MIDS - W261 Machine Learning At Scale

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Assignment - HW11

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Week: 11

Useful references

- Spark Quick Reference (http://spark.apache.org/docs/latest/quick-start.html)
- Synchronous Slides for Week 11
- Quora: L1 & L2 Regularization (https://www.quora.com/What-is-the-difference-between-L1-and-L2-regularization)
- Andrew Ng's CS229 Lecture Notes (http://cs229.stanford.edu/notes/cs229-notes1.pdf)
- Sample Logistic Regression Notebook
 (http://nbviewer.jupyter.org/urls/dl.dropbox.com/s/r20ff7q0yni5kiu/LogisticRegression-Spark-Notebook.ipvnb)
- Sample SVM Notebook (http://nbviewer.jupyter.org/urls/dl.dropbox.com/s/dm2l73iznde7y4f/SVM-Notebook-Linear-Kernel-2015-06-19.ipvnb)

Start up Spark

```
In [62]:
         import os
         import sys
         import pyspark
         from pyspark.sql import SQLContext
         # We can give a name to our app (to find it in Spark WebUI) and configur
         e execution mode
         # In this case, it is local multicore execution with "local[*]"
         app_name = "example-logs"
         master = "local[*]"
         conf = pyspark.SparkConf().setAppName(app_name).setMaster(master)
         sc = pyspark.SparkContext(conf=conf)
         sqlContext = SQLContext(sc)
         print sc
         print sqlContext
```

<pyspark.context.SparkContext object at 0x7f959c1516d0>
<pyspark.sql.context.SQLContext object at 0x7f957a1182d0>

HW11.0 Broadcast versus Caching in Spark

What is the difference between broadcasting and caching data in Spark? Give an example (in the context of machine learning) of each mechanism (at a highlevel). Feel free to cut and paste code examples from the lectures to support your answer.

Review the following Spark-notebook-based implementation of KMeans and use the broadcast pattern to make this implementation more efficient. Please describe your changes in English first, implement, comment your code and highlight your changes:

- Notebook (https://www.dropbox.com/s/41q9lqyqhy8ed5q/EM-Kmeans.ipynb?dl=0)
- Notebook via NBViewer (http://nbviewer.ipython.org/urls/dl.dropbox.com/s/41q9lgyqhy8ed5g/EM-Kmeans.ipynb)

We broadcast a variable but cache a resilient distributed dataset (RDD). When we broadcast a variable, we send the variable to each node in the cluster and store it there. When we cache an RDD, we store in the RDD in a cluster-wide cache. Both of these methods are useful for storing data that we use repeatedly. However, they are used differently. It's helpful to think about these differences through examples. When performing KMeans in Spark, we'll want to broadcast the intermediary centroid values but cache the data points for which we're attempting to find to clusters. We broadcast the centroid values so that each node in the cluster in the cluster has access to the centroid values and each map function does not need to pull the centroid data fresh. We cache the RDD because we reference the dataset multiple times. If we don't cache the dataset, each time we loop through it to find the nearest centroid for each point, then we need to reload it. If instead, we cache the dataset, then we'll store in the dataset in memory after the first iteration.

Reference: <u>Broadcast (http://spark.apache.org/docs/latest/programming-guide.html#broadcast-variables)</u>, <u>Cache (http://spark.apache.org/docs/latest/quick-start.html#caching)</u>, and <u>StackOverflow</u> (<u>http://stackoverflow.com/questions/28981359/why-do-we-need-to-call-cache-or-persist-on-a-rdd)</u>

Because I'm only submitting a single notebook, I'll only include the code snippet that changed here. For the full code, we can look at HW10 submission which had this KMeans code made more efficient.

We broadcast the intermediary centroid values to each node. Because we compare each datapoint to the list of all centroids to identify the closest centroid, we have efficiency gains by storing the centroids with each node.

In []:	

```
# set the number of iterations
ITERATIONS = 100
# set the interesting iterations
INTEREST = [1, 10, 20, 100]
# set the iterations we want
# to record errors for
ERROR INTEREST = [1, 10, 20, 30, 40, 50, 100]
# create a list to hold our
# error for each iterations
errors = []
# set the current iteration
iteration = 0
# while the iteration is less than
# the number of iterations
while iteration <= ITERATIONS:</pre>
    # BROADCASTING MODIFICATION TO CODE
    # broadcast the centroids to each node
   broad centroids = sc.broadcast(centroids)
    # take each line of data and
    # find its nearest neighbor
    nearest = parsedData.map(lambda x: findNearest(x,np.array(broad cen
troids.value)))
    # and then reduce by key
    # to get the sum of all points
    # and the number of data points
    summed = nearest.reduceByKey(lambda x,y: (x[0] + y[0], x[1] +
y[1]))
    # and then reduce by dividing
    # the sum of points by the
    # total number of points
    new centroids = summed.map(lambda x: x[1][0]/x[1][1]).collect()
    # convert the new centroids to
    # numpy array
    centroids = np.array(new centroids)
    # calculate the WSSE for this model by computing
    # the distance between each point and its assigned
    # centroid
    # first calculate the error for each point
    error each = nearest.map(lambda x: sqError(x,centroids))
    # then calculate the total error
    error total = error each.reduce(lambda x,y: x+y)
    # increment the iterator
    iteration = iteration + 1
```

```
# check to see if this is an iteration
   # where we want to record the error
   # if it is, then record it
   if iteration in ERROR_INTEREST:
        info = iteration,_error_total
        errors.append(info)
   # check to see if this an iteration
   # of interest, one that we would
   # like to plot
   if iteration in INTEREST:
        # print out the iteration
        # and the centroids
       print "Iteration", iteration
       print "WSSSE:", error total
       print "Centroids:"
       print centroids
        # plot the centroids and the data
       plotKMeans(centroids,data)
       print "\n"
# convert the errors to a numpy array
# and write them to file
errors = np.array(errors)
np.savetxt('errors.csv',errors,delimiter = ',')
```

HW11.1 Loss Functions

In the context of binary classification problems, does the linear SVM learning algorithm yield the same result as a L2 penalized logistic regession learning algorithm?

In your reponse, please discuss the loss functions, and the learnt models, and separating surfaces between the two classes.

In the context of binary classification problems, does the linear SVM learning algorithm yield the same result as a perceptron learning algorithm?

[OPTIONAL]: generate an artifical binary classification dataset with 2 input features and plot the learnt separating surface for both a linear SVM and for logistic regression. Comment on the learnt surfaces. Please feel free to do this in Python (no need to use Spark).

SVM versus Logistic Regression

In the context of binary classification problems, the linear Support Vector Machine (SVM) will yield a very similar result to the L2 penalized logistic regression learning algorithm. However, it is still important to remember the differences between the two. The SVM calculates a decision boundary to classify each example. The logistic regression algorithm calculates the problability that an example is in one or the other class. With SVM, we care only about the edge cases, those that are close to the boundary. With logistic regression, we care about all cases, even if we decrease teh weight of those examples far from the boundary with ridge regularization.

SVM Loss Function

$$\sum_{i=1}^{N} [1 - y_i * W\vec{x}_i]_{+}$$

Logistic Regression L2 Loss Function

$$\sum_{i=1}^{N} [(y_i - W\vec{x}_i)^2]$$

We can see the difference between the loss functions graphically. For logistic regression, we calculate some training error even for correctly classified examples. In the case of hinge loss for SVM, we don't worry about these clearly correctly calculated examples.

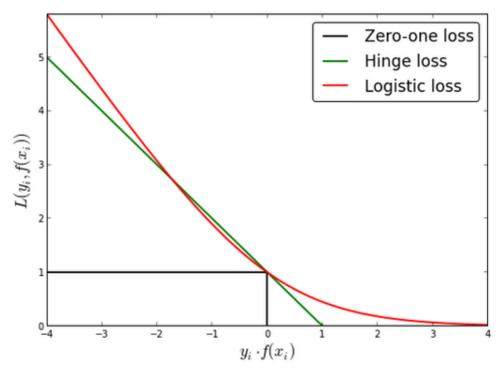


Image source:Quora (https://www.quora.com/ls-logistic-regression-with-regularization-similar-in-a-conceptual-sense-to-simple-linear-SVM)

SVM versus Perceptron

In the context of binary classification problems, the linear Support Vector Machine (SVM) algorithms does not yield the same results as a perceptron algorithm. Intuitively, we think of the perceptron algorithm as stopping once it has successfully classified all the data. However, the linear SVM attempts to find the hyperplane that is furtherest from all the datapoints. This means that it creates more of a buffer between the classes. We can also look at the loss functions as a way of understanding this.

SVM Loss Function

$$\sum_{i=1}^{N} [1 - y_i * W \vec{x}_i]_{+}$$

Perceptron Loss Function

$$\sum_{i=1}^{N} [max(0, -W\vec{x}_i * y_i)]$$

The SVM loss function is a hinge loss function that is always working. It produces continuous values that we must optimize. However, the perceptron loss function only creates discrete values, 0 or the value of the incorrectly classified point. Once all points are correctly classified, the perceptron loss function stops working.

HW11.2 Gradient descent

In the context of logistic regression describe and define three flavors of penalized loss functions. Are these all supported in Spark MLLib (include online references to support your answers)?

Descibe probabilitic interpretations of the L1 and L2 priors for penalized logistic regression (HINT: see synchronous slides for week 11 for details)

In the context of logistic regression, we can think of 3 flavors of penalized loss functions that are **all** supported by Spark's MLLib. The 3 flavors are of the regularizer:

- L1 (or Lasso) Regularization
- L2 (or Ridge) Regularization
- None (no regularization)

These three flavors all have different effects and penalize the complexity of the model in different ways. For **L1** (**Lasso**) Regularization, we penalize the model by adding to the loss function a component that sums the absolute values of the coefficients. We penalize the axes more (see image below). Therefore, with Lasso regularization we can take the noisy, but useless, features and reduce them to zero. For **L2** (**Ridge**) Regularization, we penalize the the complexity of the model by taking the square root of the sum of the squares of the coefficients. With this regularization, we do not bring the noisy, but useless, features to zero, instead we end up bringing them very close to zero. Ultimately, the goal of both types of regularization is to penalize the model-maker for making overly complex that overfit the data. The third flavor is **no regularization** which doesn't provide a penalty for model complexity. The risk with this approach is that the model can get increasingly complex until it overfits the training data.

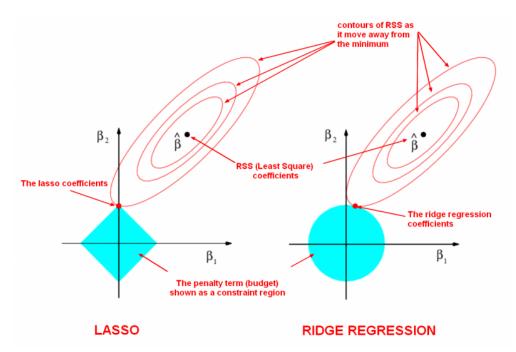


Image source (http://gerardnico.com/wiki/data_mining/lasso)

HW11.3 Logistic Regression

Generate 2 sets of linearly separable data with 100 data points each using the data generation code provided below and plot each in separate plots. Call one the training set and the other the testing set.

```
def generateData(n):
    """
    generates a 2D linearly separable dataset with n samples.
    The third element of the sample is the label
    """
    xb = (rand(n)*2-1)/2-0.5
    yb = (rand(n)*2-1)/2+0.5
    xr = (rand(n)*2-1)/2+0.5
    yr = (rand(n)*2-1)/2-0.5
    inputs = []
    for i in range(len(xb)):
        inputs.append([xb[i],yb[i],1])
        inputs.append([xr[i],yr[i],-1])
    return inputs
```

Modify this data generation code to generating non-linearly separable training and testing datasets (with approximately 10% of the data falling on the wrong side of the separating hyperplane. Plot the resulting datasets.

NOTE: For the remainder of this problem please use the non-linearly separable training and testing datasets.

Using MLLib train up a LASSO logistic regression model with the training dataset and evaluate with the testing set. What a good number of iterations for training the logistic regression model? Justify with plots and words.

Derive and implement in Spark a weighted LASSO logistic regression. Implement a convergence test of your choice to check for termination within your training algorithm.

Weight the above training dataset as follows: Weight each example using the inverse vector length (Euclidean norm):

```
weight(X)= 1/||X||,
where ||X|| = SQRT(X.X)= SQRT(X1^2 + X2^2)
Here X is vector made up of X1 and X2.
```

Evaluate your homegrown weighted LASSO logistic regression on the test dataset. Report misclassification error (1 - Accuracy) and how many iterations does it took to converge.

Does Spark MLLib have a weighted LASSO logistic regression implementation? If so, use it and report your findings on the weighted training set and test set.

Write a function generate linearly separable data

```
In [13]: import numpy as np
from numpy.random import rand

def generateData(n):
    """generates a 2D linearly separable dataset with n samples.
    The third element of the sample is the label"""

    xb = (rand(n)*2-1)/2-0.5
    yb = (rand(n)*2-1)/2+0.5
    xr = (rand(n)*2-1)/2+0.5
    yr = (rand(n)*2-1)/2-0.5
    inputs = []
    for i in range(len(xb)):
        inputs.append([xb[i],yb[i],1])
        inputs.append([xr[i],yr[i],-1])
    return np.array(inputs)
```

Generate two samples of linearly separable data

```
In [28]: import numpy as np

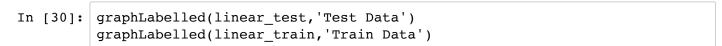
# generate the two sets and save them
linear_test = generateData(50)
linear_train = generateData(50)
np.savetxt('linear_test.csv',linear_test,delimiter=',')
np.savetxt('linear_train.csv',linear_train,delimiter=',')

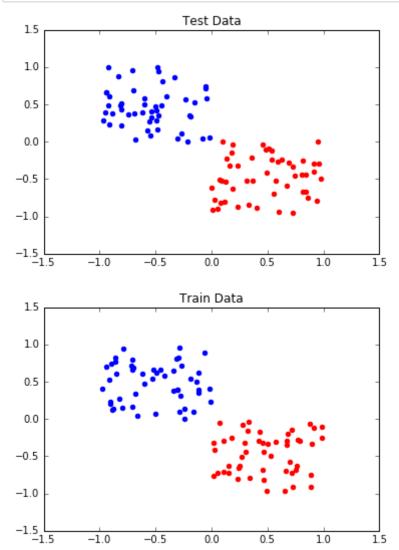
# preview one of the files
!head linear_test.csv
```

Write a function to graph the data

```
In [29]:
         import numpy as np
         import matplotlib.pyplot as plt
         def graphLabelled(data,title,color1='red',color2='blue'):
             """function that takes an input data, 2D, with
             a third column for the label. splits the data
             into two data sets and plots the two data sets
             with two different colors"""
             # split the data
             set1 = data[data[:,2]==-1]
             set2 = data[data[:,2]==1]
             # plot each set
             plt.scatter(set1[:,0],set1[:,1],color=color1)
             plt.scatter(set2[:,0],set2[:,1],color=color2)
             # set the title
             plt.title(title)
             # show the plot
             plt.show()
```

Plot the training and test data sets





Modify function to generate mostly linearly separable data

```
In [31]: import numpy as np
         from numpy.random import rand
         def generateDataMix(n,mix=0.2):
             """generates a 2D linearly separable dataset with n samples.
             The third element of the sample is the label
             we add the mix variable that controls what percentage of
             datapoints are mixed into the other set"""
             xb = (rand(n)*2-1)/2-0.5
             yb = (rand(n)*2-1)/2+0.5
             xr = (rand(n)*2-1)/2+0.5
             yr = (rand(n)*2-1)/2-0.5
             inputs = []
             for i in range(len(xb)):
                 inputs.append([xb[i],yb[i],1])
                 inputs.append([xr[i],yr[i],-1])
             # convert the inputs to a numpy
             # array
             inputs = np.array(inputs)
             # generate the indexes of the examples
             # that we would like to swap
             swap = np.random.randint(0, n, size=mix*n)
             # loop through all those we wish to swap
             # and swap their classifications
             for i in swap:
                 # reset the current class by multiplying
                 # it by negative 1
                 inputs[i][2] = inputs[i][2] * -1
             return inputs
```

Generate two samples of non-linearly separable data

```
In [34]: import numpy as np
  # generate the two sets and save them
  test nl = generateDataMix(50)
  train nl = generateDataMix(50)
  np.savetxt('test nl.csv',test nl,delimiter=',')
  np.savetxt('train_nl.csv',train_nl,delimiter=',')
  # preview one of the files
  !head test_nl.csv
  e+00
  0e+00
```

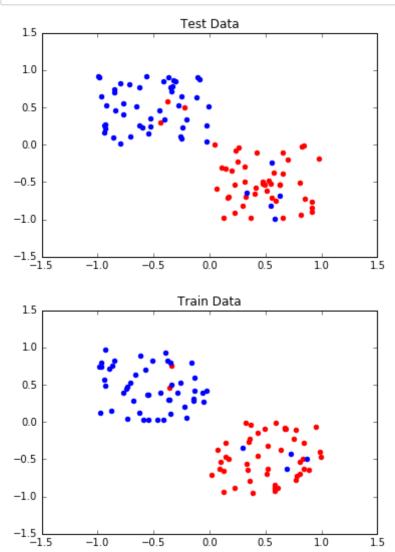
/opt/conda/envs/python2/lib/python2.7/site-packages/ipykernel/__main__.py:25: DeprecationWarning: using a non-integer number instead of an integer will result in an error in the future

1.066077316613961434e-01, -3.126209406904745247e-01, -1.00000000000000000

Plot the training and test data sets

0e+00

```
In [35]: graphLabelled(test_nl,'Test Data')
    graphLabelled(train_nl,'Train Data')
```



Write function to turn data into Spark's labelled points

```
In [77]: from pyspark.mllib.regression import LabeledPoint

def parsePoint(line):
    """takes each line in the format [x,y,label] and converts it to Spark labelled points RDD"""

# grab the values from the line
    values = [float(x) for x in line.split(',')]

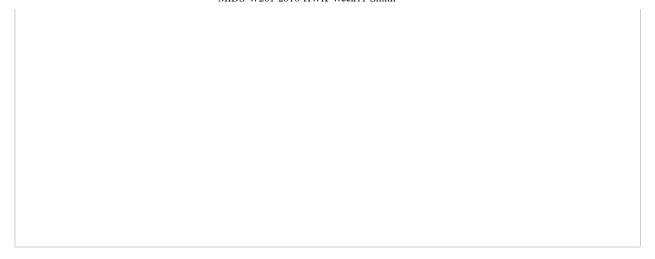
# if the classification is -1, then
    # convert it to zero
    if values[2] == -1:
        values[2] = 0

return LabeledPoint(values[2], values[0:2])
```

Convert the data to a format readable by Spark's library

Create a function to measure the accuracy of the model

```
In [83]: def accuracy(model,data):
              """takes two arguments, model and data
             where the model is the predictive model and
             data is the testing data. computes the
             predictions for each example in the test
             data and computes the accuracy as the
             portion of correctly classified examples
             over all examples"""
             # number of examples
             total = len(data)
             # set a counter for the number of correctly
             # classified examples
             correct = 0
             # predict each examples and see if its
             # accurate
             for example in data:
                 # set the true class and the coordinates
                 truth = example[2]
                 coord = list(example[0:2])
                 # conver the truth to 0,1
                 if truth == -1:
                     truth = 0
                 # get the prediction
                 prediction = model.predict(coord)
                 # if its correct increment our correct counter
                 if prediction == truth:
                      correct = correct + 1
             # return the accuracy
             accur = float(correct) / float(total)
             return accur
```



Train a logistic regression model using Spark's library

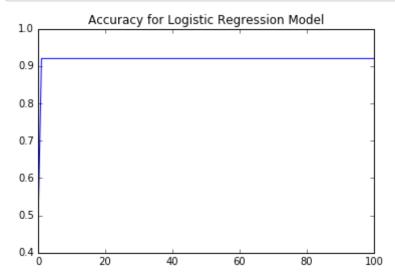
In [126]:	

from pyspark.mllib.classification import LogisticRegressionWithLBFGS # some test data that we can use based on the documentation #data = sc.parallelize([LabeledPoint(0.0, [0.0, 1.0]),LabeledPoint(1.0, [1.0, 0.0])]) # set the number of iterations ITERATIONS = 100 # set the current iteration iteration = 0# set the iterations of interest for plotting interest = [0,1,2,3,4,5,10,20,35,60,100]# create an array to store the accuracies accuracies = [] # set an array of weights that we'll update weights = [] # loop through all the intersting iterations for i in interest: # set the model model = LogisticRegressionWithLBFGS.train(trainRDD,regType='11',iter ations=i) # compute the accuracy accur = accuracy(model,test nl) # add the accuracy to the list accuracies.append(accur) # print out the accuracy and the iteration print "Iteration",i print "Accuracy:",accur print "Coefficients:", model.weights print "\n" #### OLD APPROACH # # keep going till we have 10 iterations # while iteration <= ITERATIONS: # OLD APPROACH # # # set the model with no weights if its # # # the first iteration # # if iteration == 0: # # model = LogisticRegressionWithLBFGS.train(trainRDD, regType ='11',iterations=1) # # # else begin the model with the # # # previous weights # # else: # # model = LogisticRegressionWithLBFGS.train(trainRDD, regType ='11',iterations=1,initialWeights=weights)

```
# set the weights based on the model
        weights = model.weights
      # set the model
      model = LogisticRegressionWithLBFGS.train(trainRDD,regType='11',it
erations=i)
      # calculate the accuracy
      accur = accuracy(model,test_nl)
#
      # if this one of the iterations of interest
      # plot it and compute the accuracy
      if iteration in interest:
#
          print "\n"
          print "Iteration", iteration
#
          print "Accuracy:",accur
#
      # increment the iteration
      iteration = iteration + 1
```

```
Iteration 0
Accuracy: 0.48
Coefficients: [0.0,0.0]
Iteration 1
Accuracy: 0.92
Coefficients: [-1.2040139379,1.27252761354]
Iteration 2
Accuracy: 0.92
Coefficients: [-1.72329825785,1.77836145634]
Iteration 3
Accuracy: 0.92
Coefficients: [-2.1905942677,2.18007800153]
Iteration 4
Accuracy: 0.92
Coefficients: [-2.45433288323,2.34884573967]
Iteration 5
Accuracy: 0.92
Coefficients: [-2.57776425633,2.37246864483]
Iteration 10
Accuracy: 0.92
Coefficients: [-2.71507842894,2.2345208461]
Iteration 20
Accuracy: 0.92
Coefficients: [-2.71507842894,2.2345208461]
Iteration 35
Accuracy: 0.92
Coefficients: [-2.71507842894,2.2345208461]
Iteration 60
Accuracy: 0.92
Coefficients: [-2.71507842894,2.2345208461]
Iteration 100
Accuracy: 0.92
Coefficients: [-2.71507842894,2.2345208461]
```

```
In [123]: # plot the evolving accuracies
plt.plot(interest,accuracies)
plt.title("Accuracy for Logistic Regression Model")
plt.show()
```



We can see that after even a single iteration, we have stabilized in terms of accuracy at around 92%. However, the actual coefficients don't stabilize till around 10 iterations.

Write a function to calculate each example's weight

```
In [103]: import math
          def calcWeight(line):
               """takes a point and returns that point
              with its classification and the weight"""
              # grab the values from the line
              values = [float(x) for x in line.split(',')]
              # get the class and the coordinates
              x = float(values[0])
              y = float(values[1])
              truth = int(values[2])
              # define the weight function
              def weight(x,y):
                  return math.sqrt(x**(2) + y **(2))
              # get the weight for the point
              wgt = weight(x,y)
              # return the point with all the
              # data
              return [x,y,truth,wgt]
```

Calculate the weights for the training data

```
In [108]: # load in the training data
           trainRDD = sc.textFile('train_nl.csv')
           # weight it
           train_wgt = trainRDD.map(calcWeight)
           # print out a sample
           print np.array(train_wgt.collect())[0:10]
           [[-0.66677651 0.62992274 1.
                                                     0.91727508]
            [ 0.32765501 -0.56620453 -1.
                                                     0.65417534]
                                                     0.208979061
            [-0.20250519 \quad 0.05161294 \quad 1.
            [ 0.7290459 -0.42157489 1.
                                                     0.84215991]
            [-0.34394326 \quad 0.7584167 \quad -1.
                                                     0.83276218]
            [ 0.68047352 -0.08827704 -1.
                                                     0.68617566]
            [-0.26157763 \quad 0.52208947 \quad 1.
                                                     0.583952281
            [ 0.29162002 -0.35207817 1.
                                                     0.45716657]
            [-0.96350059 \quad 0.74657127 \quad 1.
                                                     1.21889378]
                                                     0.67439552]]
            [ 0.66888864 -0.08600763 -1.
```

Make a named tuple to help us deal with all our data

In [158]: from collections import namedtuple import numpy as np # create a named tuple type of Point # that has the values: features, # class, and weight Point = namedtuple('Point', 'x y wgt') # write a function to convert a data # to the this format def readPoint(line): # set a blank array to hold # the features x = []# loop through all but the last # two elements of the array, and # append it to our array for i in line[:-2]: x.append(float(i)) # append the bias term x.append(1.0)# get the classification y = line[-2]# get the weight wgt = line[-1]return Point(x, y, wgt)

Convert the training data into our homegrown point

```
In [159]: # convert the training data to named tuple points
    train = train_wgt.map(readPoint).cache()

# print a sample
    print train.collect()[0:10]
```

[Point(x=[-0.6667765110042355, 0.6299227383386319, 1.0], y=1, wgt=0.917 2750797350934), Point(x=[0.3276550088540289, -0.5662045276381993, 1.0], y=-1, wgt=0.6541753373103653), Point(x=[-0.20250519138016065, 0.051612 9445782425, 1.0], y=1, wgt=0.20897906254922338), Point(x=[0.72904589988 71743, -0.4215748940248314, 1.0], y=1, wgt=0.84215991083306), Point(x=[-0.34394325533068537, 0.7584167005560385, 1.0], y=-1, wgt=0.8327621836 813778), Point(x=[0.6804735163940775, -0.08827703698126466, 1.0], y=-1, wgt=0.6861756639315566), Point(x=[-0.2615776286653765, 0.5220894651654 919, 1.0], y=1, wgt=0.5839522801179827), Point(x=[0.29162001661399173, -0.35207816936229186, 1.0], y=1, wgt=0.4571665685846325), Point(x=[-0.963500593763634, 0.7465712664634533, 1.0], y=1, wgt=1.218893781299962), Point(x=[0.6688886354181288, -0.08600763046501081, 1.0], y=-1, wgt=0.6743955212556889)]

Homegrown Logistic Regression Function (unweighted)

In [187]:	

import numpy as np def logisticRegressionGDUW(data, wInitial=None, learningRate=0.05, itera tions=50, regParam=0.01, regType=None): """Logistic Regression function that takes as input the data, an initial set of weights, a learning rate, a number of iterations, a regularization hyperparameter, and the type of regularization. It outputs the coefficients for the model.""" # set the feature length by taking the length # of the features in the first point featureLen = len(data.take(1)[0].x) # count the number of data points n = data.count() # if the initial coefficients are none, # then initalize a random set of coefficients # that are equal to the feature length if wInitial is None: w = np.random.normal(size=featureLen) # otherwise, set the coefficients to be the # coefficients provided by the user else: w = wInitial # loop through the number of iterations # specified by the user for i in range(iterations): # broadcast the coefficients so that # we can hold the coefficients in memory wBroadcast = sc.broadcast(w) # calculate the gradient for each point # and then reduce by summing all the # partial gradients # the partial gradient is 1 calculated as # using the formula here # https://work.caltech.edu/library/093.pdf partial gradient = data.map(lambda point: (1 / \ (1 + np.exp(-point.y*np.dot(wBroadcast.value, point.x)))-1) * \ point.y * np.array(point.x)) gradient = partial gradient.reduce(lambda a, b: a + b) # if the regularization type is 'ridge' # then use the if regType == "Ridge": # multiply the weight vector by 1 to make

wReg = w * 1

a copy of the array

```
# ignore the last value of weight vector
        # because it is the bias term,
        # ignored in regularization
       wReg[-1] = 0
    # else if we're using a 'lasso' regularization
    # type
    elif regType == "Lasso":
        # multiply the weight vector by 1 to make
        # a copy of the array
       wReg = w * 1
        # ignore the last value of coefficient vector
        # because it is the bias term,
        # ignored in regularization
       wReg[-1] = 0
        # if the coefficient is greater than 0,
        # make it 1, otherwise make it zero
       wReg = (wReg>0).astype(int) * 2-1
    # if no regularlization type is provided,
    # just don't regularize at all
   else:
        wReg = np.zeros(w.shape[0])
    # set the gradient equal to itself plus
    # the regularization parameter times the
    # current weights
    # gradient: gradient of Sqaured Error +
    # gradient of regularized term
    gradient = gradient + regParam * wReg
    # the new set of coefficients is the
    # current set of coefficients minus
    # the gradient times the learning rate
    # all over the number of exmaples
   w = w - learningRate * gradient / n
# return the coefficients
return w
```

```
In [182]: # test it out by running a simple
# regression and getting the weights
print "Homebrew logistic regression with 100 iterations:"
print logisticRegressionGDUW(train,regType='Lasso',iterations=100)

Homebrew logistic regression with 100 iterations:
[-0.10165159 0.55552201 -0.33177561]
```

Homegrown Logistic Regression Function (weighted)

In [188]:	

import numpy as np def logisticRegressionGDW(data, wInitial=None, learningRate=0.05, iterat ions=50, regParam=0.01, regType=None): """Logistic Regression function that takes as input the data, an initial set of weights, a learning rate, a number of iterations, a regularization hyperparameter, and the type of regularization. It outputs the coefficients for the model.""" # set the feature length by taking the length # of the features in the first point featureLen = len(data.take(1)[0].x) # instead of counting the number of datapoints # sum all the weights n = data.map(lambda point: point.wgt).reduce(lambda a,b: a + b) # if the initial coefficients are none, # then initalize a random set of coefficients # that are equal to the feature length if wInitial is None: w = np.random.normal(size=featureLen) # otherwise, set the coefficients to be the # coefficients provided by the user else: w = wInitial# loop through the number of iterations # specified by the user for i in range(iterations): # broadcast the coefficients so that # we can hold the coefficients in memory wBroadcast = sc.broadcast(w) # calculate the gradient for each point # and then reduce by summing all the # partial gradients # the partial gradient is 1 calculated as # using the formula here # https://work.caltech.edu/library/093.pdf # we update the formula to add a term # to weight each point partial gradient = data.map(lambda point: (((1 / \ (1 + np.exp(-point.y*np.dot(wBroadcast.value, point.x)))-1) * \ point.y * np.array(point.x))) * \ point.wqt) # we calculate the total gradient by summing across # the partial gradients gradient = partial gradient.reduce(lambda a, b: a + b) # if the regularization type is 'ridge' # then use the

```
if reqType == "Ridge":
        # multiply the weight vector by 1 to make
        # a copy of the array
       wReq = w * 1
        # ignore the last value of weight vector
        # because it is the bias term,
        # ignored in regularization
       wReg[-1] = 0
    # else if we're using a 'lasso' regularization
    # type
    elif regType == "Lasso":
        # multiply the weight vector by 1 to make
        # a copy of the array
       wReg = w * 1
        # ignore the last value of coefficient vector
        # because it is the bias term,
        # ignored in regularization
       wReg[-1] = 0
        # if the coefficient is greater than 0,
        # make it 1, otherwise make it zero
       wReg = (wReg>0).astype(int) * 2-1
    # if no regularlization type is provided,
    # just don't regularize at all
   else:
        wReg = np.zeros(w.shape[0])
    # set the gradient equal to itself plus
    # the regularization parameter times the
    # current weights
    # gradient: gradient of Sqaured Error +
    # gradient of regularized term
   gradient = gradient + regParam * wReg
    # the new set of coefficients is the
    # current set of coefficients minus
    # the gradient times the learning rate
    # all over the number of exmaples
   w = w - learningRate * gradient / n
# return the coefficients
return w
```

Write a function to help compute the accuracy of the home grown model

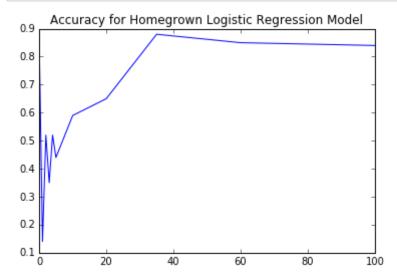
```
In [198]: import numpy as np
          def accuracyHome(coefficients, test, thresh=0.5):
               """a simple function that takes as inputs,
              the coefficients calculated by a logistic
              regression model, and the test data, and
              uses both to compute the accuracy of the
              model"""
              # keep the count of correct and the total
              # count
              total = 0
              correct = 0
              # write a subfunction to calculate the
              # the actual predictions
              def predictLog(point):
                  # get the prediction from the log odds by
                  # converting the log-odds back to calculate
                  # the prediction
                  prediction = 1 / (1+np.exp(-np.dot(coefficients,point)))
                  # use the threshold to establish the prediction
                  predict = -1.0
                  if prediction > 0.5:
                      predict = 1.0
                  # return the prediction
                  return predict
              # loop through each test example
              for i in test:
                  # get the x (features) from the point
                  # and append a 1 for the bias term
                  x = list(i[0:2])
                  x.append(1.0)
                  # get the prediction for this point
                  predict = predictLog(x)
                  # if the prediction is right, then
                  # increment correct. always increment
                  # total
                  total = total + 1
                  if predict == i[2]:
                       correct = correct + 1
              # return the accuracy
              accur = float(correct) / float(total)
              return accur
```

Run the homegrown model for many iterations and look for convergence

```
In [199]: # set the iterations of interest for plotting
          interest = [0,1,2,3,4,5,10,20,35,60,100]
          # create an array to store the accuracies
          accuracies = []
          # loop through all the intersting iterations
          for i in interest:
              # grab the coefficients
              coefficients = logisticRegressionGDW(train, regType='Lasso',iteratio
          ns=i)
              # compute the accuracy
              accur = accuracyHome(coefficients,test_nl)
              # add the accuracy to the list
              accuracies.append(accur)
              # print out the accuracy and the iteration
              print "Iteration",i
              print "Accuracy:",accur
              print "Coefficients:",coefficients
              print "\n"
```

```
Iteration 0
Accuracy: 0.87
Coefficients: [ 0.13130022  1.39845874 -0.07275296]
Iteration 1
Accuracy: 0.14
Coefficients: [ 0.56990619  0.03133693  0.12013405]
Iteration 2
Accuracy: 0.52
Coefficients: [-0.5228003 -0.15189114 1.25087885]
Iteration 3
Accuracy: 0.35
Coefficients: [ 1.12528197 -0.74934186 -0.98882026]
Iteration 4
Accuracy: 0.52
Coefficients: [ 1.10565593 -0.43907647 1.52753988]
Iteration 5
Accuracy: 0.44
Coefficients: [-0.42033692 -0.58857714 -0.26308081]
Iteration 10
Accuracy: 0.59
Coefficients: [-0.88010529 -0.19830175 -0.61124347]
Iteration 20
Accuracy: 0.65
Coefficients: [-0.14017454 0.98315338 -0.77679797]
Iteration 35
Accuracy: 0.88
Coefficients: [-1.28399497 0.17235407 0.28482233]
Iteration 60
Accuracy: 0.85
Coefficients: [ 0.2019071 2.33761949 0.17697976]
Iteration 100
Accuracy: 0.84
Coefficients: [-1.91936521 -0.53283814 -0.11461893]
```

```
In [201]: # plot the evolving accuracies
    plt.plot(interest,accuracies)
    plt.title("Accuracy for Homegrown Logistic Regression Model")
    plt.show()
```



It does not appear that my coefficients are **converging**, even though my accuracies improve drastically with more iterations (before stabilizing).

The Spark machine learning library does not have a native way to weight examples in Python. There does appear to be an option

(https://spark.apache.org/docs/1.5.2/api/java/org/apache/spark/mllib/optimization/L1Updater.html) to use weights when using Spark in Scala. However, I could find no such option in Python.

HW11.4 SVMs

Use the non-linearly separable training and testing datasets from HW11.3 in this problem.

Use the non-linearly separable training and testing datasets from HW11.3 in this problem.

Using MLLib train up a soft SVM model with the training dataset and evaluate with the testing set. What is a good number of iterations for training the SVM model? Justify with plots and words.

HW11.4.1 [Optional] Derive and Implement in Spark a weighted hard linear sym classification learning algorithm. Feel free to use the following notebook as a starting point SVM Notebook.

Evaluate your homegrown weighted linear svm classification learning algorithm on the weighted training dataset and test dataset from HW11.3 (linearly separable dataset). Report misclassification error (1 - Accuracy) and how many iterations does it took to converge? How many support vectors do you end up with?

Does Spark MLLib have a weighted soft SVM learner. If so use it and report your findings on the weighted training set and test set.

HW11.4.2 [Optional] Repeat HW11.4.2 using a soft SVM and a nonlinearly separable datasets. Compare the error rates that you get here with the error rates you achieve using MLLib's soft SVM. Report the number of support vectors in both cases (may not be available the MLLib implementation).

Write function to turn data into Spark's labelled points

```
In [110]: from pyspark.mllib.regression import LabeledPoint

def parsePoint(line):
    """takes each line in the format [x,y,label] and
    converts it to Spark labelled points RDD"""

# grab the values from the line
    values = [float(x) for x in line.split(',')]

# if the classification is -1, then
    # convert it to zero
    if values[2] == -1:
        values[2] = 0

return LabeledPoint(values[2], values[0:2])
```

Convert the data to a format readable by Spark's library

```
In [111]: import numpy as np

# convert the data to an RDD
trainRDD = sc.textFile('train_nl.csv')

# turn the data into labelled points
trainRDD = trainRDD.map(parsePoint).cache()

# print out a sample of what we've done
print trainRDD.collect()[0:5]
```

```
[LabeledPoint(1.0, [-0.666776511004,0.629922738339]), LabeledPoint(0.0,
  [0.327655008854,-0.566204527638]), LabeledPoint(1.0, [-0.20250519138,
  0.0516129445782]), LabeledPoint(1.0, [0.729045899887,-0.421574894025]),
  LabeledPoint(0.0, [-0.343943255331,0.758416700556])]
```

Train a SVM model using Spark's library

In [129]: from pyspark.mllib.classification import SVMWithSGD # some test data that we can use based on the documentation #data = sc.parallelize([LabeledPoint(0.0, [0.0, 1.0]),LabeledPoint(1.0, [1.0, 0.0])]) # set the iterations of interest for plotting interest = [0,1,2,3,4,5,10,20,35,60,75,90,100]# create an array to store the accuracies accuracies = [] # loop through all the intersting iterations for i in interest: # set the model model = SVMWithSGD.train(trainRDD,regType='11',iterations=i) # compute the accuracy accur = accuracy(model,test nl) # append the accuracy to accuracies accuracies.append(accur) # compute the misclassification rate misclas = 1.0 - accur # print out the accuracy and the iteration print "Iteration",i print "Misclassification:",misclas print "Coefficients:", model.weights print "\n"

Iteration 0

Misclassification: 0.52 Coefficients: [0.0,0.0]

Iteration 1

Misclassification: 0.08

Coefficients: [-0.447709021287,0.397602060893]

Iteration 2

Misclassification: 0.08

Coefficients: [-0.764287106238,0.678749174364]

Iteration 3

Misclassification: 0.08

Coefficients: [-0.922558334871,0.81955765388]

Iteration 4

Misclassification: 0.08

Coefficients: [-1.01043935566,0.897405969077]

Iteration 5

Misclassification: 0.08

Coefficients: [-1.07440503792,0.952233063804]

Iteration 10

Misclassification: 0.08

Coefficients: [-1.26227188448,1.10911905912]

Iteration 20

Misclassification: 0.08

Coefficients: [-1.4094900117,1.25685853017]

Iteration 35

Misclassification: 0.08

Coefficients: [-1.51991317389,1.37253485294]

Iteration 60

Misclassification: 0.08

Coefficients: [-1.63457455404,1.44165575892]

Iteration 75

Misclassification: 0.08

Coefficients: [-1.66839254922,1.46713553171]

Iteration 90

Misclassification: 0.08

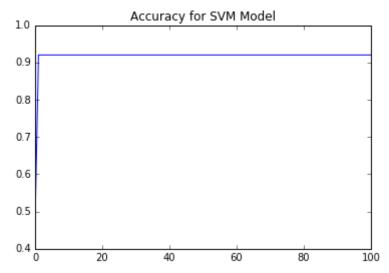
```
Coefficients: [-1.67152715048,1.46975541981]
```

Iteration 100

Misclassification: 0.08

Coefficients: [-1.67152715048,1.46975541981]

```
In [119]: # plot the evolving accuracies
    plt.plot(interest,accuracies)
    plt.title("Accuracy for SVM Model")
    plt.show()
```



We can see that after even a single iteration, we have stabilized in terms of accuracy at around 92%. However, the coefficients don't actually converge till about 90 iterations.

Optional: Write our own homegrown version of SVM (unweighted)

We borrow from the <u>sample notebook (http://nbviewer.jupyter.org/urls/dl.dropbox.com/s/dm2l73iznde7y4f/SVM-Notebook-Linear-Kernel-2015-06-19.ipynb)</u> and start with an unweighted implementation before moving to a fully weighted implementation

```
import numpy as np
# gradient descent (and with NO stochasticity!)
# Objective Function
# minw \lambda/2 w'w + 1/m \Sigma i(1 - yi(w'xi - b)) +
# gradient
                            yi(w'xi - b)) > 1 #correctly classified
#
  \lambda w
                    if
                                                 #incorrectly classified
# \lambda w + yi xi
                    Otherwise
#-----
# Wt+1 = wt + average(gradient)
# Wt+1 = wt + average(regularization + hinge loss)
def SVM_GDUW(data,w=None,eta=0.01,iter_num=1000,regPara=0.01,stopCriteri
a=0.0001):
    """a function that produces a support vector machine
    from an inputted set of data,
    an optional initial set of coefficients, a learning
    rate (eta), a number of iterations, a regularization
    parameter and a stopping criteria"""
    # this line of code prepends the classification
    # to the data. however, for our data, its already
    # all combined so we comment out this line
    # dataRDD = sc.parallelize(np.append(y[:,None],data,axis=1)).cache()
 #prepend y to X
    # grab the feature length
    featureLen = len(data.take(1)[0].x)
    # set the number of data points
    n = data.count()
    # if the user did not provide an initial set
    # of coefficients, then we generate a random
    # set
    if w==None:
       w = np.random.normal(size=featureLen)
    # loop through all the iterations
    for i in range(iter num): #label * margin
        # create the support vector by taking the
        # classification and multiplying it by the
        # dot product of the weights and the x value
        sv = data.filter(lambda point: point.y * np.dot(w,point.x)<1)</pre>
       # if the support vector is empty (that means
        # that it has converged), then go ahead and
        # break out
        if sv.isEmpty():
           break
        # set the gradient using the hing loss function
        # to first elements multiplied by the rest of
        # the elements and all summed together
        g = -sv.map(lambda point: point.y*np.array(point.x)).reduce(lamb
da x,y:x+y)/n
```

```
# make a copy of the coefficients
    wreg = w*1
    # set the bias term to 0 so that we
    # ignore it during regularization
    wreg[-1] = 0
    # calculate the change in the
    # gradient as the learning rate
    # times the gradient plus the
    # the regularization parameter
    # times the new coefficients
    wdelta = eta*(g+regPara*wreg)
    # if the amount of change we're
    # about to use is less than the
    # stopping criteria that we've
    # set, then we we break out of
    # the loop and stop doing any
    # further iterations
    if sum(abs(wdelta))<=stopCriteria*sum(abs(w)):</pre>
        break
    # otherwise, if we're still going,
    # go ahead and update the coefficients
    w = w - wdelta
# return the coefficients
return w
```

```
In [219]: # test it out
SVM_GDUW(train,iter_num=50)
Out[219]: array([ 0.20659619, -1.07756549, -1.71936608])
```

Optional: Write our own homegrown version of SVM (weighted)

In [225]:	

```
import numpy as np
# gradient descent (and with NO stochasticity!)
# Objective Function
# minw
        \lambda/2 w'w + 1/m \Sigma i(1 - yi(w'xi - b)) +
# gradient
#
  \lambda w
                            yi(w'xi - b)) > 1 #correctly classified
                    if
                                                 #incorrectly classified
# \lambda w + yi xi
                    Otherwise
#-----
# Wt+1 = wt + average(gradient)
# Wt+1 = wt + average(regularization + hinge loss)
def
SVM GDW(data, w=None, eta=0.01, iter num=1000, regPara=0.01, stopCriteria=0.0
001):
    """a function that produces a support vector machine
    from an inputted set of data,
    an optional initial set of coefficients, a learning
    rate (eta), a number of iterations, a regularization
    parameter and a stopping criteria"""
    # this line of code prepends the classification
    # to the data. however, for our data, its already
    # all combined so we comment out this line
    # dataRDD = sc.parallelize(np.append(y[:,None],data,axis=1)).cache()
 #prepend y to X
    # grab the feature length
    featureLen = len(data.take(1)[0].x)
    # instead of counting the number of datapoints
    # sum all the weights
    n = data.map(lambda point: point.wgt).reduce(lambda a,b: a + b)
    # if the user did not provide an initial set
    # of coefficients, then we generate a random
    # set
    if w==None:
       w = np.random.normal(size=featureLen)
    # loop through all the iterations
    for i in range(iter_num): #label * margin
        # create the support vector by taking the
        # classification and multiplying it by the
        # dot product of the weights and the x value
        sv = data.filter(lambda point: point.y * np.dot(w,point.x)<1)</pre>
        # if the support vector is empty (that means
        # that it has converged), then go ahead and
        # break out
        if sv.isEmpty():
           break
       # set the gradient using the hinge loss function
        # to first elements multiplied by the rest of
        # the elements and all summed together
        q = -sv.map(lambda point: point.y*np.array(point.x)*point.wqt).r
```

```
educe(lambda x,y:x+y)/n
        # make a copy of the coefficients
        wreq = w*1
        # set the bias term to 0 so that we
        # ignore it during regularization
        wreq[-1] = 0
        # calculate the change in the
        # gradient as the learning rate
        # times the gradient plus the
        # the regularization parameter
        # times the new coefficients
        wdelta = eta*(g+regPara*wreg)
        # if the amount of change we're
        # about to use is less than the
        # stopping criteria that we've
        # set, then we we break out of
        # the loop and stop doing any
        # further iterations
        if sum(abs(wdelta))<=stopCriteria*sum(abs(w)):</pre>
            break
        # otherwise, if we're still going,
        # go ahead and update the coefficients
        w = w - wdelta
    # return the coefficients
    return w
```

```
In [226]: # test it out
SVM_GDW(train,iter_num=50)
Out[226]: array([-0.74760737, -1.78180941, -0.93883008])
```

Write a function to compute the accuracy of our homegrown SVM models

In [229]: import numpy as np def accuracySVM(coefficients,test,thresh=0.5): """a simple function that takes the coefficients of a support vector machine and uses them to predict the classifications of test data""" # set up counters for the total and the # number of correct examples total = 0correct = 0# sub functiont that predicts # each individual point def prediction(point): prod = np.dot(point,coefficients) # compare it to predict = -1.0**if** prod > 0.5: predict = 1.0 # return the class that we predicted return predict # loop through each test example for i in test: # get the x (features) from the point # and append a 1 for the bias term x = list(i[0:2])x.append(1.0)# get the prediction for this point predict = prediction(x) # if the prediction is right, then # increment correct. always increment # total total = total + 1if predict == i[2]: correct = correct + 1 # compute the actual accuracy accur = float(correct)/float(total) # return the accuracy return accur

Run our homegrown model for a number of iterations to test convergence

```
In [234]: # set the iterations of interest for plotting
          interest = [0,1,2,3,4,5,10,20,35,60,100,250,500,1000,1500]
          # create an array to store the accuracies
          accuracies = []
          # loop through all the intersting iterations
          for i in interest:
              # grab the coefficients
              coefficients = SVM_GDW(train,iter_num=i)
              # compute the accuracy
              accur = accuracySVM(coefficients,test_nl)
              # add the accuracy to the list
              accuracies.append(accur)
              # print out the accuracy and the iteration
              print "Iteration",i
              print "Accuracy:",accur
              print "Coefficients:",coefficients
              print "\n"
```

```
Iteration 0
Accuracy: 0.48
Coefficients: [-0.74759883 -0.07484864 -1.07809815]
Iteration 1
Accuracy: 0.68
Coefficients: [ 0.81155744 2.61991941 -0.38742666]
Iteration 2
Accuracy: 0.21
Coefficients: [ 0.04803298 -1.9637259 -0.19864101]
Iteration 3
Accuracy: 0.25
Coefficients: [ 0.76904408  0.03922179  0.7571654 ]
Iteration 4
Accuracy: 0.48
Coefficients: [-0.0823882 -0.10741338 -0.90256635]
Iteration 5
Accuracy: 0.91
Coefficients: [-0.83038039 0.49219454 0.63233672]
Iteration 10
Accuracy: 0.52
Coefficients: [-0.14639041 0.53860456 1.29556984]
Iteration 20
Accuracy: 0.79
Coefficients: [-0.38940474 0.59443796 0.89203248]
Iteration 35
Accuracy: 0.48
Coefficients: [-0.31948492 -0.52346544 -1.11545924]
Iteration 60
Accuracy: 0.48
Coefficients: [-0.29943391 1.6402978 -1.37812231]
Iteration 100
Accuracy: 0.67
Coefficients: [-1.25080583 -0.56100595 -0.10016891]
Iteration 250
Accuracy: 0.73
```

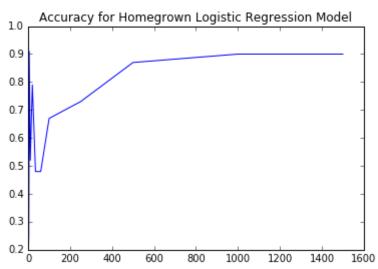
```
Coefficients: [-1.18131614 0.45598356 -0.30530493]
```

```
Iteration 500
Accuracy: 0.87
Coefficients: [-1.74355006  0.09984  0.22732044]

Iteration 1000
Accuracy: 0.9
Coefficients: [-0.93350784  1.82832282  0.07988053]

Iteration 1500
Accuracy: 0.9
Coefficients: [-1.44206363  1.22644465  0.07012011]
```

```
In [235]: # plot the evolving accuracies
    plt.plot(interest,accuracies)
    plt.title("Accuracy for Homegrown Logistic Regression Model")
    plt.show()
```



Although we see an increasing level of accuracy (that stabilizes eventually), we *unfortunately* don't see the convergence of the weights for the model.