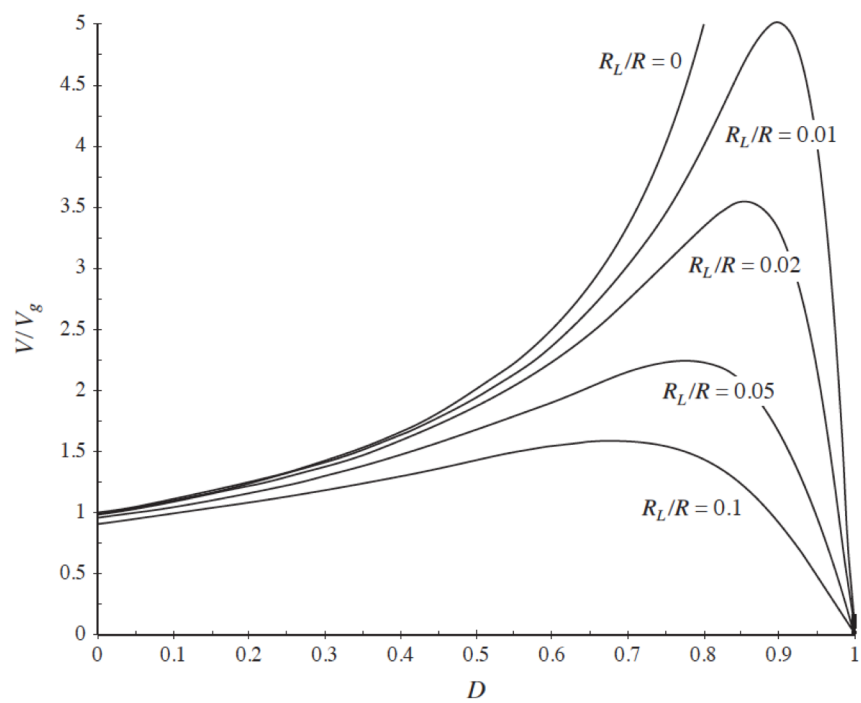
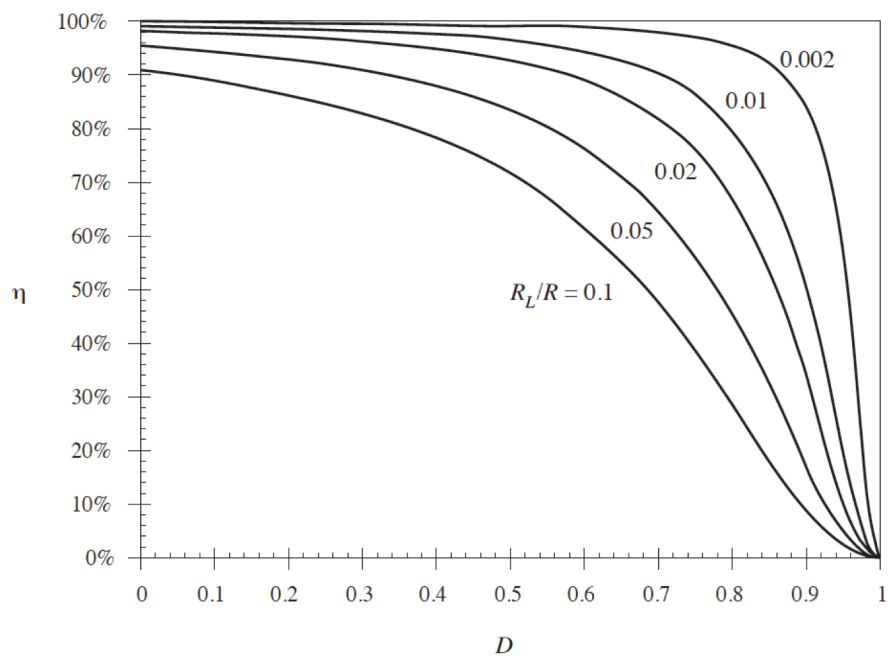
\Rightarrow want small resistances in inductor, MOSFET, diode in converter

- Simplify to get cleaner result
 - ignore diode drop V_d
 - ignore R_D & R_{on} in MOSFET & diode
- keep R_L

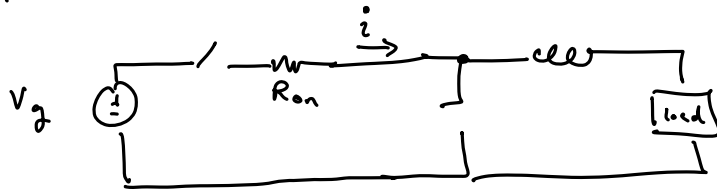
get
 $\Rightarrow \eta \approx$

$$\frac{V}{V_g} \approx$$

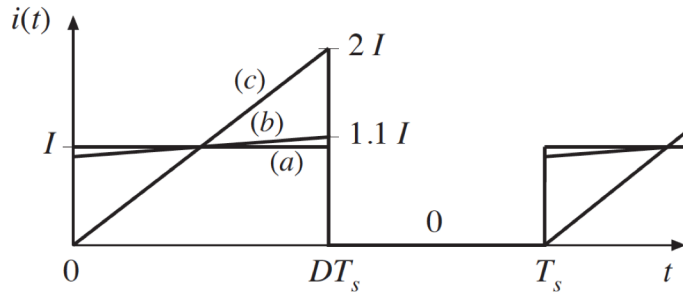
For boost example



- How Accurate is SRA ?



MOSFET current waveforms, for various ripple magnitudes:



Inductor current ripple	MOSFET rms current	Average power loss in R_{on}
(a) $\Delta i = 0$	$I \sqrt{D}$	$D^2 R_{on}$
(b) $\Delta i = 0.1 I$	$(1.00167) I \sqrt{D}$	$(1.0033) D^2 R_{on}$
(c) $\Delta i = I$	$(1.155) I \sqrt{D}$	$(1.3333) D^2 R_{on}$

- What is avg power lost in R_{on} ?

• instantaneous

$$p(t) =$$

=

• Cycle avg power lost

$$\langle p \rangle =$$

=

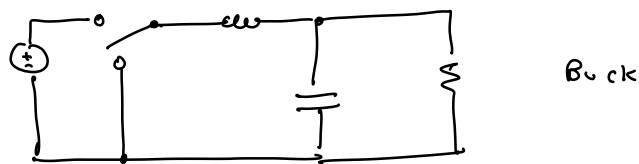
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... but our prior analysis was for avg dc component only
turns out

$$\underbrace{\langle i \rangle^2 R_{on}}_{\text{based on SRA}}$$

— Chapter 4: Switch Realization & Devices

we started out with Single Pole Double Throw model
SPDT

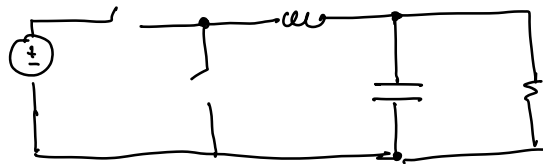


Buck

... but all power semiconductors act like
Single Pole Single Throw (SPST) switches



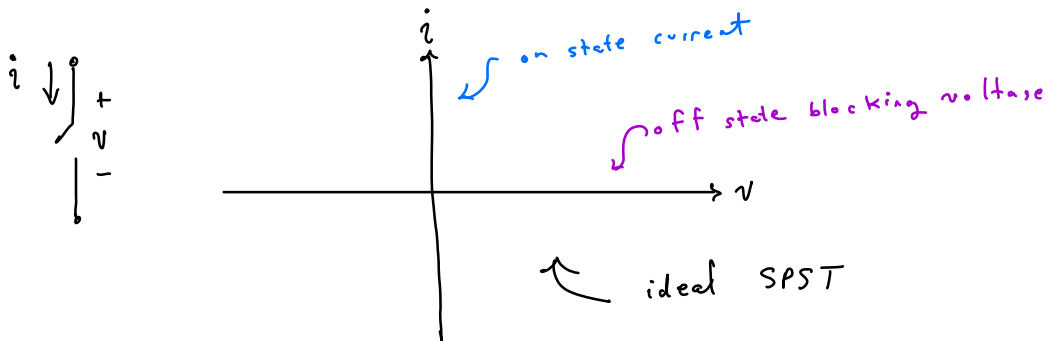
Redraw to get same functionality



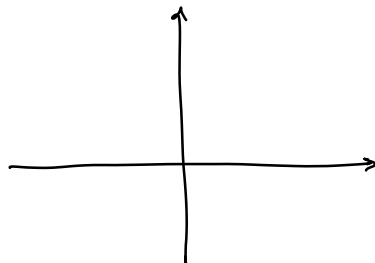
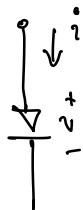
Problems with real world

- Devices aren't perfect switches
- Some can conduct current in one direction only
- block voltages in one polarity only

— Look at $v-i$ "quadrants" each device can handle



The diode



- A single quadrant device
- ⊕ i , ⊖ v only