## HW2

## Li Haolun 2022011545

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1. (a)

$$k(x_1, x_2) = -\frac{\frac{\partial U}{\partial x_1}}{\frac{\partial U}{\partial x_2}}$$
$$= -\frac{3x_1^2 x_2^5}{5x_1^3 x_2^4}$$
$$= -\frac{3x_2}{5x_1}$$

(b) We have  $\frac{3x_2}{5x_1} = \frac{p_1}{p_2}$ , which is eqivalent to  $5p_1x_1 = 3p_2x_2$ . So the expenditure share of goods 1 is  $\frac{3}{3+5} = \frac{3}{8}$ .

(c)

$$k(x_1, x_2) = -\frac{\frac{\partial U}{\partial x_1}}{\frac{\partial U}{\partial x_2}}$$
$$= -\frac{ax_2}{bx_1}$$
$$= -\frac{p_1}{p_2}$$

 $\Rightarrow bp_1x_1=ap_2x_2$  , so the expenditure share of goods 1 is  $\frac{a}{a+b}$  .

2. (a)

$$k(x_1, x_2) = -\frac{\frac{\partial U}{\partial x_1}}{\frac{\partial U}{\partial x_2}}$$

$$= \frac{1}{100 - 2x_2}$$

$$= -\frac{p_1}{p_2}$$

$$= -\frac{1}{4}$$

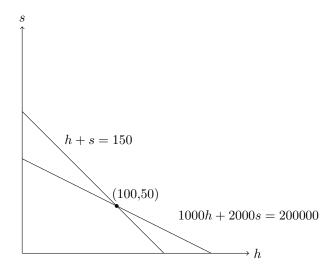
$$\Rightarrow 4 = 100 - 2x_2$$
  
 $\Rightarrow x_1^* = 308 , x_2^* = 48 .$ 

- (b) We still have  $4=100-2x_2$  , so  $x_1^*=808$  ,  $x_2^*=48$  .
- (c) From the utility function, we always have  $4=100-2x_2$ , which means that  $x_2$  is always 48. So, if the consumer consumes both goods, her income a must be larger than  $48\times 4=192$ .
- 3. (a)  $q = 0.02 \times 7500 3 \times 30 = 60$ .
  - (b) Before the price of a blind box rose, Li Hua spent 5700 Yuan on all other goods. So, Li Hua need  $5700 + 60 \times 40 = 8100$  Yuan after the price rose.

And he would buy  $q' = 0.02 \times 8100 - 3 \times 40 = 42$  boxes at this income.

- (c)  $q^{''} = 0.02 \times 7500 3 \times 40 = 30$  .
- (d) Substitution effect: q' q = -18.

Income effect:  $q^{^{\prime\prime}}-q^{^{\prime}}=-12$  .

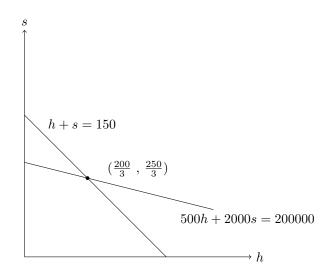


4. (a)

1000h+2000s=200000 means the hotel manager's budget constraint. h+s=150 means the hotel manager's reality constraint.

So, he will buy 100 hard mattresses.

(b)



Now he will buy  $\frac{200}{3}$  hard mattresses and  $\frac{250}{3}$  soft mattresses. Hard mattress is Giffen good for him.

5. (a)

$$k(c,r) = -\frac{\frac{\partial U}{\partial r}}{\frac{\partial U}{\partial c}}$$
$$= -\frac{c}{r}$$

For Magneto, her budget constraint is c+50r=4000 . So we have  $\frac{c}{r}=50$  . And the solution is c=2000 , r=40 .

(b)

$$\begin{cases} c + 40r = 3200 & r \ge 40 \\ c + 60r = 4000 & r < 40 \end{cases}$$

(c) No, he won't.

When  $r \ge 40$  , we have  $\frac{c}{r} = 40$  , then r = 40 .

When r<40 , we have  $\frac{c}{r}=60$  , then  $r=\frac{100}{3}$  . The best choice for Xavier is c=2000 ,  $r=\frac{100}{3}$  .

- (d) Magneto has the better job, because  $U_M = 2000 \times \frac{100}{3} > U_X = 1600 \times 40$ .
- 6. (a) He will choose 10 hours for leisure.
  - (b) His budget constraint is C + 10R = 190.

$$k(C,R) = -\frac{\frac{\partial U}{\partial R}}{\frac{\partial U}{\partial C}}$$
$$= 2R - 20$$
$$= -10$$

So we have R=5 , C=140 . He will choose to work 11 hours.

- (c) Now his budget constraint is  $C+8R=190\times0.8=152$  . We still have R=6 , then C=104 . He will choose to work 10 hours.
- 7. (a)  $m_1 + \frac{m_2}{1+r} = c_1 + \frac{c_2}{1+r}$ .
  - (b) He can consume  $m_1(1+r)+m_2$ , which is the future value of his endowment.
  - (c) He can consume  $m_1 + \frac{m_2}{(1+r)}$ , which is the present value of his endowment.
  - (d) Slope is -(1+r).
- 8. (a) In this question,  $m_1=1000$ ,  $m_2=150$ , r=-0.25. So villagers' budget constraint in present value terms is  $1200=c_1+\frac{4}{3}c_2$ .

$$k(c_1, c_2) = -\frac{\frac{\partial U}{\partial c_1}}{\frac{\partial U}{\partial c_2}}$$
$$= -\frac{c_2}{c_1}$$
$$= -(1+r) = -0.75$$

$$\Rightarrow c_1 = 600 , c_2 = 450 .$$

(b) Since the villagers can sell and buy wheat in any year, and the price is \$1 per kilo, so villagers' money can be seen as wheat, and they don't have to suffer from the loss during storage.

So villagers' budget constraint in present value terms is  $1000+150/(1+0.1)=\frac{12500}{11}=c_1+\frac{c_2}{1.1}$ .

We have  $\frac{c_2}{c_1} = 1.1$ , then  $c_2 = 625$ 

Now, the villagers will consume  $c_1 = \frac{6250}{11}$  ,  $c_2 = 625$  .

- 9. (a)  $P(m)=20=40-2m \Rightarrow m=10$  . His consumer's surplus is  $\frac{20\times 10}{2}=100$  .
  - (b) Now he will consume 15 cups per month, and his consumer's surplus is  $\frac{30\times15}{2}=225$ . So Mr. Hacker's change in consumer's surplus is +125.
- 10. (a) Oliver has quasilinear utility function. His inverse demand function is P(x) = 60 x.
  - (b) He will consume 30 bottles of wine.
  - (c) 10.
  - (d) In (b), his consumer's surplus is  $\frac{30\times30}{2}=450$  .

In (c), his consumer's surplus is  $\frac{10\times10}{2} = 50$ .

So, the change in consumer's surplus is -400.