My notes on "The Strong Factorial Conjecture" by Eric Edo and Arno van den Essen. See: https://arxiv.org/abs/1304.3956

Theorem 1 (Conjecture)**.** Let $a(X) \in \mathbb{C}[X]$ be a polynomial of degree less or equal to $m+1 \in \mathbb{N}_+$ such that $a(X) \equiv X \mod X^2$. If the first m consecutive coefficient of the compositional inverse $a^{-1}(X)$ vanish, then $a(X) = X$.

Remark. If we denote the polynomial $a(X)$ by $\sum_{k \in \mathbb{N}_0} a_k X^k$ for some $a_k \in \mathbb{C}$ for all $k \in \mathbb{N}_0$, then the condition $a(X) \equiv X \mod X^2$ amounts to $a_0 = 0$ and $a_1 = 1$.

Moreover, we have this:

A power series has a compositional inverse if and only if $a_1 \neq 0$. In that case, the inverse is unique.

See

https://www.amazon.com/dp/B00HMUGS4S

https://math.stackexchange.com/questions/2520744/finding-compositional-inverses-for-formal-power-series

My questions:

1. What if $a_0 \neq 0$? Pick $a_0 = 3$. $a(X) = 3$