

Problem 1: Chapter 15, Problem 6

What does the following Scheme function do?

```
(define (y s lis)
  (cond
    ((null? lis) '())
    ((equal? s (car lis)) lis)
    (else (y s (cdr lis)))))
```

This function returns lis if s is a top-level member of lis, and the empty set otherwise.

Problem 2: Chapter 15, Programming Exercise 13

Write a Scheme function that takes a list as a parameter and returns it with the second top-level element removed. If the given list does not have two elements, the function should return ().

```
(define (remove-second-member lst)
  (if (< (length lst) 2)
      '()
      (cons (first lst) (cddr lst))))
```

Note that this is assuming that the problem, as stated, really asks for () to be returned on *less than* two elements, instead of “does not have”. In the case that we are taking the problem statement literally, s/< (length lst) 2/not (= (length lst) 2)/.

Problem 3:

Write your own implementation of the Scheme built-in function sublist:

```
(sublist list start end)
```

Returns a newly allocated list formed from the elements of list beginning at index start (inclusive) and ending at end (exclusive). You may assume that start and end are integers that satisfy:

$0 \leq \text{start} \leq \text{end} \leq (\text{length list})$

Name your function my-sublist, since sublist is already provided as a standard operation in Scheme (you may not use sublist, list-head, or list-tail in your solution).

```
(define (my-sublist lst start end)
  (cond ((> start 0) (my-sublist (rest lst) (- start 1) (- end 1)))
        ((= start 0) (my-sublist (reverse lst) -1 (- end 1)))
        ((> (- (length lst) end) 0) (my-sublist (rest lst) -1 (+ end 1)))
        (else (reverse lst))))
```

Problem 4:

Analyze the performance of your `my-sublist` implementation, and describe its worst-case performance using big-oh notation, in terms of the number of `car` or `cdr` operations performed (including those required by any predefined operations you use). Justify your performance analysis.

The worst case scenario is $O(n)$, or linear with the number of elements in the list. This is because `my-sublist` cannot perform any more `cdrs` (rests) than there are elements in the array. Worst case scenarios involve reducing the list to one element (since it acts inclusively on start and exclusively on end), so only $(- (\text{length lst}) 1)$ rest operations can be performed.

Although `reverse` may use `car` or `cdr`, I am not sure if it does, or how many it uses. I believe `reverse` should be $O(n)$ anyway, as it can be accomplished by using an `inject` (fold-right?) method. Even if intermediate student Scheme doesn't support it, I imagine that behind the scenes, it would be performed that way. But even if it is $O(n)$, `my-sublist` would still only be $O(2n)$.