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LING 473
HW 3

Question 1

*See end of document for tables of sample spaces

For each of these questions, Bayes theorem should be applied. I was unable to produce the correct results with bayes and resorted to mapping out the sample space.

Part a

$P(X \text{ or Total} = 7) = P(\text{Dice roll}) \times P(\text{Second roll is difference of 7 and first roll})$

$P(X) = P(A) \times P(B)$

$P(X) = (6/6) \times (1/6)$

$P(X) = 6/36 = 1/6 = 1.6667$

Part b

Bayes should be used here, but I used sample space

$P(Y \text{ or total} \geq 9) = 10/36 = 0.27778$

Part c

Bayes should be used here. I used sample space.

$P(Z \text{ or Roll 1 greater than Roll 2}) = 15/36 = 0.416667$

Question 2

Part a

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Part b

$P(\cdot | nn) = 4/24$

Part c

$P(DT JJ) = 6/157$

Part d

$P(NN | DT JJ) = 5/6$

Part e

$$P(DT JJ | NN) \times P(NN) = P(NN - DT JJ) \times P(DT JJ)$$

$$P(DT JJ | NN) = \frac{P(NN|DTJJ) \times P(DTJJ)}{P(NN)}$$

$$P(DT JJ | NN) = \frac{(5/6) \times (6/157)}{24/158}$$

$$P(DT JJ | NN) = 395/1884 = 0.20966$$

Question 3

The only open vowels in this set are *gnat* and *sand*. This means that there are 10 out of 12 vowels that are close. However, given the grouping of words to select from, the probability of choosing a close vowel rather than an open one is not simply 10/12.

$$P(A) = 1/3$$

$$P(\text{Close} | A) = 1/2$$

$$P(B) = 1/3$$

$$P(\text{Close} | B) = 2/2$$

$$P(C) = 1/3$$

$$P(\text{Close} | C) = 3/4$$

$$P(\text{Close}) = P(\text{Close} - A) + P(\text{Close} - B) + P(\text{Close} - C) = 9/12 = 0.75$$

Question 4

Part a

The probability that we select a positive document from *C* is 2/6. We must multiply this probability by the probability of this same document being selected from not *C* in the next step in order to find the total probability of selecting a positive document.

$$P(X \text{ or Selecting a positive document from not } C) = P(I \text{ Choosing positive doc we know is in not } C) + (P(J \text{ Choosing doc we moved from } C) \times P(K \text{ Moving positive doc from } C \text{ to not } C))$$

$$P(X) = 1/3 + (1/3 \times 2/6) = 8/18 = 0.4444$$

Part b

For this question, we must use Bayes Theorem to find $P(B - A)$ after already knowing $P(A - B)$ from the previous question.

The probability of picking a positive doc, given that a positive doc was moved from *C* to not *C* is 2/3 because that would make 2 positive docs and 1 not positive doc in set not *C*. The probability of moving a positive doc from *C* to not *C* is 1/3. This means our first equation is:

$$P(A|B) \times P(B) = 2/3 \times 1/3 = 2/9$$

Knowing this, we can divide the left side of the equation by $P(A)$, which we take from the question above, to find $P(B|A)$:

$$\frac{P(A|B) \times P(B)}{P(A)} = \frac{2/3 \times 1/3}{8/18} = 1/2 = 0.5$$

Tables

Table 1: Q1 Part a: Two Dice Total = 7

-	1	2	3	4	5	6
1	-	-	-	-	-	X
2	-	-	-	-	X	-
3	-	-	-	X	-	-
4	-	-	X	-	-	-
5	-	X	-	-	-	-
6	X	-	-	-	-	-

Table 2: Q1 Part b: Two Dice Total = 9

-	1	2	3	4	5	6
1	-	-	-	-	-	-
2	-	-	-	-	-	-
3	-	-	-	-	-	X
4	-	-	-	-	X	X
5	-	-	-	X	X	X
6	-	-	X	X	X	X

Table 3: Q1 Part c: Second Roll Higher than First

-	1	2	3	4	5	6
1	-	X	X	X	X	X
2	-	-	X	X	X	X
3	-	-	-	X	X	X
4	-	-	-	-	X	X
5	-	-	-	-	-	X
6	-	-	-	-	-	-