

$$3 \text{ a.) } q = 0.02 = \frac{1}{N_r + 1} \rightarrow N_r = 49$$

$$T_{sw} = 2N_r \cdot T_{clk}$$

$$N_r = \frac{T_{sw}}{2T_{clk}}$$

$$q_r = \frac{1}{N_r + 1} = \frac{1}{\frac{T_{sw}}{2T_{clk}} + 1} = \frac{1}{\frac{f_{clk}}{2f_{sw}} + 1}$$

$$0.02 = \frac{1}{\frac{100 \text{ MHz}}{2f_{sw}} + 1}$$

$$f_{sw} = 1.02 \text{ MHz}$$

$$b.) \quad N_r = \frac{T_{sw}}{2T_{clk}} \rightarrow 2^{N_{pwm}} = \frac{f_{clk}}{2f_{sw}}$$

$$2^{16} = \frac{f_{clk}}{2f_{sw}} \rightarrow f_{sw} = \frac{f_{clk}}{2 \cdot 2^{16}} = \frac{100 \text{ MHz}}{2 \cdot 65,536} = 762 \text{ Hz}$$

$$c.) \quad N_r \leq 2^{N_{pwm}} - 1$$

$$N_r \leq 2^{16} - 1$$

$$N_r \leq 65,535$$

$$q = \frac{1}{N_r + 1} = \frac{1}{65,536} = 1.5 \text{ E-}5$$

$$q = \Delta D = 0.0015\%$$

$$d.) \quad V_o = V_{in} \cdot \frac{D}{\frac{nDR_{on}}{RD^l} + \frac{D^l}{n}}$$

$$\text{and } n=2, R=10, R_{on}=15 \text{ m}\Omega$$

$$\Delta V_o = \frac{V_{in} \cdot 1.5 \text{ E-}5 \cdot \Delta D}{\frac{2\Delta D R_{on}}{R(1-\Delta D)} + \frac{(1-\Delta D)}{2}} = \frac{V_{in} \cdot 1.5 \text{ E-}5}{\frac{2(1.5 \text{ E-}5)(15 \text{ E-}3)}{10(1-1.5 \text{ E-}5)} + \frac{(1-1.5 \text{ E-}5)}{2}}$$

$$\Delta V_o = 3 \text{ E-}5 V_{in}$$