# MATHSEMANTICS.STY - SEMANTIC MATH COMMANDS

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## **CONTENTS**

1	Introduction	1		
2	Package Options	2		
3	Required Packages	2		
4	Syntax         4.1 Letters          4.2 Syntax Helpers          4.3 Spacing Helpers			
5	Abbreviations 5.1 English			
6	Names			
7	Semantic Commands			
8	Additional Semantics by Topic  8.1 Manifolds: mathsemantics-manifolds.sty			

#### 1 Introduction

This package aims to provide semantic commands for ease of use in mathematics to see better *what* you semantically mean which should be distinct/split from *how* it is realised in Lagran.

The package is a spin-off and developed in the suite of packages from the former numapde-group in Chemnitz, see the original repository at https://gitlab.hrz.tu-chemnitz.de/numapde-public/numapde-latex.

Throughout this documentation most commands are directly illustrated by examples, which are both displayed as code ( or for math examples) and its rendered result in Lagrange ( ). Two examples are

$$\$$
 \bbR  $\$  \B \\ and \\\ \eg \\ \eg \\ e. g.

The aim is to first ease the use of some often used letters and low-level formats like bold face letters  $\$  \bbR \Delta \R , but also to provide high level commands that make typing mathematics easier, for example using \As\frac{1}{2} \abs\frac{1}{2}| and \As\sigma\frac{1}{2}| abs\[Big]{\frac{1}{2}| This is the main goal in Section 4 about syntactical commands for mathematics. A next more support/helping section about abbreviations and names is Section 5.

The first main part on general semantic commands is Section 7.

While all these are loaded by default. The next part, Section 8, introduces semantic commands for specific topics. These are given in separate sub-packages and can be loaded if you work in this area and want to use the commands.

The package should be loaded late, since it might overwrite a few commands, currently most prominently \d which is overwritten by cleveref in case minted is loaded. So for more flexibility, there is the alternative command \dInt.

#### 2 PACKAGE OPTIONS

shortbb

use shorter notations for the blackboard-bold math letters \C, \K, \N, \Q, \R, \Z

## 3 REQUIRED PACKAGES

amssymb.sty defines mathematical symbol fonts

ifthen.sty facilitates the definition of conditional commands

ifxetex.sty provides a way to check if a document is being processed by XATeX and company

mathtools.sty provides lots of improvements for math typesetting (includes amsmath.sty)

**⊚(•)(•)** page 2 of 25

xifthen.sty extends if then.sty by adding new boolean conditions

xparse.sty provides a high-level interface to define new commands

xspace.sty adds space depending on context

## 4 SYNTAX

The mathsemantics-syntax.sty package provides mainly symbols and short commands, which can be used in semantic definitions for ease of notation. They usually are rather simple commands without too many parameters.

## 4.1 LETTERS

babz	lower-case <b>b</b> old-face letters $\P$ \br, \bf $ extstyle r, f$
bAbZ	upper-case <b>b</b> old-face letters $\langle l \rangle$ \bR, \bF $\bigcirc$ R, F
balpha bomega	lower-case bold-face Greek letters $\$ \balpha, \boldeta $\$ $\alpha, \eta$ (the latter being an exception)
bAlphabOmega	upper-case <b>b</b> old-face Greek letters $\P$ \bGamma, \bDelta $\P$ $\Gamma$ , $\Delta$
bnull	bold-face zero 📏 \bnull 💿 0
bone	bold-face one 📏 \bone 🌑 1
cAcZ	upper-case <b>c</b> alligraphic letters $\langle 1 \rangle$ \cM, \cN $\otimes$ $\mathcal{M}$ , $\mathcal{N}$
fAfZ	upper-case fraktur letters $\P$ \fM, \fN, \fX $ extstyle  exttt{M},  extstyle  extstyl$
sAsZ	upper-case script letters $\P \$ \sM, \sN, \sX $\$ $\$ $\mathscr{M}, \mathcal{N}, \mathcal{X}$
vavz	lower-case letters with a vector accent $\langle \rangle$ \va,\vb $\vec{a},\vec{b}$
vA vZ	upper-case letters with a vector accent $\checkmark \$ $\$ $\$ $\$ $\$ $\$ $\$ $\$ $\$ $\$
valphavomega	lower-case Greek letters with a vector accent $\$ \valpha, \vbeta $\vec{\alpha}, \vec{\beta}$

Γ, Δ

vnull vector zero  $\langle \rangle$  \vnull  $\odot \vec{0}$ 

vone vector one  $\checkmark$  \ \ \vone  $\checkmark$ 

bbA,...,bbZ blackboard-bold uppercase letters

 $\begin{picture}(100,0) \put(0,0){\line(0,0){100}} \put(0,0){\line(0,0){1$ 

use the package option shortbb to introduce

 $\$  \C,\K,\N,\Q,\R,\Z  $\$   $\$   $\$   $\mathbb{C}$ ,  $\mathbb{K}$ ,  $\mathbb{N}$ ,  $\mathbb{Q}$ ,  $\mathbb{R}$ ,  $\mathbb{Z}$  if not already defined elsewhere (i. e. they are not redefined, only *provided*.

#### 4.2 SYNTAX HELPERS

enclspacing

provides spacing after the opening and before the closing delimiters for \enclose. This is by default set to be empty.

enclose

is a command which encloses some content in scaled delimiters. It is meant as a helper to facilitate the definition of other commands. Its syntax is \enclose[#1]{#2}{#3}{#4}. The first (optional) argument is used to scale the delimiters to the standard amsmath sizes. The second and fourth arguments specify the opening and closing delimiters, respectively. The third argument is the content to be enclosed.

$$\$$
 \enclose{[}{\dfrac{1}{2}}{]}  $\$  \enclose{[}

$$\$$
 \enclose[Big][{\dfrac{1}{2}}]  $\$  \enclose[Big][\dfrac{1}{2}]

$$\$$
 \enclose[auto]{[}{\dfrac{1}{2}}{]}  $\$   $\$ 

$$4$$
 \enclose[none]{[}{\dfrac{1}{2}}{]}  $\bullet$   $\frac{1}{2}$ 

**Note 1.** none is merely meant for testing when having arguments in brackets whether it is useful to omit them. You can also deactivate the absolute value vertical lines this way, so *use this option with care*.

**Note 2.** This command should normally be used only in the definition of other commands. For instance, \abs is using it internally. See \paren for the

<sup>&</sup>lt;sup>1</sup>big, Big, bigg, Bigg or auto, which uses left and right as well as none to easily deactivate brackets.

nicer command to use

#### enclspacingSet

provides spacing before and after the center delimiter \encloseSet. This is by default set to \,.

encloseSet

is a command which encloses some content in scaled delimiters. It is meant as a helper to facilitate the definition of other commands. Its syntax is \encloseSet#1]{#2}{#3}{#4}{#5}{#6}. The first (optional) argument is used to scale the delimiters including the center one to the standard amsmath sizes.¹ The second and sixth arguments specify the opening and closing delimiters, respectively. The fourth argument specifies the center delimiter and The third and fifth argument are the content to be enclosed.

**Note.** This command should normally be used only in the definition of other commands. For instance, \setDef is using it internally.

paren

is an alternative to \enclose, with a different ordering of arguments. Its syntax is \paren[#1]{#2}{#3}{#4}, which is simply mapped to \enclose[#1]{#2}{#4}{#3}.

$$\$$
 \paren[Big]{[]}{\dfrac{1}{2}}  $\$  \Q  $\left[\frac{1}{2}\right]$ 

$$\$$
 \paren[Big][]{\dfrac{1}{2}}  $\$  \(\Phi\)

$$\$$
 \paren[auto]{[}{]}{\dfrac{1}{2}}  $\$   $\$ 

#### 4.3 SPACING HELPERS

clap

complements the standard LaTeX commands \lap and \rlap. These commands horizontally smash their arguments.

mathllap

corresponds to \llap in math mode.

$$\$$
 \sum\_{\mathbb{1}i = i = j = n} X\_{ij}  $\sum_{1 \leq i \leq j \leq n} X_{ij}$ 

mathclap corresponds to \clap in math mode.

mathrlap corresponds to \rlap in math mode.

$$\$$
 \sum\_{\mathbb{1}}e i\le i\le j\le n} X\_{ij}  $\$ 

stands for *math replace* and it typesets an argument while reserving the space for another. Its syntax is  $\mrep[#1]{#2}{#3}$  The first (optional) argument is one of  $\{1,c,r\}$  and it is used to define the alignment. c is the default.

## 5 ABBREVIATIONS

#### 5.1 ENGLISH

almost all 🕩 \aa 💿 a.a.

ale almost everywhere  $\$  \ale  $\$  a.e.

eg exempli gratia (for example) 🕩 \eg e. g.

etc et cetera (and so on) </br>
\etc etc.

ie id est (id est)

iid independent and identically distributed 🂔 \iid • i. i. d.

spd symmetric positive definite \\ \spd \ s. p. d.

st such that or subject to \$\st\$ \st \@ s.t.

① D.h.

```
with respect to //> \wrt
                                             w.r.t.
wrt
5.2 GERMAN
                     beispielsweise (for example) \/> \bspw
bspw
                     bezüglich (with regard to) \> \bzgl
bzgl
                     beziehungsweise (respectively) \> \bzw
bzw
                     Das heißt (That is, beginning of phrase) </bd>
Dah
                     das heißt (that is) //> \dah
dah
                     eventuell (possibly) </>

\evtl

evtl
fs
```

In Allgemeinen (beginning of phrase) 🕩 \IA . I. A.

iA im Allgemeinen ♦ \iA • i. A.

idR in der Regel ♦ \idR • i.d.R.

iw im Wesentlichen 🕩 \iw i. W.

Iw Im Wesentlichen (beginning of phrase) ♦ \IW ■ I. W.

oBdA ohne Beschränkung der Allgemeinheit ♦ \oBdA o. B. d. A.

**OBdA** ohne Beschränkung der Allgemeinheit (beginning of phrase)

og oben genannt ♦ \og o. g.

oae oder ähnliche 🂔 🔾 o. ä

so unter anderem **\/>** \ua **①** u.a. Unter anderem (beginning of phrase) 🕩 \Ua 💿 U. a. Ua unten genannt **\\>** \ug ug und so weiter (and so on) • usw. usw unter Umständen **//>** \uU • u. U. uU UnU Unter Umständen (beginning of phrase) **\\/\>\** \UnU \ \**\©** U. U. vergleiche (compare) **//> \vgl** • vgl. vgl zum Beisiel **//>** \zB ② z.B. zΒ Zum Beispiel (beginning of phrase) </> ΖB **●** Z.B.

## 6 Names

dolfinadjoint

zHd

ADIMAT adimat AMPL ampl BibTeX ВівТеХ BibLaTeX ● BIBLATEX **●** CG cg **●** C++ срр cppmat CPPMAT dolfin ODLFIN ODLFIN-PLOT dolfinplot

ODLFIN-ADJOINT

O Doxygen doxygen femorph FEMORPH fenics FENICS ffc • FFC fmg FMG fortran FORTRAN GITLAB gitlab • GMRES gmres • GMSH gmsh IPOPT ipopt LIBSVM libsvm • LIBLINEAR liblinear MACMPEC macmpec MANIFOLDS.JL manifoldsjl MANOPT manopt manoptjl MANOPT.JL MATHEMATICA mathematica MATLAB matlab MAPLE maple maxima MAXIMA metis METIS MINRES minres

MSHR

MVIRT

mshr

mvirt

numpy	•	NumPy
paraview	•	Paraview
pdflatex	•	PDF#IEX
perl	•	Perl
petsc	•	PETSc
pymat	•	PYMAT
python	•	Рутном
scikit	•	SciKit
scikitlearn	•	SciKit-learn
scipy	•	SciPy
sphinx	•	Sphinx
subgmres	•	SubGmres
subminres	•	SubMinres
superlu	•	SuperLU
svmlight	•	SVM <sup>LIGHT</sup>
tritetmesh	•	TriTetMesh
ufl	•	UFL
uqlab	•	UQLAB
viper	•	VIPER

## 7 SEMANTIC COMMANDS

xml

XML

Build upon Syntax from Section 4 this part provides semantic mathematical commands.

abs

absolute value. Its syntax is \abs[#1]{#2}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. The second argument denotes the argument.

4 \abs[Big]{\dfrac{1}{2}}  $\bullet$   $\left|\frac{1}{2}\right|$ 

aff affine hull 🐴 \aff • aff

arcosh area hyperbolic cosine 🐴 \arcosh 💿 arcosh

arcoth area hyperbolic cotangens 🐴 \arcoth 💿 arcoth

Argmax set of maximizers of a function  $\mbox{\sc Argmax}_{x \in \mathbb{R}} f(x)$  Argmax f(x)

Argmin set of minimizers of a function  $\mbox{\sc set}$  \Argmin\_{x \in \bbR} f(x)  $\mbox{\sc Arg min } f(x)$ 

arsinh area hyperbolic cotangens 📏 \arsinh 💿 arsinh

artanh area hyperbolic tangens 🔥 \artanh 💿 artanh

bold (meaning: vector) divergence of a matrix-valued function \$\div \\ \div \\

integer larger or equal to input. Its syntax is \ceil[#1]{#2}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. The second argument denotes the argument.

 $\$  \ceil[Big]{\dfrac{1}{2}}  $\$  \(\frac{1}{2}\)

closure of the convex hull of a set </>  $\odot \overline{\operatorname{conv}} M$ clconv closure cofactor matrix  $\langle \rangle \setminus cofac(A)$   $\odot cof(A)$ cofac compact embedding of topological spaces  $\checkmark$  \compactly  $\bigcirc$   $\hookrightarrow$   $\hookrightarrow$ compactly conic hull **//**\cone cone cone convex hull of a set  $\langle \rangle$  \conv M  $\odot$  conv M conv binary operator for correspondence 🐴 A\corresponds B  $\bullet$   $A \cong B$ corresponds covariance 📏 \cov 💿 Cov cov the curl operator **\\** \curl • curl curl d, dInt integral symbol with prepended space, as in  $\sqrt{\ } \left(-x^2\right) dx$ Since \d is often overridden, \dInt is the safe alternative deviator of a matrix 4 \dev A  $\odot$  dev A dev diag diagonal matrix composed of entries in a vector, or diagonal of a matrix diam dist0p the mathematical operator denoting the distance </>
\distOp dist dist distance from a point to a set. Its syntax is \dist[#1]{#2}{#3} or \dist[#1]{#2}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.1 The second argument denotes the set. The third argument denotes the point; it can be omitted. The command \distOp is used to typeset the operator. 

```
\ \dist{\cC} \odot dist<sub>C</sub>
                                                                        </k>
✓ \dist
• dist
                                                                        divergence // \div
                                                                                                                                                div
div
                                                                        (row-wise) divergence ⟨/⟩ \Div
                                                                                                                                                                                 Div
Div
                                                                        domain 🛂 \dom
                                                                                                                                     dom
dom
                                                                        distinct union </>
dotcup
dotcup
                                                                        double contraction of matrices A: B = \sum_{i,j} A_{ij} B_{ij} = \operatorname{trace}(A^{\mathsf{T}}B)
dprod
                                                                        A \cdot A \cdot A \cdot B
dual
                                                                        duality pairing. Its syntax is \dual[#1]{#2}{#3}. The first (optional) argu-
                                                                         ment is used to scale the delimiters enclosing the arguments to the standard
                                                                         amsmath sizes.1 The second argument denotes the first factor. The third
                                                                        argument denotes the second factor.
                                                                        \langle x^* \rangle \langle x^* \rangle \langle x^* \rangle
                                                                        \langle x^*, \frac{1}{2} \rangle \\dual[Big]{x^*}{\dfrac{1}{2}} \ \@\left\(x^*, \frac{1}{2}\right)$
                                                                        Euler's number 👍 \e • e
е
                                                                        embedding of topological spaces 🐴 \embed
embed
                                                                        synonym of \ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath}\ensuremath{\ensuremath{\mbox{\ensuremath{\mbox{\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath}\ensuremath
embeds
                                                                        epigraph 🖊 \epi 💿 epi
epi
                                                                        extended real line \P \ \eR = \bbR \cup \{\pm \infty\} \overline{\mathbb{R}} = \mathbb{R} \cup \mathbb{R}
eR
                                                                         \{\pm\infty\}
essinf
                                                                        essential infimum
                                                                                                                                                                                                                           \displaystyle\essinf_{x \in \bbR} f(x)
                                                                        essential supremum
esssup
                                                                        \ \displaystyle\esssup_{x \in \bbR} f(x)
                                                                                                                                                                                                                                 \odot ess sup f(x)
                                                                                                                                                                                                                                                x \in \mathbb{R}
```

file typesets a file name (using nolinkurl) </> \file{test.txt} test.txt integer less or equal to input. Its syntax is \floor[#1]{#2}. The first (opfloor tional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes.1 The second argument denotes the argument. 4 \floor[Big]{\\dfrac{1}{2}}  $\bigcirc$   $\left|\frac{1}{2}\right|$ gradient (of a function) 👍 \grad F  $\odot$  grad Fgrad graph of a function 🔥 \Graph 🗼 Graph Graph id image of a function </>
\image
• image image injectivity (radius) 🐴 \inj inj inner product. Its syntax is \inner[#1]{#2}{#3}. The first (optional) arinner gument is used to scale the parentheses enclosing the arguments to the standard amsmath sizes.<sup>1</sup> The second argument denotes the first factor. The third argument denotes the second factor.  $\langle a \rangle$  \inner{a}{b}  $\bullet (a, b)$ interior jump of a quantity, e.g., across a finite element facet. Its syntax is \jump[#1]{#2}. jump The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. The second argument denotes the argument.  $\langle \mathbf{/} \mathbf{\rangle} \setminus \mathsf{jump}\{a\}$   $\bullet$  [a]

 $\sqrt{\ \ \ \ \ }$  \jump[Big]{\\dfrac{1}{2}}

the Laplace operator 🐴 \laplace u

laplace

 $\odot$   $\Delta u$ 

lin

linear hull of a set of vectors  $\langle v_1, v_2 \rangle$   $\langle v_1, v_2 \rangle$ 

norm

norm of a vector. Its syntax is \norm[#1]{#2}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes.¹ The second argument denotes the argument.

$$\sqrt{\frac{c}{2}}$$
 \norm[auto]{\dfrac{c}{2}}

proj0p

the mathematical operator denoting the projection 👍 \projOp • proj

proj

projection onto a set. Its syntax is \proj[#1]{#2}(#3) or \proj[#1]{#2}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set and can also be left out. The third argument denotes the point; it can be omitted. The command \projOp is used to typeset the operator.

$$\langle / \rangle \operatorname{proj}(x)$$
  $\bullet$  proj $(x)$ 

$$\$$
 \proj{\cC} • proj\_C

$$\proj[Big](\proj[X]2)$$
  $\proj(\frac{x}{2})$ 

$$\$$
 \proj[Big]{\cC}(\dfrac{x}{2}) \ \ \ \proj\_C\left(\frac{x}{2}\right)

prox0p

the mathematical operator denoting the proximal map

prox

the proximal operator of a function. Its syntax is \prox[#1]{#2}(#3) or \prox[#1]{#2}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes. The second argument denotes the set. The third argument denotes the point; it can be omitted. The command \prox0p is used to typeset the operator.

 $\$  \prox{\lambda F}  $\odot$  prox<sub> $\lambda F$ </sub>  $\$  \prox{\lambda F}(x)  $\$  prox $_{\lambda F}(x)$ rank range of some operator **\\** \range \range range restriction/evaluation. Its syntax is \restr[#1]{#2}{#3}. The first (optional) restr argument is used to scale the deliminters enclosing the arguments to the standard amsmath sizes.1 The second argument denotes the argument to be restricted/evaluated. The third argument denotes the restriction set/evaluation point. relative interior 🐴 \ri 💿 ri ri define a set, where \setMid serves as the center divider. Its syntax is \setDef[#1]{#2}{#3}. setDef The first (optional) argument is used to scale the parentheses enclosing the argument and the center divider to the standard amsmath sizes.1 The second argument denotes the left part of the definition, naming the potential elements of the set being defined. The third argument denotes the condition to include the elements in the set.  $\$  \setDef{x\in\bbR}{x>5}  $\$   $\$   $\$   $\{x \in \mathbb{R} \mid x > 5\}$ divider within \setDef (set definitions). setMid sign 🔥 \sgn 💿 sgn sgn sign (set valued) 🔥 \Sgn 💿 Sgn Sgn support (of a function)  $\checkmark \searrow \searrow F$   $\bigcirc$  supp Fsupp symmetric part (of a matrix) 🐴 \sym A  $\odot$  sym A sym

trace (of a matrix)  $\checkmark$  \trace A •• trace A

**transp** transpose of a vector or matrix.

4 A^\transp  $\bullet$   $A^{\mathsf{T}}$ 

**transposeSymbol** symbol to use for the transpose

var variance 📏 \var 💿 Var

weakly weak convergence of a sequence ⟨♠⟩ \weakly • →

weaklystar weak star convergence of a sequence ♦ \ \weaklystar \ • \ \\*

## 8 Additional Semantics by Topic

While semantic commands might be suitable for all mathematical topics, the following subsections collect commands which are most useful in one particular mathematical area and hence might clutter the general semantic file. Any semantic topic files should always build on mathsemantics-semantic. sty.

#### 8.1 Manifolds: mathsemantics-manifolds.sty

The semantic file mathsemantics-manifolds.sty collects definitions and notations for Riemannian manifolds.

bitangentSpace the bi tangent space. Its syntax is \bitangent{#1}[#2]. The first argument

denotes the base point. The second (optional) argument denotes the manifold,

which defaults to  $\mathcal{M}$ .

 $\begin{cases} $ \begin{cases} $ \begin{cases$ 

 $\label{eq:parameters} \$  \bitangentSpace{q}[\cN]  $\$   $\$   $\mathcal{T}_q^{**}\mathcal{N}$ 

bitangentSpaceSymbol the symbol used within \bitangentSpace.

 $\begin{tabular}{ll} \begin{tabular}{ll} \beg$ 

#### cotangentSpace

the cotangent space. Its syntax is  $\operatorname{cotangentSpace}\{\#1\}[\#2]$ . The first argument denotes the base point. The second (optional) argument denotes the manifold, which defaults to  $\mathcal{M}$ .

 $\langle \mathbf{/} \rangle$  \cotangentSpace{p}  $\odot \mathcal{T}_p^* \mathcal{M}$ 

#### cotangentBundle

the cotangent bundle. Its syntax is  $\operatorname{cotangentBundle}[\#1]$ . The (optional) argument denotes the manifold, which defaults to  $\mathcal{M}$ .

cotangentSpaceSymbol the symbol used within \cotangent.

#### covariantDerivative

is the covariant derivative. Its syntax is \covariantDerivative{#1}[#2]. The first argument is the vector (or vector field) determining the direction of differentiation. The second (optional) argument denotes the tensor field being differentiated.

 $\langle X \rangle \sim D_X Y$ 

covariantDerivativeSymbble symbol used for the covariant derivative \covariantDerivative.

⟨**/**\$ \covariantDerivativeSymbol
◆ D

### exponential

the exponential map. Its syntax is \exponential[#1]{#2}(#3). The first argument can be used to scale the third. The second argument denotes the base point and is mandatory. The third argument denotes the tangent vector, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

**expOp** the symbol used within the \exponential.

geodesic

a geodesic. Its syntax is  $\ensuremath{\mbox{\mbox{$\setminus$}} \ensuremath{\mbox{$\setminus$}} \ensuremath{\mbox{$\setminus$ 

 $\$  \geodesic<s>  $\bigcirc$   $\gamma$ 

 $\$  \geodesic<s>(t)  $\$   $\gamma(t)$ 

 $\$  \geodesic<\p\{q\}  $\$  \ $\gamma(\cdot;p,q)$ 

 $\$  \geodesic<\p\{q\(t)\)  $\$  \geodesic<\p\{q\(t)\)

 $\langle \mathbf{q} \rangle$  \geodesic<a>{p}{q}  $\mathcal{Q} \gamma_{\widehat{p},q}$ 

\$\quad \quad \qua

 $\protect\$  \geodesic\{p\{X\} \phi\{Y}\_{p,X}

 $\$  \geodesic|\dot\gamma|{p}{X}(t)  $\$   $\dot{y}_{p,X}(t)$ 

geodesicSymbol symbol to use for the geodesic in \geodesic

 $\$  \inverseRetract{p}q  $\$  retr $_p^{-1}q$ 

$$\$$
 \inverseRetract{p}(q)  $\$  retr $_p^{-1}(q)$ 

$$\$$
 \inverseRetract[Big]{p}(q)  $\$  retr $_p^{-1}(q)$ 

logarithm

the logarithmic map. Its syntax is \logarithm[#1]{#2}(#3). The first argument can be used to scale the third. The second argument denotes the base point and is mandatory. The third argument denotes another point, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

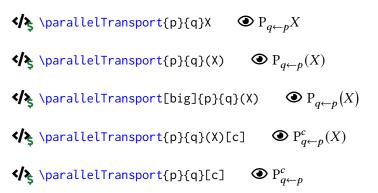
log0p

the symbol used within the \logarithm.

#### parallelTransport

the parallel transport.

Its syntax is \parallelTransport[#1]{#2}{#3}(#4){5}. The first (optional) argument is used to scale the parentheses enclosing the argument #4.1 The second argument is the start point of parallel transport on a manifold. The third argument is the end point of parallel transport on a manifold. The fourth (optional) argument is the tangent vector that is transported. Putting it in brackets enables the scaling by the first argument. The fifth (optional) argument specifies an exponent, for example to parallel transport along a curve c



parallelTransportDir similar to \parallelTransport, but the third argument is a direction to transport into. This can be rewritten to the classical notation applying an exponential map from the base point (#2) to th direction (#3). The fifth (optional) argument specifies an exponent, for example to parallel transport along a curve c

 $\begin{tabular}{ll} $\P_{p,Y}X$ & $\P_{p,Y}$ 

 $\protect\$  \parallelTransportDir{p}{Y}(X)  $\protect\$   $\protect\$ 

 $\label{eq:parallelTransportDir[big]} \$  \parallelTransportDir[big]\{p}\{Y}\(X) \ \emptyred \text{P}\_{p,Y}(X)

 $\label{eq:parallelTransportDir} \$  \parallelTransportDir $\{p\}\{Y\}[c]$   $\$   $\$   $P_{p,Y}^c$ 

parallelTransportSymbol the symbol to use within \parallelTransport and \parallelTransportDir

⟨**/**⟩ \parallelTransportSymbol
• P

retract a retraction.

Its syntax is \retract[#1]{#2}{#3}. The first argument can be used to scale the third. The second argument denotes the base point. The third argument denotes the tangent vector, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

$$\P$$
 \retract[Big]{p}(\frac{X}{2})  $\P$  retr $_p(\frac{X}{2})$ 

retractionSymbol

symbol to use for a retraction and an inverse retraction, see \retract and \inverseRetract.

riemannian

the Riemannian metric (family of inner products on the tangent spaces). Its syntax is \riemannian[#1]{#2}{#3}[#4]. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the first factor. The third argument denotes the second factor. The fourth (optional) argument denotes the base point of the tangent space.

$$\$$
 \riemannian{Y\_1}{Y\_2}[q]  $\$   $(Y_1, Y_2)_q$ 

\riemannian[Big]{\dfrac{1}{2}X\_1}{X\_2}[p]

 $\bullet$   $\left(\frac{1}{2}X_1, X_2\right)_{\mathbf{p}}$ 

riemanniannorm

the norm induced by the Riemannian metric.

Its syntax is \riemanniannorm[#1]{#2}[#3]. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.1 The second argument denotes the argument. The third (optional) argument denotes the base point of the tangent space.

 $\langle \rangle$  \riemanniannorm{X}  $\bigcirc ||X||$ 

 $\$  \riemanniannorm{Y}[p]  $\$  \(\Pi\)

**secondCovariantDerivative** is the second-order covariant derivative.

Its syntax is \secondCovariantDerivative{#1}{#2}[#3]. The first argument is the vector (or vector field) determining the first direction of differentiation. The second argument is the vector (or vector field) determining the second direction of differentiation. The third (optional) argument denotes the tensor field being differentiated.

the symbol used for the second covariant derivative. secondCovariantDerivativeSymbol

This is used within \secondCovariantDerivative.

\$\secondCovariantDerivativeSymbol

tangentSpace

the tangent space. Its syntax is \tangentSpace{#1}[#2]. The first argument denotes the base point. The second (optional) argument denotes the manifold, which defaults to  $\mathcal{M}$ .

tangentBundle

the tangent bundle. Its syntax is \tangentBundle[#1]. The (optional) argument denotes the manifold, which defaults to  $\mathcal{M}$ .

 $\$  \tangentBundle  $\odot \mathcal{TM}$ 

 $\$  \tangentBundle[\cN]  $\$   $\mathcal{T}\mathcal{N}$ 

tangentSpaceSymbol the symbol used within \tangent.



#### tensorBundle

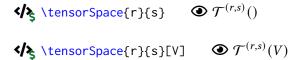
the tensor bundle. Its syntax is  $\tensorBundle{#1}{#2}[#3]$ . The first argument denotes the number r of elements of the cotangent space the tensors accept. The second argument denotes the number s of elements of the tangent space the tensors accept. The third (optional) argument denotes the manifold, which defaults to  $\mathcal{M}$ .

$$\fill \fill \fil$$

$$\fint{1.5} $$ \end{1.5} $$ \end{1.5} \fint{1.5} \fint$$

#### tensorSpace

a tensor space over a vector space V. Its syntax is \tensorSpace{#1}{#2}[#3]. The first argument denotes the number r of elements of the dual space  $V^*$  the tensors accept. The second argument denotes the number s of elements of the space V the tensors accept. The third (optional) argument denotes the vector space, which defaults to empty.



#### tensorSpaceSymbol

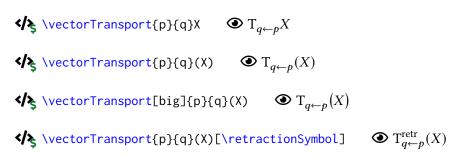
the symbol used within \tensorSpace and \tensorBundle.



#### vectorTransport

a vector transport.

Its syntax is \vectorTransport[#1]{#2}{#3}(#4)[#5]. The first (optional) argument is used to scale the parentheses enclosing the argument #4.¹ The second argument is the start point of vector transport on a manifold. The third argument is the end point of vector transport on a manifold. The fourth (optional) argument is the tangent vector that is transported. Putting it in brackets enables the scaling by the first argument. Finally a retraction symbol can be added in the exponent to distinguish vector transports as #5.



## vectorTransportDir

similar to \vectorTransport, but the third argument is a direction to transport into. This can be rewritten to the classical notation applying an retraction

from the base point (#2) to th direction (#3).

 $\protect\$  \vectorTransportDir{p}{Y}(X)  $\protect\$   $\protect\$ 

 $\$  \vectorTransportDir{p}{Y}(X)[\retractionSymbol]  $\$   $\$   $T_{p,Y}^{retr}(X)$ 

vectorTransportSymbol the symbol to use within \vectorTransport and \vectorTransportDir

⟨/≥ \vectorTransportSymbol
▼ T

#### 8.2 Optimization: mathsemantics-optimization.sty

The semantic file mathsemantics-optimization.sty collects definitions and notations related to optimization.

#### linearizingcone

the linearizing cone. Its syntax is \linearizingcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

#### normalcone

the normal cone. Its syntax is \normalcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

polarcone

the polar cone of a set  $\P$  \polarcone{A}  $ext{ } A^{\circ}$ 

radialcone

the radial cone. Its syntax is \radialcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

\\ \radialcone{A}{x} \@ 
$$\mathcal{K}_A(x)$$
\\ \radialcone{A}{x^2} \@  $\mathcal{K}_A(x^2)$ 
\\ \radialcone[big]{A}{x^2} \@  $\mathcal{K}_A(x^2)$ 

tangentcone

the tangent cone. Its syntax is \tangentcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

