

Homework 4: Classification

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1. Estimate the conditional probabilities for $P(A|+)$, $P(B|+)$, $P(C|+)$, $P(A|-)$, $P(B|-)$, $P(C|-)$.

- a. $P(A|+) = 5/7$
- b. $P(B|+) = 1/7$
- c. $P(C|+) = 6/7$
- d. $P(A|-) = 0/3$
- e. $P(B|-) = 2/3$
- f. $P(C|-) = 3/3$

2. Use the estimate of conditional probabilities given in the previous question to predict the class label for a test sample ($A=0$, $B=1$, $C=0$) using the naive Bayes approach. Work out the solution manually and show the detailed manual calculation steps.

$$P(X|+) = (2/7) * (1/7) * (1/7) = 0.00583$$

$$P(X|-) = (3/3) * (2/3) * (3/3) = 0.66666$$

$$P(X|+) * P(+) \text{ ______ } P(X|-) * P(-)$$

$$(2/343) * (7/10) \text{ ______ } (2/3) * (3/10)$$

$$(14/3430) < (2/10) \rightarrow \text{Class} = -$$

3. Estimate the conditional probabilities using the m-estimate approach, with $p = 1/2$ $m = 4$.

- a. $P(A|+) = (5+2/7+4) = 7/11$
- b. $P(B|+) = 1+2/7+4 = 3/11$
- c. $P(C|+) = 6+2/7+4 = 8/11$
- d. $P(A|-) = 0+2/3+4 = 2/7$
- e. $P(B|-) = 2+2/3+4 = 4/7$
- f. $P(C|-) = 3+2/3+4 = 5/7$