Tab. 3.1: Geometrické charakteristiky rovinných obrazců

Tvar obrazce		Obsah $A$ , poloha těžiště $t$ , momenty setrvačnosti $I$ , polární $I_t$ a deviační $D$
Obdélník	$y \downarrow x_t \downarrow y_t$ $t \downarrow x_t$ $b \downarrow x_t$	$A = bh;  x_t = \frac{b}{2};  y_t = \frac{h}{2}$ $I_{x_t} = \frac{1}{12}bh^3;  I_{y_t} = \frac{1}{12}hb^3;  I_x = \frac{1}{3}bh^3;  I_y = \frac{1}{3}hb^3$ $D_{xy} = \frac{b^2h^2}{4};  I_t = \frac{bh}{12}(b^2 + h^2)$
Čtverec	$y$ $x_t$ $y_t$ $x_t$	$A = a^{2};  x_{t} = y_{t} = \frac{a}{2}$ $I_{x_{t}} = I_{y_{t}} = \frac{a^{4}}{12};  I_{x} = I_{y} = \frac{a^{4}}{3}$ $D_{xy} = \frac{a^{4}}{4};  I_{t} = \frac{a^{4}}{6}$
Pravoúhlý trojúhelník	$\begin{array}{c c}  & x_t & y_t \\  & x_t \\  & x_t$	$A = \frac{1}{2}bh;  x_t = \frac{b}{3};  y_t = \frac{h}{3}$ $I_{x_t} = \frac{1}{36}bh^3;  I_{y_t} = \frac{1}{36}hb^3;  D_{x_ty_t} = -\frac{b^2h^2}{72}$ $I_x = \frac{1}{12}bh^3;  I_y = \frac{1}{12}hb^3;  D_{xy} = \frac{b^2h^2}{24}$ $I_{x'} = \frac{1}{4}bh^3;  I_t = \frac{bh}{36}(b^2 + h^2)$
Lichoběžník	$\begin{array}{c c}  & b \\  & x_{l} \\  & x_{$	$A = \frac{1}{2}(a+b)h;  x_t = \frac{a^2 + ab + b^2}{3(a+b)};  y_t = \frac{(a+2b)h}{3(a+b)}$ $I_{x_t} = \frac{\left(a^2 + 4ab + b^2\right)h^3}{36(a+b)};  I_{x_t} = \frac{(3a+b)h^3}{12}$ $I_x = \frac{(a+3b)h^3}{12};  D_{xy} = \frac{\left(a^2 + 2ab + 3b^2\right)h^2}{24}$
Kruh	<i>x y t x x x x x x x x x x</i>	$A = \pi r^{2} = \frac{\pi d^{2}}{4};  I_{x_{t}} = I_{y_{t}} = \frac{\pi r^{4}}{4} = \frac{\pi d^{4}}{64}$ $I_{t} = \frac{\pi r^{4}}{2} = \frac{\pi d^{4}}{32}$

## Tab. 3.1: Geometrické charakteristiky rovinných obrazců (pokračování)

	Obsah A, poloha těžiště t, momenty setrvačnosti I,				
Tvar obrazce		polární I, a deviační D			
Mezikruží	$ \begin{array}{c c} \hline z_{c} \\ \hline                                   $	$A = \pi \left(r_1^2 - r_2^2\right) = \frac{\pi}{4} \left(d_1^2 - d_2^2\right)$ $I_{x_t} = I_{y_t} = \frac{\pi}{4} \left(r_1^4 - r_2^4\right) = \frac{\pi}{64} \left(d_1^4 - d_2^4\right)$ $I_t = \frac{\pi}{2} \left(r_1^4 - r_2^4\right) = \frac{\pi}{32} \left(d_1^4 - d_2^4\right)$			
Půlkruh	$ \begin{array}{c c} y_t & \\ \hline t & \\ \hline d = 2r \end{array} $	$A = \frac{\pi r^2}{2} = \frac{\pi d^2}{8};  y_t = \frac{4r}{3\pi} = \frac{2d}{3\pi}$ $I_{x_t} = \left(\frac{\pi}{8} - \frac{8}{9\pi}\right)r^4 = \left(\frac{\pi}{8} - \frac{8}{9\pi}\right)\frac{d^4}{16}$ $I_x = \frac{\pi r^4}{8} = \frac{\pi d^4}{128} = I_{y_t};  I_o = \frac{\pi r^4}{4} = \frac{\pi d^4}{64}$			
Čtvrkruh	$y \mid x_t \mid y_t$ $0 \mid r = d/2 \mid x$	$A = \frac{\pi r^2}{4} = \frac{\pi d^2}{16};  x_t = y_t = \frac{4r}{3\pi} = \frac{2d}{3\pi}$ $I_{x_t} = I_{y_t} = \left(\frac{\pi}{16} - \frac{4}{9\pi}\right) r^4 = \left(\frac{\pi}{16} - \frac{4}{9\pi}\right) \frac{d^4}{16}$ $D_{x_t y_t} = \left(\frac{1}{8} - \frac{4}{9\pi}\right) r^4 = \left(\frac{1}{8} - \frac{4}{9\pi}\right) \frac{d^4}{16}$			
Kruhová výseč		$A = \alpha r^{2};  y_{t} = \frac{2}{3} r \frac{\sin \alpha}{\alpha}$ $I_{x_{t}} = r^{4} \left( \frac{2\alpha + \sin 2\alpha}{8} - \frac{4\sin^{2} \alpha}{9\alpha} \right);  I_{o} = \frac{\alpha r^{4}}{2}$ $I_{x} = \frac{r^{4}}{8} (2\alpha + \sin 2\alpha);  I_{y} = \frac{r^{4}}{8} (2\alpha - \sin 2\alpha)$			
Kruhová úseč	y $y$ $y$ $y$ $y$ $y$ $y$ $y$ $y$ $y$	$A = \left(\alpha - \frac{1}{2}\sin 2\alpha\right)r^{2};  y_{t} = \frac{4r\sin^{3}\alpha}{3(2\alpha - \sin 2\alpha)}$ $I_{x_{t}} = r^{4}\left(\frac{4\alpha - \sin 4\alpha}{16} - \frac{8}{9} \cdot \frac{\sin^{6}\alpha}{2\alpha - \sin 2\alpha}\right)$ $I_{x} = \frac{r^{4}}{16}(4\alpha - \sin 4\alpha);  I_{y} = \frac{r^{4}}{48}(12\alpha - 8\sin 2\alpha + \sin 4\alpha)$			

Tab. 3.1: Geometrické charakteristiky rovinných obrazců (pokračování)

Tvar obrazce		Obsah $A$ , poloha těžiště $t$ , momenty setrvačnosti $I$ , polární $I$ , a deviační $D$
Elipsa	$y_t$	$A = \pi ab$ $I_{x_i} = \frac{\pi}{4} ab^3;  I_{y_i} = \frac{\pi}{4} ba^3$ $I_{r} = \frac{\pi}{4} ab \left(a^2 + b^2\right)$
Parabolická úseč	$y_t$ $x_t$ $y_t$ $y_t$ $x_t$ $y_t$	$A = \frac{4}{3}bh;   y_t = \frac{2}{5}h$ $I_{x_t} = \frac{16}{175}bh^3; I_{y_t} = \frac{4}{15}hb^3$ $I_{x} = \frac{32}{105}bh^3; I_{x} = \frac{4}{7}bh^3$
Půl parabolické úseče	$y \nmid x_i \mid y_i  \nmid y'  x_i'  x_i' $	$A = \frac{2}{3}bh;   x_t = \frac{3}{8}b;   y_t = \frac{2}{5}h$ $I_{x_t} = \frac{8}{175}bh^3;   I_x = \frac{16}{105}bh^3;   I_{x_t} = \frac{2}{7}bh^3$ $I_{y_t} = \frac{19}{480}hb^3;   I_y = \frac{2}{15}hb^3;   I_{y_t} = \frac{3}{10}hb^3$
Parabolický trojúhelník	$y \downarrow y_i \uparrow \downarrow y' \\ x_i \downarrow x_i \\$	$A = \frac{1}{3}bh;   x_t = \frac{3}{4}b;   y_t = \frac{3}{10}h$ $I_{x_t} = \frac{37}{2100}bh^3;   I_{x} = \frac{1}{21}bh^3;   I_{x} = \frac{19}{105}bh^3$ $I_{y_t} = \frac{1}{80}hb^3;   I_{y} = \frac{1}{5}hb^3;   I_{y} = \frac{1}{30}hb^3$