Machine Problem 3 Report

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Minimax

Initial State

, ,	, ,	, ,	, ,
, ,	'B'	'W'	, ,
, ,	'W'	'B'	, ,
, ,	, ,	, ,	, ,

1. ('B', 0, 2)

, ,	, ,	'B'	, ,
, ,	'B'	'B'	, ,
, ,	'W'	'B'	, ,
, ,	, ,	, ,	, ,

2. ('W', 0, 3)

, ,	, ,	'B'	'W'
, ,	'B'	'W'	, ,
, ,	'W'	'B'	, ,
, ,	, ,	, ,	, ,

3. ('B', 1, 3)

, ,	, ,	'B'	'W'
, ,	'B'	'B'	'B'
, ,	'W'	'B'	, ,
, ,	, ,	, ,	, ,

4. ('W', 2, 3)

, ,	, ,	'B'	'W'
, ,	'B'	'B'	'W'
, ,	'W'	'W'	'W'

5. ('B', 3, 2)

, ,	, ,	'B'	'W'
, ,	'B'	'B'	'W'
, ,	'W'	'B'	'W'
, ,	, ,	'B'	, ,

6. ('W', 0, 1)

, ,	'W'	'W'	'W'
, ,	'W'	'W'	'W'
, ,	'W'	'B'	'W'
, ,	, ,	'B'	, ,

7. ('B', 1, 0)

, ,	'W'	'W'	'W'
'B'	'W'	'W'	'W'
, ,	'B'	'B'	'W'
, ,	, ,	'B'	, ,

8. ('W', 3, 0)

, ,	'W'	'W'	'W'
'B'	'W'	'W'	'W'
, ,	'W'	'B'	'W'
'W'	, ,	'B'	, ,

9. ('B', 0, 0)

'B'	'W'	'W'	'W'
'B'	'B'	'W'	'W'
, ,	'W'	'B'	'W'
'W'	, ,	'B'	, ,

10. ('W', 2, 0)

'B'	'W'	'W'	'W'
'B'	'W'	'W'	'W'
'W'	'W'	'B'	'W'
'W'	, ,	'B'	, ,

11. ('W', 3, 3)

'B'	'W'	'W'	'W'
'B'	'W'	'W'	'W'
'W'	'W'	'W'	'W'
'W'	, ,	'B'	'W'

12. ('W', 3, 1)

'B'	'W'	'W'	'W'
'B'	'W'	'W'	'W'
'W'	'W'	'W'	'W'
'W'	'W'	'W'	'W'

Terminal State

'B'	'W'	'W'	'W'
'B'	'W'	'W'	'W'
'W'	'W'	'W'	'W'
'W'	'W'	'W'	'W'

Results

(-12, [('B', 0, 2), ('W', 0, 3), ('B', 1, 3), ('W', 2, 3), ('B', 3, 2), ('W', 0, 1), ('B', 1, 0), ('W', 3, 0), ('B', 0, 0), ('W', 2, 0), ('W', 3, 3), ('W', 3, 1), ('B', -1, -1)])

Time 1: 5.76214694977 seconds

Time 2: 5.68395805359 seconds

Time 3: 5.69731211662 seconds

The player that will win the game with the given initial state will be **Player 2** ('W'). The optimal game value is -12 where there are 2 black tokens and 14 white tokens.

4x4 game terminal states visited with Minmax: 33909

Minimax-ab

4x4 game Minimax without alpha-beta pruning runtime: 1.28459596634 seconds 4x4 game Minimax with alpha-beta pruning runtime: 0.955676078796 seconds

4x4 game terminal states visited: 3754

4x4 game truncations made by alpha-beta pruning: 8532

5x5 game terminal states visited: 174016 5x5 game truncations made by alpha-beta pruning: 338821

Final state for the default 5x5 game:

'W'	'W'	'W'	٤)	()
'W'	'W'	٠,	()	()
'W'	٠,	٤)	٤)	'B'
()	٠,	٠,	'B'	'B'
٠,	٠,	'B'	'B'	'B'

The answer means that the best Player 1 can do is draw the game. If both players play optimally, then the game will always draw. If Player 1 does not play for a draw, then Player 2 will always win if they are both optimal otherwise.