

Cost Functions

Finds deviation between actual and predicted \rightarrow evaluation of model

3 main types:

1. Regression Cost Function
2. Binary Classification Cost Function
3. Multi-Class Classification Cost Function

1. Regression Cost Function - Predicting continuous values

Variables: y - actual value, y' - predicted, n - # of points

1. Mean Error (ME)

$$ME = \frac{1}{n} \cdot \sum_{i=0}^n (y - y')$$

- positives and negatives can cancel each other out \Rightarrow not good

2. Mean Absolute Error (MAE)

$$MAE = \frac{1}{n} \cdot \sum_{i=0}^n |y - y'|$$

- MAE addresses pos/neg issues, but doesn't penalize outliers or show dramatic changes.

3. Mean Squared Error (MSE)

$$MSE = \frac{1}{n} \cdot \sum_{i=0}^n (y - y')^2$$

- MSE addresses pos/neg issues, and also exaggerates any error

2/3: Classification Cost Functions

Ex: Classifying Happy, Sad, Mad Faces

"Actual" Values:

Happy $[1, 0, 0]$ or
Sad $[0, 1, 0]$ or
Mad $[0, 0, 1]$

ML model provides probability distribution: $[x_1, x_2, x_3]$

Cross Entropy Cost Function:

$A = \text{matrix of prob. distribution}$
 $B = \text{matrix of actual value}$

$$C = - B^T \log(A) = - [1 \ 0 \ 0] \begin{bmatrix} \log x_1 \\ \log x_2 \\ \log x_3 \end{bmatrix}$$
$$= - [\log x_1 + 0 + 0] = - \log x_1$$

Binary Cross Entropy - only 2 options

- Actual output, y , is either 1 or 0

- Predicted output is p , $0 \leq p \leq 1$

$$BCE = - \underbrace{(y \cdot \log(p))}_{\text{calculates both cases } y \rightarrow y=1} + \underbrace{(1-y) \cdot \log(1-p)}_{y \rightarrow y=0}$$

calculates both cases $y \rightarrow y=1$
 $y \rightarrow y=0$

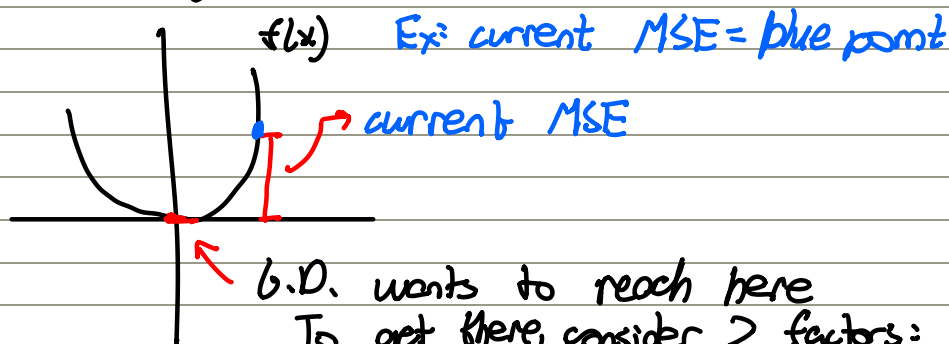
Gradient Descent (G.D)

Ex on MSE:

$$E = \frac{1}{n} \sum_{i=0}^n (y - y')^2 = \frac{1}{n} \sum_{i=0}^n (y - (mx + b))^2 \rightarrow \text{only variables to change:}$$

- " m "
- " b "

Let $f(x) = x^2$ \leftarrow since n is constant



Ex: current MSE = blue point

current MSE

To get there, consider 2 factors:

1. Direction to move
 2. Magnitude of move
- } must change m and b in error function

2 variables we can change are m, b

$$\frac{\partial E}{\partial m} = -\frac{2}{n} \sum_{i=0}^n (y - mx - b)x$$

$$\frac{\partial E}{\partial b} = -\frac{2}{n} \sum_{i=0}^n (y - mx - b)$$

$$m_{\text{new}} = m_{\text{curr}} - \eta \cdot \frac{\partial E}{\partial m}$$
$$b_{\text{new}} = b_{\text{curr}} - \eta \cdot \frac{\partial E}{\partial b}$$

η \rightarrow direction is opposite of gradient
 η \rightarrow size of "step" to take