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Recommendation for Random Number Generation Using Deterministic Random Bit Generators

National Institute of Standards and Technology Technology Administration

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C O M P U T E R S E C U R I T Y

Abstract

This Recommendation specifies mechanisms for the generation of random bits using deterministic methods. The methods provided are based on either hash functions, block cipher algorithms or number theoretic problems.

KEY WORDS: deterministic random bit generator (DRBG); entropy; hash function; random number generator

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Random Number Generation Using Deterministic Random Bit Generators

1 Authority

This document has been developed by the National Institute of Standards and Technology (NIST) in furtherance of its statutory responsibilities under the Federal Information Security Management Act (FISMA) of 2002, Public Law 107-347.

NIST is responsible for developing standards and guidelines, including minimum requirements, for providing adequate information security for all agency operations and assets, but such standards and guidelines shall not apply to national security systems. This recommendation is consistent with the requirements of the Office of Management and Budget (OMB) Circular A-130, Section 8b(3), Securing Agency Information Systems, as analyzed in A-130, Appendix IV: Analysis of Key Sections. Supplemental information is provided in A-130, Appendix III.

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Conformance testing for implementations of the deterministic random bit generators (DRBGs) that are specified in this Recommendation will be conducted within the framework of the Cryptographic Module Validation Program (CMVP), a joint effort of NIST and the Communications Security Establishment of the Government of Canada. An implementation of a DRBG must adhere to the requirements in this Recommendation in order to be validated under the CMVP. The requirements of this Recommendation are indicated by the word "shall."

2 Introduction

This Recommendation specifies techniques for the generation of random bits that may then be used directly or converted to random numbers when random values are required by applications using cryptography.

There are two fundamentally different strategies for generating random bits. One strategy is to produce bits non-deterministically, where every bit of output is based on a physical process that is unpredictable; this class of random bit generators (RBGs) is commonly known as non-

deterministic random bit generators (NRBGs)¹. The other strategy is to compute bits deterministically using an algorithm; this class of RBGs is known as Deterministic Random Bit Generators (DRBGs)². This Recommendation will specify Approved DRBG mechanisms.

A DRBG uses an algorithm that produces a sequence of bits from an initial value that is determined by a seed. Once the seed is provided and the initial value determined, the DRBG is said to be instantiated. Because of the deterministic nature of the process, a DRBG is said to produce pseudorandom bits, rather than random bits. The seed used to instantiate the DRBG must contain sufficient entropy to provide assurance of randomness. If the seed is kept secret, and the algorithm is well designed, the bits output by the DRBG will appear to be random. However, the security provided by an RBG that uses a DRBG is a system implementation issue; both the DRBG and its source of entropy must be considered when determining whether the RBG is appropriate for use by consuming applications. Therefore, in this Recommendation the acronym RBG will be used to mean a DRBG, together with its source of entropy.

3 Scope

This Recommendation includes:

- 1. Requirements for the use of deterministic random bit generator mechanisms,
- 2. Specifications for deterministic random bit generator mechanisms that use hash functions, block ciphers and number theoretic problems,
- 3. Implementation issues, and
- 4. Assurance considerations.

This Recommendation specifies several diverse DRBG mechanisms, all of which provided acceptable security when this Recommendation was published. However, in the event that new attacks are found on a particular class of mechanisms, a diversity of approved mechanisms will allow a timely transition to a different class of DRBG mechanism.

Random number generation does not require interoperability between two entities, e.g., communicating entities may use different DRBG mechanisms without affecting their ability to communicate. Therefore, an entity may choose a single appropriate DRBG mechanism for their applications; see Annex D for a discussion of DRBG selection.

The precise structure, design and development of a random bit generator is outside the scope of this Recommendation.

 $^{^{\}rm 1}$ NRBGs have also been called True Random Number (or Bit) Generators or Handware Random Number Generators.

² DRBGS have also been called Pseudorandom Bit Generators.

This Recommendation provides preliminary guidance on the selection of an entropy source and the construction of an RBG from an entropy source and an Approved DRBG. Additional guidance is under development in these areas.

4 Terms and definitions

For the purposes of this part of the Recommendation, the following terms and definitions apply.

арріу.	
Algorithm	A clearly specified mathematical process for computation; a set of rules that, if followed, will give a prescribed result.
Approved	FIPS approved or NIST Recommended. An algorithm or technique that is either 1) specified in a FIPS or NIST Recommendation, or 2) adopted in a FIPS or NIST Recommendation and specified either (a) in an appendix to the FIPS or NIST Recommendation, or (b) in a document referenced by the FIPS or NIST Recommendation
Backtracking Resistance	The assurance that the output sequence from an RBG remains indistinguishable from an ideal random sequence even to an attacker who compromises the RBG in the future, up to the claimed security strength of the RBG. For example, an RBG that allowed an attacker to "backtrack" from the current working state to generate prior outputs would not provide backtracking resistance. The complementary assurance is called Prediction Resistance.
Biased	A bitstring (or number) that is chosen from a sample space is said to be biased if one bitstring (or number) is more likely to be chosen than another bitstring (or number). Contrast with unbiased.
Bitstring	A bitstring is an ordered sequence of 0's and 1's. The leftmost bit is the most significant bit of the string and is the newest bit generated. The rightmost bit is the least significant bit of the string.
Bitwise Exclusive Or	An operation on two bitstrings of equal length that combines corresponding bits of each bitstring using an exclusive-or operation.

Block Cipher	A symmetric key cryptographic algorithm that transforms a block of information at a time using a cryptographic key. For a block cipher algorithm, the length of the input block is the same as the length of the output block.			
Consuming Application	The application (including middle ware) that uses random numbers or bits obtained from an Approved random bit generator.			
Cryptographic Key (Key)	A parameter that determines the operation of a cryptographic function such as:			
	The transformation from plain text to cipher text and vice versa,			
	2. The synchronized generation of keying material,			
	3. A digital signature computation or validation.			
Deterministic Algorithm	An algorithm that, given the same inputs, always produces the same outputs.			
Deterministic Random Bit Generator (DRBG)	An RBG that uses a deterministic algorithm to produce a pseudorandom sequence of bits from a secret initial value called a <i>seed</i> (which contains entropy and possibly a personalization string) along with other possible inputs. Additional non-deterministic inputs may allow periodic reseeding. The outputs do not always contain full entropy, contrast this with an NRBG. A DRBG is often called a Pseudorandom Number (or Bit) Generator. A DRBG has an assessed security strength and is designed with the goal of requiring an adversary to do at least the amount of work associated with that security strength in order to distinguish the output from an ideal random sequence.			
DRBG Boundary	A conceptual boundary that is used to explain the operations of a DRBG and its interaction with and relation to other processes.			
Entropy	A measure of the disorder, randomness or variability in a closed system. The entropy of X is a mathematical measure of the amount of information provided by an observation of X . As such, entropy is always relative to an observer and his or her knowledge prior to an observation. Also, see min-entropy.			

Entropy Input	The input to an RBG of a string of bits that contains entropy, that is, the entropy input is digitized and is assessed. For an NRBG, this is obtained from an entropy source. For a DRBG, this is included in the seed material.		
Entropy Input Source	A source of unpredictable data, such as thermal noise or hard drive seek times. There is no assumption that the unpredictable data has a uniform distribution.		
Equivalent Process	Two processes are equivalent if, when the same values are input to each process, the same output is produced.		
Exclusive-or	A mathematical operation, symbol \oplus , defined as: $0 \oplus 0 = 0$ $0 \oplus 1 = 1$ $1 \oplus 0 = 1$ $1 \oplus 1 = 0$. Equivalent to binary addition without carry.		
Full Entropy	An <i>m</i> -bit string has full entropy if every <i>m</i> -bit value is equally likely to occur.		
Hash Function	A (mathematical) function that maps values from a large (possibly very large) domain into a smaller range. The function satisfies the following properties: 1. (One-way) It is computationally infeasible to find any input that maps to any pre-specified output; 2. (Collision free) It is computationally infeasible to find any two distinct inputs that map to the same output.		
Implementation	An implementation of an RBG is a cryptographic device or portion of a cryptographic device that is the physical embodiment of the RBG design, for example, some code running on a computing platform. An implementation may be designed to handle more than one instatniation at a time.		
Implementation Testing for Validation	Testing by an independent and accredited party to ensure that an implemention of a standard conforms to the specifications of that standard.		
Instantiation of an RBG	An instantiation of an RBG is a specific, logically independent, initialized RBG. One instantiation is distinguished from another by a handle (e.g., an identifying number).		

Internal State	The collection of stored information about an RBG instantiation. This can include both secret and non-secret information.		
Key	See Cryptographic Key.		
Non-Deterministic Random Bit Generator (Non-deterministic RBG) (NRBG)	An RBG that produces output that is <u>fully</u> dependent on some unpredictable physical source that produces entropy. Contrast with a DRBG. Other names for non-deterministic RBGs are True Random Number (or Bit) Generators and, simply, Random Number (or Bit) Generators.		
Operational Testing	Testing within an implementation immediately prior to or during normal operation to determine that the implementation continues to perform as implemented and optionally validates		
Personalization String	An optional string of bits that is combined with a secret input and a nonce to produce a seed.		
Prediction Resistance	A compromise of the DRBG internal state has no effect on the security of future DRBG outputs. If a compromise of State _X occurs, prediction resistance provides assurance that the output sequence resulting from states after the compromise remains secure. That is, an adversary who is given access to all of any subset of the output sequence after the compromise cannot distinguish it from random; if the adversary knows only part of the future output sequence, an adversaryhe cannot predict any bit of that future output sequence that he has not already seen. The complementaty assurance is called Backtracking Resistance.		
Pseudorandom	A process or data produced by a process is said to be pseudorandom when the outcome is deterministic, yet also effectively random as long as the internal action of the process is hidden from observation. For cryptographic purposes, "effectively" means "within the limits of the intended cryptographic strength." Note: Non-cryptographic use of "pseudorandom" has less stringent meanings for "effectively."		
Pseudorandom Number Generator	See Deterministic Random Bit Generator.		
Public Key	In an asymmetric (public) key cryptosystem, that key of an entity's key pair that is publicly known.		
Public Key Pair	In an asymmetric (public) key cryposystem, the public key and associated private key.		

Random Number	For the purposes of this standard, a value in a set that has an equal probability of being selected from the total population of possibilities and hence is unpredictable. A random number is an instance of an unbiased random variable, that is, the output produced by a uniformly distributed random process.	
Random Bit Generator (RBG)	A device or algorithm that outputs a sequence of binary bits that appears to be statistically independent and unbiased.	
Random Number Generator (RNG)	A device or algorithm that can produce a sequence of random numbers that appears to be from an ideal random distribution.	
Reseed	To aquire additional bits with sufficient entropy for the desired security strength	
Security Strength	A number associated with the amount of work (that is, the number of operations) that is required to break a cryptographic algorithm or system; a security strength is specified in bits and is a specific value from the set (112, 128, 192, 256). The amount of work needed is 2 raised to the security strength.	
Seed	Noun: A string of bits that is used as input to a Deterministic Random Bit Generator (DRBG). The seed will determine a portion of the internal state of the DRBG, and its entropy must be sufficient to support the security strength of the DRBG. Verb: To aquire bits with sufficient entropy for the desired security strength. These bits will be used as input to a DRBG to determine a portion of the initial internal state. Contrast with reseed.	
Seedlife	The length of the seed period.	
Seed Period	The period of time between initializing a DRBG with one see and reseeding that DRBG with another seed.	
Sequence	An ordered set of quantities.	
Shall	Used to indicate a requirement of this Standard.	
Should	Used to indicate a highly desirable feature for a DRBG that is not necessarily required by this Standard.	

Statistically Unique	A value is said to be statistically unique when it has a negligible probability to occur again in a set of such values. When a random value is required to be statistically unique, it may be selected either with or without replacement from the sample space of possibilities; this is in contrast to when a value is required to be unique, as then it must be selected without replacement.
String	See Sequence.
Unbiased	A bitstring (or number) that is chosen from a sample space is said to be unbiased if all potential bitstrings (or numbers) have the same probability of being chosen. Contrast with biased.
Unpredictable	In the context of random bit generation, an output bit is unpredictable if an adversary has only a negligible advantage (that is, essentially not much better than chance) in predicting it correctly.
Working State	A subset of the internal state that is used by a DRBG to produce pseudorandom bits at a given point in time. The working state (and thus, the internal state) is updated to the next state prior to producing another string of pseudorandom bits.

5 Symbols and abbreviated terms
The following abbreviations are used in this document:

Abbreviation	Meaning		
AES	Advanced Encryption Standard.		
DRBG	Deterministic Random Bit Generator.		
ECDLP	Elliptic Curve Discrete Logarithm Problem.		
FIPS	Federal Information Processing Standard.		
HMAC	Keyed-Hash Message Authentication Code.		
NRBG	Non-deterministic Random Bit Generator.		
RBG	Random Bit Generator.		
TDEA	Triple Data Encryption Algorithm.		

The following symbols are used in this document.

Symbol	Meaning	
+	Addition	
[X]	Ceiling: the smallest integer $\geq X$. For example, $\lceil 5 \rceil = 5$, and $\lceil 5.3 \rceil = 6$.	
$X \oplus Y$	Bitwise exclusive-or (also bitwise addition mod 2) of two bitstrings <i>X</i> and <i>Y</i> of the same length.	
X Y .	Concatenation of two strings X and Y. X and Y are either both bitstrings, or both octet strings.	
$\mathbf{gcd}\ (x,y)$	The greatest common divisor of the integers x and y .	
len (a)	The length in bits of string a.	
x mod n	The unique remainder r (where $0 \le r \le n-1$) when integer x is divided by n . For example, 23 mod $7 = 2$.	

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Symbol	Meaning		
\bigcirc	Used in a figure to illustrate a "switch" between sources of input.		
$\{a_1,a_i\}$	The internal state of the DRBG at a point in time. The types and number of the a_i depends on the specific DRBG.		
O ^x	A string of x zero bits.		

6 General Discussion and Organization

This Recommendation is organized as follows:

- Section 7 provides a functional model for a DRBG and discusses the major DRBG components.
- Section 8 provides DRBG concepts and general requirements. This section
 provides concepts and general requirements for the implementation and use of a
 DRBG. The DRBG functions are explained and requirements for an
 implementation are provided.
- Section 9 specifies the DRBG functions introduced in Section 8. These functions use the DRBG algorithms specified in Section 10.
- Section 10 specifies Approved DRBG algorithms. Algorithms have been specified that are based on the hash functions specified in FIPS 180-2 (Secure Hash Standard), block cipher algorithms specified in FIPS 197 and NIST Special Publication 800-67 (AES and TDEA, respectively), and a number theoretic problem that is expressed in elliptic curve technology.
- Section 11 addresses assurance issues for DRBGs, including documentation requirements, implementation validation and health testing,

This Recommendation also includes the following appendices:

- Appendix A specifies additional DRBG-specific information.
- Appendix B provides conversion routines.
- Appendix C provides guidance on entropy and entropy sources.
- Appendix D provides guidance on the construction of a random bit generator from an entropy source and a DRBG.
- Appendix E discusses security considerations for implementing DRBGs.
- Appendix F provides example pseudocode for each DRBG.
- Appendix G provides a discussion on DRBG selection.
- Appendix H provides references.

7 DRBG Functional Model

Figure 1 provides a functional model of DRBGs. The components of this model are discussed in the following subsections.

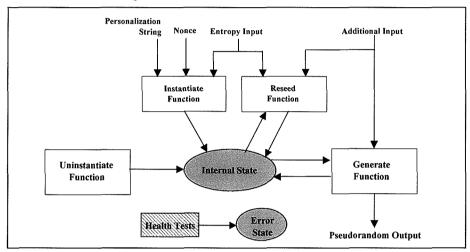


Figure 1: DRBG Functional Model

7.21 Entropy Input

The entropy input is provided to a DRBG for the seed (see Section 8.6). The entropy input and the seed **shall** be kept secret. The secrecy of this information provides the basis for the security of the DRBG. At a minimum, the entropy input **shall** provide the requested amount of entropy for a DRBG. Appropriate sources for the entropy input are discussed in Appendix C.

The DRBGs allow for some bias in the entropy input. Whenever a bitstring containing entropy is required by the DRBG, a request is made that indicates the minimum amount of entropy to be returned; the request may obtain entopy input bits from a buffer containing readily available entropy bits or may cause entropy input bits to be acquired. The request may be fulfilled by a bitstring that is equal to or greater in length than the requested entropy. The DRBG expects that the returned bitstring will contain at least the amount of entropy requested. Additional entropy beyond the amount requested is not required, but is desirable.

7.32 Other Inputs

Other information may be obtained by a DRBG as input. This information may or may not be required to be kept secret by a consuming application; however, the security of the 25

DRBG itself does not rely on the secrecy of this information. The information **should** be checked for validity when possible.

During DRBG instantiation, a nonce is required and is combined with the entropy input to create the initial DRBG seed. Criteria for the nonce are provided in Section 8.6.7.

This Recommendation strongly advizes the insertion of a personalization string during DRBG instantiation; when used, the personalization string is combined with the entropy bits and a nonce to create the initial DRBG seed. The personalization string **shall** be unique for all instantiations of the same DRBG type (e.g., **HMAC_DRBG**). See Section 8.7.1 for additional discussion on personalization strings.

Additional input may also be provided during reseeding and when pseudorandom bits are requested. See Section 8.7.2 for a discussion of this input.

7.43 The Internal State

The internal state is the memory of the DRBG and consists of all of the parameters, variables and other stored values that the DRBG uses or acts upon. The internal state contains both administrative data and data that is acted upon and/or modified during the generation of pseudorandom bits (i.e., the *working state*). The contents of the internal state is dependent on the specific DRBG and includes all information that is required to produce the pseudorandom bits from one request to the next.

7.54 The DRBG Functions

The DRBG functions handle the DRBG's internal state. The DRBGs in this Recommendation have four separate functions (exclusive of health tests):

- The instantiate function acquires entropy input and combines it with a nonce and a
 personalization string to create a seed from which the initial internal state is
 created.
- 2. The generate function generates pseudorandom bits upon request, using the current internal state, and generates a new internal state for the next request.
- 3. The reseed function acquires new entropy input and combines it with the current internal state and any additional input that is provided to create a new seed and a new internal state.
- 4. The uninstantiate function zeroizes (i.e., erases) the internal state.

7.65 Health Tests

Health testing is concerned with assessing and reacting to the health of the DRBG (i.e., testing to determine that the DRBG continues to function correctly). The health tests are discussed in Sections 9.6 and 11.4.

8. DRBG Concepts and General Requirements

8.1 DRBG Functions

A DRBG requires instantiate, uninstantiate, generate, and testing functions. A DRBG may also include a reseed function. A DRBG shall be instantiated prior to the generation of output by the DRBG. These functions are specified in Section 9.

8.2 DRBG Instantiations

A DRBG **may** be used to obtain pseudorandom bits for different purposes (e.g., DSA private keys and AES keys) and **may** be separately instantiated for each purpose.

A DRBG is instantiated using a seed and **may** be reseeded; when reseeded, the seed **shall** be different than the seed used for instantiation. Each seed defines a *seed period* for the DRBG instantiation; an instantiation consists of one or more seed periods that begin when a new seed is acquired (see Figure 2).

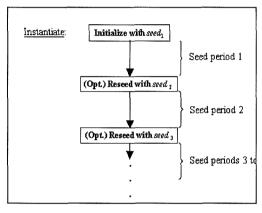


Figure 2: DRBG Instantiation

8.3 Internal States

During instantiation, an initial internal state is derived from the seed. The internal state for an instantiation includes:

1. Working state:

- a. One or more values that are derived from the seed and become part of the internal state; these values must usually remain secret, and
- b. A count of the number of requests or blocks produced since the instantiation was seeded or reseeded.
- 2. Administrative information (e.g., security strength and prediction resistance flag).

The internal state **shall** be protected at least as well as the intended use of the pseudorandom output bits requested by the consuming application. A DRBG implementation **may** be designed to handle multiple instantiations. Each DRBG instantiation **shall** have its own internal state. The internal state for one DRBG instantiation **shall not** be used as the internal state for a different instantiation.

A DRBG transitions between internal states when the generator is requested to provide new pseudorandom bits. A DRBG may also be implemented to transition in response to

internal or external events (e.g., system interrupts) or to transition continuously (e.g., whenever time is available to run the generator).

8.4 Security Strengths Supported by an Instantiation

The DRBGs specified in this Recommendation support four security strengths: 112, 128, 192 or 256 bits. The actual security strength supported by a given instantiation depends on the DRBG implementation and on the amount of entropy provided to the instantiate function. Note that the security strength actually supported by a particular instantiation **may** be less than the maximum security strength possible for that DRBG implementation (see Table 1). For example, a DRBG that is designed to support a maximum security strength of 256 bits may be instantiated to support only a 128-bit security strength.

Table 1: Possible Instantiated Security Strengths

Maximum Designed Security Strength	112	128	192	256
Possible Instantiated Security Strengths	112	112, 128	112, 128, 192	112, 128, 192, 256

A security strength for the instantiation is requested by a consuming application during instantiation, and the instantiate function obtains the appropriate amount of entropy for the requested security strength. Any security strength may be requested, but the DRBG will only be instantiated to one of the four security strengths above, depending on the DRBG implementation. A requested security strength that is below the 112-bit security strength or is between two of the four security strengths will be instantiated to the next highest level (e.g., a requested security strength of 96 bits will result in an instantiation at the 112-bit security strength).

Following instantiation, requests can be made to the generate function for pseudorandom bits. For each generate request, a security strength to be provided for the bits is requested. Any security strength can be requested up to the security strength of the instantiation, e.g., an instantiation could be instantiated at the 128-bit security strength, but a request for pseudorandom bits could indicate that a lesser security strength is actually required for the bits to be generated. The generate function checks that the requested security strength does not exceed the security strength for the instantiation. Assuming that the request is valid, the requested number of bits is returned.

When an instantiation is used for multiple purposes, the minimum entropy requirement for each purpose must be considered. The DRBG needs to be instantiated for the highest security strength required. For example, if one purpose requires a security strength of 112 bits, and another purpose requires a security strength of 256 bits, then the DRBG needs to be instantiated to support the 256-bit security strength.

8.5 DRBG Boundaries

As a convenience, this Standard uses the notion of a "DRBG boundary" to explain the operations of a DRBG and its interaction with and relation to other processes; a DRBG boundary contains all DRBG functions and internal states required for a DRBG. A DRBG boundary is entered via the DRBG's public interfaces, which are made available to consuming applications.

Within a DRBG boundary,

- 1. The DRBG internal state and the operation of the DRBG functions **shall** only be affected according to the DRBG specification.
- 2. The DRBG internal state **shall** exist solely within the DRBG boundary. The internal state **shall** be contained within the DRBG boundary and **shall not** be accessed by non-DRBG functions or other instantiations of that or other DRBGs.
- 3. Information about secret parts of the DRBG internal state and intermediate values in computations involving these secret parts **shall not** affect any information that leaves the DRBG boundary, except as specified for the DRBG pseudorandom bit outputs.

Each DRBG includes one or more cryptographic primitives (e.g., a hash function). Other applications may use the same cryptographic primitive as long as the DRBG's internal state and the DRBG functions are not affected.

A DRBG's functions may be contained within a single device, or may be distributed across

multiple devices (see Figures 3 and 4). Figure 3 depicts a DRBG for which all functions are contained within the same device. Figure 4 provides an example of DRBG functions that are distributed across multiple devices. In this case, each device has a DRBG sub-boundary that contains the DRBG functions implemented on that device, and the boundary around the entire DRBG consists of the aggregation of subboundaries providing the DRBG functionality. The use of distributed DRBG functions may be convenient for restricted environments (e.g., smart card applications) in which the primary use of the DRBG does not require repeated use of the instantiate or reseed functions.

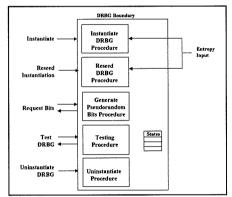


Figure 3: DRBG Functions within a Single Device

Although the entropy input is shown in the figures as originating outside the DRBG boundary, it may originate from within the boundary.

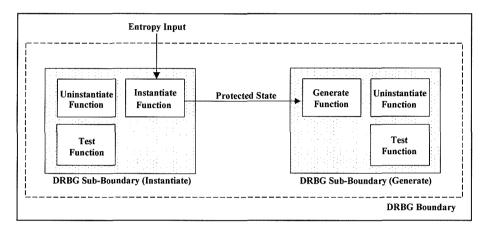


Figure 4: Distributed DRBG Functions

Each DRBG boundary or sub-boundary shall contain a test function to test the "health" of other DRBG functions within that boundary.

When DRBG functions are distributed, appropriate mechanisms **shall** be used to protect the confidentiality and integrity of the internal state or parts of the internal state that are transferred between the distributed DRBG sub-boundaries. The confidentiality and integrity mechanisms and security strength **shall** be consistent with the data to be protected by the DRBG's consuming application (see SP 800-57).

8.6 Seeds

When a DRBG is used to generate pseudorandom bits, a seed **shall** be acquired prior to the generation of output bits by the DRBG. The seed is used to instantiate the DRBG and determine the initial internal state that is used when calling the DRBG to obtain the first output bits.

Reseeding is a means of recovering the secrecy of the output of the DRBG if a seed or the internal state becomes known. Periodic reseeding is a good countermeasure to the potential threat that the seeds and DRBG output become compromised. In some implementations (e.g., smartcards), an adequate reseeding process may not be possible. In these cases, the best policy might be to replace the DRBG, obtaining a new seed in the process (e.g., obtain a new smart card).

The seed and its use by a DRBG **shall** be generated and handled as specified in the following subsections.

8.6.1 Seed Construction for Instantiation

Figure 5 depicts the seed construction process for instantiation. The seed material used to

determine a seed for instantiation consists of entropy input, a nonce and an optional personalization string. Entropy input **shall** always be used in the construction of a seed; requirements for the entropy input are discussed in item Section 8.6.3. A nonce **shall** also be used; requirements for the nonce are discussed in Section 8.6.7. This Recommendation also advises the inclusion of a personalization string; requirements for the personalization string are discussed in Section 8.7.2.

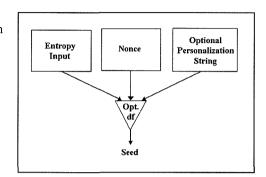


Figure 5: Seed Construction for Instantiation

Depending on the DRBG and the source

of the entropy input, a derivation function is required to derive a seed from the seed material. When full entropy input is readily available, the DRBG based on block cipher algorithms (see Section 10.2) may be implemented without a derivation function. When implemented in this manner, a nonce (as shown in Figure 5) is not used. Note, however, that the personalization string could contain a nonce, if desired.

The goal of this seed construction is to ensure that the seed is statistically unique.

8.6.2 Seed Construction for Reseeding

Figure 6 depicts the seed construction process for reseeding an instantiation. The seed material for reseeding consists of a value that is carried in the internal state³, new entropy input and, optonally, additional input. The internal state value and the entropy input are required; requirements for the entropy input are discussed in Secrtion 8.6.3. Requirements for the additional input are discussed in Section 8.7.3. As in Section 8.6.1, a derivation function may be required for reseeding. See Section 8.6.1 for further guidance.

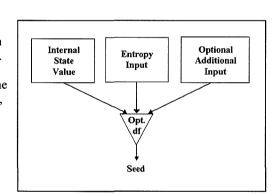


Figure 6: Seed Construction for Reseeding

8.6.3. Entropy Requirements for the Entropy Input

The entropy input for the seed **shall** contain sufficient entropy for the desired security strength. Additional entropy **may** be provided in the nonce or the optional personalization

³ See each DRBG specification for the value that is used.

string during instantiation, or in the additional input during reseeding, but this is not required. Entropy contained in the seed components is distributed across the seed (e.g., using an appropriate derivation function) by the instantiate and reseed functions.

The entropy input **shall** have entropy that is equal to or greater than the security strength of the instantiation. Note that the use of more entropy than the minimum value will offer a security "cushion". This may be useful if the assessment of the entropy provided in the entropy input is incorrect. Having more entropy than the assessed amount is acceptable; having less entropy than the assessed amount could be fatal to security. The presence of more entropy than is required, especially during the instantiatiation, will provide a higher level of assurance than the minimum required entropy.

8.6.4 Seed Length

The minimum length of the seed depends on the DRBG and the security strength required by the consuming application. See Section 10.

8.6.5 Entropy Input Source

The source of the entropy input **may** be an Approved NRBG, an Approved DRBG (or chain of Approved DRBGs) that is seeded by an Approved NRBG, or another source whose entropy characteristics are known. Further discussion about the entropy input is provided in Appendix C.

8.6.6 Entropy Input and Seed Privacy

The entropy input and the resulting seed **shall** be handled in a manner that is consistent with the security required for the data protected by the consuming application. For example, if the DRBG is used to generate keys, then the entropy inputs and seeds used to generate the keys **shall** be treated at least as well as the key (at a minimum).

8.6.7 Nonce

A nonce is required to construct a seed during instantation. The nonce shall be either:

- a. A random value with at least (security_strength/2) bits of entropy,
- b. A non-random value that is guaranteed to never repeat, or
- c. A non-random value that is expected to repeat no more often than a (security_strength/2)-bit random string would be expected to repeat.

For case a, the nonce **may** be acquired from the same source and at the same time as the entropy input. In this case, the seed could be considered to be constructed from an "extra strong" entropy input and the optional personalization string, where the entropy for the entropy input is equal to or greater than (3/2 security_strength) bits.

8.6.8 Reseeding

Generating too many outputs from a seed (and other input information) may provide

sufficient information for successfully predicting future outputs unless prediction resistance is provided (see Section 8.8). Periodic reseeding will reduce security risks, reducing the likelihood of a compromise of the data that is protected by cryptographic mechanisms that use the DRBG.

Seeds **shall** have a finite seedlife (i.e., the length of the seed period); the maximum seedlife is dependent on the DRBG used. Reseeding is accomplished by 1) an explicit reseeding of the DRBG by the application, or 2) by the generate function when prediction resistance is requested (see Section 8.8) or the limit of the seedlife is reached. An alternative to reseeding is to create an entirely new instantiation.

Reseeding of the DRBG **shall** be performed in accordance with the specification for the given DRBG. The DRBG reseed specifications within this Recommendation are designed to produce a new seed that is determined by both the old seed and newly-obtained entropy input that will support the desired security strength.

8.6.9 Seed Use

A seed that is used to initialize one instantiation of a DRBG **shall not** be intentionally used to reseed the same instantiation or used as a seed for another DRBG instantiation. Note that a DRBG does not provide output until a seed is available, and the internal state has been initialized (see Section 10).

8.6.10 Seed Separation

Seeds used by DRBGs **shall not** be used for other purposes (e.g., domain parameter or prime number generation).

8.7 Other Inputs to the DRBG

Other input may be provided during DRBG instantiation, pseudorandom bit generation and reseeding. This input may contain entropy, but this is not required. During instantiation, a personalization string may be provided and combined with entropy input and a nonce to derive a seed (see Section 8.6.1). When pseudorandom bits are requested and when reseeding is performed, additional input may be provided.

Depending on the method for acquiring the input, the exact value of the input may or may not be known to the user or application. For example, the input could be derived directly from values entered by the user or application, or the input could be derived from information introduced by the user or application (e.g., from timing statistics based on key strokes), or the input could be the output of another DRBG or an NRBG.

8.7.1 Personalization String

During instantiation, a personalization string **should** be used to derive the seed (see Section 8.6.1). The intent of a personalization string is to differentiate this DRBG instantiation from all the others that might ever appear. The personalization string **should** be set to some bitstring that is as unique as possible, and **may** include secret information.

The value of any secret information contained in the personalization string **should** be no greater than the claimed strength of the DRBG, as the DRBG's cryptographic mechanisms will protect this information from disclosure. Good choices for the personalization string contents include:

- 1. Device serial numbers,
- 2. Public keys,
- 3. User identification,
- 4. Private keys,
- 5. PINs and passwords,
- 6. Secret per-module or per-device values,
- 7. Timestamps,
- 8. Network addresses,
- 9. Special secret key values for this specific DRBG instantiation,
- 10. Application identifiers,
- 11. Protocol version identifiers,
- 12. Random numbers, and
- 13. Nonces.

8.7.2 Additional Input

During each request for bits from a DRBG and during reseeding, the insertion of additional input is allowed. This input is optional and may be either secret or publicly known; its value is arbitrary, although its length may be restricted, depending on the implementation and the DRBG. The use of additional input may be a means of providing more entropy for the DRBG internal state that will increase assurance that the entropy requirements are met. If the additional input is kept secret and has sufficient entropy, the input can provide more assurance when recovering from the compromise of the seed or one or more DRBG internal states.

8.8 Prediction Resistance and Backtracking Resistance

Figure 7 depicts the sequence of DRBG internal states that result from a given seed. Some subset of bits from each internal state are used to generate pseudorandom bits upon request by a user. The following discussions will use the figure to explain backtracking and prediction resistance.

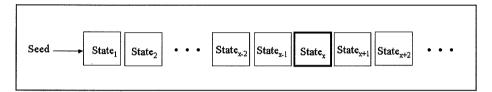


Figure 7: Sequence of DRBG States

Suppose that a compromise occurs at $State_x$, where $State_x$ contains both secret and public information.

Backtracking Resistance: Backtracking resistance means that a compromise of the DRBG internal state has no effect on the security of prior outputs. That is, an adversary who is given access to all of any subset of that prior output sequence cannot distinguish it from random; if the adversary knows only part of the prior output, he cannot determine any bit of that prior output sequence that the adversaryhe has not already seen. In other words, a compromise has no effect on the security of prior outputs.

For example, suppose that an adversary knows $State_{x_3,-}$ and also knows the output bits from $State_1$ to $State_{x-2}$. Backtracking resistance means that:

- <u>a.</u> The output bits from $State_1$ to $State_{x-1}$ cannot be distinguished from random.
- b. The prior internal state values themselves (State₁ to State_{x-1}) cannot be recovered, given knowledge of the secret information in State_{x-2} State_{x-1} and its output bits cannot be determined from knowledge of State_x (i.e., State_{x-2} cannot be "backed up"). In addition, since the output bits from State₊ to State_{x-2} appear to be random, the output bits for State_{x-1} cannot be predicted from the output bits of State₊ to State_{x-2}.

Backtracking resistance can be provided by ensuring that the DRBG algorithm is a one-way function. All DRBGs in this Recommendation have been designed to provide backtracking resistance.

Prediction Resistance: Prediction resistance means that a compromise of the DRBG internal state has no effect on the security of future DRBG outputs. If a compromise of State_X occurs, prediction resistance provides assurance that the output sequence resulting from states after the compromise remains secure. That is, an adversary who is given access to all of any subset of the output sequence after the compromise cannot distinguish it from random; if the adversary knows only part of the future output sequence, an adversary he cannot predict any bit of that future output sequence that he has not already seen. In other words, a compromise has no effect on the security of future outputs.

For example, suppose that an adversary knows Statex: and also knows the output bits from

 $State_{x+2}$ to $State_{x+n}$ -Prediction resistance means that:

- a. The output bits from $State_{x+1}$ and forward cannot be distinguished from an ideal random bitstring by the adversary.
- ____b. The future internal state values themselves (State_{x+1} and forward) <u>can</u>not <u>be</u> predicted, given knowledge of State_{x+} State_{x+1} and its output bits cannot be determined from knowledge of State_x (i.e., State_x cannot be "backed up"). In addition, since the output bits from State_{x+1} to State_{x+2} appear to be random, the output bits for State_{x+1} cannot be predicted from the output bits of State_{x+1} to State_{x+2}.

State_{x+1} and its output bits cannot be predicted from knowledge of State_x. In addition, because the output bits from $State_{x+2}$ to $State_{x+n}$ appear to be random, the output bits for $State_{x+1}$ cannot be determined from the output bits of $State_{x+2}$ to $State_{x+n}$.

Prediction resistance can be provided only by ensuring that a DRBG is effectively reseeded between DRBG requests. That is, an amount of entropy that is sufficient to support the security strength of the DRBG (i.e., an amount that is at least equal to the security strength) must be added to the DRBG in a way that ensures that knowledge of the <u>currentprevious</u> DRBG internal state does not allow an adversary any useful knowledge about future DRBG internal states or outputs.

9 DRBG Functions

The DRBG functions in this Recommendation are specified as an algorithm and an "envelope" of pseudocode around that algorithm. The pseudocode in the envelopes (provided in this section) checks the input parameters, obtains input not provided by the input parameters, accesses the appropriate DRBG algorithm and handles the internal state. A function need not be implemented using such envelopes, but the function **shall** have equivalent functionality.

In the specifications of this Recommendation, the following pseudo-functions are used for convenience. These functions are not specifically defined in this Recommendation, but have the following meaning:

• **Get_entropy**: A function that is used to obtain entropy input. The function call is:

(status, entropy_input) = **Get_entropy** (min_entropy, min_length, max_length)

which requests a string of bits (entropy_input) with at least min_entropy bits of entropy. The length for the string shall be equal to or greater than min_length bits, and less than or equal to max_length bits. A status code is also returned from the function.

• **Block_Encrypt:** A basic encryption operation that uses the selected block cipher algorithm. The function call is:

```
output\_block = Block\_Encrypt (Key, input\_block)
```

For TDEA, the basic encryption operation is called the forward cipher operation (see SP 800-67); for AES, the basic encryption operation is called the cipher operation (see FIPS 197). The basic encryption operation is equivalent to an encryption operation on a single block of data using the ECB mode.

Note that an implementation may choose to define this functionality differently; for example, for many of the DRBGs, the $min_length = min_entropy$ for the **Get_entropy** function, in which case, the second parameter could be omitted.

9.1 Instantiating a DRBG

A DRBG **shall** be instantiated prior to the generation of pseudorandom bits. The instantiate function:

- 1. Checks the validity of the input parameters,
- $2. \ \ Determines the security strength for the DRBG instantiation,$
- 3. Determines any DRBG specific parameters (e.g., elliptic curve domain parameters),
- 4. Obtains entropy input with entropy sufficient to support the security strength,
- 5. Obtains the nonce,

- 6. Determines the initial internal state using the instantiate algorithm,
- 7. Returns a state_handle for the internal state to the consuming application.

Let working_state be the working state for the particular DRBG, and let min_length, max_length, and highest_supported_security_strength be defined for each DRBG (see Section 10).

The following or an equivalent process shall be used to instantiate a DRBG.

Input from a consuming application:

- 1. requested_instantiation_security_strength: A requested security strength for the instantiation. DRBG implementations that support only one security strength do not require this parameter; however, any application using that DRBG implementation must be aware of this limitation.
- 2. prediction_resistance_flag: Indicates whether or not prediction resistance may be required by a the consuming application during one or more requests for pseudorandom bits. DRBGs that are implemented to always or never support prediction resistance do not require this parameter. However, the user of a consuming application must determine whether or not prediction resistance may be required by the application before electing to use such a DRBG implementation. If the prediction_resistance_flag is not needed (i.e., because prediction resistance is always or never performed), then the input parameter may be omitted, and the prediction_resistance_flag may be omitted from the internal state in step 11.
- 3. personalization_string: An optional input that provides personalization information (see Sections 8.6.1 and 8.7.1). The maximum length of the personalization string (max_personalization_string_length) is implementation dependent, but shall be less than or equal to the maximum length specified for the given DRBG (see Section 10). If a personalization string will never be used, then the input parameter and step 3 may be omitted, and step 9 may be modified to omit the personalization string.

Required information not provided by the consuming application:

Comment: This input **shall not** be provided by the consuming application as an input parameter during the instantiate request.

- 1. *entropy_input*: Input bits containing entropy. The maximum length of the *entropy_input* is implementation dependent, but **shall** be less than or equal to the specified maximum length for the selected DRBG (see Section 10).
- nonce: A nonce as specified in Section 8.6.7. Note that if a random value is used as
 the nonce, the entropy_input and nonce could be acquired using a single
 Get_entropy call (see step 6); in this case, the first parameter would be adjusted to
 include the entropy for the nonce (i.e., security_strength would be increased by at

least *security_strength*/2), step 8 would be omitted, and the *nonce* would be omitted from the parameter list in step 9.

Output to a consuming application:

- status: The status returned from the instantiate function. The status will indicate
 SUCCESS or an ERROR. If an ERROR is indicated, either no state_handle or an
 invalid state_handle shall be returned. A consuming application should check the
 status to determine that the DRBG has been correctly instantiated.
- 2. *state_handle*: Used to identify the internal state for this instantiation in subsequent calls to the generate, reseed, uninstantiate and test functions.

Information retained within the DRBG boundary:

The internal state for the DRBG, including the *working_state* and administrative information (see Sections 8. 3 and 10).

Process:

Comment: Check the validity of the input parameters.

- If requested_instantiation_security_strength >
 highest_supported_security_strength, then reruen an ERROR.
- 2. If prediction_resistance_flag is set, and prediction resistance is not supported, then return an ERROR.
- 3. If the length of the *personalization_string > max_personalization_string_length*, return an **ERROR**.
- 4 Set *security_strength* to the nearest security strength greater than or equal to *requested_instantiation_security_strength*.

Comment: The following step is required by the Dual_EC_DRBG when multiple curves are available (see Section 10.3.2.2.2). Otherwise, the step **should** be omitted.

5. Using security_strength, select appropriate DRBG parameters.

Comment: Obtain the entropy input.

- 6. (status, entropy_input) = **Get_entropy** (security_strength, min_length, max_length).
- 7. If an ERROR is returned in step 6, return an ERROR.
- 8. Obtain a nonce.

Comment: This step **shall** include any appropriate checks on the acceptability of the *nonce*. See Section 8.6.7.

Comment: Call the appropriate instantiate

algorithm in Section 10 to obtain values for the initial working_state.

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- 9. working_state = Instantiate_algorithm (entropy_input, nonce, personalization_string, other DRBG_parameters).
- 10. Get a *state_handle* for a currently empty internal state. If an unused internal state cannot be found, return an **ERROR**.
- 11. Set the internal state indicated by *state_handle* to the initial values for the *working_state* and administrative information, as appropriate.
- 12. Return SUCCESS and state_handle.

9.2 Reseeding a DRBG Instantiation

The reseeding of an instantiation is not required, but is recommended whenever an application and implementation are able to perform this process. Reseeding will insert additional entropy into the generation of pseudorandom bits. Reseeding may be:

- · explicitly requested by an application,
- · performed when prediction resistance is requested by an application,
- triggered by the generate function when a predetermined number of pseudorandom outputs have been produced (i.e., at the end of the seedlife), or
- triggered by external events (e.g., whenever sufficient entropy is available).

If a reseed capability is not available, a new DRBG instantiation may be created (see Section 9.1).

The reseed function:

- 1. Checks the validity of the input parameters,
- 2. Obtains entropy input with sufficient entropy to support the security strength, and
- 3. Using the reseed algorithm, combines the current working state with the new entropy input and any additional input to determine the new working state.

Let working_state be the working state for the particular DRBG, and let min_length and max_length be defined for each DRBG (see Section 10).

The following or an equivalent process shall be used to reseed the DRBG instantiation.

Input from a consuming application:

- state_handle: A pointer or index that indicates the internal state to be reseeded.
 This value was returned from the instantiate function specified in Section 9.1.
- 2) additional_input: An optional input. The maximum length of the additional_input (max_additional_input_length) is implementation dependent, but shall be less than

or equal to the maximum value specified for the given DRBG (see Section 10). If *additional_input* will never be used, then the input parameter and step 2 may be omitted, and step 2 may be modified to remove the *additional_input* from the parameter list.

Required information not provided by the consuming application:

Comment: This input **shall not** be provided by the consuming application in the input parameters.

- 1. *entropy_input*: Input bits containing entropy. The maximum length of the *entropy_input* is implementation dependent, but **shall** be less than or equal to the specified maximum length for the selected DRBG (see Section 10).
- 2. Internal state values required by the DRBG for reseeding for the *working_state* and administrative information, as appropriate.

Output to a consuming application:

1. *status*: The status returned from the function. The *status* will indicate **SUCCESS** or an **ERROR**.

Information retained within the DRBG boundary:

Replaced internal state values (i.e., the working_state).

Process:

Comment: Get the current internal state and check the input parameters.

- 1. Using *state_handle*, obtain the current internal state. If *state_handle* indicates an invalid or unused internal state, return an **ERROR**.
- 2. If the length of the *additional_input > max_additional_input_length*, return an **ERROR**.

Comment: Obtain the entropy input.

- 3. (status, entropy_input) = **Get_entropy** (security_strength, min_length, max_length).
- 4. If an ERROR is returned in step 3, return an ERROR.

Comment: Get the new *working_state* using the appropriate reseed algorithm in Section 10.

- 5. working_state = Reseed_algorithm (working_state, entropy_input, additional_input).
- 6. Replace the working_state in the internal state indicated by state_handle with the

new values.

7. Return SUCCESS.

9.3 Generating Pseudorandom Bits Using a DRBG

This function is used to generate pseudorandom bits after instantiation or reseeding (see Sections 9.1 and 9.2). The generate function:

- 1. Checks the validity of the input parameters,
- Calls the reseed function to obtain sufficient entropy if the instantiation needs additional entropy because the end of the seedlife has been reached or prediction resistance is required,
- 3. Generates the requested pseudorandom bits using the generate algorithm. The generate algorithm will check that two consecutive states are not the same.
- 4. Updates the working state.
- 5. Returns the requested pseudorandom bits to the consuming application.

Let outlen be the length of the output block of the cryptographic primitive (see Section 10).

The following or an equivalent process shall be used to generate pseudorandom bits.

Input from a consuming application:

- 1. state_handle: A pointer or index that indicates the internal state to be used.
- 2. requested_number_of_bits: The number of pseudorandom bits to be returned from the generate function. The max_number_of_bits_per_request is implementation dependent but shall be less than or equal to the value provided in Section 10 for a specific DRBG.
- 3. requested_security_strength: The security strength to be associated with the requested pseudorandom bits. DRBG implementations that support only one security strength do not require this parameter; however, any application using that DRBG implementation must be aware of this limitation.
- 4. prediction_resistance_request: Indicates whether or not prediction resistance is to be provided. DRBGs that are implemented to always or never support prediction resistance do not require this parameter. However, the user of a consuming application must determine whether or not prediction resistance may be required by the application before electing to use such a DRBG implementation.

If prediction resistance is never provided, then the *prediction_resistance_request* input parameter and step 5 may be omitted, and step 7 may be modified to omit the check for the *prediction resistance request*.

If prediction resistance is always performed, then the *prediction_resistance_request* input parameter and step 5 may be omitted, and steps 7 and 8 are replaced by:

status = Reseed (state_handle, additional_input).

If status indicates an ERROR, then return ERROR.

Using state_handle, obtain the new internal state.

(status, pseudorandom_bits, working_state) = Generate_algorithm (working_state, requested_number_of_bits).

Note that if *additional_input* is never provided, then the *additional_input* parameter in the Reseed call above may be omitted.

5. additional_input: An optional input. The maximum length of the additional_input (max_additional_input_length) is implementation dependent, but shall be less than or equal to the specified maximum length for the selected DRBG (see Section 10). If additional_input will never be used, then the input parameter, step 4, step 7.4 and the additional_input input parameter in step 8 may be omitted.

Required information not provided by the consuming application:

1. Internal state values required for generation for the *working_state* and administrative information, as appropriate.

Output to a consuming application:

- 1. *status*: The status returned from the function. The *status* will indicate **SUCCESS** or an **ERROR**.
- 2. pseudorandom_bits: The pseudorandom bits that were requested.

Information retained within the DRBG boundary:

Replaced internal state values (i.e., the working_state).

Process:

Comment Get the internal state and check the input parameters.

- Using state_handle, obtain the current internal state for the instantiation. If state_handle indicates an invalid or unused internal state, then return an ERROR.
- 2. If requested_number_of_bits > max_number_of_bits_per_request, then return an ERROR.
- 3. If requested_security_strength > the security_strength indicated in the internal state, then return an **ERROR**.
- 4. If the length of the *additional_input > max_additional_input_length*, then return an **ERROR**.
- 5. If *prediction_resistance_request* is set, and *prediction_resistance_flag* is not set, then return an **ERROR**.

6. Clear the reseed_required_flag.

Comment: Get the requested pseudorandom bits.

7. If reseed_required_flag is set, or if prediction_resistance_request is set, then

Comment: Reseed the instantiation (see Section 9.2).

- 7.1 status = **Reseed** (state_handle, additional_input).
- 7.2 If status indicates an ERROR, then return an ERROR.
- 7.3 Using *state handle*, obtain the new internal state.
- 7.4 additional_input = the Null string.
- 7.5 Clear the reseed_required_flag.

Comment: Request the generation of *pseudorandom_bits* using the appropriate generate algorithm in Section 10.

- 8. (status, pseudorandom_bits, working_state) = Generate_algorithm (working_state, requested_number_of_bits, additional_input).
- 9. If *status* indicates that a reseed is required before the requested bits can be generated, then
 - 9.1 Set the reseed_required_flag.
 - 9.2 Go to step 7.

Comment: If an **ERROR** is returned, two consecutive states are the same.

- 10. If an ERROR is returned from step 8,
 - 10.1 Delete all instantiations using the uninstantiate function.
 - 10.2 Return the ERROR received from step 8.
- 11. Replace the old *working_state* in the internal state indicated by *state_handle* with the new *working_state*.
- 12. Return SUCCESS and pseudorandom_bits.

Implementation notes:

If a reseed capability is not available, then steps 6 and 7 may be removed; and step 9 is replaced by:

9. If *status* indicates that a reseed is required before the requested bits can be generated, then

- 9.1 status = Uninstantiate (state_handle).
- 9.2 If an ERROR is returned in step 9.1, then return the ERROR.
- 9.3 Return an indication that the DRBG instantiation can no longer be used.

9.4 Removing a DRBG Instantiation

The internal state for an instantiation may need to be "released". The uninstantiate function:

- 1. Checks the input parameter for validity.
- 2. Empties the internal state.

The following or an equivalent process **shall** be used to remove (i.e., uninstantiate) a DRBG instantiation:

Input from a consuming application:

1. state_handle: A pointer or index that indicates the internal state to be "released".

Output to a consuming application:

 status: The status returned from the function. The status will indicate SUCCESS or ERROR.

Information retained within the DRBG boundary:

An empty internal state.

Process:

- 1. If state_handle indicates an invalid state, then return an ERROR.
- 2. Erase the contents of the internal state indicated by *state_handle*.
- 3. Return SUCCESS.

9.5 Auxilliary Functions

Derivation functions are internal functions that are used during DRBG instantiation and reseeding to either derive internal state values or to distribute entropy throughout a bitstring. Two methods are provided. One method is based on hash functions (see Section 9.6.1), and the other method is based on block cipher algorithms (see 9.6.2). The block cipher derivation function uses a **Block_Cipher_Hash** function that is specified in Section 9.6.3.

9.5.1 Derivation Function Using a Hash Function (Hash_df)

This derivation function is used by the **Hash_DRBG** and **Dual_EC_DRBG** specified in Section 10. The hash-based derivation function hashes an input string and returns the requested number of bits. Let **Hash (...)** be the hash function used by the DRBG, and let

outlen be its output length.

The following or an equivalent process **shall** be used to derive the requested number of bits.

Input:

- 1. input_string: The string to be hashed.
- 2. no_of_bits_to_return: The number of bits to be returned by **Hash_df**. The maximum length (max_number_of_bits) is implementation dependent, but **shall** be less than or equal to (255 × outlen). no_of_bits_to_return is represented as a 32-bit integer.

Output:

- status: The status returned from Hash_df. The status will indicate SUCCESS or ERROR.
- 2. requested_bits: The result of performing the Hash_df.

Process:

- 1. If no_of_bits_to_return > max_number_of_bits, then return an ERROR.
- 2. *temp* = the Null string.

3.
$$len = \left\lceil \frac{no_of_bits_to_return}{outlen} \right\rceil$$

- 4. *counter* = an 8-bit binary value representing the integer "1".
- 5. For i = 1 to len do

Comment: In step 5.1, no_of_bits_to_return is used as a 32-bit string.

- 5.1 temp = temp || **Hash** (counter || no_of_bits_to_return || input_string).
- 5.2 counter = counter + 1.
- 6. requested_bits = Leftmost (no_of_bits_to_return) of temp.
- 7. Return **SUCCESS** and *requested_bits*.
- 9.5.2 Derivation Function Using a Block Cipher Algorithm (Block_Cipher_df)

This derivation function is used by the CTR_DRBG that is specified in Section 10.2. Let **Block_Cipher_Hash** be the function specified in Section 9.6.3. Let Let *outlen* be its output block length, which is a multiple of 8 bits for the Approved block cipher algorithms, and let *keylen* be the key length.

The following or an equivalent process shall be used to derive the requested number of bits.

Input:

- 1. input_string: The string to be operated on. This string shall be a multiple of 8 bits.
- 2. no_of_bits_to_return: The number of bits to be returned by **Block_Cipher_df**. The maximum length (max_number_of_bits) is 512 bits for the currently approved block cipher algorithms.

Output:

- status: The status returned from Block_Cipher_df. The status will indicate SUCCESS or ERROR.
- 2. requested_bits: The result of performing the Block_Cipher_df.

Process:

- 1. If (number_of_bits_to_return > max_number_of_bits), then return an ERROR.
- 2. $L = len (input_string)/8$.

Comment: *L* is the bitstring represention of the integer resulting from **len** (*input_string*)/8. *L* **shall** be represented as a 32-bit integer.

3. $N = number_of_bits_to_return/8$.

Comment: N is the bitsting represention of the integer resulting from number_of_bits_to_return/8. N shall be represented as a 32-bit integer.

Comment: Prepend the string length and the requested length of the output to the *input_string*.

3. $S = L || N || input_string || 0x80.$

Comment: Pad S with zeros, if necessary.

4. While (len (S) mod outlen) $\neq 0$, $S = S \parallel 0 \times 00$.

Comment: Compute the starting value.

- 5. *temp* = the *Null* string.
- 6. i = 0.

Comment : i shall be represented as a 32-bit integer, i.e., len (i) = 32.

- 7. K = Leftmost keylen bits of 0x010203...1F.
- 8. While len(temp) < keylen + outlen, do
 - 8.1 $IV = i \parallel 0^{outlen len (i)}$.

Comment: The 32-bit integer representaion of *i* is padded with zeros to *outlen* bits.

8.2 $temp = temp \parallel \mathbf{Block_Cipher_Hash} (K, (IV \parallel S)).$

Comment: Compute the requested number of bits

- 9. K = Leftmost keylen bits of temp.
- 10. X = Next outlen bits of temp.
- 11. temp = the Null string.
- 12. While len (temp) < number_of_bits_to_return, do
 - 12.1 X =**Block_Encrypt** (K, X).
 - 12.2 temp = temp || X.
- 13. requested_bits = Leftmost number_of_bits_to_return of temp.
- 14. Return SUCCESS and requested bits.

9.5.4 Block_Cipher_Hash Function

Let outlen be the length of the output block of the block cipher algorithm to be used.

The following or an equivalent process shall be used to derive the requested number of bits.

Input:

- 1. Key: The key to be used for the block cipher opeation.
- 2. data_to_hash: The data to be operated upon. Note that the length of data_to_hash must be a multiple of outlen. This is guaranteed by steps 4 and 8.1 in Section 9.6.2.

Output:

1. $output_block$: The result to be returned from the **Block_Cipher_Hash** operation.

Process:

- 1. $chaining_value = 0^{outlen}$. Comment: Set the first chaining value to *outlen* zeros.
- 2. $n = \text{len } (data_to_hash)/outlen$.
- 3. Split the $data_to_hash$ into n blocks of outlen bits each forming $block_1$ to $block_n$.
- 4. For i = 1 to n do
 - 4.1 $input_block = chaining_value \oplus block_i$.
 - 4.2 chaining_value = Block_Encrypt (Key, input_block).
- 5. output_block = chaining_value.
- 6. Return output_block.

9.6 Self-Testing of the DRBG

A DRBG **shall** perform self testing to obtain assurance that the implementation continues to operate as designed and implemented (health testing). The testing function(s) within a DRBG boundary (or sub-boundary) **shall** test each DRBG function within that boundary.

Errors occurring during testing **shall** be perceived as complete DRBG failures. The condition causing the failure **shall** be corrected and the DRBG re-instantiated before requesting pseudorandom bits (also, see Section 9.7)

9.6.1 Testing the Instantiate Function

Known-answer tests on the instantiate function **shall** be performed prior to creating each operational instantiation. However, if several instantiations are performed in quick succession using the same input parameters, then the testing **may** be reduced to testing prior to creating the first instantiation using that parameter set.

The security_strength and prediction_resistance_flag to be used in the operational invocation shall be used during the test. Representative fixed values and lengths of the entropy_input, nonce and personalization_string (if allowed) shall be used; the value of the entropy_input used during testing shall not be intentionally reused during normal operations (either by the instantiate or the reseed functions). Error handling shall be also be tested, including an error in obtaining the entropy_input (e.g., the entropy_input source is broken).

If the values used during the test produce the expected results, and errors are handled correctly, then the instantiate function may be used to instantiate using the tested values of *security_strength* and *prediction_resistance_flag*.

An implementation **should** provide a capability to test the instantiate function on demand.

9.6.2 Testing the Generate Function

Known-answer tests **shall** be performed on the generate function before the first use of the function and at reasonable intervals defined by the implementer. The implementer **shall** document the intervals and provide a justification for the selected intervals.

The known-answer tests **shall** be performed for each implemented *security_strength*. Representative fixed values and lengths for the *requested_number_of_bits* and *additional_input* (if allowed) and the working state of the internal state value (see Sections 8.3 and 10) **shall** be used. If prediction resistance is available, then each combination of the *security_strength*, *prediction_resistance_request* and *prediction_resistance_flag* **shall** be tested. The error handling for each input parameter **shall** also be tested, and testing **shall** include setting the *reseed_counter* to meet or exceed the *reseed_interval* in order to check that the implementation is reseeded or that the DRBG is "shut down", as appropriate.

If the values used during the test produce the expected results, and errors are handled correctly, then the generate function may be used during normal operations.

Bits generated during health testing shall not be output as pseudorandom bits.

An implementation should provide a capability to test the generate function on demand.

Note that the generate function performs a continuous test by comparing sequential output blocks.

9.6.3 Testing the Reseed Function

A known-answer test of the reseed function **shall** use the *security_strength* in the internal state of the instantiation to be reseeded. Representative values of the *entropy_input* and *additional_input* (if allowed) and the working state of the internal state value **shall** be used (see Sections 8.3 and 10). Error handling **shall** also be tested, including an error in obtaining the *entropy_input* (e.g., the *entropy_input* source is broken).

If the values used during the test produce the expected results, and errors are handled correctly, then the reseed function may be used to reseed the instantiation.

The reseed function may be called every time that the generate function is called if prediction resistance is available, and considerbly less frequently otherwise. Self-test **shall** be performed as follows:

- 1. When prediction resistance is available in an implementation, the reseed function **shall** be tested whenever the generate function is tested (see above).
- 2. When prediction resistance is not available in an implementation, the reseed function **shall** be tested whenever the reseed function is invoked and before the reseed is performed on the operational instantiation.

An implementation should provide a capability to test the reseed function on demand.

9.6.4 Testing the Uninstantiate Function

The uninstantiate function **shall** be tested whenever other functions are tested. Testing **shall** attempt to demonstrate that error handling is performed correctly, and the internal state has been "emptied".

9.7 Error Handling

The expected errors are indicated for each DRBG function (see Sections 9.1 - 9.4) and for the derivation functions in Section 9.5. The error handling routines **should** indicate the type of error. For catastrophic errors (e.g., entropy input source failure), the DRBG **shall not** produce further output until the source of the error is corrected.

Many errors during normal operation may be caused by an application's improper DRBG request. In these cases, the application user is responsible for correcting the request within the limits of the user's organizational security policy. For example, if a failure indicating an invalid requested security strength is returned, a security strength higher than the DRBG or the DRBG instantiation can support has been requested. The user **may** reduce the requested security strength if the organization's security policy allows the information to

be protected using a lower security strength, or the user **shall** use an appropriately instantiated DRBG.

Failures that indicate that the entropy source has failed or that the DRBG failed health testing (see Sections 9.6 and 11.4) **shall** be handled as complete DRBG failures. The indicated DRBG problem **shall** be corrected, and the DRBG **shall** be re-instantiated before the DRBG can be used to produce pseudorandom bits.

10 DRBG Algorithm Specifications

Several DRBGs are specified in this Recommendation. The selection of a DRBG depends on several factors, including the security strength to be supported and what cryptographic primitives are available. An analysis of the consuming application's requirements for random numbers **shall** be conducted in order to select an appropriate DRBG. A detailed discussion on DRBG selection is provided in Appendix G. Pseudocode examples for each DRBG are provided in Appendix F. Conversion specifications required for the DRBG implementations (e.g., between integers and bitstrings) are provided in Appendix B.

10.1 Deterministic RBGs Based on Hash Functions

A DRBG may be based on a hash function that is non-invertible or one-way. The hash DRBGs specified in this Recommendation have been designed to use any Approved hash function and may be used by applications requiring various security strengths, providing that the appropriate hash function is used and sufficient entropy is obtained for the seed.

The following are provided as DRBGs based on hash functions:

- 1. The **Hash_DRBG** specified in Section 10.1.1.
- 2. The HMAC_DRBG specified in Section 10.1.2.

The maximum security strength that could be supported by each hash function is provided in SP 800-57. However, this Recommendation supports only four security strengths: 112, 128, 192, and 256. Table 2 specifies the values that **shall** be used for the function envelopes and DRBG algorithm for each Approved hash function.

Table 2: Definitions for Hash-Based DRBGs

	SHA-1	SHA-224	SHA-256	SHA-384	SHA-512	
Supported security strengths	See SP 800-57					
highest_supported_security_strength	See SP 800-57					
Output Block Length (outlen)	160	224	256	384	512	
Required minimum entropy for instantiate and reseed	security_strength					
Minimum entropy input length (min_length)	security_strength					
Maximum entropy input length	$\leq 2^{35}$ bits					
(max_ length)						
Seed length (seedlen) for Hash_DRBG	440	440	440	888	888	

	SHA-1	SHA-224	SHA-256	SHA-384	SHA-512	
Maximum personalization string length (max_personalization_string_length)	***************************************	1	$\leq 2^{35}$ bits	I.,	I	
Maximum additional_input length (max_additional_input_length)			$\leq 2^{35}$ bits			
max_number_of_bits_per_request	$\leq 2^{19}$ bits					
Number of requests between reseeds (reseed_interval)			≤ 2 ⁴⁸			

Note that since SHA-224 is based on SHA-256, there is no efficiency benefit for using the SHA-224; this is also the case for SHA-384 and SHA-512, i.e., the use of SHA-256 or SHA-512 instead of SHA-224 or SHA-384, respectively, is preferred. The value for *seedlen* is determined by subtracting the count field (in the hash fu ction specification) and one byte of padding from the hash function input block length; in the case of SHA-1, SHA-224 and SHA 256, seedlen = 512 - 64 - 8 = 440; for SHA-384 and SHA-512, seedlen = 1024 - 128 - 8 = 888.

10.1.1 Hash_DRBG

Figure 8 presents the normal operation of the Hash_DRBG. The Hash_DRBG requires the use of a hash function during the instantiate, reseed and generate functions; the same hash function shall be used in all functions. The hash function to be used shall meet or exceed the desired security strength of the consuming application.

Implementation validation testing and health testing are discussed in Sections 9.6 and 11.

10.1.1.1 Hash_DRBG Internal State

The internal_state for Hash_DRBG consists of:

- 1. The working_state:
 - a. A value (V) of seedlen bits that is updated during each call to the DRBG.
 - b. A constant C of seedlen bits that depends on the seed.
 - c. The *previous_output_block*; this will be used to perform a continuous test on the output from the generate function.
 - d. A counter (*reseed_counter*) that indicates the number of requests for pseudorandom bits since new *entropy_input* was obtained during instantiation or reseeding.
- 2. Administrative information:

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- a. The *security_strength* of the DRBG instantiation.
- b. A prediction_resistance_flag
 that indicates whether or not a
 prediction resistance
 capability is required for the
 DRBG.

The values of V and C are the critical values of the internal state upon which the security of this DRBG depends (i.e., V and C are the "secret values" of the internal state).

10.1.1.2 Instantiation of Hash_DRBG

Notes for the instantiate function:

The instantiation of **Hash_DRBG** requires a call to the instantiate function specified in Section 9.1; step 9 of that function calls the instantiate algorithm in this section. For this DRBG, step 5 **should** be omitted.

The values of

highest_supported_security_strength and min_length are provided in Table 2 of Section 10.1. The contents of the internal state are provided in Section 10.1.1.1.

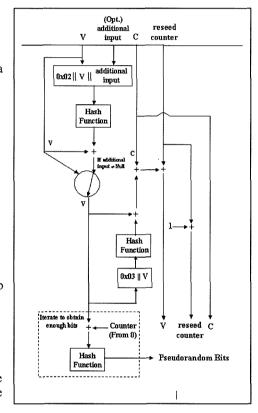


Figure 8: Hash_DRBG

The instantiate algorithm:

Let **Hash_df** be the hash derivation function specified in Section 9.5.1 using the selected hash function. The output block length (*outlen*), seed length (*seedlen*) and appropriate *security_strengths* for the implemented hash function are provided in Table 2 of Section 10.1.

The following process or its equivalent **shall** be used as the instantiate algorithm for this DRBG (see step 9 in Section 9.1).

Input:

- 1. entropy_input: The string of bits obtained from the entropy input source.
- 2. nonce: A string of bits as specified in Section 8.6.7.
- 3. personalization_string: The personalization string received from the consuming

application. If a *personalization_string* will never be used, then steps 1 and 2 may be combined as follows:

seed = Hash_df (entropy_input, seedlen).

Output:

1. working_state: The inital values for V, C, previous_output_block and reseed_counter (see Section 10.1.1.1).

Process:

- 1. seed_material = entropy_input || nonce || personalization_string.
- 2. seed = **Hash_df** (seed_material, seedlen).
- 3. V = seed.
- 4. $C = \mathbf{Hash_df} ((0x00 \parallel V), seedlen)$. Comment: Preced V with a byte of zeros.
- 5. reseed_counter = 1.

Comment: Generate the initial block for comparing with the first DRBG output block (for continuous testing).

- 6. $previous_output_block = Hash(V)$.
- 7. H =**Hash** (0x03 || V).
- 8. $V = (V + H + C + reseed_counter) \mod 2^{seedlen}$
- 9. $reseed_counter = 2$.
- 10. **Return** V, C, $previous_output_block$ and $reseed_counter$ as the $working_state$.

10.1.1.3 Reseeding a Hash_DRBG Instantiation

Notes for the reseed function:

The reseeding of a **Hash_DRBG** instantiation requires a call to the reseed function specified in Section 9.2; step 5 of that function calls the reseed algorithm specified in this section. The values for *min_length* are provided in Table 2 of Section 10.1.

The reseed algorithm:

Let **Hash_df** be the hash derivation function specified in Section 9.5.1 using the selected hash function. The value for *seedlen* is provided in Table 2 of Section 10.1.

The following process or its equivalent **shall** be used as the reseed algorithm for this DRBG (see step 5 in Section 9.2):

Input:

1. working_state: The current values for V, C, previous_output_block and

reseed_counter (see Section 10.1.1.1).

- 2. entropy_input: The string of bits obtained from the entropy input source.
- 3. *additional_input*: The additional input string received from the consuming application. If *additional_input* will never be provided, then step 1 may be modified to remove the *additional_input*.

Output:

 working_state: The new values for V, C, previous_output_block and reseed counter

Process:

- 1. $seed_material = 0x01 \parallel V \parallel entropy_input \parallel additional_input$.
- 2. $seed = Hash_df (seed_material, seedlen)$.
- 3. V = seed.
- 4. $C = \mathbf{Hash_df} ((0x00 \parallel V), seedlen)$. Comment: Preced with a byte of all zeros.
- 5. $reseed_counter = 1$.
- 6. Return *V*, *C*, *previous_output_block* and *reseed_counter* for the new *working_state*.

10.1.1.4 Generating Pseudorandom Bits Using Hash_DRBG

Notes for the generate function:

The generation of pseudorandom bits using a **Hash_DRBG** instantiation requires a call to the generate function specified in Section 9.3; step 8 of that function calls the generate algorithm specified in this section. The values for <code>max_number_of_bits_per_request</code> and <code>outlen</code> are provided in Table 2 of Section 10.1.

The generate algorithm:

Let **Hash** be the selected hash function. The seed length (*seedlen*) and the maximum interval between reseeding (*reseed_interval*) are provided in Table 2 of Section 10.1. Note that for this DRBG, the reseed counter is used to update the value of *V* as well as to count the number of generation requests.

The following process or its equivalent **shall** be used as the generate algorithm for this DRBG (see step 8 of Section 9.3):

Input:

- 1. working_state: The current values for *V*, *C*, previous_output_block and reseed_counter (see Section 10.1.1.1).
- 2. requested_number_of_bits: The number of pseudorandom bits to be returned to

the generate function.

3. *additional_input*: The additional input string received from the consuming application. If *additional_input* will never be provided, then step 3 may be omitted.

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Output:

- 1. *status*: The status returned from the function. The *status* will indicate **SUCCESS**, **ERROR**, or indicate that a reseed is required before the requested pseudorandom bits can be generated.
- 2. returned_bits: The pseudorandom bits to be returned to the generate function.
- 3. *working_state*: The new values for *V*, *C*, *previous_output_block* and *reseed_counter*.

Process:

- 1. If reseed_counter > reseed_interval, then return an indication that a reseed is required.
- 2. If $(additional_input \neq Null)$, then do
 - 3.1 w =**Hash** $(0x02 \parallel V \parallel additional_input).$
 - $3.2 V = (V + w) \mod 2^{seedlen}.$
- 4. (status, returned_bits, previous_output_block) = **Hashgen** (requested_number_of_bits, V, previous_output_block).
- 5. If an ERROR is returned in step 4, then return ERROR.
- 6. $H = \text{Hash } (0x03 \parallel V)$.
- 7. $V = (V + H + C + reseed_counter) \mod 2^{seedlen}$
- 8. $reseed_counter = reseed_counter + 1$.
- 9. Return SUCCESS, returned_bits, and the new values of V, C, previous_output_block and reseed_counter for the new working_state.

Hashgen (...):

Input:

- 1. requested_no_of_bits: The number of bits to be returned.
- 2. V: The current value of V.
- 3. *previous_output_block*: The last output block from the previous generate request.

Output:

1. status: The status returned from this routine. The status will indicate

SUCCESS or an ERROR.

- 2. returned_bits: The generated bits to be returned to the generate function.
- 3. previous_output_block: The last output block generated using this routine.

Process:

1.
$$m = \left\lceil \frac{requested_no_of_bits}{outlen} \right\rceil$$
.

- 2. data = V.
- 3. W =the Nullstring.
- 4. For i = 1 to m

$$4.1 w_i = \text{Hash} (data).$$

- 4.2 If $(w_i = previous_output_block)$, then return an **ERROR**.
- $4.3 \ previous_output_block = w_i$.
- $4.4 W = W || w_i$
- $4.5 data = (data + 1) \mod 2^{seedlen}.$
- 5. returned_bits = Leftmost (requested_no_of_bits) bits of W.
- 6. Return SUCCESS, returned_bits, previous_output_block.

10.1.2 HMAC_DRBG (...)

HMAC_DRBG uses multiple occurrences of an Approved keyed hash function, which is based on an Approved hash function. The same hash function **shall** be used throughout. The hash function used **shall** meet or exceed the security requirements of the consuming application.

Figure 9 depicts the **HMAC_DRBG** in stages. **HMAC_DRBG** is specified using an internal function (**Update**). This function is called during the **HMAC_DRBG** instantiate,

generate and reseed algorithms to adjust the internal state when new entropy or additional input is provided. The operations in the top portion of the figure are only performed if the additional input is not null. Figure 10 depicts the **Update** function.

10.1.2.1 HMAC_DRBG Internal State

The internal state for **HMAC_DRBG** consists of:

- 1. The working_state:
 - a. The value *V* of *outlen* bits, which is updated each time another *outlen* bits of output are produced (where *outlen* is specified in Table 2 of Section 10.1).
 - b. The *Key* of *outlen* bits, which is updated at least once each time that the DRBG generates pseudorandom bits.
 - c. A counter (reseed_counter) that indicates the number of requests for pseudorandom bits since instantiation or reseeding.
- 2. Administrative information:
 - a. The *security_strength* of the DRBG instantiation.
 - b. A *prediction_resistance_flag* that indicates whether or not a

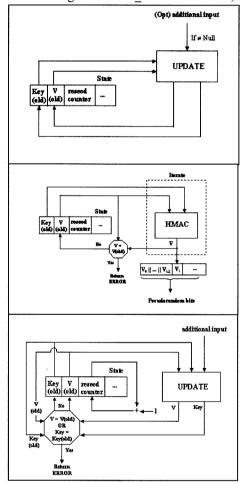


Figure 9: HMAC_DRBG Generate Function

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prediction resistance capability is required for the DRBG.

The values of V and Key are the critical values of the internal state upon which the security of this DRBG depends (i.e., V and Key are the "secret values" of the internal state).

10.1.2.2 The Update Function (Update)

The **Update** function updates the internal state of **HMAC_DRBG** using the *provided_data*. Note that for this DRBG, the **Update** function also serves as a derivation function for the instantiate and reseed functions.

Let **HMAC** be the keyed hash function specified in FIPS 198 using the hash function selected for the DRBG from Table 2 in Section 10.1.

The following or an equivalent process shall be used as the Update function.

Input:

- 1. provided_data: The data to be
- 2. K: The current value of Key.
- 3. V: The current value of V.

Output:

- 1. K: The new value for Key.
- 2. V: The new value for V.

Process:

- 1. $K = \mathbf{HMAC}(K, V \parallel 0 \times 00 \parallel provided_data)$.
- 2. $V = \mathbf{HMAC}(K, V)$.
- 3. If $(provided_data = Null)$, then return K and V.
- 4. $K = HMAC(K, V || 0x01 || provided_data).$
- 5. V = HMAC(K, V).
- 6. Return K and V.

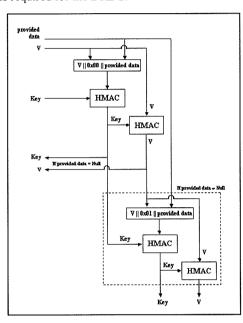


Figure 10: HMAC_DRBG Update Function

10.1.2.3 Instantiation of HMAC_DRBG

Notes for the instantiate function:

The instantiation of **HMAC_DRBG** requires a call to the instantiate function specified in Section 9.2; step 9 of that function calls the instantiate algorithm specified in this section. For this DRBG, step 5 **should** be omitted. The values of *highest_supported_security_strength* and *min_length* are provided in Table 2 of Section 10.1. The contents of the internal state are provided in Section 10.1.2.1.

The instantiate algorithm:

Let **Update** be the function specified in Section 10.1.2.2. The ouput block length (*outlen*) is provided in Table 2 of Section 10.1.

The following process or its equivalent shall be used as the instantiate algorithm for this DRBG (see step 8 of Section 9.1):

Input:

- 1. entropy_input: The string of bits obtained from the entropy input source.
- 2. nonce: A string of bits as specified in Section 8.6.7.
- 3. *personalization_string*: The personalization string received from the consuming application. If a *personalization_string* will never be used, then step 1 may be modified to remove the *personalization_string*.

Output:

1. *working_state*: The inital values for *V*, *Key* and *reseed_counter* (see Section 10.1.2.1).

Process:

- 1. seed_material = entropy_input || nonce || personalization_string.
- 2. $Key = 0x00\ 00...00$.

Comment: outlen bits.

3. $V = 0x01 \ 01...01$.

Comment: outlen bits.

Comment: Update Key and V.

4. $(Key, V) = Update (seed_material, Key, V)$.

Comment: Generate the initial block for comparing with the first DRBG output block (for continuous testing).

- 5. $V = \mathbf{HMAC} (Key, V)$.
- 6. $(Key, V) = Update (seed_material, Key, V)$
- 7. $reseed_counter = 1$.

8. Return *V*, *Key* and *reseed_counter* as the initial *working_state*.

10.1.2.4 Reseeding an HMAC_DRBG Instantiation

Notes for the reseed function:

The reseeding of an **HMAC_DRBG** instantiation requires a call to the reseed function specified in Section 9.2; step 5 of that function calls the reseed algorithm specified in this section. The values for *min_length* are provided in Table 2 of Section 10.1.

The reseed algorithm:

Let **Update** be the function specified in Section 10.1.2.2. The following process or its equivalent **shall** be used as the reseed algorithmn for this DRBG (see step 5 of Section 9.2):

Input:

- 1. working_state: The current values for *V*, *Key* and *reseed_counter* (see Section 10.1.2.1).
- 2. entropy_input: The string of bits obtained from the entropy input source.
- 3. *additional_input*: The additional input string received from the consuming application. If *additional_input* will never be used, then step 1 may be modified to remove the *additional_input*.

Output:

1. working_state: The new values for V, Key and reseed_counter.

Process:

- $1. \ \ \textit{seed_material} = \textit{entropy_input} \parallel \textit{additional_input}.$
- 2. $(Key, V) = Update (seed_material, Key, V)$.
- 3. $reseed_counter = 1$.
- 4. **Return** *V*, *Key* and *reseed_counter* as the new *working_state*.

10.1.2.5 Generating Pseudorandom Bits Using HMAC_DRBG

Notes for the generate function:

The generation of pseudorandom bits using an **HMAC_DRBG** instantiation requires a call to the generate function specified in Section 9.3; step 8 of that function calls the generate algorithm specified in this section. The values for <code>max_number_of_bits_per_request</code> and <code>outlen</code> are provided in Table 2 of Section 10.1.

The generate algorithm:

Let **HMAC** be the keyed hash function specified in FIPS 198 using the hash function selected for the DRBG. The value for *reseed_interval* is defined in Table 2 of Section

10.1.

The following process or its equivalent **shall** be used as the generate algorithm for this DRBG (see step 8 of Section 9.3):

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Input:

- 1. *working_state*: The current values for *V*, *Key* and *reseed_counter* (see Section 10.1.2.1).
- 2. requested_number_of_bits: The number of pseudorandom bits to be returned to the generate function.
- 3. additional_input: The additional input string received from the consuming application. If an implementation will never use additional_input, then step 3 may be omitted. If an implementation does not include the additional_input parameter as one of the calling parameters, or if the implementation allows additional_input, but a given request does not provide any additional_input, then a Null string shall be used as the additional_input in step 7.

Output:

- 1. *status*: The status returned from the function. The *status* will indicate **SUCCESS**, an **ERROR** or indicate that a reseed is required before the requested pseudorandom bits can be generated.
- 2. returned bits: The pseudorandom bits to be returned to the generate function.
- 3. working_state: The new values for V, Key and reseed counter.

Process:

- 1. If $reseed_counter > reseed_interval$, then return an indication that a reseed is required.
- 2. $V_old = V$.
- 3. If $additional_input \neq Null$, then $(Key, V) = \mathbf{Update}$ ($additional_input$, Key, V).
- 4. temp = Null.
- 5. While (len (temp) < requested_number_of_bits) do:
 - 5.1 $V = \mathbf{HMAC} (Key, V)$.

Comment: Continuous test – check that successive values of V are not identical.

- 5.2 If $(V = V_old)$, then return an **ERROR**.
- 5.3 $V_old = V$.
- 5.4 $temp = temp \parallel V$.
- 6. returned_bits = Leftmost requested_number_of_bits of temp.

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- 7. $(Key, V) = \mathbf{Update} (additional_input, Key, V).$
- 8. $reseed_counter = reseed_counter + 1$.
- 9. Return SUCCESS, $returned_bits$, and the new values of Key, V and $reseed_counter$ as the $working_state$).

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10.2 DRBGs Based on Block Ciphers

A block cipher DRBG is based on a block cipher algorithm. The block cipher DRBG specified in this Recommendation has been designed to use any Approved block cipher algorithm and may be used by applications requiring various levels of security, providing that the appropriate block cipher algorithm and key length are used, and sufficient entropy is obtained for the seed.

10.2.1 CTR_DRBG

CTR_DRBG uses an Approved block cipher algorithm in the counter mode as specified in SP 800-38A. The same block cipher algorithm and key length shall be used for all block cipher operations. The block cipher algorithm and key length shall meet or exceed the security requirements of the consuming application.

CTR_DRBG is specified using an internal function (Update). Figure 11 depicts the Update function. This function is called by the instantiate, generate and reseed algorithms to adjust the internal state when new entropy or additional input is provided. Figure 12 depicts the CTR_DRBG in three stages. The operations in the top portion of the figure are only performed if the additional input is not null.

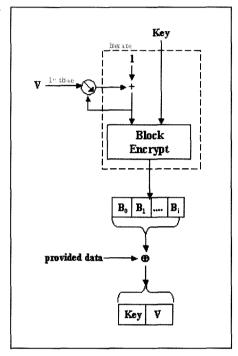


Figure 11: CTR_DRBG Update Function

Table 3 specifies the values that **shall** be used for the function envelopes and DRBG algorithms.

Table 3: Definitions for the CTR_DRBG

	3 Key TDEA	AES-128	AES-192	AES-256	
Supported security strengths	See SP 800-57				
highest_supported_security_strength	See SP 800-57				
Output block length (outlen)	64	128	128	128	
Key length (keylen)	168	128	192	256	
Required minimum entropy for instantiate and reseed	security_strength				

	3 Key TDEA	AES-128	AES-192	AES-256	
Seed length ($seedlen = outlen + keylen$)	232	256	320	384	
A derivation function is used:					
Minimum entropy input length (min _length)	security_strength				
Maximum entropy input length (max_length)	$\leq 2^{35}$ bits				
Maximum personalization string length (max_personalization_string_length)	$\leq 2^{35}$ bits				
Maximum additional_input length (max_additional_input_length)	$\leq 2^{35}$ bits				
A derivation function is not used (full entropy is available):					
Minimum entropy input length (min _length) (outlen + keylen)	seedlen				
Maximum entropy input length (max_length) (outlen + keylen)	seedlen				
Maximum personalization string length (max_personalization_string_length)	seedlen				
Maximum additional_input length (max_additional_input_length)	seedlen				
max_number_of_bits_per_request	$\leq 2^{13}$ $\leq 2^{19}$				
Number of requests between reseeds (reseed_interval)	≤ 2 ³²		≤ 2 ⁴⁸		

The CTR_DRBG may be implemented to use the block cipher derivation function specified in Section 9.5.2. However, the DRBG is specified to allow an implementation tradeoff with respect to the use of this derivation function. If a source for full entropy input is always available to provide entropy input when requested, the use of the derivation function is optional; otherwise, the derivation function shall be used. Table 3 provides lengths required for the <code>entropy_input</code>, <code>personalization_string</code> and <code>additional_input</code> for each case.

When full entropy is available, and a derivation function is not used by an implementation, the seed construction (see Section 8.6.1) **shall not** use a nonce⁴.

When using TDEA as the selected block cipher algorithm, the keys **shall** be handled as 64-bit blocks containing 56 bits of key and 8 bits of parity as specified for the TDEA engine specified in SP 800-67.

10.2.1.1 CTR_DRBG Internal State

The internal state for CTR_DRBG consists of:

- 1. The working_state:
 - a. The value V of outlen bits, which is updated each time another outlen bits of output are produced (see Table 3 in Section 10.2.1).
 - b. The Key of keylen bits, which is updated whenever a predetermined number of output blocks are generated.
 - c. The previous_output_block;
 this is required to perform a continuous test on the output from the generate function.
 - d. A counter
 (reseed_counter) that
 indicates the number of
 requests for

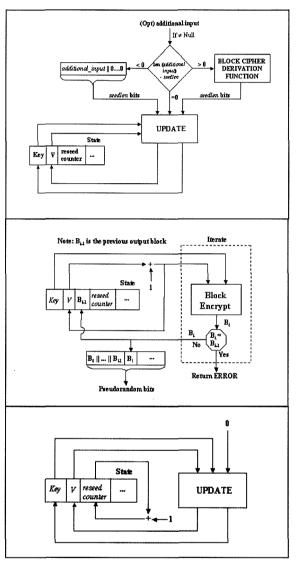


Figure 12: CTR-DRBG

⁴ The specifications in this Standard do not accommodate the special treatment required for a nonce in this case.

pseudorandom bits since instantiation or reseeding.

- 2. Administrative information:
 - a. The security_strength of the DRBG instantiation.
 - b. A *prediction_resistance_flag* that indicates whether or not a prediction resistance capability is required for the DRBG.

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The values of V and Key are the critical values of the internal state upon which the security of this DRBG depends (i.e., V and Key are the "secret values" of the internal state).

10.2.1.2 The Update Function (Update)

The **Update** function updates the internal state of the **CTR_DRBG** using the *provided_data*. The values for *outlen*, *keylen* and *seedlen* are provided in Table 3 of Section 10.2.1. The block cipher operation in step 2.2 uses the selected block cipher algorithm (also see Section 9).

The following or an equivalent process shall be used as the Update function.

Input:

- 1. provided_data: The data to be used. This must be exactly seedlen bits in length; this length is guaranteed by the construction of the provided_data in the instantiate, reseed and generate functions.
- 2. Key: The current value of Key.
- 3. V: The current value of V.

Output:

- 1. K: The new value for Key.
- 2. V: The new value for V.

Process:

- 1. temp = Null.
- 2. While (len (temp) < seedlen) do
 - 2.1 $V = (V+1) \mod 2^{outlen}$.
 - 2.2 output_block = Block_Encrypt (Key, V).
 - 2.3 $temp = temp || ouput_block.$
- 3. temp = Leftmost seedlen bits of temp.
- 4 $temp = temp \oplus provided_data$.
- 5. Key = Leftmost keylen bits of temp.

- 6. V =Rightmost *outlen* bits of *temp*.
- 7. Return the new values of Key and V.

10.2.1.3 Instantiation of CTR_DRBG

Notes for the instantiate function:

The instantiation of CTR_DRBG requires a call to the instantiate function specified in Section 9.1; step 9 of that function calls the instantiate algorithm specified in this section. For this DRBG, step 5 should be omitted. The values of highest_supported_security_strength and min_length are provided in Table 3 of Section 10.2.1. The contents of the internal state are provided in Section 10.2.1.1.

The instantiate algorithm:

Let **Update** be the function specified in Section 10.2.1.2, and let **Block_Cipher_df** be the derivation function specified in Section 9.5.2 using the chosen block cipher algorithm and key size. The output block length (*outlen*), key length (*keylen*), seed length (*seedlen*) and *security_strengths* for the block cipher algorithms are provided in Table 3 of Section 10.2.1.

The following process or its equivalent **shall** be used as the instantiate algorithm for this DRBG:

Input:

- 1. entropy_input: The string of bits obtained from the entropy input source.
- 2. *nonce*: A string of bits as specified in Section 8.6.7; this string **shall not** be present when a derivation function is not used.
- 3. *personalization_string*: The personalization string received from the consuming application.

Output:

1. working_state: The inital values for V, Key, previous_output_block and reseed_counter (see Section 10.2.1.1).

Process:

- 1. If the block cipher derivation function is available, then
 - 1.1 seed_material = entropy_input || nonce || personalization_string.
 - 1.2 seed_material = Block_Cipher_df (seed_material, seedlen).

Else

Comment: The block cipher derivation function is not used and full entropy is known to be available.

1.3 temp = len (personalization_string).

- 1.4 If (temp < seedlen), then personalization_string = personalization_string $\parallel 0^{seedlen-temp}$.
- 1.5 seed_material = entropy_input ⊕ personalization_string.
- 2. $Key = 0^{keylen}$.

Comment: keylen bits of zeros.

3. $V = 0^{outlen}$.

Comment: outlen bits of zeros.

- 4. $(Key, V) = Update (seed_material, Key, V)$.
- 5. $reseed\ counter = 1$.

Comment: Generate the initial block for comparing with the first DRBG output block (for continuous testing).

- 6. previous_output block = Block_Encrypt (Key, V).
- 7. $zeros = 0^{seedlen}$.

Comment: Produce a string of seedlen zeros.

- 8. (Key, V) = Update (zeros, Key, V).
- Return V, Key, previous_output_block and reseed_counter as the working_state.

Implementation notes:

1. If a *personalization_string* will never be provided from the instantiate function and a derivation function will be used, then step 1.1 becomes:

seed_material = Block_Cipher_df (entropy_input, seedlen).

2. If a personalization_string will never be provided from the instantiate function, a full entropy source will be available and a derivation function will not be used, then step 1 becomes

seed_material = entropy_input.

That is, steps 1.3 - 1.6 collapse into the above step.

10.2.1.4 Reseeding a CTR_DRBG Instantiation

Notes for the reseed function:

The reseeding of a CTR_DRBG instantiation requires a call to the reseed function specified in Section 9.2; step 5 of that function calls the reseed algorithm specified in this section. The values for *min_length* are provided in Table 3 of Section 10.2.1.

The reseed algorithm:

Let **Update** be the function specified in Section 10.2.1.2, and let **Block_Cipher_df** be the derivation function specified in Section 9.5.2 using the chosen block cipher algorithm and key size. The seed length (*seedlen*) is provided in Table 3 of Section

10.2.1.

If a block cipher derivation function is to be used, then the **Block_Cipher_df** specified in Section 9.5.2 **shall** be implemented using the chosen block cipher algorithm and key size; in this case, step 1 below **shall** consist of steps 1.1 and 1.2 (i.e., steps 1.3 to 1.5 **shall not** be used).

DRAFT

If full entropy is available whenever entropy input is required, and a block cipher derivation function is not to be used, then step 1 below **shall** consist of steps 1.3 to 1.5 (i.e., steps 1.1 and 1.2 **shall not** be used).

The following process or its equivalent shall be used as the reseed algorithm for this DRBG (see step 5 of Section 9.2):

Input:

- 1. working_state: The current values for *V*, *Key* and *reseed_counter* (see Section 10.2.1.1).
- 2. entropy_input: The string of bits obtained from the entropy input source.
- 3. *additional_input*: The additional input string received from the consuming application.

Output:

1. working_state: The new values for V, Key, previous_output_block and reseed_counter.

Process:

- 1. If the block cipher derivation function is available, then
 - 1.1 seed_material = entropy_input || additional_input.
 - 1.2 seed_material = Block_Cipher_df (seed_material, seedlen).

Else

Comment: The block cipher derivation function is not used because full entropy is known to be available.

- 1.3 temp = len (additional_input).
- 1.4 If (temp < seedlen), then $additional_input = additional_input || <math>0^{seedlen-temp}$.
- $1.5 \quad seed_material = entropy_input \oplus additional_input.$
- 2. $(Key, V) = Update (seed_material, Key, V)$.
- 3. $reseed_counter = 1$.
- 4. Return V, Key, previous_output_block and reseed_counter as the

working_state.

Implementation notes:

1. If additional_input will never be provided from the reseed function and a derivation function will be used, then step 1.1 becomes:

seed_material = Block_Cipher_df (entropy_input, seedlen).

2. If additional_input will never be provided from the reseed function, a full entropy source will be available and a derivation function will not be used, then step 1 becomes

 $seed_material = entropy_input.$

That is, steps 1.3 - 1.6 collapse into the above step.

10.2.1.5 Generating Pseudorandom Bits Using CTR_DRBG

Notes for the generate function:

The generation of pseudorandom bits using a CTR_DRBG instantiation requires a call to the generate function specified in Section 9.3, step 8 of that function calls the generate algorithm specified in this section. The values for <code>max_number_of_bits_per_request</code> and <code>outlen</code> are provided in Table 3 of Section 10.2.1. If the derivation function is not used, then the maximum allowed length of <code>additional_input = seedlen</code>.

Let **Update** be the function specified in Section 10.2.1.2. The seed length (*seedlen*) and the value of *reseed_interval* are provided in Table 3 of Section 10.2.1. Step 5.2 below uses the selected block cipher algorithm. If a derivation function is not used for a DRBG implementation, then step 3.2 **shall** be omitted.

If a block cipher derivation function is to be used, then the **Block_Cipher_df** specified in Section 9.5.2 **shall** be implemented using the chosen block cipher algorithm and key size; in this case, step 3.2 below **shall** be included.

If full entropy is available whenever entropy input is required, and a block cipher derivation function is not to be used, then step 3.2 below **shall not** be used.

The following process or its equivalent shall be used as generate algorithm for this DRBG (see step 8 of Section 9.3):

Input:

- 1. working_state: The current values for V, Key, previous_output_block and reseed_counter (see Section 10.2.1.1).
- 2. requested_number_of_bits: The number of pseudorandom bits to be returned to the generate function.
- 3. additional_input: The additional input string received from the consuming application. If additional_input will never be provided, then step 3 may be

omitted.

Output:

- 1. *status*: The status returned from the function. The *status* will indicate **SUCCESS**, an **ERROR** or indicate that a reseed is required before the requested pseudorandom bits can be generated.
- 2. returned_bits: The pseudorandom bits returned to the generate function.
- 3. working_state: The new values for V, Key, previous_output_block and reseed_counter.

Process:

- If reseed_counter > reseed_interval, then return an indication that a reseed is required.
- 2. $V_old = V$.
- 3. If (additional_input \neq Null), then

Comment: If the length of the *additional* input is > seedlen, derive seedlen bits.

3.1 $temp = len (additional_input)$.

Comment: If a block cipher derivation function is used:

3.2 If (temp > seedlen), then additional_input = Block_Cipher_df (additional_input, seedlen).

Comment: If the length of the additional_input is < seedlen, pad with zeros to seedlen bits.

- 3.3 If (temp < seedlen), then $additional_input = additional_input || 0^{seedlen}$.
- 3.4 $(Key, V) = \mathbf{Update} (additional_input, Key, V).$
- 4. temp = Null.
- 5. While (len (temp) < requested_number_of_bits) do:
 - 5.1 $V = (V+1) \mod 2^{outlen}$.
 - 5.2 output_block = Block_Encrypt (Key, V).

Comment: Continuous test – Check that the old and new output blocks are different.

5.3 If (output_block = previous_output_block), then return an ERROR.

- 5.4 previous_output_block = output_block.
- 5.5 $temp = temp || ouput_block.$
- 6. returned_bits = Leftmost requested_number_of_bits of temp.

Comment: Update for backtracking resistance.

7. $zeros = 0^{seedlen}$.

Comment: Produce a string of seedlen zeros.

- 8. (Key, V) = Update(zeros, Key, V).
- 9. reseed_counter = reseed_counter + 1.
- 10 Return SUCCESS and returned_bits; also return Key, V, previous_output_block and reseed_counter as the new working_state.

10.3 Deterministic RBGs Based on Number Theoretic Problems

A DRBG can be designed to take advantage of number theoretic problems (e.g., the discrete logarithm problem). If done correctly, such a generator's properties of randomness and/or unpredictability will be assured by the difficulty of finding a solution to that problem. This section specifies a DRBG based on the elliptic curve discrete logarithm problem.

10.3.1 Dual Elliptic Curve Deterministic RBG (Dual_EC_DRBG)

Dual_EC_DRBG is based on the following hard problem, sometimes known as the "elliptic curve discrete logarithm problem" (ECDLP): given points P and Q on an elliptic curve of order n, find a such that Q = aP.

Dual_EC_DRBG uses a seed that is m bits in length (i.e., seedlen = m) to initiate the generation of *outlen*-bit pseudorandom strings by performing scalar multiplications on two points in an elliptic curve group, where the curve is defined over a field approximately 2^m in size. For all the NIST curves given in this Standard, $m \ge 163$. Figure 13 depicts the **Dual_EC_DRBG**.

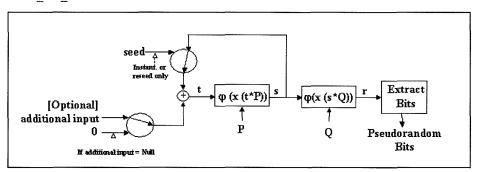


Figure 13: Dual EC DRBG

The instantiation of this DRBG requires the selection of an appropriate elliptic curve and curve points specified in Annex A.1 for the desired security strength. The *seed* used to determine the initial value (s) of the DRBG **shall** have entropy that is at least *security_strength* + 64 bits. Further requirements for the *seed* are provided in Section 8.6.

Backtracking resistance is inherent in the algorithm, even if the internal state is compromised. As shown in Figure 14,

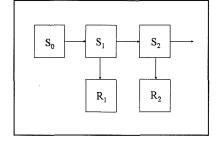


Figure 14: Dual_EC_DRBG (...)
Backtracking Resistance

Dual_EC_DRBG generates a *seedlen*-bit number for each step i = 1, 2, 3, ..., as follows:

$$S_i = \varphi(x(S_{i-1} * P))$$

$$R_i = \varphi(x(S_i * Q)).$$

Each arrow in the figure represents an Elliptic Curve scalar multiplication operation, followed by the extraction of the x coordinate for the resulting point and for the random output R_{i_1} and by truncation to produce the output. Following a line in the direction of the arrow is the normal operation; inverting the direction implies the ability to solve the ECDLP for that specific curve. An adversary's ability to invert an arrow in the figure implies that the adversary has solved the ECDLP for that specific elliptic curve. Backtracking resistence is built into the design, as knowledge of S_1 does not allow an adversary to determine S_0 (and so forth) unless the adversary is able to solve the ECDLP for that specific curve. In addition, knowledge of R_1 does not allow an adversary to determine S_1 (and so forth) unless the adversary is able to solve the ECDLP for that specific curve.

Table 4 specifies the values that **shall** be used for the envelope and algorithm for each curve. Complete specifications for each curve are provided in Annex A.1. Note that all curves except the P-224 curve can be instantiated at a security strength lower than its highest possible security strength. For example, the highest security strength that can be supported by curve P-384 is 192 bits; however, this curve can alternatively be instantiated to support only the 112 or 128-bit security strengths).

Table 4: Definitions for the Dual_EC_DRBG

	P-224	P-256	P-384	P-521
Supported security strengths	See SP 800-57			
highest_supported_ security_strength	See SP 800-57			
Output block length (max_outlen = largest multiple of 8 less than seedlen - (13 + log ₂ (the cofactor))	208	240	368	504
Required minimum entropy for instantiate and reseed	security_strength			
Minimum entropy input length $(min_length = 8 \times \lceil seedlen/8 \rceil)$	224	256	384	528
Maximum entropy input length (max_length)	$\leq 2^{13}$ bits			
Maximum personalization string length (max_personalization_string_length)	$\leq 2^{13}$ bits			
Supported security strengths	See SP 800-57			

	P-224	P-256	P-384	P-521
Seed length (seedlen = m)	224	256	384	521
Appropriate hash functions	SHA-1, SHA-224 SHA-384, SI	,	SHA-224, SHA-256, SHA-384, SHA-512	SHA-256, SHA-384, SHA-512
max_number_of_bits_per_request	max_outlen × reseed_interval			
Number of blocks between reseeding (reseed_interval)	≤ 2 ³² blocks			

Validation and Operational testing are discussed in Section 11. Detected errors **shall** result in a transition to the error state.

10.3.1.1 Dual_EC_DRBG Internal State

The internal state for Dual EC DRBG consists of:

- 1. The working state:
 - a. A value (s) that determines the current position on the curve.
 - b. The elliptic curve domain parameters (seedlen, p, a, b, n), where seedlen is the length of the seed; a and b are two field elements that define the equation of the curve, and n is the order of the point G. If only one curve will be used by an implementation, these parameters need not be present in the working state.
 - c. Two points *P* and *Q* on the curve; the generating point *G* specified in FIPS 186-3 for the chosen curve will be used as *P*. If only one curve will be used by an implementation, these points need not be present in the *working_state*.
 - d. r old, the previous output block.
 - e. A counter (*block_counter*) that indicates the number of blocks of random produced by the **Dual_EC_DRBG** since the initial seeding or the previous reseeding.
- 2. Administrative information:
 - a. The security strength provided by the instance of the DRBG,
 - b. A *prediction_resistance_flag* that indicates whether prediction resistance is required by the DRBG.

The value of s is the critical value of the internal state upon which the security of this DRBG depends (i.e., s is the "secret value" of the internal state).

10.3.1.2 Instantiation of Dual_EC_DRBG

Notes for the instantiate function:

The instantiation of **Dual_EC_DRBG** requires a call to the instantiate function specified in Section 9.1; step 9 of that function calls the instantiate algorithm in this section.

In step 5 of the instantiate function, the following step **shall** be performed to select an appropriate curve if multiple curves are available.

5. Using the *security_strength* and Table 4 in Section 10.3.1, select the smallest available curve that has a security strength ≥ *security strength*.

The values for seedlen, p, a, b, n, P, Q are determined by that curve.

It is recommended that the default values be used for P and Q as given in Annex A.1. However, an implementation **may** use different pairs of points, provided that they are *verifiably random*, as evidenced by the use of the procedure specified in Annex A.2.1 and the self-test procedure described in Annex A.2.2.

The values for *highest_supported_security_strength* and *min_length* are determined by the selected curve (see Table 4 in Section 10.3.1).

The instantiate algorithm:

Let **Hash_df** be the hash derivation function specified in Section 9.5.1 using an appropriate hash function from Table 4 in Section 10.3.1. Let *seedlen* be the appropriate value from Table 4.

The following process or its equivalent **shall** be used as the instantiate algorithm for this DRBG (see step 9 of Section 9.1):

Input:

- 1. entropy input: The string of bits obtained from the entropy input source.
- 2. nonce: A string of bits as specified in Section 8.6.7.
- personalization_string: The personalization string received from the consuming application.

Output:

- 1. s: The initial secret value for the working_state.
- 2. r_old : The initial output block (which will not be used).
- 3. block_counter: The initialized block counter for reseeding.

Process:

1. seed_material = entropy_input || nonce || personalization_string.

Comment: Use a hash function to ensure that

the entropy is distributed throughout the bits, and s is m (i.e., seedlen) bits in length.

2. $s = Hash_df$ (seed_material, seedlen).

Comment: Generate the initial block for comparing with the 1st DRBG output block (for continuous testing).

- 3. $r \ old = \varphi(x(s * Q))$.
- Comment: r is a seedlen-bit number.
- 4. $block_counter = 0$.
- 5. Return s, r old and block counter for the working state.

10.3.1.3 Reseeding of a Dual_EC_DRBG Instantiation

Notes for the reseed function:

The reseed of **Dual_EC_DRBG** requires a call to the reseed function specified in Section 9.2; step 5 of that function calls the reseed algorithm in this section. The values for *min_length* are provided in Table 4 of Section 10.3. 1.

The reseed algorithm:

Let **Hash_df** be the hash derivation function specified in Section 9.6.2 using an appropriate hash function from Table 4 in Section 10.3. 1.

The following process or its equivalent **shall** be used to reseed the **Dual_EC_DRBG** process after it has been instantiated (see step 4 in Section 9.2):

Input:

- 1. s: The current value of the secret parameter in the working state.
- 2. entropy input: The string of bits obtained from the entropy input source.
- additional input: The additional input string received from the consuming application.

Output:

- 1. s: The new value of the secret parameter in the working state.
- 2. block_counter: The re-initialized block counter for reseeding.

Process:

Comment: **pad8** returns a copy of s padded on the right with binary 0's, if necessary, to a multiple of 8.

- 1. $seed\ material = pad8\ (s)\ \|\ entropy_input\ \|\ additional_input_string.$
- 2. $s = Hash_df$ (seed_material, seedlen).

- 3. $block_counter = 0$.
- 4. Return s and block counter for the new working state.

Implementation notes:

If an implementation never allows *additional_input*, then step 1 may be modified as follows:

seed material = $pad8(s) \parallel entropy input$.

10.3.1.4 Generating Pseudorandom Bits Using Dual_EC_DRBG

Notes for the generate function:

The generation of pseudorandom bits using a **Dual_EC_DRBG** instantiation requires a call to the generate function specified in Section 9.3; step 8 of that function calls the generate algorithm specified in this section. The values for <code>max_number_of_bits_per_request</code> and <code>max_outlen</code> are provided in Table 4 of Section 10.3.1. <code>outlen</code> is the number of pseudorandom bits taken from each x-coordinate as the <code>Dual_EC_DRBG</code> steps. For performance reasons, the value of <code>outlen</code> should be set to the maximum value as provided in Table 4. However, an implementation <code>may</code> set <code>outlen</code> to any multiple of 8 bits less than or equal to <code>max_outlen</code>. The bits that become the <code>Dual_EC_DRBG</code> output are always the rightmost bits, i.e., the least significant bits of the x-coordinates.

The generate algorithm:

Let **Hash_df** be the hash derivation function specified in Section 9.5.1 using an appropriate hash function from Table 4 in Section 10.3.1. The value of *reseed_interval* is also provided in Table 4.

The following are used by the generate algorithm:

- a. **pad8** (bitstring) returns a copy of the *bitstring* padded on the right with binary 0's, if necessary, to a multiple of 8.
- b. **Truncate** (bitstring, in_len, out_len) inputs a bitstring of in_len bits, returning a string consisting of the leftmost out_len bits of bitstring. If in_len < out_len, the bitstring is padded on the right with (out_len in_len) zeroes, and the result is returned.
- c. x(A) is the x-coordinate of the point A on the curve, given in affine coordinates. An implementation may choose to represent points internally using other coordinate systems; for instance, when efficiency is a primary concern. In this case, a point **shall** be translated back to affine coordinates before x() is applied.
- d. $\varphi(x)$ maps field elements to non-negative integers, taking the bit vector representation of a field element and interpreting it as the binary expansion of an integer.

The precise definition of $\varphi(x)$ used in steps 6 and 7 below depends on the field representation of the curve points. In keeping with the convention of FIPS 186-2, the following elements will be associated with each other (note that m = seedlen):

B:
$$|c_{m-1}|c_{m-2}| \dots |c_1|c_0|$$
, a bitstring, with c_{m-1} being leftmost

$$Z: c_{m-1}2^{m-1} + \ldots + c_22^2 + c_12^1 + c_0 \in Z;$$

Fa:
$$c_{m-1}2^{m-1} + \ldots + c_22^2 + c_12^1 + c_0 \mod p \in GF(p)$$
;

Thus, any field element x of the form Fa will be converted to the integer Z or bitstring B, and vice versa, as appropriate.

e. * is the symbol representing scalar multiplication of a point on the curve.

The following process or its equivalent **shall** be used to generate pseudorandom bits (see step 8 in Section 9.3):

Input:

- 1. working_state: The current values for s, seedlen, p, a, b, n, P, Q, r_old and reseed counter (see Section 10.3.1.1).
- 2. requested_number_of_bits: The number of pseudorandom bits to be returned to the generate function.
- 3. *additional_input*: The additional input string received from the consuming application.

Output:

- 1. *status*: The status returned from the function. The *status* will indicate **SUCCESS**, **ERROR** or an indication that a reseed is required before the requested pseudorandom bits can be generated.
- 2. returned bits: The pseudorandom bits to be returned to the generate function.
- 3. s: The new value for the secret parameter in the working state.
- 4. r old: The last output block.
- 5. block_counter: The updated block counter for reseeding.

Process:

Comment: Check whether a reseed is required.

1. If
$$\left(block_counter + \left\lceil \frac{requested_number_of_bits}{outlen} \right\rceil \right) > reseed_interval$$
, then

return an indication that a reseed is required.

Comment: If additional_input is Null, set to

seedlen zeroes; otherwise, **Hash_df** to seedlen bits.

2. If (additional_input_string = Null), then additional_input = 0

Else additional_input = **Hash_df** (pad8 (additional input string), seedlen).

Comment: Produce requested_no_of_bits, outlen bits at a time:

3. temp = the Null string.

4 i = 0.

5. $t = s \oplus additional_input$.

Comment: *t* is to be interpreted as a *seedlen*-bit unsigned integer. To be precise, *t* should be reduced mod *n*; the operation * will effect this.

6. $s = \varphi(x(t * P))$.

Comment: s is a seedlen-bit number.

7. $r = \varphi(x(s * Q))$.

Comment: *r* is a *seedlen*-bit number.

Comment: Continuous test – Compare the old and new output blocks to assure that they are different.

8. If $(r = r \ old)$, then return an **ERROR**.

9. $r_old = r$.

10. $temp = temp \parallel (rightmost outlen bits of r)$.

11. additional input=0

Comment: seedlen zeroes;

additional_input_string is added only on the

first iteration.

12. $block\ counter = block\ counter + 1$.

13. i = i + 1.

14. If (len (temp) < requested_number_of_bits), then go to step 5.

15 $returned_bits = Truncate$ (temp, $i \times outlen$, requested number of bits).

16. Return SUCCESS, returned_bits, and s, r_old and block_counter for the working_state.

11 Assurance

A user of a DRBG for cryptographic purposes requires assurance that the generator

actually produces random and unpredictable bits. The user needs assurance that the design of the generator, its implementation and its use to support cryptographic services are adequate to protect the user's information. In addition, the user requires assurance that the generator continues to operate correctly. The assurance strategy for the DRBGs in this Recommendation is depicted in Figure 15.

The design of each DRBG in this Recommendation has received an evaluation of its security properties prior to its selection for inclusion in this Recommendation.

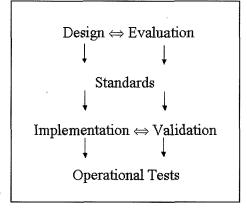


Figure 15: DRBG Assurance Strategy

An implementation **shall** be validated for conformance to this Recommendation by a NVLAP accredited laboratory (see Section 11.2). The consuming application or cryptographic service that uses a DRBG **should** also be validated and periodically tested for continued correct operation. However, this level of testing is outside the scope of this Recommendation. Such validations provide a higher level of assurance that the DRBG is correctly implemented. Validation testing for DRBG processes consists of testing whether or not the DRBG process produces the expected result, given a specific set of input parameters (e.g., entropy input).

Operational (i.e., health) tests on the DRBG **shall** be implemented within a DRBG boundary or sub-boundary in order to determine that the process continues to operate as designed and implemented. See Section 11.3 for further information.

A cryptographic module containing a DRBG **shall** be validated (see FIPS 140-2). The consuming application or cryptographic service that uses a DRBG **should** also be validated and periodically tested for continued correct operation. However, this level of testing is outside the scope of this Recommendation.

Note that any entropy input used for testing (either for validation testing or operational/health testing) may be publicly known. Therefore, entropy input used for testing **shall not** knowingly be used for normal operational use.

11.1 Minimal Documentation Requirements

This Recommendation requires the development of a set of documentation that will provide assurance to users and (optionally) validators that the DRBGs in this

Recommendation have been implemented properly. Much of this documentation may be placed in a user's manual. This documentation **shall** consist of the following as a minimum:

- Document how the implementation has been designed to permit implementation validation and operational testing.
- Document the type of DRBG (e.g., CTR_DRBG, Dual_EC_DRBG), and the cryptographic primitives used (e.g., AES-128, SHA-256).
- Document the security strengths supported by the implementation.
- Document features supported by the implemention (e.g., prediction resistance, the available elliptic curves, etc.).
- In the case of the CTR_DRBG, indicate whether a derivation function is provided.
 If a derivation function is not used, documentation shall clearly indicate that the
 implementation can only be used when full entropy input is available.
- Document any support functions other than operational testing.

11.2 Implementation Validation Testing

A DRBG process **shall** be tested for conformance to this Recommendation. A DRBG **shall** be designed to be tested to ensure that the product is correctly implemented. A testing interface **shall** be available for this purpose in order to allow the insertion of input and the extraction of output for testing.

Implementations to be validated shall include the following:

- Documentation specified in Section 11.1.
- Any documentation or results required in derived test requirements.

11.3 Operational/Health Testing

11.3.1 Overview

A DRBG implementation **shall** perform self-tests to ensure that the DRBG continues to function properly. Self-tests of the DRBG processes **shall** be performed as specified in Section 9.6. A DRBG implementation may optionally perform other self-tests for DRBG functionality in addition to the tests specified in this Recommendation.

All data output from the DRBG boundary **shall** be inhibited while these tests are performed. The results from known-answer-tests (see Section 11.3.2) **shall not** be output as random bits during normal operation.

When a DRBG fails a self-test, the DRBG **shall** enter an error state and output an error indicator. The DRBG **shall not** perform any DRBG operations while in the error state, and no pseudorandom bits **shall** be output when an error state exists. When in an error state, user intervention (e.g., power cycling, restart of the DRBG) **shall** be required to exit the

error state (see Section 9.6).

11.3.2 Known Answer Testing

Known-answer testing **shall** be conducted as specified in Section 9.6. A known-answer test involves operating the DRBG with data for which the correct output is already known and determining if the calculated output equals the expected output (the known answer). The test fails if the calculated output does not equal the known answer. In this case, the DRBG **shall** enter an error state and output an error indicator (see Section 9.7).

The generalized known-answer testing is specified in Section 9.6. Testing **shall** be performed on all DRBG functions implemented.

Appendix A: (Normative) Application-Specific Constants

[May need to include Hash_DRBG constants]

A.1 Constants for the Dual EC DRBG

The **Dual_EC_DRBG** requires the specifications of an elliptic curve and two points on the elliptic curve. One of the following NIST approved curves and points **shall** be used in applications requiring certification under FIPS 140-2. More details about these curves may be found in FIPS PUB 186-3, the Digital Signature Standard.

Each of following curves is given by the equation:

$$y^2 = x^3 - 3x + b \pmod{p}$$

Notation:

p - Order of the field F_p , given in decimal

r - order of the Elliptic Curve Group, in decimal. Note that r is used here for consistency with FIPS 186-3 but is referred to as n in the description of the Dual_EC_DRBG (...)

a-(-3) in the above equation

b - coefficient above

The x and y coordinates of the base point, ie generator G, are the same as for the point P.

A.1.1 Curve P-224

 $p = 26959946667150639794667015087019630673557916 \setminus \\ 260026308143510066298881$

 $r = 26959946667150639794667015087019625940457807 \setminus \\ 714424391721682722368061$

 $b = b4050a85 \ 0c04b3ab \ f5413256 \ 5044b0b7 \ d7bfd8ba \ 270b3943 \ 2355ffb4$

Px = b70e0cbd 6bb4bf7f 321390b9 4a03c1d3 56c21122 343280d6 115c1d21

Py = bd376388 b5f723fb 4c22dfe6 cd4375a0 5a074764 44d58199 85007e34

Qx = 68623591 6elladfa f080a451 477fa27a f21248be 916d3458 a583a3c9

Qy = 6060018a 24b35be6 caecf3f0 7f2c6b43 4e47479e 55362c8f 5707adca

A.1.2 Curve P-256

- $p = 11579208921035624876269744694940757353008614 \setminus 3415290314195533631308867097853951$
- $r = 11579208921035624876269744694940757352999695 \$ 5224135760342422259061068512044369
- b = 5ac635d8 aa3a93e7 b3ebbd55 769886bc 651d06b0 cc53b0f6 3bce3c3e 27d2604b
- Px = 6b17d1f2 e12c4247 f8bce6e5 63a440f2 77037d81 2deb33a0 f4a13945 d898c296
- Qx = c97445f4 5cdef9f0 d3e05ele 585fc297 235b82b5 be8ff3ef ca67c598 52018192
- Qy = b28ef557 ba31dfcb dd21ac46 e2a91e3c 304f44cb 87058ada 2cb81515 1e610046

A.1.3 Curve P-384

- $p = 39402006196394479212279040100143613805079739 \ 27046544666794829340424572177149687032904726 \ 6088258938001861606973112319$
- b=b3312fa7 e23ee7e4 988e056b e3f82d19 181d9c6e fe814112 0314088f
 5013875a c656398d 8a2ed19d 2a85c8ed d3ec2aef
- Px = aa87ca22 be8b0537 8eb1c71e f320ad74 6e1d3b62 8ba79b98 59f741e0 82542a38 5502f25d bf55296c 3a545e38 72760ab7
- Py = 3617de4a 96262c6f 5d9e98bf 9292dc29 f8f41dbd 289a147c e9da3113 b5f0b8c0 0a60b1ce 1d7e819d 7a431d7c 90ea0e5f
- Qx = 8e722de3 125bddb0 5580164b fe20b8b4 32216a62 926c5750 2ceede31 c47816ed d1e89769 124179d0 b6951064 28815065
- Qy = 023b1660 dd701d08 39fd45ee c36f9ee7 b32e13b3 15dc0261

Oaalb636 e346df67 1f790f84 c5e09b05 674dbb7e 45c803dd

A.1.4 Curve P-521

- $p = 68647976601306097149819007990813932172694353 \\ 00143305409394463459185543183397656052122559 \\ 64066145455497729631139148085803712198799971 \\ 6643812574028291115057151$
- $r = 68647976601306097149819007990813932172694353 \ 00143305409394463459185543183397655394245057 \ 74633321719753296399637136332111386476861244 \ 0380340372808892707005449$
- b = 051953eb 9618e1c9 a1f929a2 1a0b6854 0eea2da7 25b99b31 5f3b8b48 9918ef10 9e156193 951ec7e9 37b1652c 0bd3bb1b f073573d f883d2c3 4f1ef451 fd46b503 f00
- Px = c6858e06 b70404e9 cd9e3ecb 662395b4 429c6481 39053fb5
 21f828af 606b4d3d baa14b5e 77efe759 28fe1dc1 27a2ffa8
 de3348b3 c1856a42 9bf97e7e 31c2e5bd 66
- Py = 11839296 a789a3bc 0045c8a5 fb42c7d1 bd998f54 449579b4
 46817afb d17273e6 62c97ee7 2995ef42 640c550b 9013fad0
 761353c7 086a272c 24088be9 4769fd16 650
- Qx = 1b9fa3e5 18d683c6 b6576369 4ac8efba ec6fab44 f2276171 a4272650 7dd08add 4c3b3f4c lebc5b12 22ddba07 7f722943 b24c3edf a0f85fe2 4d0c8c01 591f0be6 f63
- Qy = 1f3bdba5 85295d9a 1110d1df 1f9430ef 8442c501 8976ff34 37ef91b8 1dc0b813 2c8d5c39 c32d0e00 4a3092b7 d327c0e7 a4d26d2c 7b69b58f 90666529 11e45777 9de

A.2 Using Alternative Points in the Dual_EC_DRBG()

The security of **Dual_EC_DRBG()** requires that the points *P* and *Q* be properly generated. To avoid using potentially weak points, the points specified in Annex A.1 **should** be used. However, an implementation may use different pairs of points provided that they are *verifiably random*, as evidenced by the use of the procedure specified in Appendix A.2.1 below, and the self-test procedure in Appendix A.2.2. An implementation that uses alternative points generated by this Approved method **shall** have them "hardwired" into its source code, or hardware, as appropriate, and loaded into the *working_state* at instantiation. To conform to this Recommendation, points **shall** use the procedure given in Appendix A.2.1, and verify their generation using Appendix A.2.2.

A.2.1 Generating Alternative P,Q

The curve **shall** be one of the NIST curves from FIPS 186-3 that is specified in Appendix A.1 of this Recommendation, and **shall** be appropriate for the desired *security_strength*, as specified in Table 4, Section 10.3.1.

The point P shall remain the generator point G given in Appendix A.1 for the selected curve. (This minor restriction simplifies the test procedure to verify just one point each time.)

The point *Q* shall be generated using the procedure specified in ANS X9.62. The following input is required:

An elliptic curve $E = (F_q, a, b)$, cofactor h, prime n, a bit string SEED, and hash function Hash(). The curve parameters are given in Appendix A.1 of this Recommendation. The minimum length m of SEED shall conform to Section 10.3.1, Table 4, under "Seed length". The bit length of SEED may be larger than m. The hash function shall be SHA-512 in all cases.

If the output from the ANS X9.62 generation procedure is "failure", a different SEED will have to be used.

Otherwise, the output point shall be used as the point Q.

A.2.2 Additional Self-testing Required for Alternative P,Q

To insure that the point Q has been generated appropriately, an additional self-test procedure **shall** be performed whenever the instantiate function is invoked. Section 9.6.2 specifies that known-answer tests on the instantiate function be performed prior to creating an operational instantiation. As part of those tests, an implementation of the generation procedure in ANS X9.62 **shall** be called with the SEED value used to generate the alternate Q. The point returned **shall** be compared with the stored value of Q used in place of the default value (see Appendix A.1 of this Recommendation). If the generated value does not match the stored value, the implementation **shall** halt with an error condition.

Appendix B: (Normative) Conversion and Auxilliary Routines

B.1 Bitstring to an Integer

Input:

1. $b_1, b_2, ..., b_n$ The bitstring to be converted.

Output:

1. *x* The requested integer representation of the bitstring.

Process:

1. Let $(b_1, b_2, ..., b_n)$ be the bits of b from leftmost to rightmost.

2. $x = \sum_{i=1}^{n} 2^{(n-i)} b_i$.

3. Return x.

In this Standard, the binary length of an integer x is defined as the smallest integer n satisfying $x < 2^n$.

B.2 Integer to a Bitstring

Input:

1. x The non-negative to be converted.

Output:

1. $b_1, b_2, ..., b_n$ The bitstring representation of the integer x.

Process:

1. Let $(b_1, b_2, ..., b_n)$ represent the bitstring, where $b_1 = 0$ or 1, and b_1 is the most significant bit, while b_n is the least significant bit.

2. For any integer n that satisfies $x < 2^n$, the bits b_i shall satisfy:

$$x = \sum_{i=1}^{n} 2^{(n-i)} b_i .$$

3. Return $b_1, b_2, ..., b_n$.

In this Standard, the binary length of the integer x is defined as the smallest integer n that satisfies $x < 2^n$.

B.3 Integer to an Octet String

Input:

1. A non-negative integer x, and the intended length n of the octet string satisfying $2^{8n} > x$.

Output:

1. An octet string O of length n octets.

Process:

- 1. Let $O_1, O_2, ..., O_n$ be the octets of O from leftmost to rightmost.
- 2. The octets of O shall satisfy:

$$x = \sum 2^{8(n-i)}O_i$$

for i = 1 to n.

3. Return O.

B.4 Octet String to an Integer

Input:

1. An octet string O of length n octets.

Output:

1. A non-negative integer x.

Process:

- 1. Let O_1 , O_2 , ..., O_n be the octets of O from leftmost to rightmost.
- 2. x is defined as follows:

$$x = \sum 2^{8(n-i)} O_i$$

for i = 1 to n.

3. Return x.

B.5 Converting Random Numbers from/to Random Bits

The random values required for cryptographic applications are generally of two types: either a random bitstring of a specified length or a random integer in a specified interval. In some cases, a DRBG may return a random number in a specified interval that needs to be converted into random bits; in other cases, a DRBG returns a random bitstring that needs to be converted to a random number in a specific range.

B.5.1 Converting Random Bits into a Random Number

In some cryptographic applications sequences of random numbers are required (a_0, a_1, a_2) where:

i) Each integer a_i satisfies $0 \le a_i \le r-1$, for some positive integer r (the range of the

random numbers);

- ii) The equation $a_i = s$ holds, with probability almost exactly 1/r, for any $i \ge 0$ and for any s ($0 \le s \le r-1$);
- iii) Each value a_i is statistically independent of any set of values a_i $(j \neq i)$.

Four techniques are specified for generating sequences of random numbers from sequences of random bits.

If the range of the number required is $a \le a_i \le b$ rather than $0 \le a_i \le r-1$, then a random number in the desired range can be obtained by computing $a_i + a$, where a_i is a random number in the range $0 \le a_i \le b-a$ (that is, when r = b-a+1).

B.5.1.1 The Simple Discard Method

Let m be the number of bits needed to represent the value (r-1). The following method may be used to generate the random number a:

- 1. Use the random bit generator to generate a sequence of m random bits, (b_0, b_1, b_{m-1}) .
- 2. Let $c = \sum_{i=0}^{m-1} 2^i b_i$.
- 3. If c < r then put a = c, else discard c and go to Step 1.

This method produces a random number a with no skew (no bias). A possible disadvantage of this method, in general, is that the time needed to generate such a random a is not a fixed length of time because of the conditional loop.

The ratio $r/2^m$ is a measure of the efficiency of the technique, and this ratio will always satisfy $0.5 < r/2^m \le 1$. If $r/2^m$ is close to 1, then the above method is simple and efficient. However, if $r/2^m$ is close to 0.5, then the simple discard method is less efficient, and the more complex method below is recommended.

B.5.1.2 The Complex Discard Method

Choose a small positive integer t (the number of same-size random number outputs desired), and then let m be the number of bits in (r'-1). This method may be used to generate a sequence of t random numbers $(a_0, a_1, \ldots, a_{t-1})$:

- 1. Use the random bit generator to generate a sequence of m random bits, $(b_0, b_1, ..., b_{m-1})$.
- 2. Let $c = \sum_{i=0}^{m-1} 2^i b_i$.
- 3. If $c < r^t$, then

let $(a_0, a_1, ..., a_{t-1})$ be the unique sequence of values satisfying $0 \le a_i \le r - 1$ such

that
$$c = \sum_{i=0}^{t-1} r^i a_i$$

else discard c and go to Step 1.

This method produces random numbers $(a_0, a_1, \ldots, a_{t-1})$ with no skew. A possible disadvantage of this method, in general, is that the time needed to generate these numbers is not a fixed length of time because of the conditional loop. The complex discard method is guaranteed to produce a sequence of random outputs for each iteration and, therefore, may have better overall performance than the simple discard method if many random numbers are needed.

The ratio $r^I/2^m$ is a measure of the efficiency of the technique, and this ratio will always satisfy $0.5 < r^I/2^m \le 1$. Hence, given r, it is recommended to choose t so that t is the smallest value such that $r^I/2^m$ is close to 1. For example, if t = 3, then choosing t = 3 means that t = 3 (as t = 1) and t = 1 means that t = 1

B.5.1.3 The Simple Modular Method

Let m be the number of bits needed to represent the value (r-1), and let $\frac{3}{8}$ be a security parameter. The following method may be used to generate one random number a:

- 1. Use the random bit generator to generate a sequence of $m+\frac{2}{3}$ random bits, $(b_0, b_1, \dots, b_{m+\frac{2}{3}-1})$.
- 2. Let $c = \sum_{i=0}^{m+s-1} 2^i b_i$.
- 3. Let $a=c \mod r$.

The simple modular method can be coded to take constant time. This method produces a random value with a negligible skew, that is, the probability that $a_i = w$ for any particular value of w ($0 \le w \le r-1$) is not exactly 1/r. However, for a large enough value of w and 1/r is negligible. The value of w shall be greater than or equal to w [Why 64? What is the relationship between s and the security strength?]

B.5.1.4 The Complex Modular Method

Choose a small positive integer t (the number of same-size random number outputs desired) and a security parameter $\frac{1}{2}$; let m be the number of bits in $(r^t - 1)$. The following method may be used to generate a sequence of t random numbers $(a_0, a_1, ..., a_{t-1})$:

1. Use the random bit generator to generate a sequence of m+1 random bits, $(b_0, b_1, ..., b_m, \frac{1}{3})$.

2. Let
$$c = \sum_{i=0}^{m+l-1} 2^i b_i \mod r^l$$
.

3. Let $(a_0, a_1, ..., a_{r-1})$ be the unique sequence of values satisfying $0 \le a_i \le r-1$ such that $c = \sum_{i=0}^{r-1} r^i a_i$.

The complex modular method is guaranteed to produce a sequence of random outputs with each iteration and, therefore, may have better overall performance than the simple modular method if many random numbers are needed. This method produces a random value with a negligible skew; that is, the probability that a_i —w for any particular value of w ($0 \le w \le r$ -1) is not exactly 1/r. However, for a large enough value of s, the difference between the probability that a_i —w for any particular value of s and 1/r is negligible. The value of s shall be greater than or equal to s. The complex modular method coincides with the simple modular method when t=1.

B.5.2 Converting a Random Number into Random Bits

B.5.2.1 The No Skew (Variable Length Extraction) Method

This is a method of extracting random unbiased bits from a random number modulo a number n. First, a toy example is provided in order to explain how the method works, and then pseudocode is given.

For the toy example, the insight is to look at the modulus n and the random number r as bits, from left to right, and to partition the possible values of r into disjoint sets based on the largest size of random bits that might be extracted. As a small example, if n = 11, then the binary representation of n is b'1011', and the possible values of r (in binary) are as follows:

0000, 0001, 0010, 0011, 0100, 0101, 0110, 0111, 1000, 1001, 1010.

Let the leftmost bit be considered as the bit 4, and the rightmost bit be considered as the bit 1.

- 1. As the 4th bit of n is b'1', look at the 4th bit of r.
- 2. If the 4th bit of r is 0, then the remaining 3 bits can be extracted as unbiased random bits. This forms a class of [0000, 0001, 0010, 0011, 0100, 0101, 0110, 0111] and maps each respective element into the 3-bit sequences [000, 001, 010, 011, 100, 0101, 110, 111], each of which is unbiased, and the process is completed
- 3. If the 4th bit of r is b'1', then r falls into the remainder [1000, 1001, 1010], and the process needs to continue with step 4 in order to extract unbiased bits.
- 4. As the 3rd bit of *n* is b'0', the 3rd bit of *r* is always b'0' in the class determined in step 3; therefore the 3rd bit of *r* is already known to be biased, so the analysis moves to the next bit (step 5).

5. The 2nd bit of *n* is b'1', so this forms a subclass [1000, 1001], from which one random unbiased bit can be extracted, namely the 1st bit.

The remaining value of 1010 cannot be used to extract random bits. However, obtaining this value is not usual. For this tiny example: 8/11 of the time, 3 unbiased random bits can be extracted; 2/11 of the time, 1 unbiased bit can be extracted; and 1/11, no unbiased bits can be extracted. As can be seen, it is not known ahead of time how many unbiased bits will be able to be extracted, although the average will be known.

Let both the modulus n and the random r values have m bits. This means that n(m) = b'1', although r(m) may be either b'1' or b'0'.

- 1. outlen = 0.
- 2. Do i = m to 1 by -1

Comment: if n(i) = 0, or r(i) = 1, then this is a skew situation; the routine cannot extract i-1 unbiased bits, so the index is shifted right to check next bit

- 2.1 If ((n(i) = b'0')) or (r(i) = b'1'), then go to step 2.5.
- 2.2 outlen = i-1.
- 2.3 output = r(outlen, 1).
- 2.4 i = 1

Comment: all unbiased bits possible have been extracted, so exit .

2.5 Continue

The extraction takes a variable amount of time, but this varying amount of time does not leak any information to a potential adversary that can be used to attack the method.

B.5.2.2 The Negligible Skew (Fixed Length Extraction) Method

A possible disadvantage of the No Skew (Variable Length Extraction) Method of Appendix B.5.2.1 is that it takes a variable amount of time to extract a variable number of random bits. To address this concern and to simplify the extraction method, the following method is specified that extracts a fixed length of random bits with a negligible skew. This method exploits the fact that the modulus *n* is known before the extraction occurs.

- 1. Examine the modulus considered as a binary number from left to right, and determine the index bit such that there are at least 16 '1' bits to the left. Call this bit *i*.
- 2. Extract random bits from the random number r by truncating on the left up to bit i. This is the output = r(i,1).

This method is especially appropriate when the high order bits of the modulus are all set to

'1' for efficiency reasons, as is the case with the NIST elliptic curves over prime fields.

This method is acceptable for elliptic curves, based on the following analysis. When considering the no skew method, once the random bits are extracted, it is obvious that less than the full number of random bits can be extracted, and the extraction result will still be random. The truncation of more bits than necessary is acceptable. What about truncation of too few bits? For a random number, the no skew extraction process would continue only if the 16 bits of *r* corresponding to the '1' bits in *n* are all zero. For a random number, this occurs about once every 2¹⁶ times. As the modulus is at least 160 bits, this means that 144 bits with a skew are extracted in this case. On average, once every 9,437,184 output bits (or more), there will be a 144-bit substring somewhere in that total that has a skew, which will have the leftmost bit or bits tending to a binary zero bit or bits. This skew could be as little as one bit. However, an adversary will not know exactly where this skewed substring occurs. The 9,437,184 total output bits will still be overwhelmingly likely to be within the statistical variation of a random bitstring; that is, the statistical variation almost certainly will be much greater than this negligible skew.

Appendix C: (Normative) Entropy and Entropy Sources

An examination of the DRBG algorithms in this Recommendation reveals a common feature: each of them takes a *seed* and applies an algorithm to produce a potentially large number of pseudo-random bits. The most important feature of the interaction between the seed and the algorithm is that if an adversary doesn't know the seed, then he can't tell the difference between the pseudo-random bits and a stream of truly random bits. Conversely, if he knows (or can guess) the seed, then he can easily distinguish the output from random, since the algorithm is deterministic. Thus, the security of the DRBG output is directly related to the adversary's inability to guess the seed.

C.1 What is Entropy?

The word "entropy" is used to describe a measure of randomness, i.e., a description of how hard a value is to guess. Entropy is a measure of uncertainty or unpredictability and is dependent on the probabilities associated with the possible results for a given "event" (e.g., a throw of a die or flip of a coin).

In this Recommendation, entropy is relative to an adversary and his ability to observe/predict a value. If the adversary has no uncertainty about the value, then the entropy is zero (and so is the security of the relying application). Any assessment of the entropy of a particular value is actually an assessment of how much of the value is unknown to the adversary.

C.2 Entropy Source

Entropy is obtained from an entropy source. The entropy input required to seed or reseed a DRBG **shall** be obtained either directly or indirectly from an entropy source (see Appendix D for further information on RBG construction). The entropy source is the critical component of an RBG that provides un-guessable values for the deterministic algorithm to use as seeds for the random bit generation process.

Every entropy source must include some process that is unpredictable. An intuitive (though often impractical) example is tossing a coin and recording the sequence of heads and tails. More likely, the entropy source will be an electronic process, such as a noisy diode, which receives a constant input voltage level and outputs a continuous, normally distributed analog voltage level. Other possibilities include thermal noise or radioactive decay that are measured by appropriate instruments. The unpredictability could involve human interaction with an otherwise deterministic system, such as the sampling of a high-speed counter whenever a human operator presses a key on a keyboard. In any case, there must be something happening that is unpredictable to an adversary, either fundamentally unpredictable (e.g., when the next particle is detected by a Geiger counter), or unpredictable from a practical point of view (e.g., the adversary won't know the exact value of a high-speed counter if he isn't close enough to the human pressing a key).

Figure C-1 provides a generic model for an entropy source. A noise source (e.g., a noisy

diode or a coin flip) provides the entropy, which is then converted to bits (i.e., digitized). Collecting entropy from an entropy source requires obtaining numerous samples, where each sample is the result from a given type of event). Once sufficient samples have been gathered, they generally need to be converted to bits (e.g. an analog voltage will be mapped to some digital value, or coin tosses could be mapped to ones and zeros). Some entropy sources will perform further processing (conditioning) on the resulting bits, perhaps guaranteeing unbiased output. An entropy source may even process the bits to the

point where the output bitstring will have full entropy; i.e. the entropy of the bitstring will be (nearly) the same as its length. An assessment is made of the amount of entropy that has been obtained, perhaps on the digitalized data or on the data resulting from the conditioning process (see Appendix C.2). Health tests are performed to determine that the entropy source is performing correctly.

Before a source of entropyan entropy source is selected for seeding a DRBG, a thorough evaluation of the amount of entropy it is capable of providing must be determined. When a suitable entropy source is selected, a further assessment

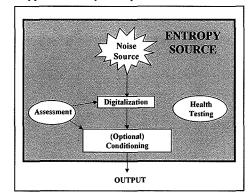


Figure C-1: Entropy Source Model

may be required to ensure that adequate entropy is actually provided when required by the DRBG (see Appendix C.2).

Guidance on the selection and use of entropy sources is currently under development and is expected to be provided as a NIST Recommendation in the future.

C.2 Entropy Assessment

A DRBG requires a predetermined amount of entropy in the entropy input that is used to seed or reseed an instantiation in order to provide the requested DRBG security strength. Therefore, the amount of actual entropy obtained from an entropy source **shall** be assessed before providing it as entropy input; a means of measuring the entropy is required. Note that the actual entropy provided in a given string of entropy input bits is less than or equal to the length of that bitstring; i.e., each bit of the entropy input has (at most) one bit of entropy; multiple bits of the entropy input may be required to provide one bit of entropy.

There are many entropy measures defined in information theory; this Recommendation uses a very conservative measure that is known as min-entropy (H_{min}), and is defined as

$$H_{min} = -\lg_2(p_{max})$$

where each possible value is p_i , and p_{max} is the maximum probability of the p_i . H_{min} is

expressed in bits and is the amount of entropy that is expected in each event that produces a value of p_i .

For example, suppose that a noisy diode is used as a source of entropy, and the diode possible voltages divided into 16 intervals (column 1), with each interval assigned a 4-bit string value from 0000 to 1111 (column 2). Whenever the diode is sampled, the result is digitized and converted to the 4-bit value indicagted in Table C-1. The probability of each interval has been determined for this diode and is provided in column 3. Note that other diodes may behave differently.

Collecting entropy from an entropy source requires obtaining numerous samples, where each sample is the result from a given type of event). Once sufficient samples have been gathered, they generally need to be converted to bits (e.g. an analog voltage will be mapped to some digital value, or coin tosses could be mapped to ones and zeros).

Table C-1: Voltages Digitaization Ranges and Probabilities

Sampled Voltage	Digitized Output	Probability (pi)
$-\infty < Z < 2.5$	0000	0.000233
2.5 ≤ Z < 3	0001	0.001117
$3 \le Z < 3.5$	0010	0.004860
$3.5 \le Z < 4$	0011	0.016540
4 ≤ Z < 4.5	0100	0.044057
4.5 ≤ Z < 5	0101	0.091848
5 ≤ Z < 5.5	0110	0.149882
5.5 ≤ Z < 6	0111	0.191462
6 ≤ Z < 6.5	1000	0.191462
6.5 ≤ Z < 7	1001	0.149882

Sampled Voltage	Digitized Output	Probability (pi)
7 ≤ Z < 7.5	1010	0.091848
$7.5 \le Z < 8$	1011	0.044057
8 ≤ Z < 8.5	1100	0.016540
8.5 ≤ Z < 9	1101	0.004860
9 ≤ Z < 9.5	1110	0.001117
9.5 ≤ <i>Z</i> < ∞	1111	0.000233

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For this diode, the most likely digitized outputs are 0111 and 1000, each with a probability of 0.191462. Therefore, $p_{max} = 0.191462$. Using the min-entropy formula above:

$$H_{min} = -\lg_2(p_{max}) = -\lg_2(0.19462) = 2.38487.$$

This means that for each 4-bit sample from this diode, an entropy of 2.38487 bits is expected.

One useful fact about min-entropy is that if two samples are independent (e.g., samplings of the same noisy diode), then the entropy of their concatenation is the sum of their entropy. This makes sense; if the samples are independent, then guessing one sample provides no information for guessing another one. If various events are concatenated, then the min-entropy for each event is added to find the min-entropy of the concatenated events. In the noisy diode example, if sample has a min-entropy of 2.38487 bits, then ten samples taken together have a min-entropy of 23.8487 bits, and one hundred samples have a min-entropy of 238.487 bits.

These entropy measures relate directly to the security strengths of the Approved DRBG algorithms. For example, to provide entropy input for a seed that is appropriate to instantiate a DRBG with a security strength of 128 bits, at least 54 samplings of the diode are required ($128/2.38487 = 53.67 \approx 54$) and would result in a bitstring of 216 bits to provide at least 128 bits of entropy. Note that the samplings could actually contain more or less entropy than expected.

Appendix D: Constructing a Random Bit Generator (RBG) from Entropy Sources and DRBG Mechanisms

This Recommendation is primarily concerned with the DRBG algorithms for generating pseudorandom outputs and how they are to be implemented. Some discussion of entropy sources that may be used to provide entropy input are provided in Appendix C. This appendix briefly describes how to combine the entropy source with a DRBG mechanism to create an Approved RBG.

D.1 Entropy Input for a DRBG

Section 8.6.5 states that the source of a DRBG's entropy input may be 1) an Approved Non-deterministic Random Bit Generator (NRBG), 2) an Approved DRBG (or chain of Approved DRBGs) or 3) an Approved entropy source whose entropy characteristics are known. A clarification of concepts may be helpful at this point.

- a. An entropy source provides entropy source output (see Appendix C.1). This entropy source output may be used as the entropy input for a DRBG; i.e., the entropy input source may be the output of an entropy source (see Figure 22).
- b. An NRBG contains an entropy source (see Appendix C.1) and performs algorithmic processing on the entropy source output in order to produce an output with full entropy (see Figure 22).
- c. A DRBG is defined in the body of this Recommendation.
- d. To form a chain of DRBGs (see Figure 22), the entropy input for the first DRBG (the highest DRBG in the chain) shall be obtained from a "true" source of entropy (i.e., an Approved NRBG or an Approved entropy source whose entropy characteristics are known). The entropy shall be equal to or greater than the entropy required by any of the subordinate DRBGs.
 - <u>Each subordinate DRBG is instantiated with entropy input acquired from an entropy request to a higher DRBG in the chain. The entropy input **shall** contain sufficient entropy to support the requested security level.</u>
- e. An Approved entropy source by itself (i.e., not part of an NRBG) may or may not provide full entropy. However, if full entropy is not provided, the amount of entropy provided in a given sequence of outputs is known.

When designing an RBG using a DRBG, there are a number of concerns to be addressed in addition to the DRBG to be selected, including the entropy <u>input</u> source to be used, how readily the entropy input to the DRBG can be provided, and how the DRBG maintains its internal state information from one request to the next. Appendix G provides a discussion on DRBG selection, and Appendix C provides some basic discussion on entropy sources. This appendix includes discussions about using entropy <u>input</u> sources whose output may or

may not be readily available and discusses internal state persistance.

D.42 Availability of Entropy Input for a DRBG

The source of a DRBG's entropy input may be an Approved NRBG. an Approved DRBG or an Approved entropy source whose entropy characteristics are known (see Section 8.6.5). The choice of entropy input source may will determine the specific "features" that an RBG can offer a consuming application (e.g., whether reseeding or prediction resistance is practical). Whenever entropy input is requested by a DRBG, the entropy input source must provide sufficient entropy to support the security strength intended for the DRBG. The entropy input source may be able to provide entropy whenever requested (i.e., entropy is readily available on demand), or too slowly to honor "frequent" requests (e.g., the entopy input source may, in practice, be able to provide entropy only during instantiation). In addition, the entropy input must be provided to the DRBG via a secure (i.e., private and authentic) channel.

the entropy provided for instantiation must be provided over a secure (private and authentic) channel.

Over time, a DRBG may be able to accumulate additional entropy from inputs provided by the user or consuming application (i.e., additional_input). For this reason, the DRBG implementation should accept additional input whenever possible. Implementations that have values that may have some entropy, such as timestamps or nonces from protocol runs, should provide these values to the DRBG as additional inputs.

D.2.14 Using a Readily Available Entropy Input Source

The ideal situation for a DRBG is to have ready access to some entropy <u>input</u> source that provides entropy input (immediately) upon request. The entropy <u>input</u> source provides bitstrings, along with a promise about how much entropy is available.

When the DRBG has a readily available source of entropy <u>input</u>, reseeding and instantiation can be done on demand, requests for prediction resistance can be honored, and a DRBG can be reseeded when it has produced the maximum number of outputs (i.e., the *reseed interval* is reached).

Upon each request for entropy input, the status of the request is returned to the calling function (i.e., the instantiate or reseed function). A failure of the entropy <u>input</u> source has the following consequences:

- If the failure of the entropy source is detected, the DRBG functions are designed to indicate the error and enter the error state (see Section 9.7). No further output is produced until the failure is corrected.
- If the failure is not immediately detected, the DRBG will continue to provide output, based on the entropy currently available in the internal state.

If the failure occurs prior to or during instantiation, an undetected failure would be catastrophic, as the DRBG would totally fail to provide the promised security strength. Therefore, extreme care must be taken to ensure that a DRBG is instantiated with sufficient entropy.

If the failure occurred subsequent to instantiation, a request for prediction resistance would not result in prediction resistance being provided; however, the security strength of the output would be based on whatever entropy had previously been obtained.

If the failure occurs prior to or during a normal reseed (at the end of the <code>reseed_interval</code>), the security strength of the output would be based on whatever entropy had previously been obtained. If the implemented <code>reseed_interval</code> is the maximum that can be supported by the DRBG (see the tables in Section 10), then the security provided by the DRBG algorithm is no longer assured. Therefore, the use of a <code>reseed_interval</code> that is significantly less than the maximum interval is recommended. This would provide additional time for the entropy source failure to be detected.

D.2.2 No Readily Available Entropy Input Source

Many implementations of DRBGs will not have ready access to an entropy <u>input</u> source. An implementation of this type has the following requirements:

The DRBG must be instantiated at a time when the DRBG has access to some <u>reliable</u> entropy <u>input</u> source. In some applications, the entropy <u>input</u> source is only available during manufacture or device setup; in others, it is occasionally available (e.g., when a user is moving the mouse around on a laptop).

The DRBG must maintain its internal state for as long as the DRBG may be called upon to generate outputs. This typically requires some kind of persistent memory (e.g., flash memory) or a means of securely saving the internal state to avoid losing the internal state during power down.

Over time, a DRBG may be able to accumulate additional entropy from inputs provided by the user or consuming application (i.e., additional input). For this reason, the DRBG implementation **should** accept additional input whenever possible. Implementations that have values that may have some entropy, such as timestamps or nonces from protocol runs, **should** provide these values to the DRBG as additional inputs.

D.32 Persistance Considerations Saving the Internal State

A DRBG is provided with entropy input during instantiation, and the instantiation exists for as long as the internal state is maintained. In many environments, the internal state can be maintained for a very long time because power is continually available during that time or the internal state is stored in persistent memory (e.g., flash memory) that is not affected by power fluctuations.

However, there are environments in which a DRBG does not have continual power or persistant memory for maintaining the internal state. In this case, a DRBG can only be instantiated when power is provided, and the DRBG instantiation only exists for as long as the power is available. Whenever power is available, entropy input must be provided if the DRBG is to be instantiated.

An example of this might be a smart card that contains a DRBG and is only powered up when it is inserted into a reader. The reader provides not only the power, but must provide entropy input for the DRBG in the smart card (i.e., the smart card either is provided with entropy input that is passed along to the smart card's DRBG, or the reader produces the entropy input). This example will be used to explain possible methods for addressing the case in which a DRBG instantiation is short-lived. The method is an adaptation of a concept that uses seed files in currently implemented RNGs.

For simplicity, assume that the reader produces the entropy input for the smart card's DRBG (DRBG_{short-lived}). The reader could contain an Approved NRBG or Approved entropy source (see Appendix D.1). Alternatively, the reader could contain a DRBG (DRBG_{source}) whose output would be used to provide entropy input for DRBG_{short-lived}. Also for simplicity, assume that the reader has continual power or persistant memory that can be used to maintain the internal state of its DRBG. In this case, DRBG_{source} must be instantiated as discussed in Appendix D.1 with sufficient entropy to support any DRBG_{short-lived} that "connects" to it (i.e., a chain of DRBGs is formed, with DRBG_{short-lived} at the end of the chain, and DRBG_{source} immediately above it. The following is a common method for interacting between the two DRBGs.

- 1. Whenever DRBG_{short-lived} is "connected" to DRBG_{source}, a generate request is sent to DRBG_{source}. DRBG_{source} generates the requested out and provides it to DRBG_{short-lived} as entropy input for instantiation. The application using DRBG_{short-lived} may provide additional input to the DRBG as a personalization string during the instantiation process.
- 2. If the application has data containing entropy, the data is saved and provided to DRBG_{source} in one-byte calls as *additional_input*. Each call will result in changes to the internal state of DRBG_{source}; each output from DRBG_{source} is ignored.
- 3. After DRBG_{short-lived} provides output as requested by its application. *k*-bits of additional output is generated by DRBG_{short-lived} and provided as *additional_input* to DRBG_{source} in a generate request, along with any other application data that might contain entropy. This will result in another update of the internal state of DRBG_{source}. Any resulting output from this request is ignored.

John: I'm not sure what to do with the following:

A DRBG's internal state may be saved in a *StateFile* that is securely maintained for a DRBG instantiation⁵. It can be used to save the internal state in case the power to the DRBG goes down and persistent memory is not available.

⁵ The StateFile is often called a SEEDFILE.

A seedfile is persistent storage kept for a DRBG. It is used both to protect against silent failure of its entropy source, and also to allow externally seeded DRBGs to instantiate itself on power up and save all the entropy in its state back to the seedfile whenever necessary. Seedfiles are used and described in many cryptographic PRNGs, including /dev/random and Yarrow 160.

In X9.82, a seedfile is simply a DRBG instance whose working state is stored in some kind of persistent storage. Let SEEDFILE be the DRBG which is being used as a seedfile, and whose working state is stored in persistent storage. The following explains how the seedfile is used to support a DRBG (CURRENT) whose state is stored in volatile storage, but which may accumulate entropy over time from additional inputs:

- •SEEDFILE is instantiated from some entropy source (possibly another RBG) when it is available, such as during manufacturing or device setup.
- •At power up, CURRENT is instantiated. This is done by requesting a seed from SEEDFILE's generate routine and using that seed to instantiate CURRENT. Any additional input which is available from the application should be provided in the personalization string during CURRENT's instantiation.
- During operation, application data which might contain some entropy should be stored up, and periodically used as additional input in one byte generate requests to SEEDFILE. The resulting one byte outputs are discarded.
- •At power down, CURRENT generates a k bit output. This output is used as additional input, along with any other available application data which might have some entropy, in a one byte generate request to SEEDFILE. The one byte output is discarded.
- If the application rarely or never has a power down, then a k-bit value from CURRENT should periodically (e.g., once a day) be generated and used as additional input in a one-byte generate request to SEEDFILE, and the resulting output byte should be discarded.

D.4 Seeding Many DRBGs from One DRBG

Some applications may benefit from using different DRBGs for different applications. Each of these DRBGs must be seeded with sufficient entropy to support the DRBG's security strength. If an entropy source is not readily available for doing so, several DRBGs may be seeded from a single DRBG (the parent DRBG) or chain (e.g., hierarchy) of DRBGs. However, this must be done with some care, to avoid introducing new weaknesses.

- •The parent DRBG shall be instantiated with as much entropy as possible. The entropy shall be equal to or greater than the entropy required by any of the subordinate DRBGs.
- •Each subordinate DRBG is instantiated with entropy input acquired from an entropy

request to the parent DRBG (or a higher DRBG in the chain). The entropy input shall contain sufficient entropy to support the requested security level.

Appendix E: (Informative) Security Considerations

E.1 Extracting Bits in the Dual_EC_DRBG (...)

E.1.1 Potential Bias Due to Modular Arithmetic for Curves Over F_0

For the mod p curves (i.e, a *Prime field curve*), there is a potential bias in the output due to the modular arithmetic. Two approaches to correcting the bias are presented. The Negligible Skew Method described in Appendix B.5.2.2 is appropriate for the NIST curves, since all were selected to be over prime fields near a power of 2 in size. Each NIST prime has at least 32 leading 1's in its binary representation, and at least 16 of the leftmost (high-order) bits are discarded in each block produced. These two facts imply that there is a small fraction ($\leq 1/2^{32}$) of *outlen* outputs for which a bias to 0 may occur in one or more bits. This can only happen when the first 32 bits of an x-coordinate are all zero. As the leftmost 16 bits (at least) are discarded, an adversary can never be certain when a "biased" block has occurred. Thus, any bias due to the modular arithmetic may safely be ignored.

E.1.2 Adjusting for the missing bit(s) of entropy in the x coordinates.

In a truly random sequence, it should not be possible to predict any bits from previously observed bits. With the **Dual_EC_DRBG** (...), the full output block of bits produced by the algorithm is "missing" some entropy. Fortunately, by discarding some of the bits, those bits remaining can be made to have nearly "full strength", in the sense that the entropy that they are missing is negligibly small.

To illustrate what can happen, suppose that a mod p curve with m = 256 is selected, and that all 256 bits produced were output by the generator, i.e. that outlen = 256 also. Suppose also that 255 of these bits are published, and the 256-th bit is kept "secret". About $\frac{1}{2}$ the time, the unpublished bit could easily be determined from the other 255 bits. Similarly, if 254 of the bits are published, about $\frac{1}{2}$ of the time the other two bits could be predicted. This is a simple consequence of the fact that only about $\frac{1}{2}$ of all $\frac{2}{2}$ bitstrings of length m occur in the list of all x coordinates of curve points.

The "abouts" in the preceding example can be made more precise, taking into account the difference between 2^m and p, and the actual number of points on the curve (which is always within $2 * p^{1/2}$ of p). For the NIST curves, these differences won't matter at the scale of the results, so they will be ignored. This allows the heuristics given here to work for any curve with "about" $(2^m)/f$ points, where f = 1 is the curve's cofactor.

The basic assumption needed is that the approximately $(2^m)/(2f) x$ coordinates that do occur are "uniformly distributed": a randomly selected *m*-bit pattern has a probability 1/2f of being an *x* coordinate. The assumption allows a straightforward calculation,--albeit approximate--for the entropy in the rightmost (least significant) *m-d* bits of **Dual EC_DRBG** output, with d << m.

The formula is
$$E = -\sum_{j=0}^{2^d} \left[2^{m-d} binomprob \left(2^d, z, 2^d - j \right) \right] p_j \log_2 p_j$$
, where E is the entropy.

The term in braces represents the approximate number of (m-d)-bitstrings, which fall into one of $1+2^d$ categories as determined by the number of times j it occurs in an x coordinate; z = (2f-1)/2f is the probability that any particular string occurs in an x coordinate; $p_j = (j*2f)/2^m$ is the probability that a member of the j-th category occurs. Note that the j=0 category contributes nothing to the entropy (randomness).

The values of E for d up to 16 are:

```
log2(f): 0 d: 0 entropy: 255.00000000 m-d: 256
log2(f): 0 d: 1 entropy: 254.50000000 m-d: 255
log2(f): 0 d: 2 entropy: 253.78063906 m-d: 254
log2(f): 0 d: 3 entropy: 252.90244224 m-d: 253
log2(f): 0 d: 4 entropy: 251.95336161 m-d: 252
log2(f): 0 d: 5 entropy: 250.97708960 m-d: 251
log2(f): 0 d: 6 entropy:
                        249.98863897 m-d: 250
log2(f): 0 d: 7 entropy: 248.99434222 m-d: 249
log2(f): 0 d: 8 entropy:
                        247.99717670 m-d: 248
log2(f): 0 d: 9 entropy:
                        246.99858974 m-d: 247
log2(f): 0 d: 10 entropy:
                        245.99929521 m-d: 246
log2(f): 0 d: 11 entropy:
                        244.99964769 m-d: 245
log2(f): 0 d: 12 entropy:
                         243.99982387 m-d: 244
log2(f): 0 d: 13 entropy:
                         242.99991194 m-d: 243
log2(f): 0 d: 14 entropy:
                         241.99995597 m-d: 242
log2(f): 0 d: 15 entropy:
                         240.99997800 m-d: 241
log2(f): 0 d: 16 entropy:
                         239.99998900 m-d: 240
```

Observations:

- a) The table starts where it should, at 1 missing bit;
- b) The missing entropy rapidly decreases;
- c) For $\log_2(f) = 0$, i.e, the mod p curves, d=13 leaves 1 bit of information in every $10,000 \ (m-13)$ -bit outputs.

Based on these calculations, for the mod p curves, it is recommended that an

implementation shall remove at least the **leftmost** (most significant) 13 bits of every *m*-bit output.

For ease of implementation, the value of d should be adjusted upward, if necessary, until the number of bits remaining, m-d= outlen, is a multiple of 8. By this rule, the recommended number of bits discarded from each x-coordinate will be either 16 or 17. As noted in Section 10.3.1.4, an implementation may decide to truncate additional bits from each x-coordinate, provided the number retained is a multiple of 8.

Because only half of all values in [0,1,...,p-1] are valid x-coordinates on an elliptic curve defined over F_p , it is clear that full x-coordinates **should not** be used as pseudorandom bits. The solution to this problem is to truncate these x-coordinates by removing the high order 16 or 17 bits. The entropy loss associated with such truncation amounts has been demonstrated to be minimal (see the above chart).

One might wonder if it would be desirable to truncate more than this amount. The obvious drawback to such an approach is that increasing the truncation amount hinders the already sluggish performance. However, there is an additional reason that argues against increasing the truncation. Consider the case where the low s bits of each x-coordinate are kept. Given some subinterval I of length 2^s contained in [0, p), and letting N(I) denote the number of x-coordinates in I, recent results on the distribution of x-coordinates in [0, p) provide the following bound:

$$|N(I)/(p/2) - 2^{s}/p| < k * \log^{2} p / \operatorname{sqrt} p$$

where k is some constant derived from the asymptotic estimates given in [Shparlinski]. For the case of P-521, this is roughly equivalent to:

$$|N(I)-2^{(s-1)}| < k*2^{277}$$

where the constant k is independent of the value of s. For $s < 2^{277}$, this inequality is weak and provides very little support for the notion that these truncated x-coordinates are uniformly distributed. On the other hand, the larger the value of s, the sharper this inequality becomes, providing stronger evidence that the associated truncated x-coordinates are uniformly distributed. Therefore, by keeping truncation to an acceptable minimum, the performance is increased, and certain guarantees can be made about the uniform distribution of the resulting truncated quantities.

Appendix F: (Informative) Example Pseudocode for Each DRBG

The internal states in these examples are considered to be an array of states, identified by *state_handle*. A particular state is addressed as *internal_state* (*state_handle*), where the value of *state_handle* begins at 0 and ends at *n*-1, and *n* is the number of internal states provided by an implementation. A particular element in the internal state is addressed by *internal state* (*state_handle*).*element*.

The pseudocode in this annex does not include the necessary conversions (e.g., integer to bitstring) for an implementation. When conversions are required, they must be accomplished as specified in Appendix B.

The following routine is defined for these pseudocode examples:

Find_state_space (): A function that finds an unused internal state. The function returns a *status* (either "Success" or a message indicating that an unused internal state is not available) and, if *status* = "Success", a *state_handle* that points to an available *internal_state* in the array of internal states. If *status* ≠ "Success", an invalid *state handle* is returned.

When the uninstantantiate function is invoked in the following examples, the function specified in Section 9.4 is called.

F.1 Hash DRBG Example

This example of **Hash_DRBG** uses the SHA-1 hash function, and prediction resistance is supported in the example. Both a personalization string and additional input are allowed. A 32-bit incrementing counter is used as the nonce for instantiation (*instantiation_nonce*); the nonce is initialized when the DRBG is installed (e.g., by a call to the clock or by setting it to a fixed value) and is incremented for each instantiation.

A total of 10 internal states are provided (i.e., 10 instantiations may be handled simultaneously).

For this implementation, the functions and algorithms are "inline", i.e., the algorithms are not called as separate routines from the function envelopes.

The internal state contains values for V, C, $previous_output_block$, $reseed_counter$, $security_strength$ and $prediction_resistance_flag$, where V and C are bitstrings, and $reseed_counter$, $security_strength$ and the $prediction_resistance_flag$ are integers. A requested prediction resistance capability is indicated when $prediction_resistance_flag = 1$. Note: an empty internal state is represented as $\{Null, Null, 0, 0, 0, 0\}$.

In accordance with Table 2 in Section 10.1, the 112 and 128 bit security strengths may be supported. Using SHA-1, the following definitions are applicable for the instantiate, generate and reseed functions and algorithms:

1. highest supported security strength = 128.

- 2. Output block length (outlen) = 160 bits.
- 3. Required minimum entropy for instantiation and reseed = security strength.
- 4. Minimum entropy input length (min_length) = security_strength.
- 5. Seed length (seedlen) = 440 bits.
- Maximum number of bits per request (max_number_of_bits_per_request) = 5000 bits.
- 7. Reseed interval (reseed interval) = 100,000 requests.
- 8. Maximum length of the personalization string (max_personalization_string_length) = 512 bits.
- 9. Maximum length of additional_input (max_additional_input_string_length) = 512 bits.
- 10. Maximum length of entropy input (max length) = 1000 bits.

F.1.1 Instantiation of Hash_DRBG

This implementation will return a text message and an invalid state handle (-1) when an error is encountered. Note that the value of *instantiation_nonce* is an internal value that is always available to the instantiate function.

Note that this implementation does not check the *prediction_resistance_flag*, since the implementation can handle prediction resistance. However, if an application actually wants prediction resistance, the implementation expects that *prediction_resistance_flag* = 1 during instantiation; this will be used in the generate function in Appendixx F.1.3.

Instantiate_Hash_DRBG (...):

Input: integer (requested_instantiation_security_strength, prediction_resistance_flag), bitstring personalization_string).

Output: string status, integer state_handle.

Process:

Comment: Check the input parameters.

- If (requested_instantiation_security_strength > 128), then Return ("Invalid requested instantiation security strength", -1).
- 2. If (len (personalization_string) > 512), then Return ("Personalization_string too long", -1).

Comment: Set the *security_strength* to one of the valid security strengths.

3. If (requested instantiation_security strength \leq 112), then security strength =

112

Else security strength = 128.

Comment: Get the entropy input.

- 4. (status, entropy_input) = Get_entropy (security_strength, security_strength, 1000).
- 5. If (status ≠ "Success"), then **Return** ("Failure indication returned by the *entropy input* source:" || status, -1).

Comment: Increment the nonce; actual coding must ensure that it wraps when it's storage limit is reached.

6. instantiation nonce = instantiation nonce +1.

Comment: The instantiate algorithm is provided in steps 7-14.

- 7. seed_material = entropy_input || instantiation_nonce || personalization_string.
- 8. $seed = Hash_df (seed_material, 440)$.
- 9. V = seed.
- 10. C =**Hash df** ((0x00 || V), 440).

Comment: Generate the initial block for comparing with the first DRBG output block (for continuous testing).

- 11. $previous_output_block = V$.
- 12. H =**Hash** $(0x03 \parallel V)$.
- 13. $V = (V + H + C + 1) \mod 2^{seedlen}$.
- 14. reseed counter = 2.

Comment: Find an unused internal state and save the initial values.

- 15. (status, state handle) = Find_state_space().
- 16. If ($status \neq$ "Success"), then **Return** (status, -1).
- 17. internal_state (state_handle) = {V, C, previous_output_block, reseed_counter, security_strength, prediction_resistance_flag}.
- 18. Return ("Success", state handle).

F.1.2 Reseeding a Hash_DRBG Instantiation

The implementation is designed to return a text message as the *status* when an error is

encountered.

Reseed Hash DRBG Instantiation (...):

Input: integer state handle, bitstring additional input.

Output: string status.

Process:

Comment: Check the validity of the state handle.

1. If ((state_handle < 0) or (state_handle > 9) or (internal_state (state_handle) = {Null, Null, Null, 0, 0, 0})), then **Return** ("State not available for the state handle").

Comment: Get the internal state values needed to determine the new internal state.

2. Get the appropriate internal_state values, e.g., V = internal_state(state_handle).V, security_strength = internal_state(state_handle).security_strength.

Check the length of the additional_input.

3. If (len (additional_input) > 512), then Return ("Additional_input too long").

Comment: Get the entropy input.

- 4. (status, entropy_input) = Get_entropy (security_strength, security_strength, 1000).
- 5. If (status ≠ "Success"), then **Return** ("Failure indication returned by the entropy_input source:" || status).

Comment: The reseed algorithm is provided in steps 6-10.

- 6. $seed_material = 0x01 \parallel V \parallel entropy_input \parallel additional_input$.
- 7. seed = Hash df (seed material, 440).
- 8. V = seed.
- 9. $C = \text{Hash_df}((0x00 \parallel V), 440)$.
- 10. $reseed\ counter = 1$.

Comment: Update the *working_state* portion of the internal state.

- 11. Update the appropriate state values.
 - 11.1 $internal_state$ ($state_handle$). V = V.

- 11.2 internal state (state handle). C = C.
- 11.3 internal state (state handle).reseed counter = reseed counter.
- 12. Return ("Success").

F.1.3 Generating Pseudorandom Bits Using Hash_DRBG

The implementation returns a Null string as the pseudorandom bits if an error has been detected. Prediction resistance is requested when prediction resistance request = 1.

In this implementation, prediction resistance is requested by supplying *prediction_resistance_request* = 1 when the **Hash_DRBG** function is invoked.

Hash_DRBG (...):

Input: integer (state_handle, requested_no_of bits, requested_security_strength, prediction_resistance_request), bitstring additional_input.

Output: string status, bitstring pseudorandom bits.

Process:

Comment: Check the validity of the state handle.

If ((state_handle < 0) or (state_handle > 9) or (state (state_handle) = {Null, Null, Null, 0, 0, 0})), then Return ("State not available for the state_handle", Null).

Comment: Get the internal state values.

2. V = internal_state (state_handle).V, C = internal_state (state_handle).C, previous_output_block = internal_state (state_handle).previous_output_block, reseed_counter = internal_state (state_handle).reseed_counter, security_strength = internal_state (state_handle).security_strength, prediction_resistance_flag = internal_state (state_handle).prediction_resistance_flag.

Comment: Check the validity of the other input parameters.

- If (requested_no_of_bits > 5000) then Return ("Too many bits requested", Null).
- 4. If (requested_security_strength > security_strength), then **Return** ("Invalid requested security strength", Null).
- If (len (additional_input) > 512), then Return ("Additional_input too long", Null).
- 6. If ((prediction_resistance_request = 1) and (prediction_resistance_flag ≠ 1)), then **Return** ("Prediction resistance capability not instantiated", Null).

Comment: Reseed if necessary. Note that since the instantiate algorithm is inline with the functions, this step has been written as a combination of steps 6 and 7 of Section 9.3 and step 1 of the generate algorithm in Section 10.1.1.4. Because of this combined step, step 9 of Section 9.3.is not required.

- 7. If $((reseed_counter > 100,000) \text{ OR } (prediction_resistance_request = 1))$, then
 - 7.1 status = Reseed_ Hash_DRBG_Instantiation (state_handle, additional_input).
 - 7.2 If (status ≠ "Success"), then **Return** (status, Null).

Comment: Get the new internal state values that have changed.

- 7.3 V = internal_state (state_handle).V, C = internal_state (state_handle).C, reseed_counter = internal_state (state_handle).reseed_counter.
- 7.4 additional input = Null.

Comment: Steps 8-16 provide the rest of the generate algorithm. Note that in this implementation, the **Hashgen** routine is also inline as steps 9-13.

- 8. If $(additional_input \neq Null)$, then do
 - 7.1 w =**Hash** $(0x02 || V || additional_input).$

7.2
$$V = (V + w) \mod 2^{440}$$
.

9.
$$m = \left\lceil \frac{requested_no_of_bits}{outlen} \right\rceil$$
.

- 10. data = V.
- 11. W = the Null string.
- 12. For i = 1 to m
 - 12.1 $w_i = \mathbf{Hash} (data)$.
 - 12.2 If $(w_i = previous_output_block)$, then **Return** ("Fatal error: output blocks match", *Null*).
 - 12.3 previous output block = w_i .
 - 12.4 $W = W || w_i$.
 - 12.5 $data = (data + 1) \mod 2^{seedlen}$.

- 13. pseudorandom_bits = Leftmost (requested_no_of_bits) bits of W.
- 14. H = Hash (0x03 || V).
- 15. $V = (V + H + C + reseed \ counter) \mod 2^{440}$.
- 16. $reseed\ counter = reseed\ counter + 1$.

Comments: Update the working state.

- 13. Update the changed values in the state.
 - 13.1 internal state (state handle). V = V.
 - 13.2 internal_state (state_handle).previous_output_block = previous_output_block.
 - 13.3 internal state (state handle).reseed counter = reseed counter.
- 14. Return ("Success", pseudorandom bits).

F.2 HMAC_DRBG Example

This example of **HMAC_DRBG** uses the SHA-256 hash function. Reseeding and prediction resistance are not provided. The nonce for instantiation consists of a random value with *security_strength*/2 bits of entropy; the nonce is obtained by increasing the call for entropy bits via the **Get_entropy** call by *security_strength*/2 bits (i.e., by adding *security_strength*/2 bits to the *security_strength* value).

A personalization string is allowed, but additional input is not. A total of 3 internal states are provided. For this implementation, the functions and algorithms are written as separate routines.

The internal state contains the values for V, Key, reseed_counter, and security_strength, where V and C are bitstrings, and reseed_counter and security_strength are integers.

In accordance with Table 2 in Section 10.1, security strengths of 112, 128, 192 and 256 may supported. Using SHA-256, the following definitions are applicable for the instantiate and generate functions and algorithms:

- 1. highest supported security strength = 256.
- 2. Output block (outlen) = 256 bits.
- 3. Required minimum entropy for the entropy input at instantiation = 3/2 *security strength* (this includes the entropy required for the nonce).
- 4. Minimum entropy input length (*min _length*) = 3/2 *security_strength* (this includes the minimum length for the nonce).
- 5. Seed length (seedlen) = 440 bits.
- 6. Maximum number of bits per request (max_number_of_bits_per_request) = 7500 bits.

- 7. Reseed interval (reseed interval) = 10,000 requests.
- 8. Maximum length of the personalization string (max_personalization_string_length) = 160 bits.
- 9. Maximum length of the entropy input $(max \ length) = 1000$ bits.

F.2.1 Instantiation of HMAC_DRBG

This implementation will return a text message and an invalid state handle (-1) when an error is encountered.

Instantiate HMAC DRBG (...):

Input: integer (requested_instantiation_security_strength), bitstring personalization_string.

Output: string status, integer state_handle.

Process:

Check the validity of the input parameters.

- 1. If (requested_instantiation_security_strength > 256), then **Return** ("Invalid requested instantiation security strength", -1).
- 2. If (len (personalization_string)>160), then Return ("Personalization_string too long", -1)

Comment: Set the *security_strength* to one of the valid security strengths.

If (requested_security_strength ≤ 112), then security_strength = 112
 Else (requested_security_strength ≤ 128), then security_strength = 128
 Else (requested_security_strength ≤ 192), then security_strength = 192
 Else security_strength = 256.

Comment: Get the *entropy_input* and the nonce.

- 4. $min\ entropy = 1.5 \times security\ strength$.
- 5. (status, entropy input) = Get entropy (min entropy, min entropy, 1000).
- 6. If (status ≠ "Success"), then **Return** ("Failure indication returned by the entropy source:" || status, -1).

Comment: Invoke the instantiate algorithm. Note that the *entropy_input* contains the nonce.

7. (V, Key, reseed_counter) = Instantiate_algorithm (entropy_input,

personalization_string).

Comment: Find an unused internal state and save the initial values.

- 8. (status, state_handle) = Find_state_space().
- 9. If (status ≠ "Success"), then **Return** ("No available state space:" || status, -1).
- 10. internal state (state handle) = $\{V, Key, reseed counter, security strength\}$.
- 11. Return ("Success" and state_handle).

Instantiate_algorithm (...):

Input: bitstring (entropy input, personalization string).

Output: bitstring (V, Key), integer reseed_counter.

Process:

- 1. seed material = entropy input || personalization string.
- 2. Set Key to outlen bits of zeros.
- 3. Set V to outlen/8 bytes of 0x01.
- 4. (Key, V) = Update (seed material, Key, V).
- 5. $V = \mathbf{HMAC} (Key, V)$.
- 6. (Key, V) = Update (seed material, Key, V).
- 7. $reseed\ counter = 1$.
- 8. Return (V, Key, reseed_counter).

F.2.2 Generating Pseudorandom Bits Using HMAC_DRBG

The implementation returns a Null string as the pseudorandom bits if an error has been detected. This function uses the Update function specified in Section 10.1.2.2, and the Uninstantiate function in Section 9.4.

HMAC_DRBG(...):

Input: integer (state_handle, requested_no_of_bits, requested_security_strength).

Output: string (status), bitstring pseudorandom_bits.

Process:

Comment: Check for a valid state handle.

1. If ((state handle < 0) or (state handle > 3) or (internal_state (state handle) = {Null, Null, 0, 0}), then Return ("State not available for the indicated state_handle", Null).

Comment: Get the internal state.

2. V = internal_state (state_handle).V, Key = internal_state (state_handle).Key, security_strength = internal_state (state_handle).security_strength, reseed counter = internal_state (state_handle).reseed counter.

Comment: Check the validity of the rest of the input parameters.

- If (requested_no_of_bits > 7500), then Return ("Too many bits requested", Null).
- 4. If (requested_security_strength > security_strength), then **Return** ("Invalid requested security strength", Null).

Comment: Invoke the generate algorithm.

- 6. (status, pseudorandom_bits, V, Key, reseed_counter) = Generate_algorithm (V, Key, reseed counter, requested number of bits).
- 7. If (status = "Reseed required"), then **Return** ("DRBG can no longer be used. Please re-instantiate or reseed", Null).
- 8. If (status = "ERROR: outputs match"), then
 - 8.1 For i = 0 to 3, do
 - 8.1.1 status = Uninstantiate(i).
 - 8.1.2 If (status ≠ "Success"), then **Return** ("DRBG FAILURE: Successive outputs match, and uninstantiate failed", Null).
 - 8.2 Return ("DRBG" || status, Null).

Comment: Update the internal state.

- 9. internal_state (state_handle) = {V, Key, security_strength, reseed_counter}.
- 10. Return ("Success", pseudorandom bits).

Generate_algorithm (...):

Input: bitstring (*V*_old, *Key*), integer (reseed_counter, requested_number_of_bits). **Output**: string status, bitstring (pseudorandom_bits, *V*, *Key*), integer reseed_counter. **Process**:

- 1 If (reseed_counter ≥ 10,000), then **Return** ("Reseed required", Null, V, Key, reseed counter).
- 2. temp = Null.
- 3 While (len (temp) < requested_no of bits) do:
 - 3.1 $V = \mathbf{HMAC}(Key, V)$.

- 3.2 If $(V = V_old)$, then **Return** ("ERROR: outputs match", *Null*, *V*, *Key*, *reseed_counter*).
- 3.3 V old = V.
- 3.4 temp = temp || V.
- 4. pseudorandom bits = Leftmost (requested no of bits) of temp.
- 5. $(Key, V) = \mathbf{Update}$ (additional input, Key, V).
- 6. $reseed_counter = reseed_counter + 1$.
- 7. **Return** ("Success", pseudorandom_bits, V, Key, reseed_counter).

F.3 CTR DRBG Example Using a Derivation Function

This example of CTR_DRBG uses AES-128. The reseed and prediction resistance capabilities are available, and a block cipher derivation function using AES-128 is used. Both a personalization string and additional input are allowed. A total of 5 internal states are available. For this implementation, the functions and algorithms are written as separate routines. The Block Encrypt function uses AES-128 in the ECB mode.

The nonce for instantiation (*instantiation_nonce*) consists of a 32-bit incrementing counter. The nonce is initialized when the DRBG is installed (e.g., by a call to the clock or by setting it to a fixed value) and is incremented for each instantiation.

The internal state contains the values for V, Key, $previous_output_block$, $reseed_counter$, and $security_strength$, where V, Key and $previous_output_block$ are strings, and all other values are integers. Since prediction resistance is always available, there is no need for $prediction\ resistance\ flag\ in$ the internal state.

In accordance with Table 3 in Section 10.2.1, security strengths of 112 and 128 may be supported. Using AES-128, the following definitions are applicable for the instantiate, reseed and generate functions:

- 1. highest_supported_security_strength = 128.
- 2. Output block length (outlen) = 128 bits.
- 3. Key length (keylen) = 128 bits.
- 4. Required minimum entropy for the entropy input at instantiate and reseed = *security strength*.
- 5. Minimum entropy input length (min length) = security strength bits.
- 6. Maximum entropy input length (max length) = 1000 bits.
- 7. Maximum personalization string input length (max personalization string input length) = 800 bits.
- 8. Maximum additional input length (max_additional_input_length) = 800 bits.

- 9. Seed length (seedlen) = 256 bits.
- 10. Maximum number of bits per request (max_number of bits per_request) = 4000
- 11. Reseed interval (reseed interval) = 100,000 requests. Note that for this value, the instantiation count will not repeat during the reseed interval.

F.3.1 The Update Function

Update (...):

Input: bitstring (provided data, Key, V).

Output: bitstring (Key, V).

Process:

- 1. temp = Null.
- 2. While (len (temp) < 256) do
 - 3.1 $V = (V+1) \mod 2^{128}$.
 - 3.2 $output block = AES_ECB_Encrypt (Key, V)$.
 - 3.3 temp = temp || ouput block.
- 4. temp = Leftmost 256 bits of temp.
- 5 $temp = temp \oplus provided_data$.
- 6. Key = Leftmost 128 bits of temp.
- 7. V =Rightmost 128 bits of temp.
- 8. Return (Key, V).

F.3.2 Instantiation of CTR_DRBG Using a Derivation Function

This implementation will return a text message and an invalid state handle (-1) when an error is encountered. Block Cipher df is the derivation function in Section 9.5.2, and uses AES-128 in ECB mode as the **Block Encrypt** function.

Note that this implementation does not include the prediction resistance flag in the input parameters, nor save it in the internal state, since prediction resistance is always available.

Instantiate_CTR_DRBG (...):

Input: integer (requested instantiation security_strength), bitstring personalization string.

Output: string status, integer state handle.

Process:

Comment: Check the validity of the input

parameters.

- 1. If (requested_instantiation_security_strength > 128) then **Return** ("Invalid requested_instantiation_security_strength", -1).
- 2. If (len (personalization_string) > 800), then Return ("Personalization_string too long", -1).
- If (requested_instantiation_security_strength ≤ 112), then security_strength = 112

Else security strength = 128.

Comment: Get the entropy input.

- 4. (status, entropy_input) = **Get_entropy** (security_strength, security_strength, 1000).
- 5. If (*status* ≠ "Success"), then **Return** ("Failure indication returned by the entropy source" || *status*, -1).

Comment: Increment the nonce; actual coding must ensure that the nonce wraps when its storage limit is reached, and that the counter pertains to all instantiations, not just this one.

6. instantiation nonce = instantiation nonce + 1.

Comment: Invoke the instantiate algorithm.

7. (V, Key, previous_output_block, reseed_counter) = Instantiate_algorithm (entropy_input, instantiation_nonce, personalization_string).

Comment: Find an available internal state and save the initial values.

- 9. (status, state_handle) = Find_state_space ().
- 10. If (status ≠ "Success"), then **Return** ("No available state space:" || status, -1).

Comment: Save the internal state.

- 11. internal_state_(state_handle) = {V, Key, previous_output_block, reseed counter, security strength}.
- 12. Return ("Success", state_handle).

Instantiate_algorithm (...):

Input: bitstring (entropy_input, nonce, personalization_string).

Output: bitstring (*V*, *Key*), integer (*reseed counter*).

Process:

- 1. seed_material = entropy_input || nonce || personalization_string.
- 2. seed material = Block Cipher df (seed material, 256).

3. $Key = 0^{128}$.

Comment: 128 bits.

4. $V = 0^{128}$.

Comment: 128 bits.

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- 5. $(Key, V) = Update (seed_material, Key, V)$.
- 6. $reseed_counter = 1$.
- 7. previous_output_block = AES_ECB_Encrypt (Key, V).
- 8. $zeros = 0^{seedlen}$.

Comment: Produce a string of *seedlen* zeros.

- 9. (Key, V) = Update(zeros, Key, V).
- 10. Return (V, Key, previous output block, reseed counter).

F.3.3 Reseeding a CTR_DRBG Instantiation Using a Derivation Function

The implementation is designed to return a text message as the *status* when an error is encountered.

Reseed_CTR_DRBG_Instantiation (...):

Input: integer (state handle), bitstring additional input.

Output: string status.

Process:

Comment: Check for the validity of state handle.

1. If ((state_handle < 0) or (state_handle > 5) or (internal_state(state_handle) = {Null, Null, Null, 0, 0}), then **Return** ("State not available for the indicated state_handle").

Comment: Get the internal state values.

- 2. V = internal_state (state_handle).V, Key = internal_state (state_handle).Key, previous_output_block = internal_state (state_handle).previous_output_block, security_strength = internal_state (state_handle).security_strength.
- 3. If (len (additional input) > 800), then Return ("Additional input too long").
- 4. (status, entropy_input) = **Get_entropy** (security_strength, security_strength, 1000).
- 6. If (*status* ≠ "Success"), then **Return** ("Failure indication returned by the entropy source:" || *status*).

Comment: Invoke the reseed algorithm.

- 7. (V, Key, reseed_counter) = Reseed_algorithm (V, Key, reseed_counter, entropy input, additional input).
- 8. internal_state (state_handle) = {V, Key, previous_output_block, reseed_counter, security_strength}.
- 9. Return ("Success").

Reseed_algorithm (...):

Input: bitstring (V, Key), integer (reseed_counter), bitstring (entropy_input, additional_input).

Output: bitstring (V, Key), integer (reseed_counter).

Process:

- 1. seed material = entropy input || additional input.
- 2. seed material = Block Cipher df (seed material, 256).
- 3. (Key, V) = Update (seed material, Key, V).
- 4. $reseed\ counter = 1$.
- 5. Return V, Key, reseed counter).

F.3.4 Generating Pseudorandom Bits Using CTR_DRBG

The implementation returns a *Null* string as the pseudorandom bits if an error has been detected.

CTR DRBG(...):

Input: integer (state_handle, requested_no_of_bits, requested_security_strength, prediction_resistance_request), bitstring additional_input.

Output: string status, bitstring pseudorandom_bits.

Process:

Comment: Check the validity of state_handle.

1. If ((state_handle < 0) or (state_handle > 5) or (internal_state (state_handle) = {Null, Null, Null, 0, 0}), then **Return** ("State not available for the indicated state handle", Null).

Comment: Get the internal state.

V = internal_state (state_handle).V, Key = internal_state (state_handle).Key,
 previous_output_block = internal_state (state_handle).previous_output_block,
 security_strength = internal_state (state_handle).security_strength,
 reseed_counter = internal_state (state_handle).reseed_counter.

Comment: Check the rest of the input parameters.

- If (requested_no_of_bits > 4000), then Return ("Too many bits requested", Null).
- 4. If (requested_security_strength > security_strength), then Return ("Invalid requested_security_strength", Null).
- If (len (additional_input) > 800), then Return ("Additional_input too long", Null).
- 6. $reseed_required_flag = 0$.
- 7. If (reseed required flag = 1), then
 - 7.1 status = Reseed_CTR_DRBG_Instantiation (state_handle, additional input).
 - 7.2 If (status ≠ "Success"), then Return (status, Null).

Comment: Get the new working state values; the administrative information was not affected.

- 7.3 V = internal_state (state_handle).V, Key = internal_state (state_handle).Key, previous_output_block = internal_state (state_handle). previous_output_block, reseed_counter = internal_state (state_handle).reseed_counter.
- 7.4 additional_input = Null.
- 7.5 $reseed_required_flag = 0$.

Comment: Generate bits using the generate algorithm.

- 8. (status, pseudorandom_bits, V, Key, previous_output_block, reseed_counter) = Generate_algorithm (V, Key, previous_output_block, reseed_counter, requested_number_of_bits, additional_input).
- 9. If (status = "Reseed required"), then
 - 9.1 $reseed_required_flag = 1$.
 - 9.2 Go to step 7.
- 10. If (status = "ERROR: outputs match"), then
 - 10.1 For i = 0 to 5, do
 - 8.1.1 status = Uninstantiate(i).
 - 8.1.2 If (status ≠ "Success"), then **Return** ("DRBG FAILURE:

Successive outputs match, and uninstantiate failed", Null).

- 10.2 Return ("DRBG: " || status, Null).
- 11. internal_state (state_handle) = {V, Key, previous_output_block, security strength, reseed counter).
- 12. Return ("Success", pseudorandom bits).

Generate algorithm (...):

Input: bitstring (*V_old*, *Key_old*, *previous_output_block*), integer (*reseed_counter*, requested_number_of_bits) bitstring additional_input.

Output: string *status*, bitstring (*returned_bits*, *V*, *Key*, *previous_output_block*), integer *reseed counter*.

Process:

- 1. If (reseed_counter > 100,000), then **Return** ("Failure", Null, V, Key, previous output block, reseed counter).
- 2. If (additional input $\neq Null$), then
 - 2.1 $temp = len (additional_input)$.
 - 2.2 If (temp > 256), then additional_input = Block_Cipher_df (additional_input, 256).
 - 2.3 If (temp < 256), then $additional_input = additional_input || <math>0^{256-temp}$.
 - 2.4 $(Key, V) = Update (additional_input, Key_old, V_old).$
 - 2.5 If($(Key = Key_old)$) or $(V = V_old)$), then **Return** ("ERROR: outputs match", *Null*, V, Key, previous output block, reseed counter).
- 3. temp = Null.
- 4. While (len (temp) < requested number of bits) do:
 - 4.1 $V = (V+1) \mod 2^{128}$.
 - 4.2 output block = AES ECB Encrypt (Key, V).
 - 4.3 If (output_block = previous_output_block), then **Return** ("ERROR: outputs match", Null, V, Key, previous_output_block, reseed counter).
 - 4.4 previous output block = output block.
 - 4.5 $temp = temp || ouput_block.$
- 5. returned_bits = Leftmost (requested_number_of_bits) of temp.
- 6. $zeros = 0^{256}$. Comment: Produce a string of 256 zeros.

- 7. (Key, V) = Update(zeros, Key, V)
- 8. $reseed\ counter = reseed\ counter + 1$.
- 9. **Return** ("Success", returned_bits, V, Key, previous_output_block, reseed counter).

F.4 CTR DRBG Example Without a Derivation Function

This example of CTR_DRBG is the same as the previous example except that a derivation function is not used (i.e., full entropy is always available). As before the CTR_DRBG uses AES-128. The reseed and prediction resistance capabilities are available. Both a personalization string and additional input are allowed. A total of 5 internal states are available. For this implementation, the functions and algorithms are written as separate routines. The **Block_Encrypt** function uses AES-128 in the ECB mode.

The nonce for instantiation (*instantiation_nonce*) consists of a 32-bit incrementing counter that is prepended to the personalization string. The nonce is initialized when the DRBG is installed (e.g., by a call to the clock or by setting it to a fixed value) and is incremented for each instantiation.

The internal state contains the values for *V*, *Key*, *previous_output_block*, *reseed_counter*, and *security_strength*, where *V*, *Key* and *previous_output_block* are strings, and all other values are integers. Since prediction resistance is always available, there is no need for *prediction_resistance flag* in the internal state.

In accordance with Table 3 in Section 10.2.1, security strengths of 112 and 128 may be supported. The definitions are the same as those provided in Appendix F.3, except that the maximum size of the *personalization_string* is 224 bits in order to accommodate the 32-bits of the *instantiation_nonce* (i.e., len (*instantiation_nonce*) + len (*personalization_string*) must be \leq seedlen). In addition, the maximum size of any additional input is 256 bits (i.e., len (additional input \leq seedlen).

F.4.1 The Update Function

The update function is the same as that provided in Annex F.3.1.

F.4.2 Instantiation of CTR_DRBG Without a Derivation Function

This implementation will return a text message and an invalid state handle (-1) when an error is encountered.

Note that this implementation does not include the *prediction_resistance_flag* in the input parameters, nor save it in the internal state, since prediction resistance is always available.

Instantiate CTR DRBG (...):

Input: integer (requested_instantiation_security_strength), bitstring personalization_string.

Output: string status, integer state_handle.

Process:

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Comment: Check the validity of the input parameters.

- 1. If (requested_instantiation_security_strength > 128) then Return ("Invalid requested_instantiation_security_strength", -1).
- 2. If (len (personalization_string) > 224), then Return ("Personalization_string too long", -1).
- If (requested_instantiation_security_strength ≤ 112), then security_strength = 112

Else security strength = 128.

Comment: Get the entropy input.

- 4. (status, entropy_input) = **Get_entropy** (security_strength, security_strength, 1000).
- 5. If (status ≠ "Success"), then **Return** ("Failure indication returned by the entropy source" || status, -1).

Comment: Increment the nonce; actual coding must ensure that the nonce wraps when its storage limit is reached, and that the counter pertains to all instantiations, not just this one.

6. $instantiation_nonce = instantiation_nonce + 1$.

Comment: Invoke the instantiate algorithm.

- 7. personalization_string = instantiation_nonce || personalization_string.
- 8. (V, Key, previous_output_block, reseed_counter) = Instantiate_algorithm (entropy input, personalization string).

Comment: Find an available internal state and save the initial values.

- 9. (status, state_handle) = Find_state_space ().
- 10. If (status ≠ "Success"), then **Return** ("No available state space:" || status, -1).

Comment: Save the internal state.

- 11. internal_state_(state_handle) = {V, Key, previous_output_block, reseed_counter, security_strength}.
- 12. Return ("Success", state handle).

Instantiate_algorithm (...):

Input: bitstring (entropy input, nonce, personalization string).

Output: bitstring (V, Key), integer (reseed counter).

Process:

- 1. temp = len (personalization string).
- 2. If (temp < 256), then personalization_string = personalization_string $\parallel 0^{256\text{-temp}}$.
- 3. seed material = entropy input \oplus personalization string.
- 4. $Key = 0^{128}$. Comment: 128 bits.
- 5. $V = 0^{128}$.

Comment: 128 bits.

- 6. (Key, V) = Update (seed material, Key, V).
- 7. $reseed_counter = 1$.
- 8. previous output block = AES ECB_Encrypt (Key, V).
- 9. $zeros = 0^{seedlen}$.

Comment: Produce a string of seedlen zeros.

- 10. (Key, V) = Update (zeros, Key, V).
- 11. Return (V, Key, previous output block, reseed counter).

F.4.3 Reseeding a CTR_DRBG Instantiation Without a Derivation Function

The implementation is designed to return a text message as the *status* when an error is encountered.

Reseed_CTR_DRBG_Instantiation (...):

Input: integer (state handle), bitstring additional input.

Output: string status.

Process:

Comment: Check for the validity of state handle.

1. If ((state_handle < 0) or (state_handle > 5) or (internal_state(state_handle) = {Null, Null, Null, 0, 0}), then **Return** ("State not available for the indicated state_handle").

Comment: Get the internal state values.

- 2. V = internal_state (state_handle).V, Key = internal_state (state_handle).Key, previous_output_block = internal_state (state_handle).previous_output_block, security_strength = internal_state (state_handle).security_strength.
- 3. If (len (additional input) > 256), then Return ("Additional input too long").
- 4. (status, entropy input) = Get entropy (security strength, security strength,

1000).

6. If (status ≠ "Success"), then **Return** ("Failure indication returned by the entropy source:" || status).

Comment: Invoke the reseed algorithm.

7. (V, Key, reseed counter) = Reseed algorithm (V, Key, reseed counter, entropy input, additional input).

Comment: Save the new internal state.

- 8. internal state (state handle) = $\{V, Key, previous output block, \}$ reseed counter, security strength \.
- 9. Return ("Success").

Reseed algorithm (...):

Input: bitstring (*V*, *Key*), integer (*reseed_counter*), bitstring (*entropy_input*, additional input).

Output: bitstring (V, Key), integer (reseed counter).

Process:

- 1. temp = len (personalization string).
- 2. If (temp < 256), then personalization_string = personalization_string $\parallel 0^{256\text{-temp}}$.
- 3. $seed material = entropy input \oplus personalization string$.
- 4. (Key, V) =**Update** (seed material, Key, V).
- 5. $reseed\ counter = 1$.
- 6. Return ("Success", V, Key, reseed_counter).

F.4.4 Generating Pseudorandom Bits Using CTR_DRBG

The generate function is the same as that provided in Annex E.3.5.

F.5 Dual EC DRBG Example

This example of **Dual EC DRBG** allows a consuming application to instantiate using any of the four prime curves, depending on the security strength. A reseed capability is available, but prediction resistance is not available. Both a personalization string and an additional_input are allowed. A total of 10 internal states are provided. For this implementation, the algorithms are provided as inline code within the functions.

The nonce for instantiation (instantiation nonce) consists of a random value with security strength/2 bits of entropy; the nonce is obtained by a separate call to the Get entropy routine.

The internal state contains values for s, seedlen, p, a, b, n, P, Q, r_old, block_counter and

security_strength. In accordance with Table 4 in Section 10.3.1, security strengths of 112, 128, 192 and 256 may be supported. SHA-256 has been selected as the hash function. The following definitions are applicable for the instantiate, reseed and generate functions:

- 1. highest_supported security_strength = 256.
- 2. Output block length (outlen): See Table 4.
- 3. Required minimum entropy for the entropy input at instantiation and reseed = *security strength*.
- 4. Minimum entropy input length (min length): See Table 4.
- 5. Maximum entropy input length (max length) = 1000 bits.
- 6. Maximum personalization string length (max_personalization_string_length) = 800 bits.
- 7. Maximum additional input length (max additional input length) = 800 bits.
- 8. Seed length (seedlen): See Table 4.
- 9. Maximum number of bits per request (max_number_of_bits_per_request) = 1000 bits.
- 10. Reseed interval (reseed interval) = 10,000 blocks.

F.5.1 Instantiation of Dual_EC_DRBG

This implementation will return a test message and an invalid state handle (-1) when an **ERROR** is encountered. **Hash df** is specified in Section 9.5.1.

Instantiate Dual EC DRBG (...):

Input: integer (requested_instantiation_security_strength), bitstring personalization_string.

Output: string status, integer state handle.

Process:

Comment: Check the validity of the input parameters.

- 1. If (requested_instantiation_security_strength > 256) then **Return** ("Invalid requested_instantiation_security_strength", -1).
- 2. If (len (personalization_string) > 800), then Return ("personalization_string too long", -1).

Comment: Select the prime field curve in accordance with the requested_instantiation_security_strength

3. If (requested instantiation security strength ≤ 112), then

```
{security_strength = 112; seedlen = 224; outlen = 208; min_entropy_input_len = 224}
```

Else if (requested instantiation security strength \leq 128), then

```
{security_strength = 128; seedlen = 256; outlen = 240; min_entropy_input_len = 256}
```

Else if (requested_instantiation_security_strength \leq 192), then

```
{security_strength = 192;, seedlen = 384; outlen = 368;
min entropy input_len = 384}
```

Else {security_strength = 256;, seedlen = 521; outlen = 504; min entropy input len = 528}.

4. Select elliptic curve P-seedlen from Annex A to obtain the domain parameters p, a, b, n, P, and Q.

Comment: Request entropy input.

- 5. (status, entropy_input) = Get_entropy (security_strength, min_entropy_input_length, 1000).
- 6. If (status ≠ "Success"), then **Return** ("Failure indication returned by the entropy_input source:" || status, -1).
- 7. (status, instantiation_nonce) = **Get_entropy** (security_strength/2, security_strength/2, 1000).
- 8. If (*status* ≠ "Success"), then **Return** ("Failure indication returned by the random nonce source:" || *status*, -1).

Comment: Perform the instantiate algorithm.

9. seed_material = entropy_input || instantiation_nonce || personalization_string.

$$10. s =$$
Hash df (seed material, seedlen).

- 11. $r \ old = \varphi(x(s * Q))$.
- 12. $block_counter = 0$.

Comment: Find an unused internal state and save the initial values.

- 13. (status, state_handle) = Find_state_space ().
- 14. If ($status \neq$ "Success"), then **Return** (status, -1).
- 15. internal_state (state_handle) = {s, seedlen, p, a, b, n, P, Q, r_old, block counter, security strength}.

16. Return ("Success", state_handle).

F.5.2 Reseeding a Dual_EC_DRBG Instantiation

The implementation is designed to return a text message as the status when an error is encountered.

Reseed_Dual_EC_DRBG_Instantiation (...):

Input: integer *state_handle*, string *additional_input_string*.

Output: string status.

Process:

Comment: Check the input parameters.

- 1. If ((state_handle < 0) or (state_handle > 10) or (internal_state (state handle).security strength = 0)), then Return ("State not available for the state handle").
- 2. If (len (additional input) > 800), then Return ("Additional input too long").

Comment: Get the appropriate state values for the indicated state handle.

3. $s = internal_state$ (state_handle).s, seedlen = internal_state (state handle).seedlen, security strength = internal state (state handle) security strength.

> Comment: Request new entropy input with the appropriate entropy and bit length.

- 3. (status, entropy input) = Get entropy (security strength, min entropy input length, 1000).
- 4. If (status ≠ "Success"), then **Return** ("Failure indication returned by the entropy source:" || status).

Comment: Perform the reseed algorithm.

- 5. $seed_material = pad8(s) \parallel entropy_input \parallel additional_input.$
- 6. s =**Hash df** (seed material, seedlen).

Comment: Update the changed values in the

- 7. $internal_state\ (state_handle).s = s$.
- 8. internal state.block counter = 0.
- 9. Return ("Success").

F.5.3 Generating Pseudorandom Bits Using Dual_EC_DRBG

The implemenation returns a *Null* string as the pseudorandom bits if an error is encountered.

Dual_EC DRBG (...):

Input: integer (state_handle, requested_security_strength, requested_no_of_bits), bitstring additional_input.

Output: string status, bitstring pseudorandom bits.

Process:

Comment: Check for an invalid state handle.

1. If ((state_handle < 0) or (state_handle > 10) or (internal_state (state_handle) = 0)), then **Return** ("State not available for the state handle", Null).

Comment: Get the appropriate *state* values for the indicated *state* handle.

 s = internal_state (state_handle).s, seedlen = internal_state (state_handle).seedlen, P = internal_state (state_handle).P, Q = internal_state (state_handle).Q, r_old = internal_state (state_handle).r_old, block_counter = internal_state (state_handle).block_counter.

Comment: Check the rest of the input parameters.

- 3. If (requested_number_of_bits > 1000), then **Return** ("Too many bits requested", Null).
- 4. If (requested_security_strength > security_strength), then **Return** ("Invalid requested strength", Null).
- 5. If (len (additional_input) > 800), then Return ("Additional_input too long", Null).

Comment: Check whether a reseed is required.

- 6. If $(block_counter + \left\lceil \frac{requested_number_of_bits}{outlen} \right\rceil > 10,000)$, then
 - 6.1 **Reseed_Dual_EC_DRBG_Instantiation** (state_handle, additional input).
 - 6.2 If ($status \neq$ "Success"), then **Return** (status).
 - 6.3 s = internal state (state handle).s, block counter = internal state

(state_handle).block_counter.

6.4 additional input = Null.

Comment: Execute the generate algorithm.

7. If (additional input = Null) then additional input = 0

Comment: additional_input set to m zeroes.

Else additional_input = Hash_df (pad8 (additional_input), seedlen).

Comment: Produce requested_no_of_bits, outlen bits at a time:

- 8. temp = the Null string.
- 9. i = 0.
- 10. $t = s \oplus additional input$.
- 11. $s = \varphi(x(t * P)).$
- $12. r = \varphi(x(s * Q)).$
- 13. If $(r = r_old)$, then **Return** ("ERROR: outputs match", *Null*).
- 14. $r_old = r$.
- 15. $temp = temp \parallel (rightmost outlen bits of r)$.
- 16. additional_input=0^{seedlen}. Comment: seedlen zeroes; additional_input is added only on the first iteration.
- 17. $block\ counter = block\ counter + 1$.
- 18. i = i + 1.
- 19. If (len (temp) < requested_no_of_bits), then go to step 10.
- 20. $pseudorandom_bits = Truncate (temp, i \times outlen, requested_no_of_bits).$

Comment: Update the changed values in the *state*.

- 21. $internal_state.s = s$.
- 22. $internal_state.r_old = r_old.$
- 23. internal state.block counter = block counter.
- 24. Return ("Success", pseudorandom bits).

Appendix G: (Informative) DRBG Selection

Almost no application or system designer starts with the primary purpose of generating good random bits. Instead, he typically starts with some goal that he wishes to accomplish, then decides on some cryptographic mechanisms, such as digital signatures or block ciphers that can help him achieve that goal. Typically, as he begins to understand the requirements of those cryptographic mechanisms, he learns that he will also have to generate some random bits, and that this must be done with great care, or he may inadvertently weaken the cryptographic mechanisms that he has chosen to implement. At this point, there are two things that may guide the designer's choice of a DRBG:

- a. He may already have decided to include a set of cryptographic primitives as part of his implementation. By choosing a DRBG based on one of these primitives, he can minimize the cost of adding that DRBG. In hardware, this translates to lower gate count, less power consumption, and less hardware that must be protected against probing and power analysis. In software, this translates to fewer lines of code to write, test, and validate.
 - For example, a module that generates RSA signatures has available some kind of hashing engine, so a hash-based DRBG is a natural choice.
- b. He may already have decided to trust a block cipher, hash function, keyed hash function, etc., to have certain properties. By choosing a DRBG based on similar properties, he can minimize the number of algorithms he has to trust.
 - For example, an AES-based DRBG might be a good choice when a module provides encryption with AES. Since the DRBG is based for its security on the strength of AES, the module's security is not made dependent on any additional cryptographic primitives or assumptions.
- c. Multiple cryptographic primitives may be available within the system or application, but there may be restrictions that need to be addressed (e.g.,code size or performance requirements).

The DRBGs specified in this Standard have different performance characteristics, implementation issues, and security assumptions.

G.1 Hash_DRBG

[Need to insert text here]

G.2 HMAC_DRBG

HMAC_DRBG is a DRBG built around the use of some approved hash function in the HMAC construction. To generate pseudorandom bits from a secret key (*Key*) and a starting value *V*, the DRBG computes

 $V = \mathbf{HMAC} (Kev, V).$

At the end of a generation request, the DRBG regenerates Key and V, each requiring one HMAC computation.

Security. The security of HMAC_DRBG is based on the assumption that an approved hash function used in the HMAC construction is a pseudorandom function family. Informally, this just means that when an attacker doesn't know the key used, HMAC outputs look random, even given knowledge and control over the inputs. In general, even relatively weak hash functions seem to be quite strong when used in the HMAC construction. On the other hand, there is not a reduction proof from the hash function's collision resistance properties to the security of the DRBG; the security of HMAC_DRBG depends on the security of the underlying hash function, but it is possible, in principle, for HMAC_DRBG to be broken by someone who cannot find collisions or preimages for the underlying hash function. [That said, the pseudorandomness of HMAC is a widely used assumption in designing cryptographic protocols.

Performance. HMAC_DRBG produces pseudorandom outputs considerably more slowly than the underlying hash function processes inputs; for SHA-256, a long generate request produces output bits at about 1/4 of the rate that the hash function can process input bits. Each generate request also involves additional overhead equivalent to processing 2048 extra bits with SHA-256. Note, however, that hash functions are typically quite fast; few if any applications are expected to need output bits faster than **HMAC_DRBG** can provide them.

Resources. Any entropy input source may be used with **HMAC_DRBG**, as it uses HMAC to process all its inputs. **HMAC_DRBG** requires access to a hashing engine or an HMAC implementation, and the storage space required for the internal state (see Section 10.1.2.1.

Algorithm Choices. The choice of algorithms that may be used by **HMAC_DRBG** is discussed in Section 10.1.

G.3 CTR_DRBG

CTR_DRBG is a DRBG based on using an Approved block cipher in counter mode. At the time of this writing, only three-key TDEA and AES are approved for use within ANS X9.82. Pseudorandom outputs are generated by encrypting successive values of a counter; after a generate request, a new key and new starting counter value are generated.

Security. The security of **CTR_DRBG** is directly based on the security of the underlying block cipher, in the sense that, so long as some limits on the total number of outputs are observed, any attack on **CTR_DRBG** represents an attack on the underlying block cipher.

Constraints on Outputs. For shown in Table 3 of Section 10.2.1, for each of the three AES key sizes, up to 2⁴⁸ generate requests may be made, each of up to 2¹⁹ bits, with a negligible chance of any weakness that does not represent a weakness in AES. However, the smaller block size of TDEA imposes more constraints; each generate request is limited

to 2¹³ bits, and at most 2³² such requests may be made.

Performance. For large generate requests, **CTR_DRBG** produces outputs at the same speed as the underlying block cipher encrypts data. Furthermore, **CTR_DRBG** is parallelizeable. At the end of each generate request, work equivalent to 2, 3 and 4 block encryptions is done to derive new keys and counters for the next generation request.

Resources. CTR_DRBG is ideal for situations in which 1) prediction resistance is often required, and 2) an Approved entropy source or another RBG is readily available to provide entropy input so that a derivation function is not required. Without the readily available source of entropy input, a derivation function must be used each time additional entropy input is required, thus slowing down the random bit generation process. For instantiation and reseeding without frequent requests for prediction resistance, however, the use of a derivation function should not lead to an important performance penalty, since both these operations are done only very rarely. CTR_DRBG implementations may also suffer a substantial performance penalty if they process additional input with generate requests, since the derivation function may be required in this case as well, unless the length of the additional input is limited to be less than or equal to the seed length (seedlen). CTR_DRBG requires access to a block cipher engine, including the ability to change keys, and the storage space required for the internal state (see Section 10.2.1.1).

Algorithm Choices. . The choice of algorithms that may be used by **CTR_DRBG** is discussed in Section 10.2.1.

G.4 DRBGs Based on Hard Problems

The **Dual_EC_DRBG** bases its security on a "hard" number-theoretic problem. For the types of curves used in the **Dual_EC_DRBG**, the Elliptic Curve Discrete Logarithm Problem has no known attacks that are better than the "meet-in-the-middle" attacks, with a work factor of sqrt (2^m) .

This algorithm is decidedly less efficient to implement than the other DRBGs. However, in those cases where security is the utmost concern, as in SSL or IKE exchanges, the additional complexity is not usually an issue. Except for dedicated servers, time spent on the exchanges is just a small portion of the computational load; overall, there is no impact on throughput by using a number-theoretic algorithm. As for SSL or IPSEC servers, more and more of these servers are getting hardware support for cryptographic primitives like modular exponentiation and elliptic curve arithmetic for the protocols themselves. Thus, it makes sense to utilize those same primitives (in hardware or software) for the sake of high-security random numbers.

Implementation Considerations

Random bits are produced in blocks of bits representing the x-coordinates on an elliptic curve.

Because of the various security strengths allowed by this Standard there are multiple curves available, with differing block sizes. The size is always a multiple of 8, about 16

bits less than a curve's underlying field size. Blocks are concatenated and then truncated, if necessary, to fullfil a request for any number of bits up to a maximum per call of 10,000 times the block length. The smallest blocksize is 216, meaning that at least 2M bits can be requested on each call.)

An important detail concerning the **Dual_EC_DRBG** is that every call for random bits, whether it be for 2 million bits or a single bit, requires that at least one full block of bits be produced; no unused bits are saved internally from the previous call. Each block produced requires two point multiplications on an elliptic curve—a fair amount of computation. Applications such as IKE and SSL are encouraged to aggregate all their needs for random bits into a single call to **Dual_EC_DRBG**, and then parcel out the bits as required during the protocol exchange. A C language structure, for example, is an ideal vehicle for this.

To avoid unnecessarily complex implementations, note that *every* curve in the Standard need not be available to an application. To improve efficiency, there has been much research done on the implementation of elliptic curve arithmetic; descriptions and source code are available in the open literature.

As a final comment on the implementation of the **Dual_EC_DRBG**, note that having fixed base points offers a distinct advantage for optimization. Tables can be precomputed that allow n^p to be attained as a series of point additions, resulting in an 8 to 10-fold speedup, or more, if space permits.

Appendix H: (Informative) References

Federal Information Processing Standard 140-2, Security Requirements for Cryptographic Modules, May 25, 2001.

Federal Information Processing Standard 180-2, Secure Hash Standard (SHS), August 2002.

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