



Reduced-Dimensional Retrievals of Precipitation from the TRMM Microwave Imager: Physical Insight and Information Content

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Introduction

- TRMM:

- Launched in Nov 1997

- Latitude range: 40S ~ 40N

- Precipitation Radar (PR): 5km/247km

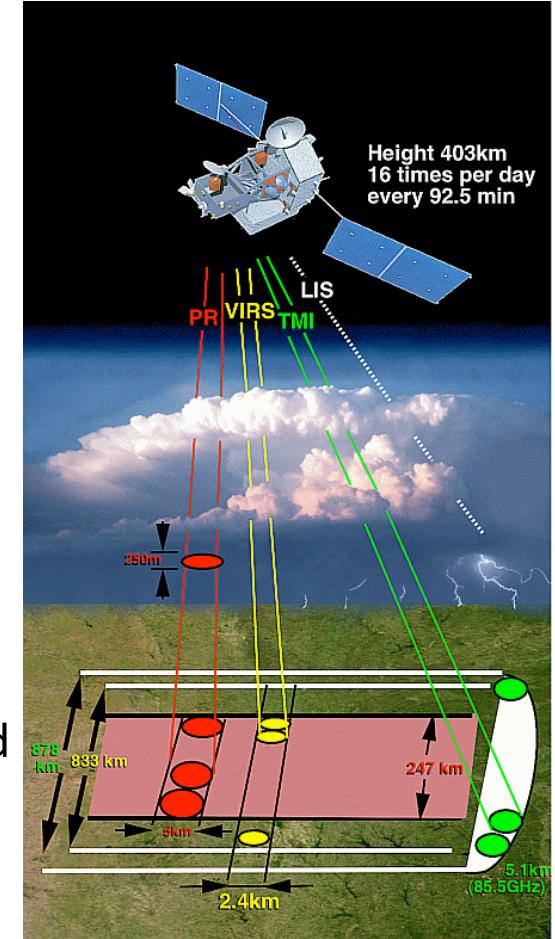
- Microwave Imager (TMI):

- 15km/833km (resolution of 19GHz)

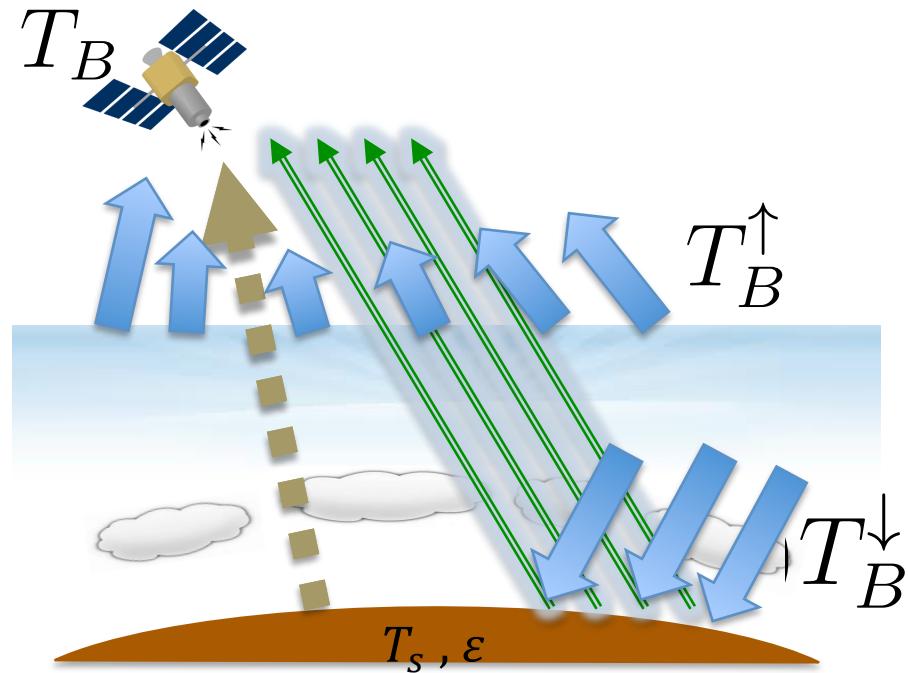
- Microwave channels:

- 10, 19, 37, 85.5GHz (vertical and horizontal), and
21GHz vertical

- Microwave Channels (features)
- Bayesian estimation methods (Petty 2012)
- Three most important physical signatures for TRMM rain-rate retrieval
- How important is each component?



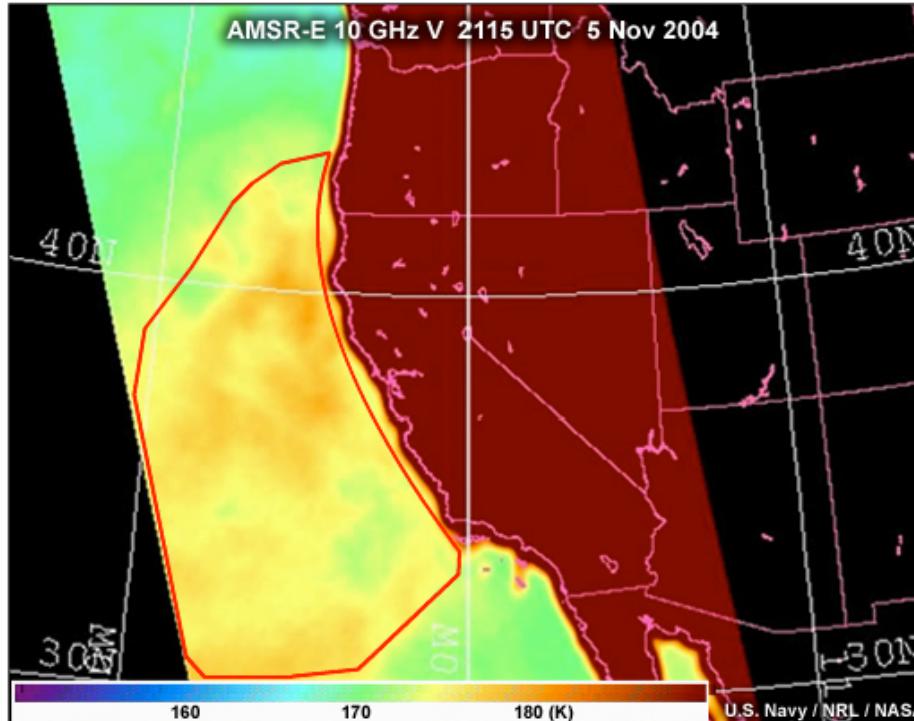
Passive Microwave Remote Sensing



$$T_B = T_B^{\uparrow} + \tau(0, \infty)[\varepsilon_s T_s + (1 - \varepsilon_s)T_B^{\downarrow}]$$

Background: Ocean and Land

Ocean background: cold + strong polarization



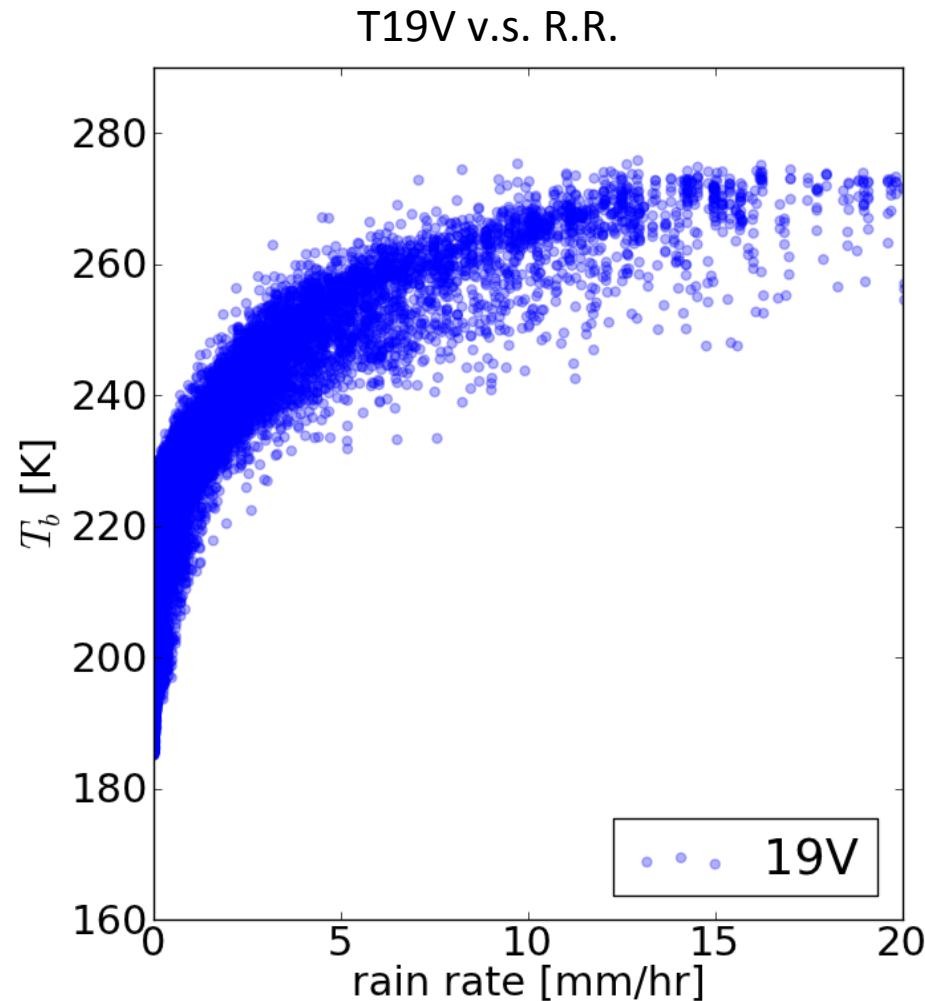
- Polarization: Vertical (V) and Horizontal (H) for 10, 19, 37, and 85.5GHz
- Over the ocean, emissivity:

$$\varepsilon_H < \varepsilon_V < 1 \quad \text{strong polarization}$$

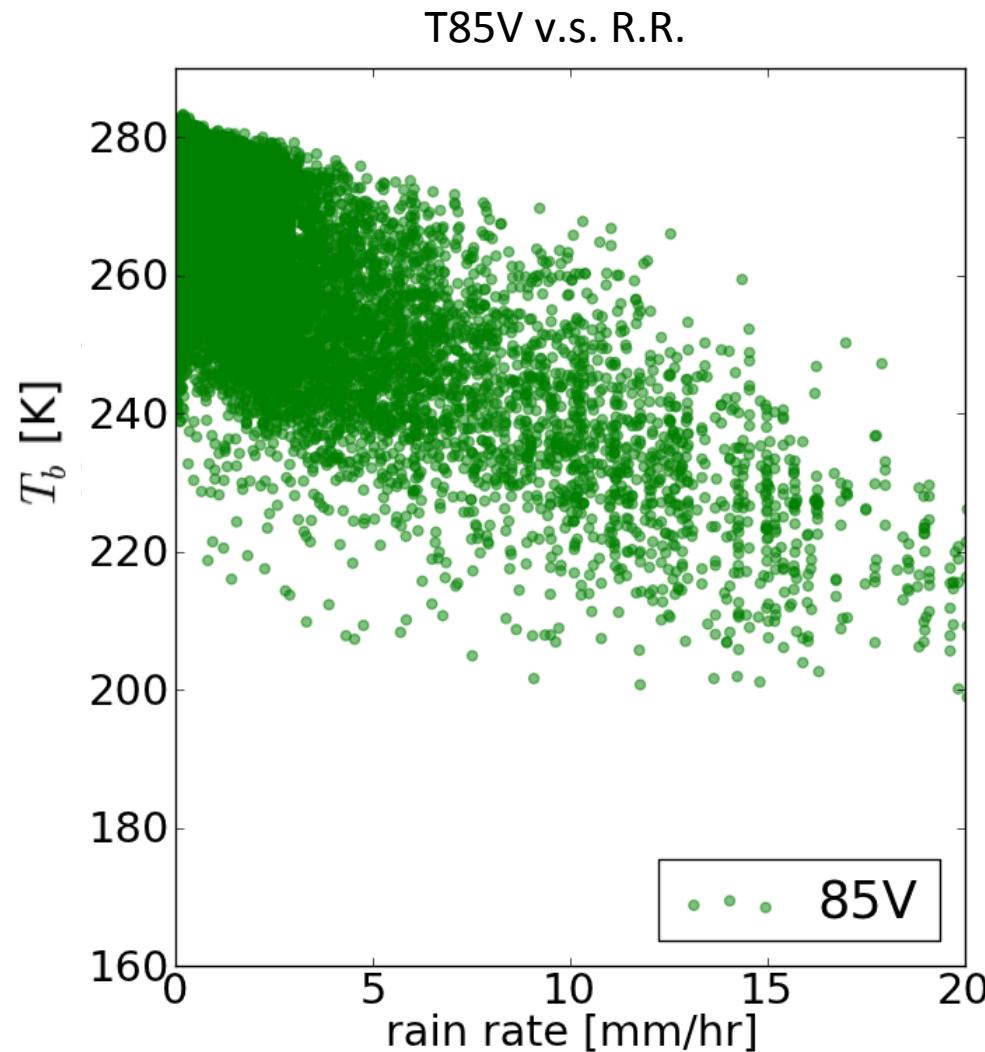
- Over the land, emissivity:

$$\varepsilon_H \approx \varepsilon_V \approx 1 \quad \text{weak polarization}$$

Frequency and rain rate



Frequency and rain rate



Bayesian Retrievals

- Bayes' theorem (Bayes and Price, 1763)

$$P(A|B) \propto P(A) \cdot P(B|A)$$

- Bayesian Monte Carlo (MBC):
 - Large data base for PDF collect candidate solutions(L'Ecuyer and Stephens, 2002)
- Bayesian with Cloud resolving models:
 - Matching Tb (Kummerow 2006)

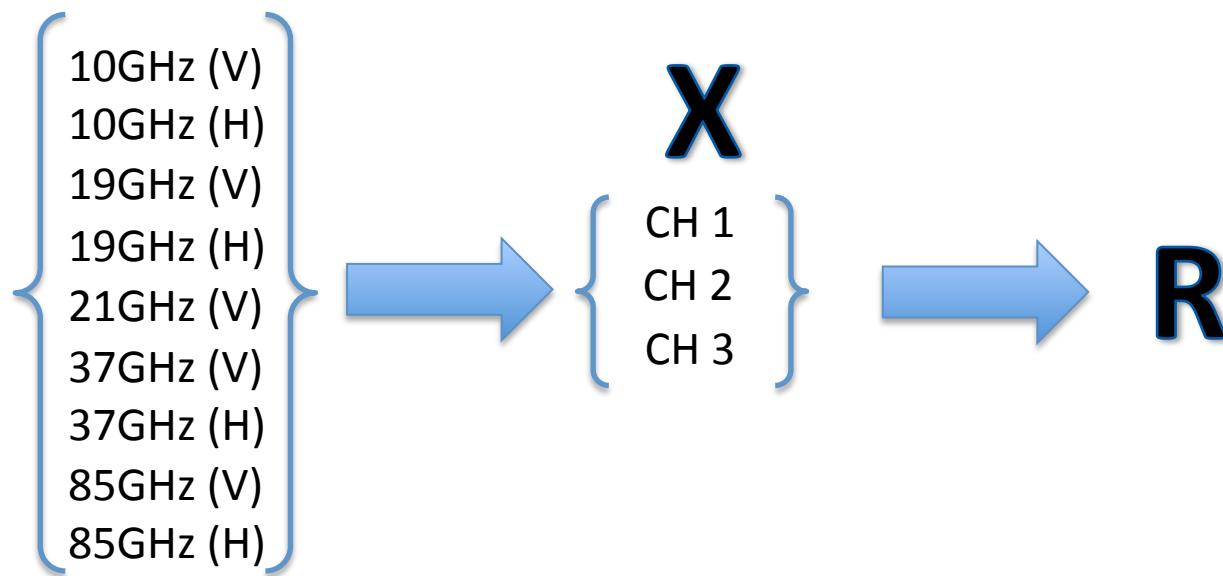
UW Bayesian Algorithm

- Uses TMI-PR matchup data, no cloud resolving models
- No conceptual distinguish between ocean and land
- No ‘screening’
- Pre-averages a priori database into 5D lookup table
- No weighting for candidate solutions
- Produces posterior distribution and averaged rain rate to replace ‘error bar’

(Petty and Li, 2013a,b)

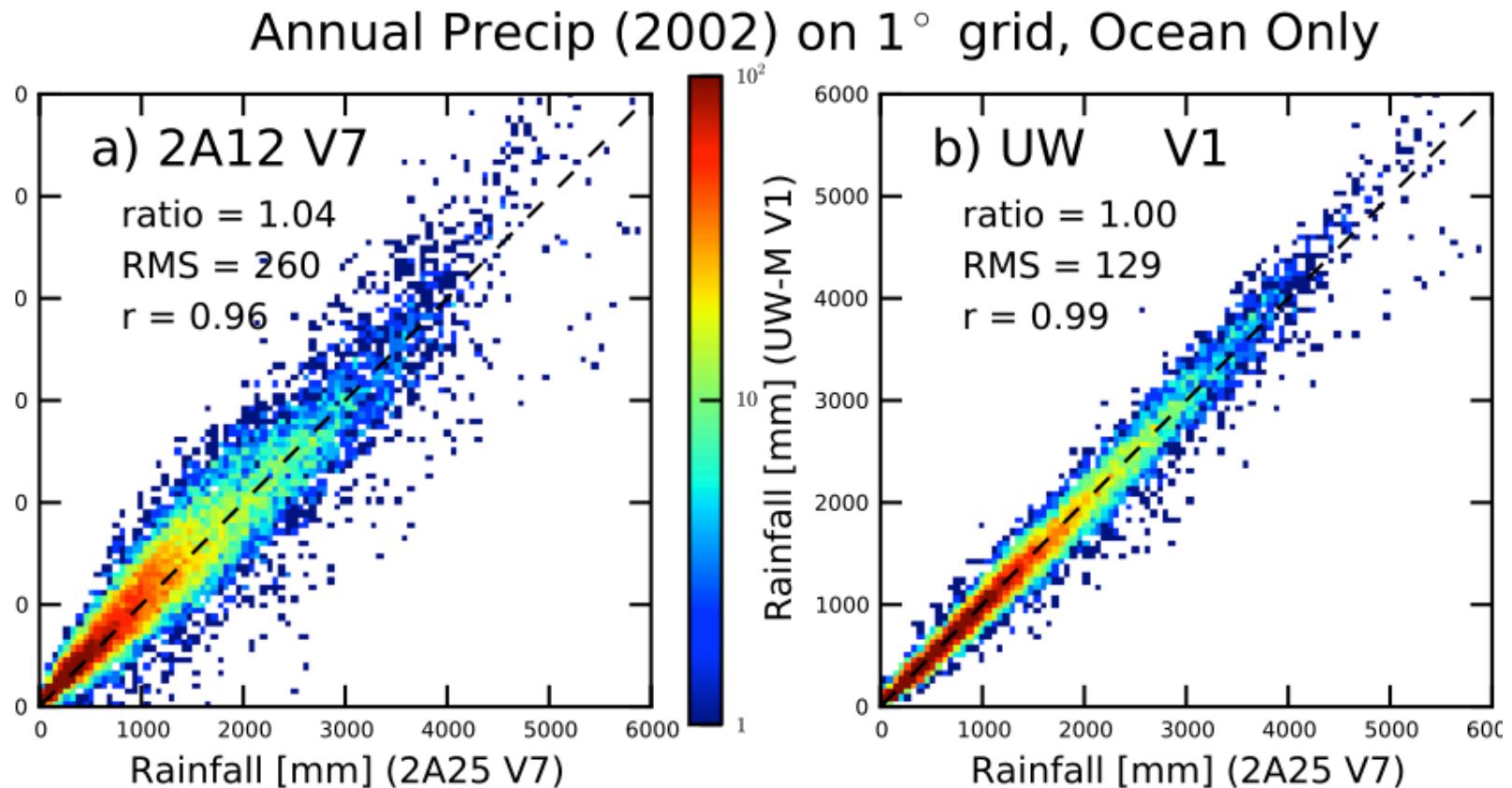
Dimensional Reduction

- Noise reduction
- Sample density maintaining
- Memory requirement reduction



- Principle Component Analysis (Petty 2012)
 - Step 1: Normalize the geophysical noise among non-rain samples
 - Step 2: Collect sensitivity from the desired variable (e.g. rain)

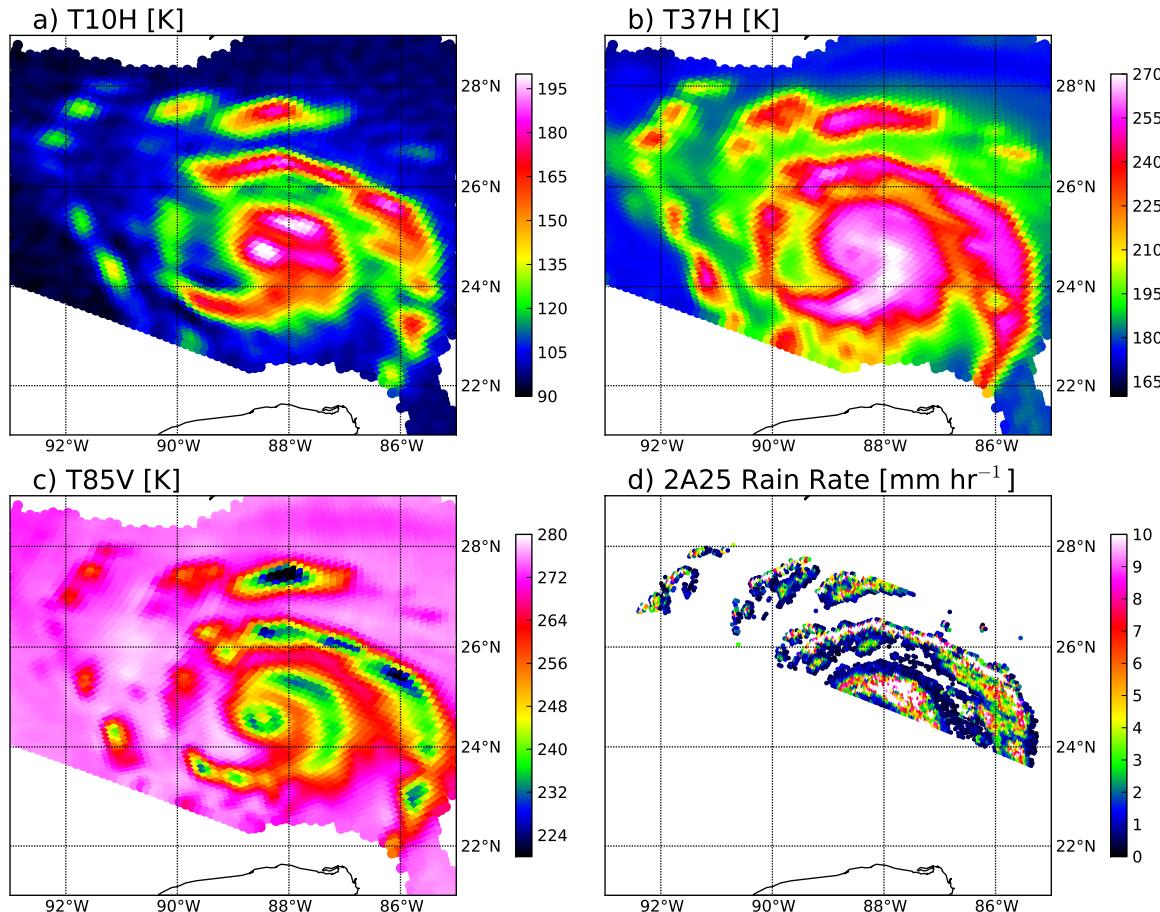
UW algorithm and 2A12



(Petty and Li 2013b)

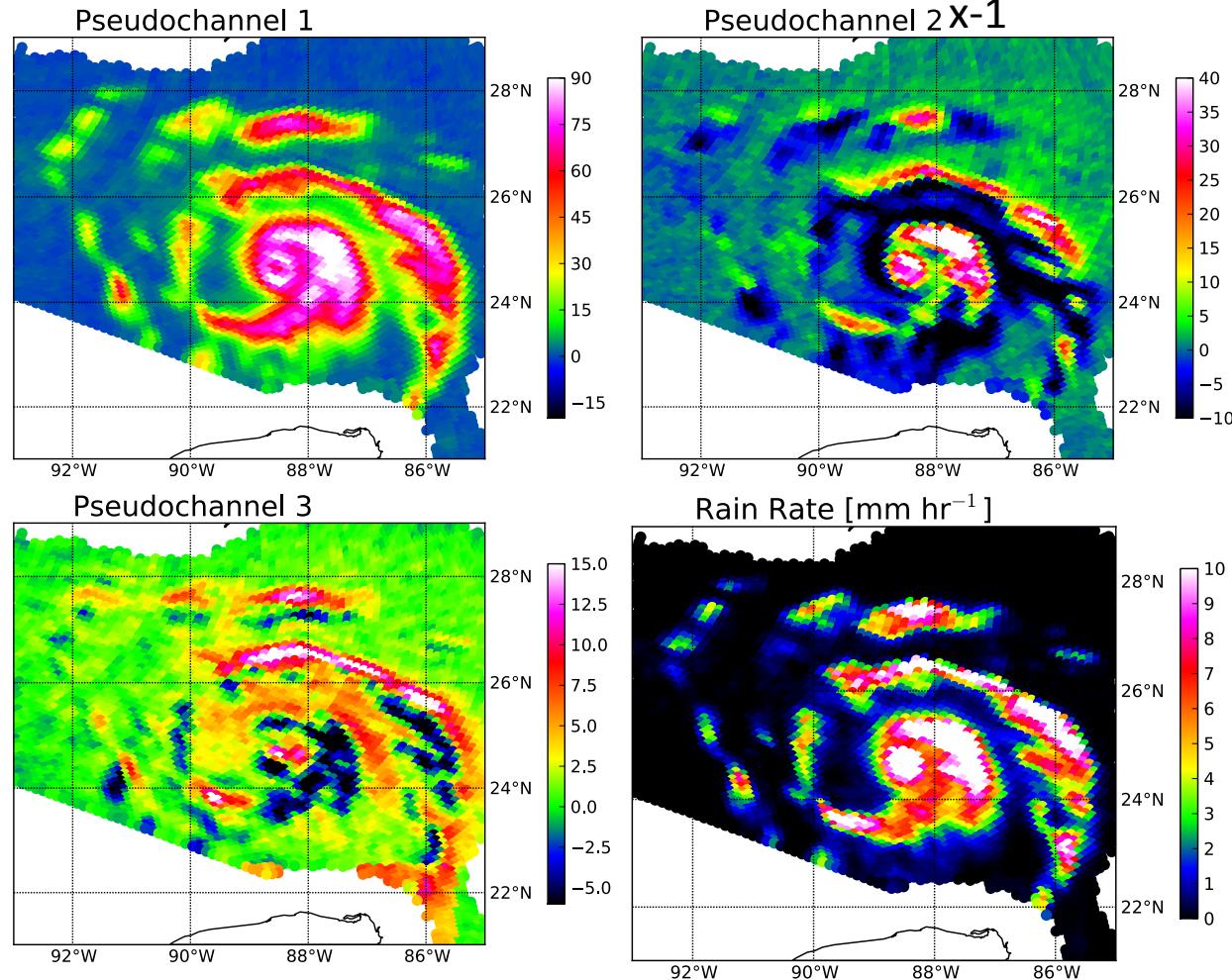
Hurricane Lili, 2 Oct, 2002

Physical Channels

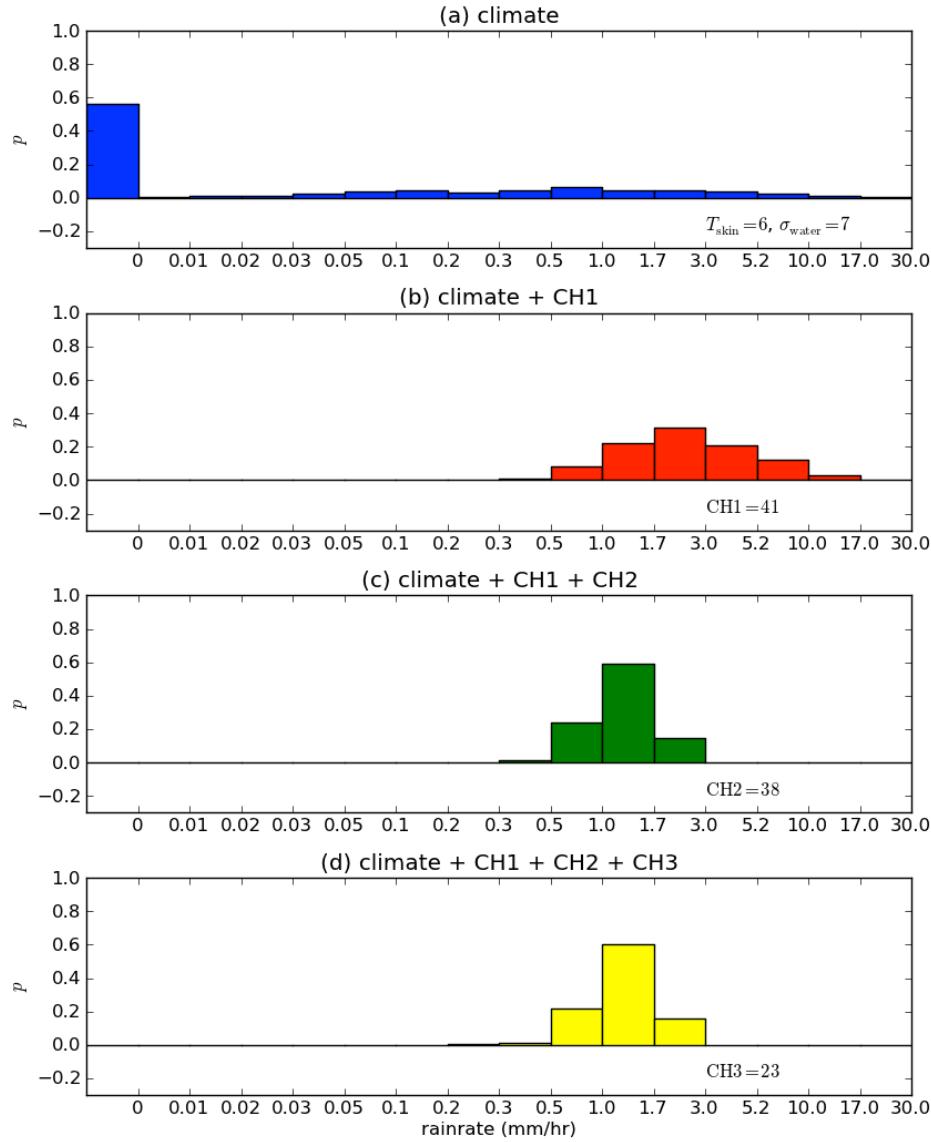


Hurricane Lili, 2 Oct, 2002

Pseudo-channels



Posterior PDFs



So Far...

- UW algorithm for RR retrieval shows significant improvement.
- Leading features of storms to determine rain-rate revealed:
 - CH1: emission of cloud liquid water
 - CH2:
 - >0: anvil of precipitating clouds
 - <0: ice scattering of storm clouds
 - CH3: responsible to storm edges and gradients
- How important are each CHs?

Information Theory

- Shannon Entropy Difference
 - Measures changes in dispersion
 - (Shannon, 1948, 1956)
- Relative Entropy
 - Measures surprise
 - (Kullback and Leibler, 1951)
 - (Kullback 1997)
- Research:
 - Radar signals (Xu, 2006)
 - Electrical signal analysis ...

Shannon Entropy

‘Dispersion Index’

$$SE \equiv - \sum p_i \ln p_i$$

$$\Delta SE(p \rightarrow q) = SE_q - SE_p$$

Shannon Entropy ‘Dispersion Index’



$$p : \{0.5, 0.5\} \rightarrow q : \{0.9, 0.1\}$$

$$\Delta SE(p \rightarrow q) = SE_q - SE_p = 0.33 - 0.69 = -0.36$$

Relative Entropy

‘Surprise Index’

$$RE(p \rightarrow q) \equiv \sum q_i \ln [q_i/p_i]$$

Relative Entropy

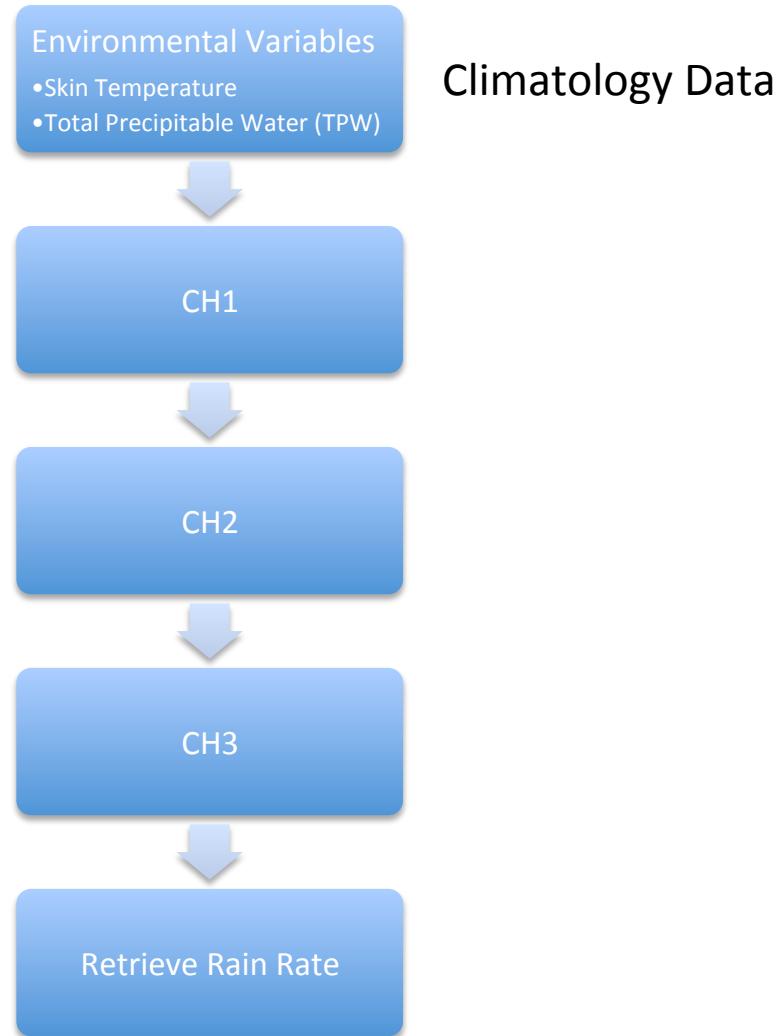
'Surprise Index'



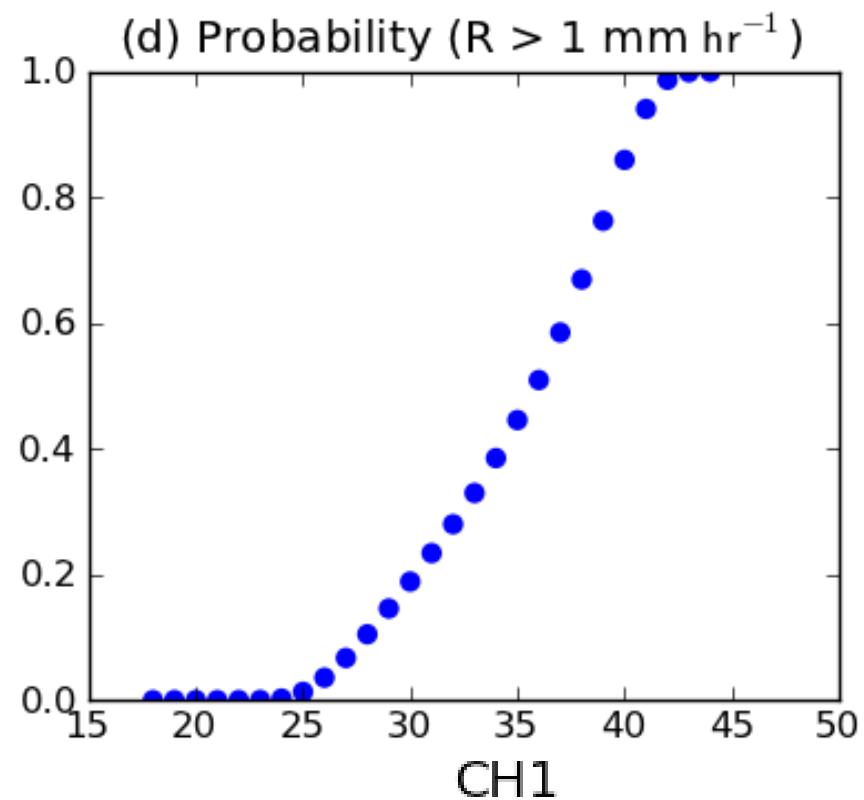
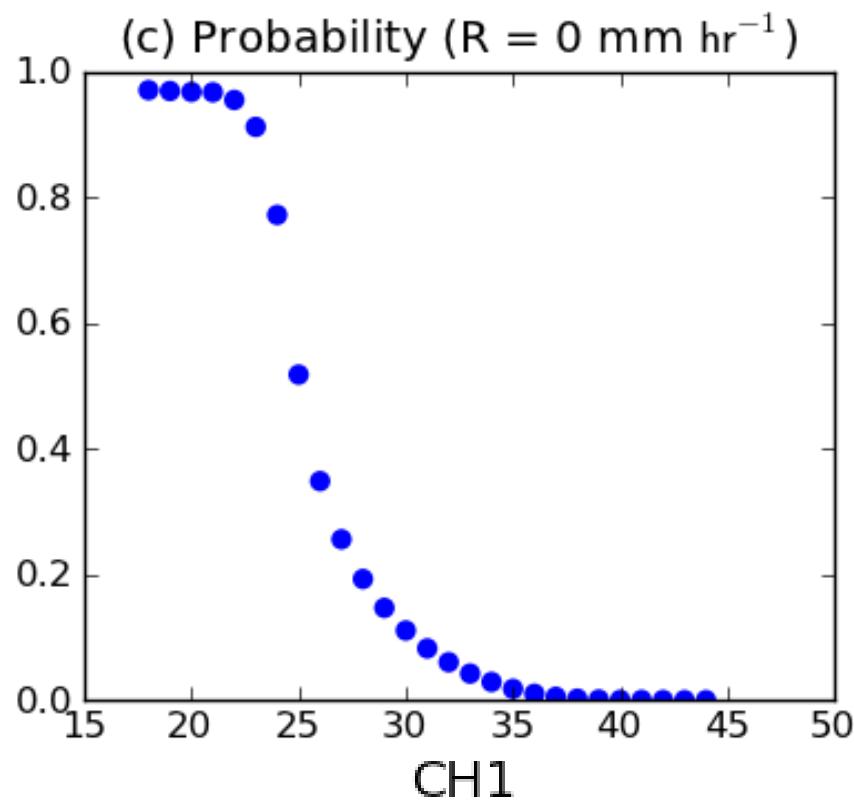
$$p : \{0.5, 0.5, 0.0\} \rightarrow q : \{0.05, 0.05, 0.9\}$$

$$RE(p \rightarrow q) = RE(q, p) = \sum q_i \ln(q_i/p_i) = (-0.1) + (-0.1) + \infty = +\infty$$

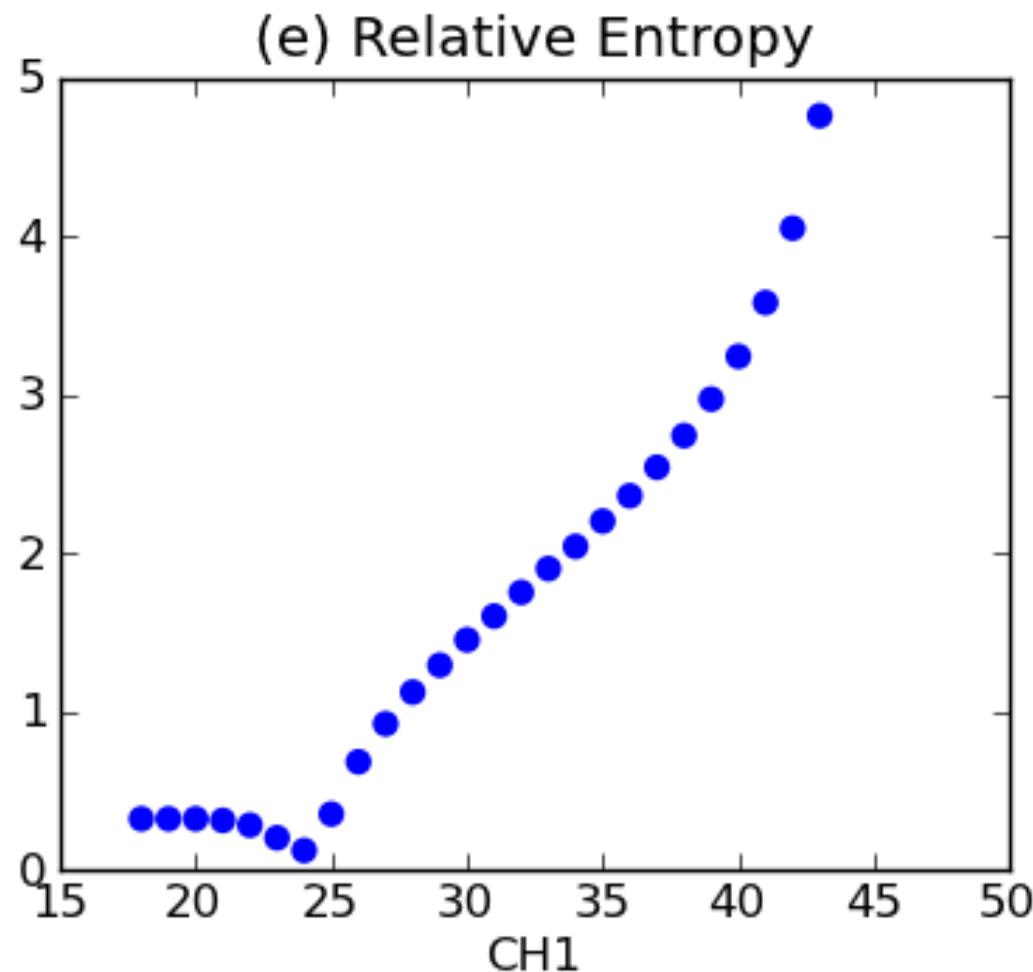
Necessary Condition



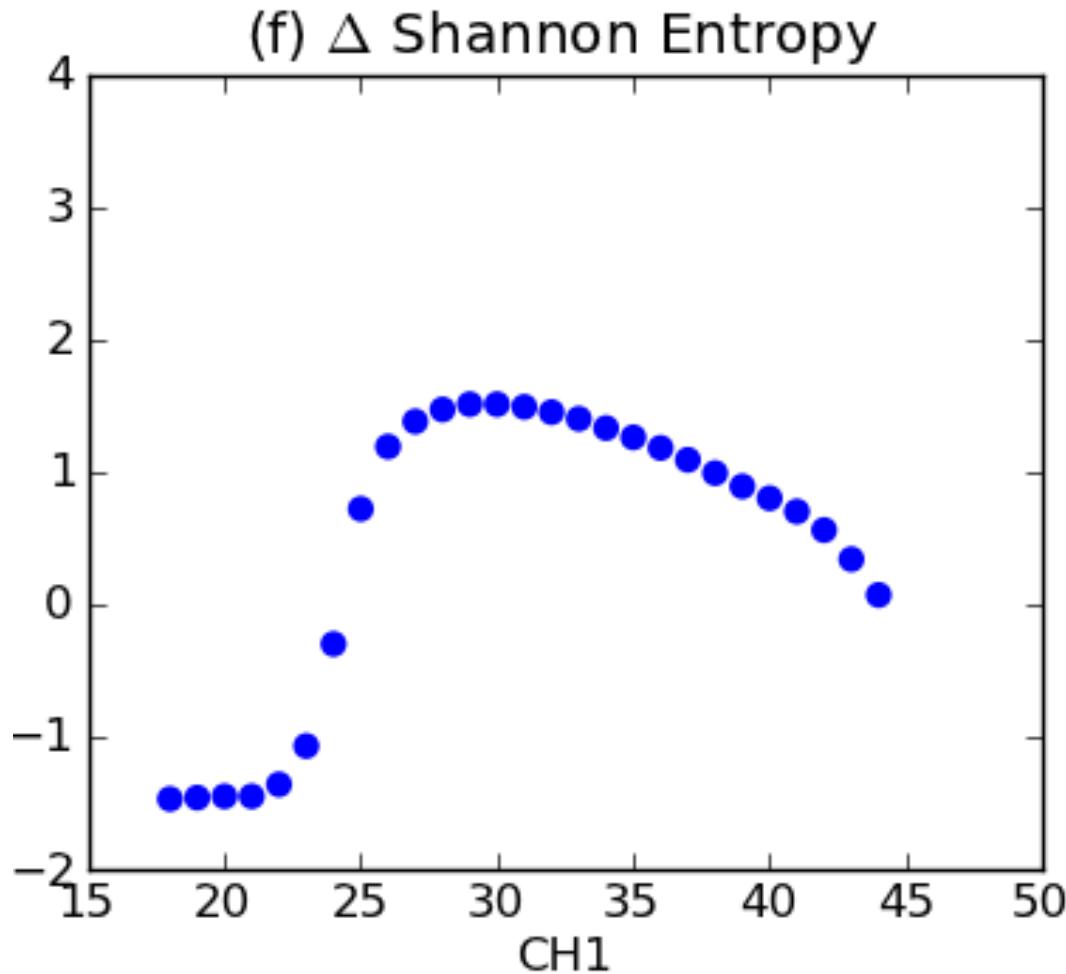
CH1: Cloud Liquid Water Emission Precipitation Distribution



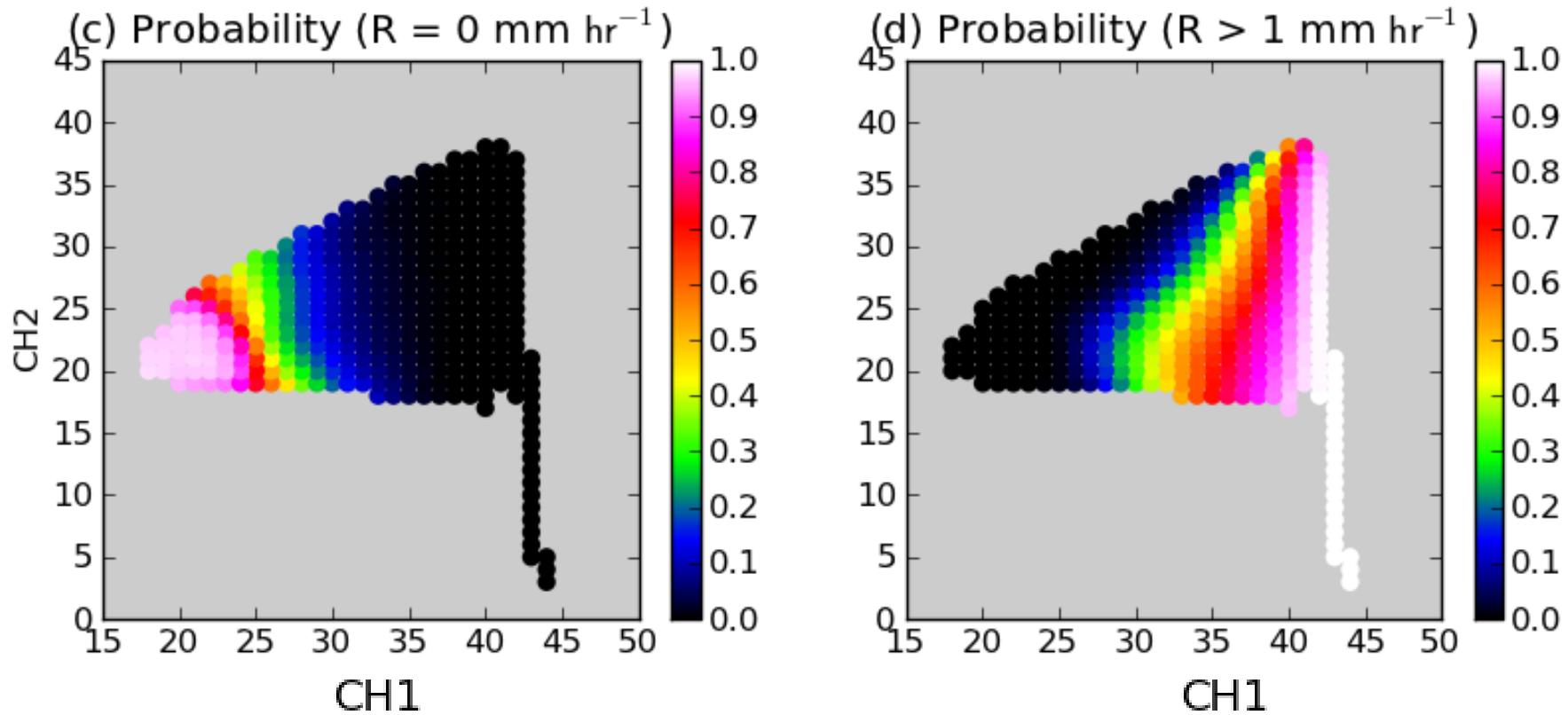
CH1: Cloud Liquid Water Emission ‘Surprises’



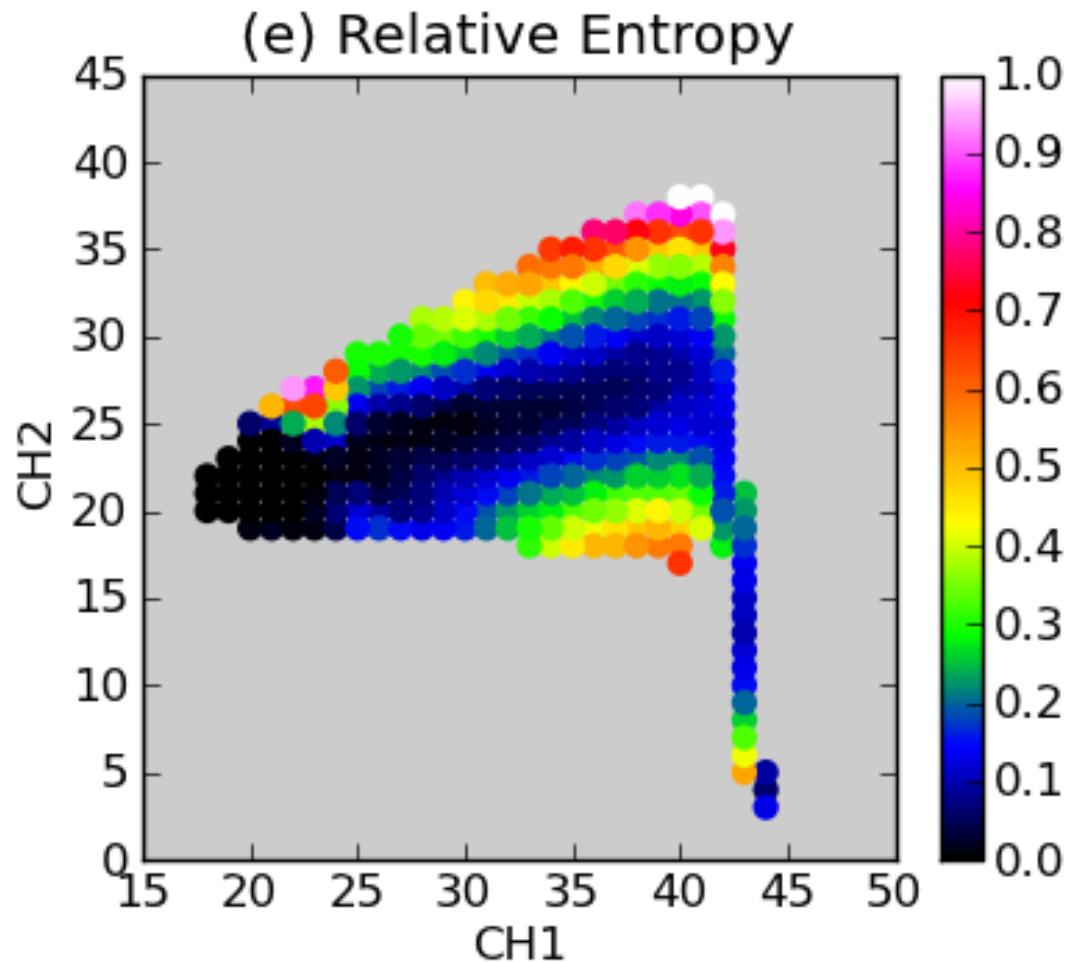
CH1: Cloud Liquid Water Emission ‘Dispersion’



CH2: Anvil v.s. Deep Convection Precipitation Distribution

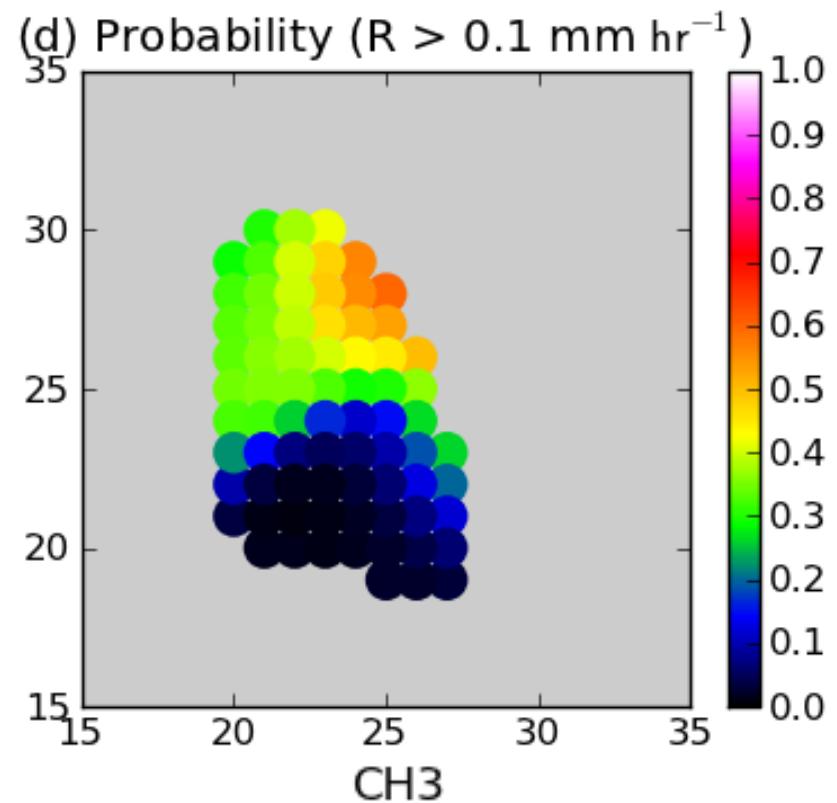
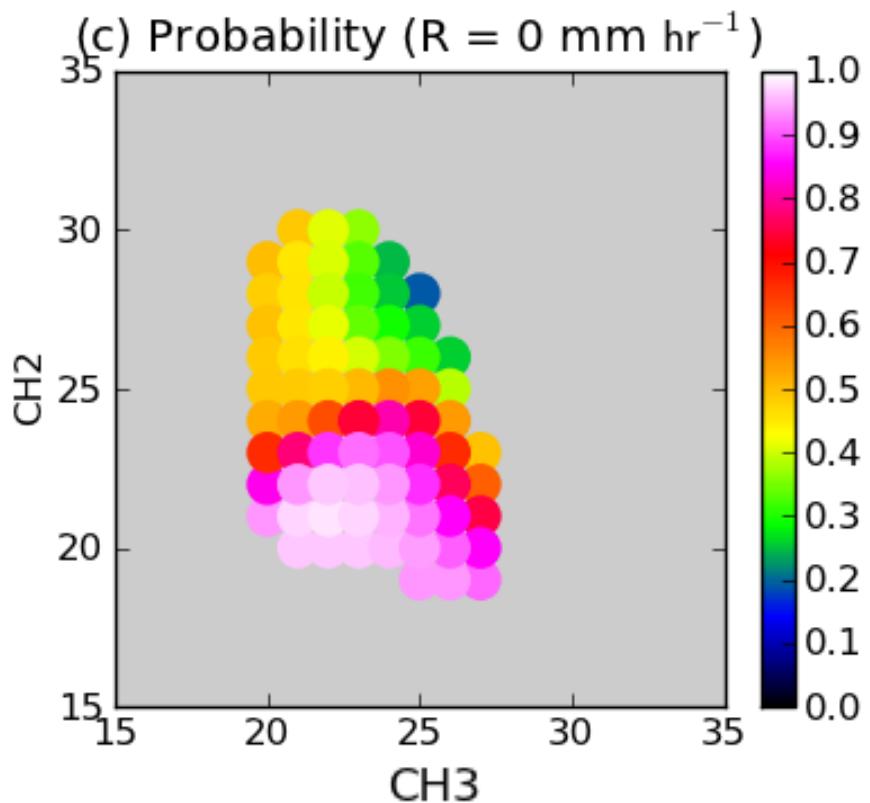


CH2: Anvil v.s. Deep Convection ‘Surprise’



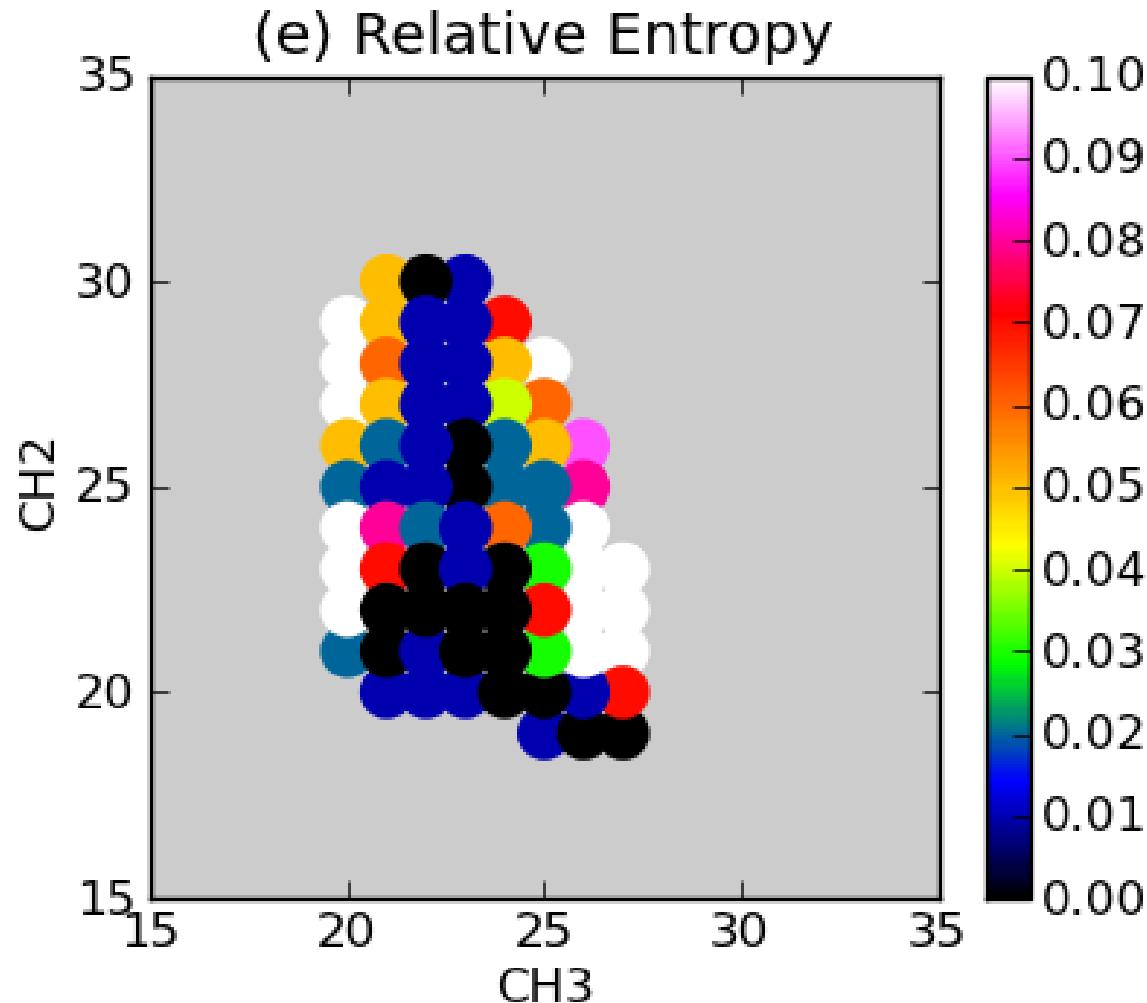
CH₃

Low Rain Rate Retrieval

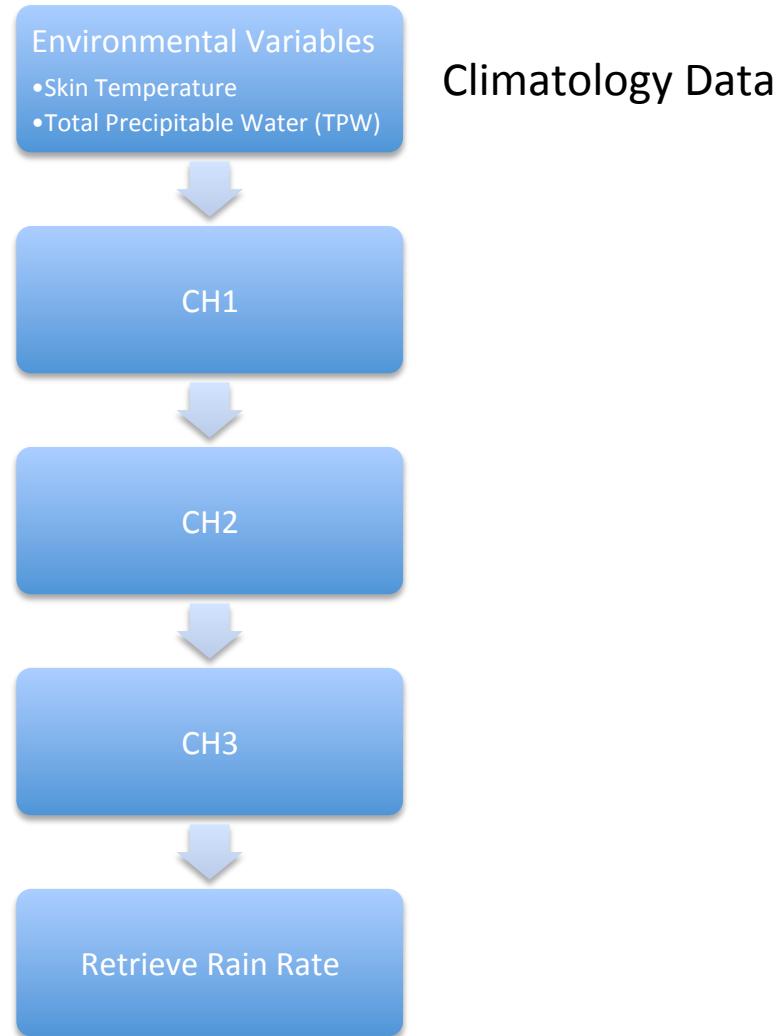


CH₃

Low Rain Rate Retrieval

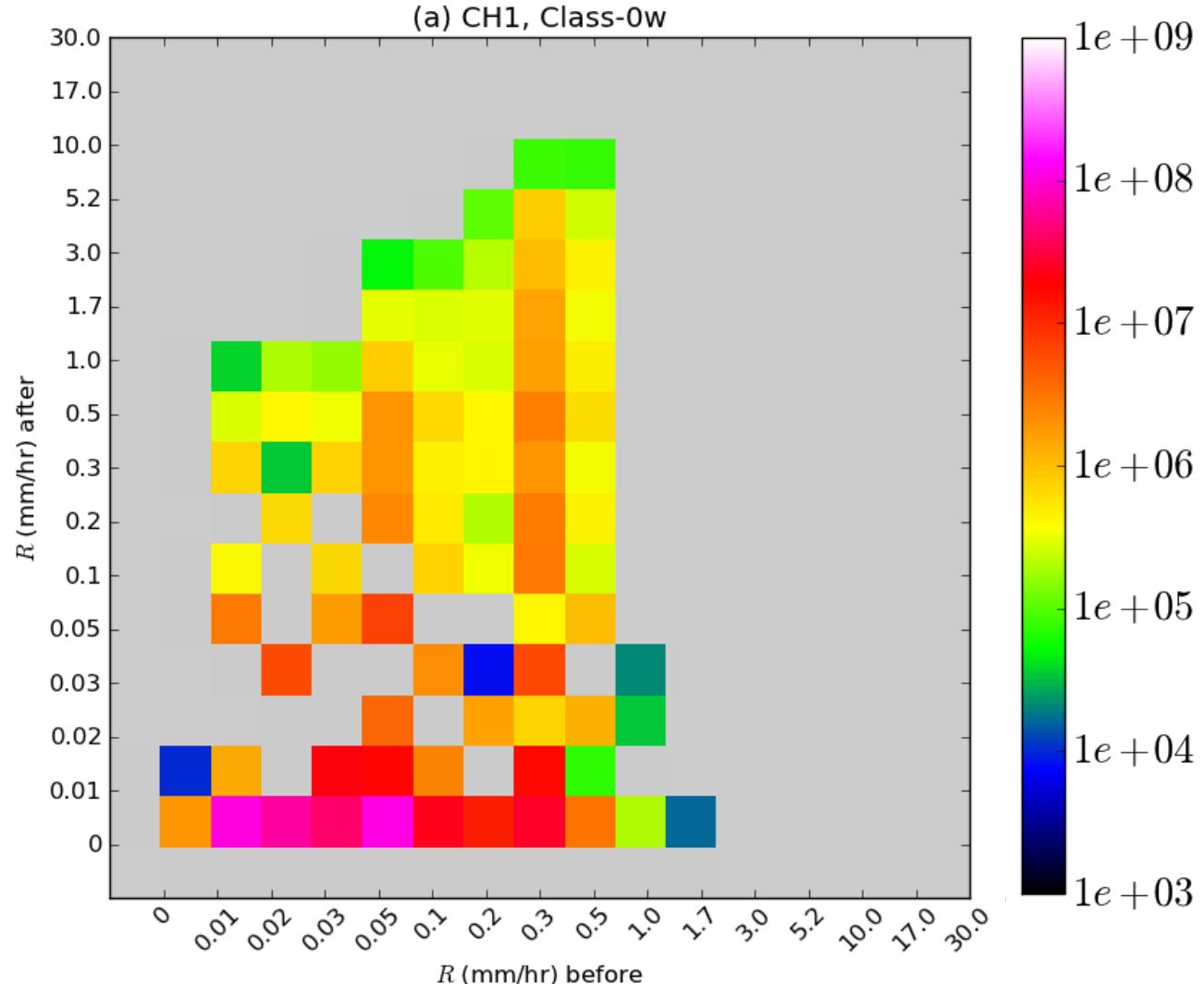


Sufficient Condition



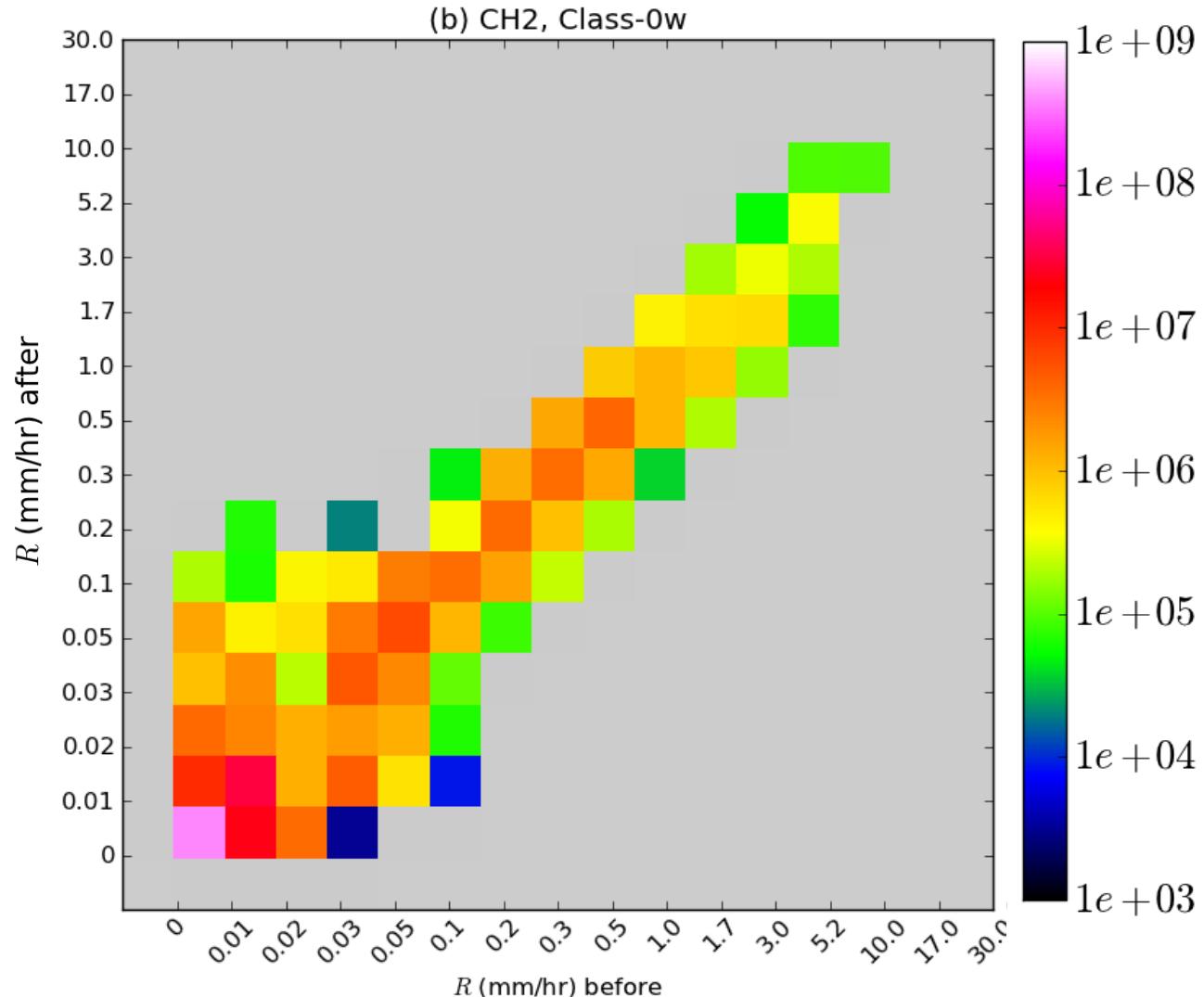
Information content – Sufficiency

Adding CH1



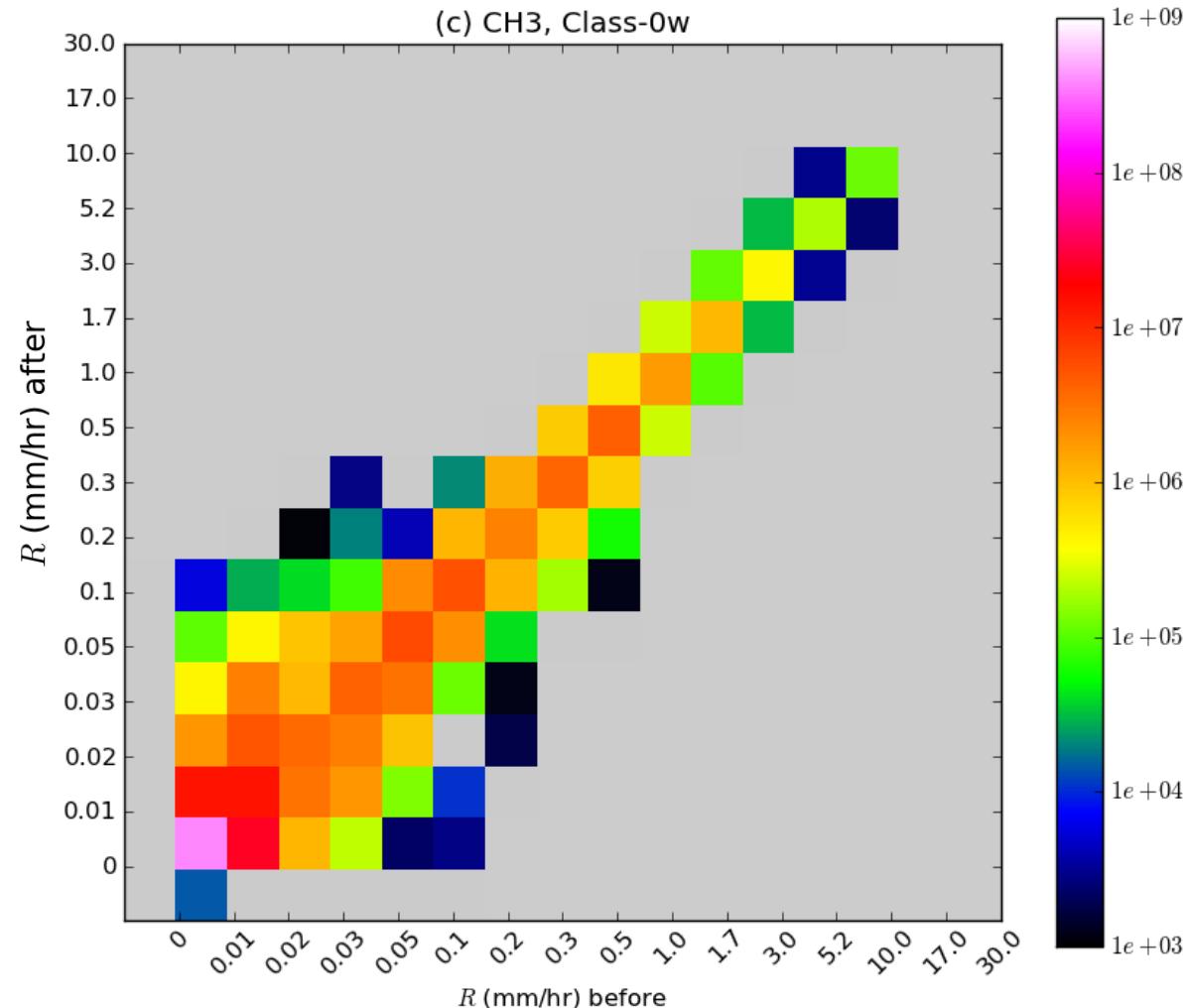
Information content – Sufficiency

Adding CH2



Information content – Sufficiency

Adding CH3



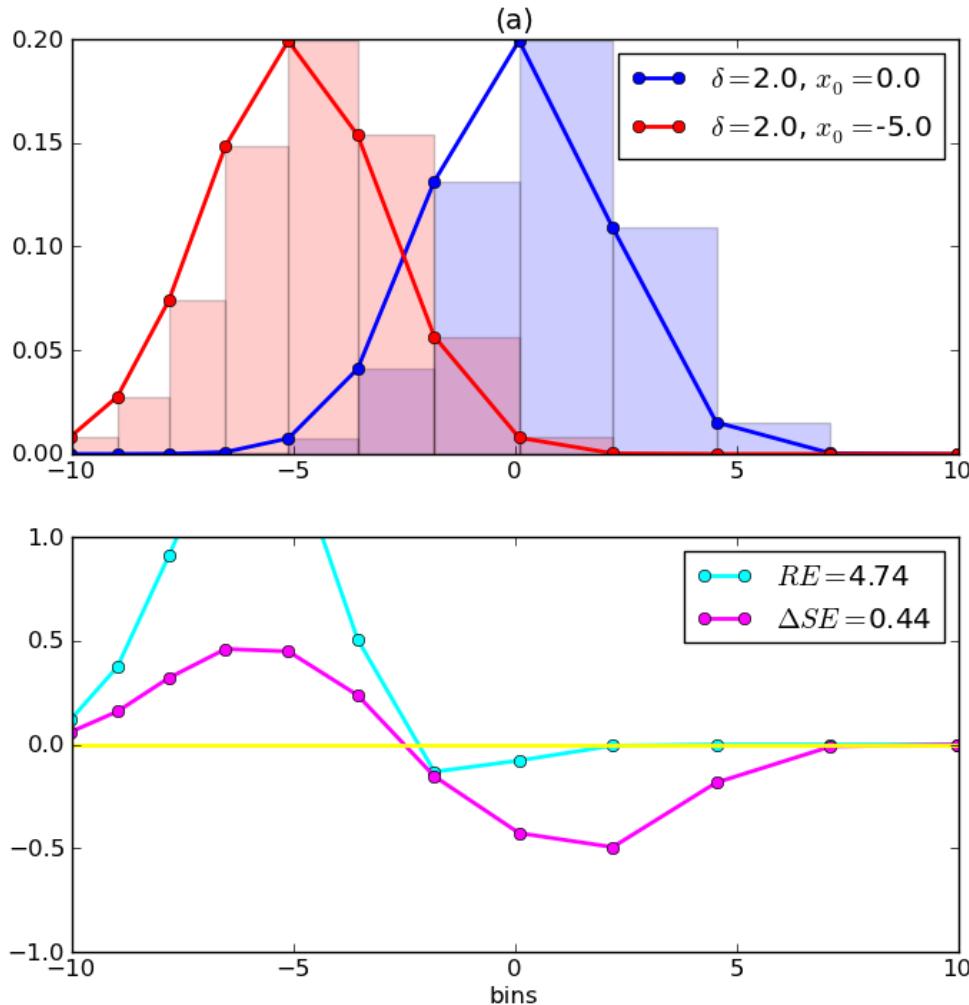
Conclusions

- CH1 and CH2: major information content
- CH3: little information content
 - Exceptions: at rare combination of CH1 and CH2
- Adding CH4:
 - greatly increases memory requirement
 - Reduced sample density
 - provides less information content



Questions?

Relative Entropy ‘Surprise Index’



Shannon Entropy ‘Certainty Index’

