

MATHSEMANTICS.STY – SEMANTIC MATH COMMANDS

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
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1 INTRODUCTION

This package aims to provide semantic commands for ease of use in mathematics to see better *what* you semantically mean which should be distinct/split from *how* it is realised in \LaTeX .




The package is a spin-off and developed in the suite of packages from the former numapde-group in Chemnitz, see the original repository at <https://gitlab.hrz.tu-chemnitz.de/numapde-public/numapde-latex>.

Throughout this documentation most commands are directly illustrated by examples, which are both displayed as code (`</>` or `</>` for math examples) and its rendered result in \LaTeX (). Two examples are

`</> \bbR`  \mathbb{R}

and

`</> \eg`  e. g.

The aim is to first ease the use of some often used letters and low-level formats like bold face letters `</> \bbR`  \mathbb{R} , but also to provide high level commands that make typing mathematics easier, for example using `</> \abs{\frac{1}{2}}`  $|\frac{1}{2}|$ and `</> \abs[Big]{\frac{1}{2}}`  $\left|\frac{1}{2}\right|$. This is the main goal in [Section 4](#) about syntactical commands for mathematics. A next more support/helping section about abbreviations and names is [Section 5](#).

The first main part on general semantic commands is [Section 7](#).

While all these are loaded by default. The next part, [Section 8](#), introduces semantic commands for specific topics. These are given in separate sub-packages and can be loaded if you work in this area and want to use the commands.

The package should be loaded late, since it might overwrite a few commands, currently most prominently `\d` which is overwritten by `cleveref` in case `minted` is loaded. So for more flexibility, there is the alternative command `\dInt`.

2 PACKAGE OPTIONS

`shortbb` use shorter notations for the blackboard-bold math letters `\C`, `\K`, `\N`, `\Q`, `\R`, `\Z`

3 REQUIRED PACKAGES

amssymb.sty defines mathematical symbol fonts

ifthen.sty facilitates the definition of conditional commands

ifxetex.sty provides a way to check if a document is being processed by \XeTeX and company

mathtools.sty provides lots of improvements for math typesetting (includes `amsmath.sty`)

xifthen.sty extends `ifthen.sty` by adding new boolean conditions

xparse.sty provides a high-level interface to define new commands





xspace.sty adds space depending on context

4 SYNTAX

The mathsemantics-syntax.sty package provides mainly symbols and short commands, which can be used in semantic definitions for ease of notation. They usually are rather simple commands without too many parameters.


4.1 LETTERS

ba...bz	lower-case bold-face letters $\backslash br, \backslash bf$ r, f
bA...bZ	upper-case bold-face letters $\backslash bR, \backslash bF$ R, F
balpha...bomega	lower-case bold-face Greek letters $\backslash balpha, \boldsymbol{\det}$ α, η (the latter being an exception)
bAlpha...bOmega	upper-case bold-face Greek letters $\backslash bGamma, \backslash bDelta$ Γ, Δ
bnull	bold-face zero $\backslash bnull$ 0
bone	bold-face one $\backslash bone$ 1
cA...cZ	upper-case calligraphic letters $\backslash cM, \backslash cN$ \mathcal{M}, \mathcal{N}
fA...fZ	upper-case fraktur letters $\backslash fM, \backslash fN, \backslash fX$ $\mathfrak{M}, \mathfrak{N}, \mathfrak{X}$
sA...sZ	upper-case script letters $\backslash sM, \backslash sN, \backslash sX$ $\mathscr{M}, \mathscr{N}, \mathscr{X}$
va...vz	lower-case letters with a vector accent $\backslash va, \backslash vb$ \vec{a}, \vec{b}
vA...vZ	upper-case letters with a vector accent $\backslash vA, \backslash vB$ \vec{A}, \vec{B}
valpha...vomega	lower-case Greek letters with a vector accent $\backslash valpha, \backslash vbeta$ $\vec{\alpha}, \vec{\beta}$
vAlpha...vOmega	upper-case Greek letters with a vector accent $\backslash vGamma, \backslash vDelta$ $\vec{\Gamma}, \vec{\Delta}$


vnull	vector zero <code>\vnull</code>  $\vec{0}$
vone	vector one <code>\vone</code>  $\vec{1}$
bbA,...,bbZ	blackboard-bold uppercase letters <code>\bbC,\bbK,\bbN,\bbQ,\bbR,\bbS,\bbZ</code>  $\mathbb{C}, \mathbb{K}, \mathbb{N}, \mathbb{Q}, \mathbb{R}, \mathbb{S}, \mathbb{Z}$ use the package option shortbb to introduce <code>\C,\K,\N,\Q,\R,\Z</code>  $\mathbb{C}, \mathbb{K}, \mathbb{N}, \mathbb{Q}, \mathbb{R}, \mathbb{Z}$ if not already defined elsewhere (i. e. they are not redefined, only <i>provided</i>).

4.2 SYNTAX HELPERS

enclspacing	provides spacing after the opening and before the closing delimiters for <code>\enclose</code> . This is by default set to be empty.
enclose	is a command which encloses some content in scaled delimiters. It is meant as a helper to facilitate the definition of other commands. Its syntax is <code>\enclose[#1]{#2}{#3}{#4}</code> . The first (optional) argument is used to scale the delimiters to the standard amsmath sizes. ¹ The second and fourth arguments specify the opening and closing delimiters, respectively. The third argument is the content to be enclosed.

`\enclose{[]}{\dfrac{1}{2}}{[]}`  $\left[\frac{1}{2}\right]$

`\enclose[Big][\dfrac{1}{2}]`  $\left[\frac{1}{2}\right]$

`\enclose[auto]{[]}{\dfrac{1}{2}}{[]}`  $\left[\frac{1}{2}\right]$

`\enclose[none]{[]}{\dfrac{1}{2}}{[]}`  $\frac{1}{2}$



Note 1. none is merely meant for testing when having arguments in brackets whether it is useful to omit them. You can also deactivate the absolute value vertical lines this way, so *use this option with care*.



Note 2. This command should normally be used only in the definition of other commands. For instance, `\abs` is using it internally. See `\paren` for the nicer command to use

¹big, Big, bigg, Bigg or auto, which uses left and right as well as none to easily deactivate brackets.

`enclspacingSet` provides spacing before and after the center delimiter `\encloseSet`. This is by default set to `\,`.



`encloseSet` is a command which encloses some content in scaled delimiters. It is meant as a helper to facilitate the definition of other commands. Its syntax is `\encloseSet[#1]{#2}{#3}{#4}{#5}{#6}`. The first (optional) argument is used to scale the delimiters including the center one to the standard `ams-math` sizes.¹ The second and sixth arguments specify the opening and closing delimiters, respectively. The fourth argument specifies the center delimiter and The third and fifth argument are the content to be enclosed.

 `\encloseSet[big]{\{\}\{x\in\mathbb{R}\}{|}\{x>5\}\}`  $\{x \in \mathbb{R} \mid x > 5\}$



 `\encloseSet[auto]{\{\}\{x\in\mathbb{R}\}{|}\{x>\dfrac{1}{2}\}\}` 
 $\left\{x \in \mathbb{R} \mid x > \frac{1}{2}\right\}$

Note. This command should normally be used only in the definition of other commands. For instance, `\setDef` is using it internally.

`paren` is an alternative to `\enclose`, with a different ordering of arguments. Its syntax is `\paren[#1]{#2}{#3}{#4}`, which is simply mapped to `\enclose[#1]{#2}{#4}{#3}`.

 `\paren[Big]{\{\}\{\}\{\dfrac{1}{2}\}}`  $\left[\frac{1}{2}\right]$

 `\paren[Big]{\{\}\{\dfrac{1}{2}\}}`  $\left[\frac{1}{2}\right]$

 `\paren[auto]{\{\}\{\}\{\dfrac{1}{2}\}}`  $\left[\frac{1}{2}\right]$

4.3 SPACING HELPERS

`clap` complements the standard \LaTeX commands `\llap` and `\rlap`. These commands horizontally smash their arguments.

 Let us `\llap{smash}` something.  Let us ~~smash~~ something.


 Let us `\clap{smash}` something.  Let us ~~smash~~ something.

 Let us `\rlap{smash}` something.  Let us ~~smash~~ something.


`mathllap` corresponds to `\llap` in math mode.

`</> \sum_{\mathllap{1\leq i\leq j\leq n}} X_{ij}`  $\sum_{1\leq i\leq j\leq n} X_{ij}$


mathclap corresponds to `\clap` in math mode.


`</> \sum_{\mathclap{1\leq i\leq j\leq n}} X_{ij}`  $\sum_{1\leq i\leq j\leq n} X_{ij}$


mathrlap corresponds to `\rlap` in math mode.

`</> \sum_{\mathrlap{1\leq i\leq j\leq n}} X_{ij}`  $\sum_{1\leq i\leq j\leq n} X_{ij}$

mrep stands for *math replace* and it typesets an argument while reserving the space for another. Its syntax is `\mrep[#1]{#2}{#3}`. The first (optional) argument is one of {l,c,r} and it is used to define the alignment. c is the default.

`</> \mrep[l]{1}{-1}-1`  $1 - 1$


`</> \mrep[c]{1}{-1}-1`  $1 - 1$


`</> \mrep[r]{1}{-1}-1`  $1 - 1$


5 ABBREVIATIONS


5.1 ENGLISH


aa almost all `</> \aa`  a.a.


ale almost everywhere `</> \ale`  a.e.


eg exempli gratia (for example) `</> \eg`  e. g.


etc et cetera (and so on) `</> \etc`  etc.

ie id est (id est) `</> \ie`  i. e.


iid independent and identically distributed `</> \iid`  i. i. d.


spd symmetric positive definite `</> \spd`  s. p. d.


st such that or subject to `</> \st`  s. t.


wrt with respect to \langle / \rangle `\wrt`  w.r.t.

5.2 GERMAN

bspw beispielsweise (for example) \langle / \rangle `\bspw`  bspw.


bzgl bezüglich (with regard to) \langle / \rangle `\bzgl`  bzgl.


bzw beziehungsweise (respectively) \langle / \rangle `\bzw`  bzw.


Dah Das heißt (That is, beginning of phrase) \langle / \rangle `\Dah`  D. h.

dah das heißt (that is) \langle / \rangle `\dah`  d. h.

evtl eventuell (possibly) \langle / \rangle `\evtl`  evtl.


fs fast sicher \langle / \rangle `\fs`  f. s.

fue fast überall \langle / \rangle `\fue`  f. ü.


IA Im Allgemeinen (beginning of phrase) \langle / \rangle `\IA`  I. A.

iA im Allgemeinen \langle / \rangle `\iA`  i. A.


idR in der Regel \langle / \rangle `\idR`  i. d. R.

IdR In der Regel (beginning of phrase) \langle / \rangle `\IdR`  I. d. R.


iW im Wesentlichen \langle / \rangle `\iW`  i. W.


IW Im Wesentlichen (beginning of phrase) \langle / \rangle `\IW`  I. W.


mE meines Erachtens \langle / \rangle `\mE`  m. E.












oBdA ohne Beschränkung der Allgemeinheit \langle / \rangle `\oBdA`  o. B. d. A.

OBdA ohne Beschränkung der Allgemeinheit (beginning of phrase)

\langle / \rangle `\OBdA`  O. B. d. A.

og oben genannt \langle / \rangle `\og`  o. g.

oae oder ähnliche \langle / \rangle `\oae`  o. ä.

so	siehe oben <code></> \so</code>  s. t.
ua	unter anderem <code></> \ua</code>  u. a.
Ua	Unter anderem (beginning of phrase) <code></> \Ua</code>  U. a.
ug	unten genannt <code></> \ug</code>  u. g.
usw	und so weiter (and so on)  usw.
uU	unter Umständen <code></> \uU</code>  u. U.
UnU	Unter Umständen (beginning of phrase) <code></> \UnU</code>  U. U.
vgl	vergleiche (compare) <code></> \vgl</code>  vgl.
zB	zum Beisiel <code></> \zB</code>  z. B.
ZB	Zum Beispiel (beginning of phrase) <code></> \ZB</code>  Z. B.
zHd	zu Händen <code></> \zHd</code>  z. Hd.

6 NAMES

adimat	 ADiMAT
ampl	 AMPL
BibTeX	 BiBTeX
BibLaTeX	 BiBLaTeX
cg	 CG
cpp	 C++
cppmat	 CPPMAT
dolfin	 DOLFIN
dolfinplot	 DOLFIN-PLOT
dolfinadjoint	 DOLFIN-ADJOINT

doxygen	 DOXYGEN
femorph	 FEMORPH
fenics	 FENICS
ffc	 FFC
fmg	 FMG
fortran	 FORTRAN
gitlab	 GITLAB
gmres	 GMRES
gmsh	 GMSH
ipopt	 IPOPT
libsvm	 LIBSVM
liblinear	 LIBLINEAR
macmpec	 MACMPEC
manifoldsjl	 MANIFOLDS.JL
manopt	 MANOPT
manoptjl	 MANOPT.JL
mathematica	 MATHEMATICA
matlab	 MATLAB
maple	 MAPLE
maxima	 MAXIMA
metis	 METIS
minres	 MINRES
mshr	 MSHR
mvirt	 MVIRT

numpy	👁 NUMPy
paraview	👁 PARAVIEW
pdflatex	👁 PDFL ^A T _E X
perl	👁 PERL
petsc	👁 PETSc
pymat	👁 PYMAT
python	👁 PYTHON
scikit	👁 SciKit
scikitlearn	👁 SciKit-LEARN
scipy	👁 SciPy
sphinx	👁 SPHINX
subgmres	👁 SUBGMRES
subminres	👁 SUBMINRES
superlu	👁 SUPERLU
svmlight	👁 SVM ^{LIGHT}
tritetmesh	👁 TriTETMESH
ufl	👁 UFL
uqlab	👁 UQLAB
viper	👁 VIPER
xml	👁 XML

7 SEMANTIC COMMANDS

Build upon Syntax from [Section 4](#) this part provides semantical mathematical commands.



abs	absolute value. Its syntax is <code>\abs[#1]{#2}</code> . The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. ¹ The second argument denotes the argument.
	$\backslash\abs{a}$ $ a $
	$\backslash\abs[Big]{\dfrac{1}{2}}$ $\left \frac{1}{2}\right $
	$\backslash\abs[auto]{\dfrac{1}{2}}$ $\left \frac{1}{2}\right $
aff	affine hull $\backslash\aff$ aff
arcosh	area hyperbolic cosine $\backslash\arcosh$ arcosh
arcoth	area hyperbolic cotangens $\backslash\arcoth$ arcoth
argmax	maximizer of a function $\backslash\argmax_{\{x \in \mathbb{R}\}} f(x)$ $\arg \max_{x \in \mathbb{R}} f(x)$
Argmax	set of maximizers of a function $\backslash\Argmax_{\{x \in \mathbb{R}\}} f(x)$ $\text{Arg} \max_{x \in \mathbb{R}} f(x)$
argmin	minimizer of a function $\backslash\argmin_{\{x \in \mathbb{R}\}} f(x)$ $\arg \min_{x \in \mathbb{R}} f(x)$
Argmin	set of minimizers of a function $\backslash\Argmin_{\{x \in \mathbb{R}\}} f(x)$ $\text{Arg} \min_{x \in \mathbb{R}} f(x)$
arsinh	area hyperbolic cotangens $\backslash\arsinh$ arsinh
artanh	area hyperbolic tangens $\backslash\artanh$ artanh
bdiv	bold (meaning: vector) divergence of a matrix-valued function $\backslash\bdiv$ div
ceil	integer larger or equal to input. Its syntax is <code>\ceil[#1]{#2}</code> . The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. ¹ The second argument denotes the argument.
	$\backslash\ceil{a}$ $\lceil a \rceil$
	$\backslash\ceil[Big]{\dfrac{1}{2}}$ $\left\lceil\frac{1}{2}\right\rceil$

clconv	closure of the convex hull of a set <code>\clconv</code> M $\overline{\text{conv}} M$
closure	closure of a set <code>\closure</code> M $\text{cl } M$
cofac	cofactor matrix <code>\cofac</code> (A) $\text{cof}(A)$
compactly	compact embedding of topological spaces <code>\compactly</code> \hookrightarrow
cone	conic hull <code>\cone</code> cone
conv	convex hull of a set <code>\conv</code> M $\text{conv } M$
corresponds	binary operator for correspondence <code>A \corresponds B</code> $A \cong B$
cov	covariance <code>\cov</code> Cov
curl	the curl operator <code>\curl</code> curl
d, dInt	integral symbol with prepended space, as in $\int_{\mathbb{R}} \exp(-x^2) \, dx$ Since <code>\d</code> is often overridden, <code>\dInt</code> is the safe alternative
dev	deviator of a matrix <code>\dev</code> A $\text{dev } A$
diag	diagonal matrix composed of entries in a vector, or diagonal of a matrix $\text{diag}(a)$ $\text{diag}(A)$
diam	diameter <code>\diam</code> (M) $\text{diam}(M)$
distOp	the mathematical operator denoting the distance dist
dist	distance from a point to a set. Its syntax is <code>\dist[#1]{#2}{#3}</code> or <code>\dist[#1]{#2}</code> . The first (optional) argument is used to scale the parantheses enclosing the argument to the standard amsmath sizes. ¹ The second argument denotes the set. The third argument denotes the point; it can be omitted. The command <code>\distOp</code> is used to typeset the operator. $\text{dist}_C\left(\frac{x}{2}\right)$

	<code>\dist{\cC}</code> dist_C
	<code>\dist</code> dist
div	divergence <code>\div</code> div
Div	(row-wise) divergence <code>\Div</code> Div
dom	domain <code>\dom</code> dom
dotcup	distinct union <code>\dotcup</code> \cup
dprod	double contraction of matrices $A : B = \sum_{i,j} A_{ij} B_{ij} = \text{trace}(A^T B)$
	<code>A \dprod B</code> $A : B$
dual	duality pairing. Its syntax is <code>\dual[#1]{#2}{#3}</code> . The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. ¹ The second argument denotes the first factor. The third argument denotes the second factor.
	<code>\dual{x^*}{x}</code> $\langle x^*, x \rangle$
	<code>\dual[Big]{x^*}{\dfrac{1}{2}}</code> $\left\langle x^*, \frac{1}{2} \right\rangle$
e	Euler's number <code>\e</code> e
embed	embedding of topological spaces <code>\embed</code> \hookrightarrow
embeds	synonym of <code>\embed</code> <code>\embeds</code> \hookrightarrow
epi	epigraph <code>\epi</code> epi
eR	extended real line <code>\eR = \bbR \cup \{\pm\infty\}</code> $\overline{\mathbb{R}} = \mathbb{R} \cup \{\pm\infty\}$
essinf	essential infimum
	<code>\displaystyle\essinf_{x \in \bbR} f(x)</code> $\text{ess inf}_{x \in \mathbb{R}} f(x)$
esssup	essential supremum
	<code>\displaystyle\esssup_{x \in \bbR} f(x)</code> $\text{ess sup}_{x \in \mathbb{R}} f(x)$

file	typesets a file name (using nolinkurl) $\backslash\text{file}\{\text{test.txt}\}$ test.txt
floor	integer less or equal to input. Its syntax is $\backslash\text{floor}[\#1][\#2]$. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. ¹ The second argument denotes the argument. $\backslash\text{floor}\{a\}$ $\lfloor a \rfloor$ $\backslash\text{floor}[\text{Big}][\backslash\text{dfrac}\{1\}\{2\}]$ $\left\lfloor \frac{1}{2} \right\rfloor$
grad	gradient (of a function) $\backslash\text{grad } F$ $\text{grad } F$
Graph	graph of a function $\backslash\text{Graph}$ Graph
id	identity operator $\backslash\text{id}$ id
image	image of a function $\backslash\text{image}$ image
inj	injectedivity (radius) $\backslash\text{inj}$ inj
inner	inner product. Its syntax is $\backslash\text{inner}[\#1][\#2][\#3]$. The first (optional) argument is used to scale the parentheses enclosing the arguments to the standard amsmath sizes. ¹ The second argument denotes the first factor. The third argument denotes the second factor. $\backslash\text{inner}\{a\}\{b\}$ (a, b) $\backslash\text{inner}[\text{Big}][a][\backslash\text{dfrac}\{b\}\{2\}]$ $\left(a, \frac{b}{2}\right)$
interior	$\backslash\text{interior}$ int
jump	jump of a quantity, e. g., across a finite element facet. Its syntax is $\backslash\text{jump}[\#1][\#2]$. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. ¹ The second argument denotes the argument. $\backslash\text{jump}\{a\}$ $\llbracket a \rrbracket$ $\backslash\text{jump}[\text{Big}][\backslash\text{dfrac}\{1\}\{2\}]$ $\left\llbracket \frac{1}{2} \right\rrbracket$
laplace	the Laplace operator $\backslash\text{laplace } u$ Δu

lin	linear hull of a set of vectors $\langle / \rangle \text{ \textcolor{blue}{\lin}\{v_1,v_2\} } \quad \text{👁} \text{ lin}\{v_1, v_2\}$
norm	<p>norm of a vector. Its syntax is $\text{ \textcolor{blue}{\norm}\{ \#1 \} \{ \#2 \} }$. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes.¹ The second argument denotes the argument.</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\norm}\{a\} } \quad \text{👁} \ a\$</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\norm}\text{[Big]}\{\text{\textcolor{blue}{\dfrac}\{c\}\{2\}}\} } \quad \text{👁} \left\ \frac{c}{2} \right\$</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\norm}\text{[auto]}\{\text{\textcolor{blue}{\dfrac}\{c\}\{2\}}\} } \quad \text{👁} \left\ \frac{c}{2} \right\$</p>
projOp	the mathematical operator denoting the projection $\langle / \rangle \text{ \textcolor{blue}{\projOp} } \quad \text{👁} \text{ proj}$
proj	<p>projection onto a set. Its syntax is $\text{ \textcolor{blue}{\proj}\{ \#1 \} \{ \#2 \} (\#3) }$ or $\text{ \textcolor{blue}{\proj}\{ \#1 \} \{ \#2 \} }$. The first (optional) argument is used to scale the parantheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set and can also be left out. The third argument denotes the point; it can be omitted. The command $\text{ \textcolor{blue}{\projOp} }$ is used to typeset the operator.</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\proj} } \quad \text{👁} \text{ proj}$</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\proj}(x) } \quad \text{👁} \text{ proj}(x)$</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\proj}\{\text{\textcolor{blue}{\cC}\}} } \quad \text{👁} \text{ proj}_C$</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\proj}\{\text{\textcolor{blue}{\cC}\}}(x) } \quad \text{👁} \text{ proj}_C(x)$</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\proj}\text{[Big]}\(\text{\textcolor{blue}{\dfrac}\{x\}\{2\}}\) } \quad \text{👁} \text{ proj}\left(\frac{x}{2}\right)$</p> <p>$\langle / \rangle \text{ \textcolor{blue}{\proj}\text{[Big]}\{\text{\textcolor{blue}{\cC}\}}(\text{\textcolor{blue}{\dfrac}\{x\}\{2\}}) } \quad \text{👁} \text{ proj}_C\left(\frac{x}{2}\right)$</p>
proxOp	the mathematical operator denoting the proximal map
prox	<p>$\langle / \rangle \text{ \textcolor{blue}{\proxOp} } \quad \text{👁} \text{ prox}$</p> <p>the proximal operator of a function. Its syntax is $\text{ \textcolor{blue}{\prox}\{ \#1 \} \{ \#2 \} (\#3) }$ or $\text{ \textcolor{blue}{\prox}\{ \#1 \} \{ \#2 \} }$. The first (optional) argument is used to scale the parantheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the point; it can be omitted. The command $\text{ \textcolor{blue}{\proxOp} }$ is used to typeset the operator.</p>

	$\backslash prox$  $prox$
	$\backslash prox\{\backslash lambda F\}$  $prox_{\lambda F}$
	$\backslash prox\{\backslash lambda F\}(x)$  $prox_{\lambda F}(x)$
	$\backslash prox[auto]\{\backslash lambda F\}(\backslash dfrac{x}{2})$  $prox_{\lambda F}\left(\frac{x}{2}\right)$
rank	rank (of a matrix) $\backslash rank$  $rank$
range	range of some operator $\backslash range$  $range$
restr	restriction/evaluation. Its syntax is $\backslash restr[\#1]\{\#2\}\{\#3\}$. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. ¹ The second argument denotes the argument to be restricted/evaluated. The third argument denotes the restriction set/evaluation point.
	$\backslash restr[auto]\{\backslash frac{d}{dt}\{f \circ \gamma\}(t)\}\{t=0\}$  $\left.\frac{d}{dt}(f \circ \gamma)(t)\right _{t=0}$
ri	relative inerior $\backslash ri$  ri
setDef	define a set, where $\backslash setMid$ serves as the center divider. Its syntax is $\backslash setDef[\#1]\{\#2\}\{\#3\}$. The first (optional) argument is used to scale the parantheses enclosing the argument and the center divider to the standard amsmath sizes. ¹ The second argument denotes the left part of the definition, naming the potential elements of the set being defined. The third argument denotes the condition to include the elements in the set.
	$\backslash setDef\{x \in \mathbb{R}\}\{x > 5\}$  $\{x \in \mathbb{R} \mid x > 5\}$
	$\backslash setDef[Big]\{x \in \mathbb{R}\}\{x > \backslash dfrac{1}{2}\}$  $\left\{x \in \mathbb{R} \mid x > \frac{1}{2}\right\}$
setMid	divider within $\backslash setDef$ (set definitions). This defaults to $\backslash setMid$  $ $.
sgn	sign $\backslash sgn$  sgn
Sgn	sign (set valued) $\backslash Sgn$  Sgn
supp	support (of a function) $\backslash supp F$  $supp F$
sym	symmetric part (of a matrix) $\backslash sym A$  $sym A$

trace	trace (of a matrix) $\langle \! / \rangle_{\$} \backslash \text{trace} A$ $\text{trace } A$
transp	transpose of a vector or matrix. $\langle \! / \rangle_{\$} A^{\backslash \text{transp}}$ A^T
transposeSymbol	symbol to use for the transpose $\langle \! / \rangle_{\$} \backslash \text{transposeSymbol}$ T
var	variance $\langle \! / \rangle_{\$} \backslash \text{var}$ Var
weakly	weak convergence of a sequence $\langle \! / \rangle_{\$} \backslash \text{weakly}$ \rightharpoonup
weaklystar	weak star convergence of a sequence $\langle \! / \rangle_{\$} \backslash \text{weaklystar}$ \rightharpoonup^*

8 ADDITIONAL SEMANTICS BY TOPIC

While semantic commands might be suitable for all mathematical topics, the following subsections collect commands which are most useful in one particular mathematical area and hence might clutter the general semantic file. Any semantic topic files should always build on numapde-semantic.sty.

8.1 MANIFOLDS: numapde-manifolds.sty

The semantic file numapde-manifolds.sty collects definitions and notations for Riemannian manifolds.

bitangentSpace	the bitangent space. Its syntax is $\backslash \text{bitangentSpace}\{\#1\}[\#2]$. The first argument denotes the base point. The second (optional) argument denotes the manifold, which defaults to \mathcal{M} . $\langle \! / \rangle_{\$} \backslash \text{bitangentSpace}\{p\}$ $\mathcal{T}_p^{**}\mathcal{M}$ $\langle \! / \rangle_{\$} \backslash \text{bitangentSpace}\{q\}[\backslash cN]$ $\mathcal{T}_q^{**}\mathcal{N}$
bitangentSpaceSymbol	the symbol used within $\backslash \text{bitangentSpace}$. $\langle \! / \rangle_{\$} \backslash \text{bitangentSpaceSymbol}$ \mathcal{T}^{**}
cotangentSpace	the cotangent space. Its syntax is $\backslash \text{cotangentSpace}\{\#1\}[\#2]$. The first argument denotes the base point. The second (optional) argument denotes the

manifold, which defaults to \mathcal{M} .

$\backslash\cotangentSpace\{p\}$ $\mathcal{T}_p^*\mathcal{M}$

$\backslash\cotangentSpace\{q\}[\backslash\mathrm{cN}]$ $\mathcal{T}_q^*\mathcal{N}$

`cotangentBundle` the cotangent bundle. Its syntax is $\backslash\cotangentBundle[\#1]$. The (optional) argument denotes the manifold, which defaults to \mathcal{M} .

$\backslash\cotangentBundle$ $\mathcal{T}^*\mathcal{M}$

$\backslash\cotangentBundle[\backslash\mathrm{cN}]$ $\mathcal{T}^*\mathcal{N}$

`cotangentSpaceSymbol` the symbol used within $\backslash\cotangent$.

$\backslash\cotangentSpaceSymbol$ \mathcal{T}^*

`covariantDerivative` is the covariant derivative. Its syntax is $\backslash\covariantDerivative\{\#1\}[\#2]$. The first argument is the vector (or vector field) determining the direction of differentiation. The second (optional) argument denotes the tensor field being differentiated.

$\backslash\covariantDerivative\{X\}\{Y\}$ $D_X Y$

`covariantDerivativeSymbol` the symbol used for the covariant derivative $\backslash\covariantDerivative$.

$\backslash\covariantDerivativeSymbol$ D

`exponential` the exponential map. Its syntax is $\backslash\exponential[\#1]\{\#2\}(\#3)$. The first argument can be used to scale the third. The second argument denotes the base point and is mandatory. The third argument denotes the tangent vector, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

$\backslash\exponential\{p\}X$ $\exp_p X$

$\backslash\exponential\{p\}(X)$ $\exp_p(X)$

$\backslash\exponential[\mathrm{Big}]\{p\}(\frac{X}{2})$ $\exp_p\left(\frac{X}{2}\right)$

`expOp` the symbol used within the $\backslash\exponential$.

$\backslash\expOp$ \exp

geodesic

a geodesic. Its syntax is `\geodesic#1|<#2>[#3]{#4}{#5}(<#6>)`. The first argument can be used to use a different symbol (locally) for the geodesic. The second (optional) argument is used to modify the style of the geodesic (symbol, long, arc or plain, where the last is the default). The third (optional) argument is used to scale the parentheses enclosing the argument to the standard ams-math sizes.¹ It is ignored when the sixth argument is not given. The fourth argument denotes the initial point (at $t = 0$). The fifth argument denotes either the final point (at $t = 1$) for types l and a, or the initial tangent vector for type p. The sixth (optional) argument denotes the evaluation point. The command `\geodesicSymbol` is used to typeset the geodesic symbol default (i.e. globally)

`</> \geodesic<s>` γ

`</> \geodesic<s>(t)` $\gamma(t)$

`</> \geodesic<l>\{p\}\{q\}` $\gamma(\cdot; p, q)$

`</> \geodesic<l>\{p\}\{q\}(t)` $\gamma(t; p, q)$

`</> \geodesic<a>\{p\}\{q\}` $\widehat{\gamma_{p,q}}$

`</> \geodesic<a>[Big]\{p\}\{q\}(\dfrac{t}{2})` $\widehat{\gamma_{p,q}}\left(\frac{t}{2}\right)$

`</> \geodesic<p>\{p\}\{X\}` $\gamma_{p,X}$

`</> \geodesic<p>\{p\}\{X\}(t)` $\gamma_{p,X}(t)$

`</> \geodesic<p>[Big]\{p\}\{X\}(\dfrac{t}{2})` $\gamma_{p,X}\left(\frac{t}{2}\right)$

`</> \geodesic[big]\{p\}\{X\}((1-t)t)` $\gamma_{p,X}((1-t)t)$

`</> \geodesic|\dot{\gamma}|\{p\}\{X\}(t)` $\dot{\gamma}_{p,X}(t)$

geodesicSymbol

symbol to use for the geodesic in `\geodesic`

`</> \geodesicSymbol` γ

inverseRetract

use an inverse retraction, the arguments are similar to `\logarithm` but use the `\retractionSymbol`

`</> \inverseRetract\{p\}q` $\text{retr}_p^{-1}q$

`</> \inverseRetract\{p\}(q)` $\text{retr}_p^{-1}(q)$

$$\backslash inverseRetract[Big]\{p\}(q) \quad \log_p^{-1}(q)$$

logarithm

the logarithmic map. Its syntax is `\logarithm[#1]{#2}(\#3)`. The first argument can be used to scale the third. The second argument denotes the base point and is mandatory. The third argument denotes another point, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

$$\backslash logarithm\{p\}q \quad \log_p q$$

$$\backslash logarithm\{p\}(q) \quad \log_p(q)$$

$$\backslash logarithm[Big]\{p\}(q) \quad \log_p(q)$$

logOp

the symbol used within the `\logarithm`.

$$\backslash logOp \quad \log$$

parallelTransport

the parallel transport.

Its syntax is `\parallelTransport[#1]{#2}{#3}(\#4){#5}`. The first (optional) argument is used to scale the parantheses enclosing the argument #4.¹ The second argument is the start point of parallel transport on a manifold. The third argument is the end point of parallel transport on a manifold. The fourth (optional) argument is the tangent vector that is transported. Putting it in brackets enables the scaling by the first argument. The fifth (optional) argument specifies an exponent, for example to parallel transport along a curve c

$$\backslash parallelTransport\{p\}\{q\}X \quad P_{q \leftarrow p}X$$

$$\backslash parallelTransport\{p\}\{q\}(X) \quad P_{q \leftarrow p}(X)$$

$$\backslash parallelTransport[big]\{p\}\{q\}(X) \quad P_{q \leftarrow p}(X)$$

$$\backslash parallelTransport\{p\}\{q\}(X)[c] \quad P_{q \leftarrow p}^c(X)$$

$$\backslash parallelTransport\{p\}\{q\}[c] \quad P_{q \leftarrow p}^c$$

parallelTransportDir

similar to `\parallelTransport`, but the third argument is a direction to transport into. This can be rewritten to the classical notation applying an exponential map from the base point (#2) to th direction (#3). The fifth (optional) argument specifies an exponent, for example to parallel transport along a curve c

`\parallelTransportDir{p}{Y}X` $P_{p,Y}X$

`\parallelTransportDir{p}{Y}(X)` $P_{p,Y}(X)$

`\parallelTransportDir[big]{p}{Y}(X)` $P_{p,Y}(X)$

`\parallelTransportDir{p}{Y}(X)[c]` $P_{p,Y}^c(X)$

`\parallelTransportDir{p}{Y}[c]` $P_{p,Y}^c$

`parallelTransportSymbol` the symbol to use within `\parallelTransport` and `\parallelTransportDir`

`\parallelTransportSymbol` P

`retract`

a retraction.

Its syntax is `\retract[#1]{#2}{#3}`. The first argument can be used to scale the third. The second argument denotes the base point. The third argument denotes the tangent vector, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

`\retract{p}X` $\text{retr}_p X$

`\retract{p}(X)` $\text{retr}_p(X)$

`\retract[Big]{p}(\frac{X}{2})` $\text{retr}_p\left(\frac{X}{2}\right)$

`retractionSymbol` symbol to use for a retraction and an inverse retraction, see `\retract` and `\inverseRetract`.

`\retractionSymbol` retr










`riemannian`

the Riemannian metric (family of inner products on the tangent spaces). Its syntax is `\riemannian[#1]{#2}{#3}[#4]`. The first (optional) argument is used to scale the parantheses enclosing the argument to the standard ams-math sizes.¹ The second argument denotes the first factor. The third argument denotes the second factor. The fourth (optional) argument denotes the base point of the tangent space.

`\riemannian{X_1}{X_2}` (X_1, X_2)

`\riemannian{Y_1}{Y_2}[q]` $(Y_1, Y_2)_q$

`\riemannian[Big]{\dfrac{1}{2}X_1}{X_2}[p]` $\left(\frac{1}{2}X_1, X_2\right)_p$

riemanniannorm	<p>the norm induced by the Riemannian metric.</p> <p>Its syntax is <code>\riemanniannorm[#1]{#2}[#3]</code>. The first (optional) argument is used to scale the parantheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the argument. The third (optional) argument denotes the base point of the tangent space.</p> <p><code></></code> <code>\riemanniannorm{X}</code>  $\ X\$</p> <p><code></></code> <code>\riemanniannorm{Y}[p]</code>  $\ Y\ _p$</p> <p><code></></code> <code>\riemanniannorm[Big]{\dfrac{1}{2}X}[p]</code>  $\left\ \frac{1}{2}X\right\ _p$</p>
secondCovariant-Derivative	<p>is the second-order covariant derivative.</p> <p>Its syntax is <code>\secondCovariantDerivative{#1}{#2}[#3]</code>. The first argument is the vector (or vector field) determining the first direction of differentiation. The second argument is the vector (or vector field) determining the second direction of differentiation. The third (optional) argument denotes the tensor field being differentiated.</p> <p><code></></code> <code>\secondCovariantDerivative{X}{Y}{T}</code>  $D_{X,Y}^2 T$</p>
secondCovariant-DerivativeSymbol	<p>the symbol used for the second covariant derivative.</p> <p>This is used within <code>\secondCovariantDerivative</code>.</p> <p><code></></code> <code>\secondCovariantDerivativeSymbol</code>  D^2</p>
tangentSpace	<p>the tangent space. Its syntax is <code>\tangentSpace{#1}[#2]</code>. The first argument denotes the base point. The second (optional) argument denotes the manifold, which defaults to \mathcal{M}.</p> <p><code></></code> <code>\tangentSpace{p}</code>  $\mathcal{T}_p \mathcal{M}$</p> <p><code></></code> <code>\tangentSpace{q}[\cN]</code>  $\mathcal{T}_q \mathcal{N}$</p>
tangentBundle	<p>the tangent bundle. Its syntax is <code>\tangentBundle[#1]</code>. The (optional) argument denotes the manifold, which defaults to \mathcal{M}.</p> <p><code></></code> <code>\tangentBundle</code>  $\mathcal{T} \mathcal{M}$</p> <p><code></></code> <code>\tangentBundle[\cN]</code>  $\mathcal{T} \mathcal{N}$</p>
tangentSpaceSymbol	<p>the symbol used within <code>\tangent</code>.</p> <p><code></></code> <code>\tangentSpaceSymbol</code>  \mathcal{T}</p>

tensorBundle	<p>the tensor bundle. Its syntax is <code>\tensorBundle{#1}{#2}[#3]</code>. The first argument denotes the number r of elements of the cotangent space the tensors accept. The second argument denotes the number s of elements of the tangent space the tensors accept. The third (optional) argument denotes the manifold, which defaults to \mathcal{M}.</p> <p><code>\tensorBundle{r}{s}</code> $\mathcal{T}^{(r,s)}\mathcal{M}$</p> <p><code>\tensorBundle{r}{s}[\cN]</code> $\mathcal{T}^{(r,s)}\mathcal{N}$</p>
tensorSpace	<p>a tensor space over a vector space V. Its syntax is <code>\tensorSpace{#1}{#2}[#3]</code>. The first argument denotes the number r of elements of the dual space V^* the tensors accept. The second argument denotes the number s of elements of the space V the tensors accept. The third (optional) argument denotes the vector space, which defaults to empty.</p> <p><code>\tensorSpace{r}{s}</code> $\mathcal{T}^{(r,s)}()$</p> <p><code>\tensorSpace{r}{s}[V]</code> $\mathcal{T}^{(r,s)}(V)$</p>
tensorSpaceSymbol	<p>the symbol used within <code>\tensorSpace</code> and <code>\tensorBundle</code>.</p> <p><code>\tensorSpaceSymbol</code> \mathcal{T}</p>
vectorTransport	<p>a vector transport.</p> <p>Its syntax is <code>\vectorTransport[#1]{#2}{#3}(#4)[#5]</code>. The first (optional) argument is used to scale the parantheses enclosing the argument #4.¹ The second argument is the start point of vector transport on a manifold. The third argument is the end point of vector transport on a manifold. The fourth (optional) argument is the tangent vector that is transported. Putting it in brackets enables the scaling by the first argument. Finally a retraction symbol can be added in the exponent to distinguish vector transports as #5.</p> <p><code>\vectorTransport{p}{q}X</code> $T_{q \leftarrow p}X$</p> <p><code>\vectorTransport{p}{q}(X)</code> $T_{q \leftarrow p}(X)$</p> <p><code>\vectorTransport[big]{p}{q}(X)</code> $T_{q \leftarrow p}(X)$</p> <p><code>\vectorTransport{p}{q}(X)[\retractionSymbol]</code> $T_{q \leftarrow p}^{\text{retr}}(X)$</p>
vectorTransportDir	<p>similar to <code>\vectorTransport</code>, but the third argument is a direction to transport into. This can be rewritten to the classical notation applying an retraction from the base point (#2) to th direction (#3).</p>

$\backslash\text{vectorTransportDir}\{p\}\{Y\}X$ $\mathcal{T}_{p,Y}X$

$\backslash\text{vectorTransportDir}\{p\}\{Y\}(X)$ $\mathcal{T}_{p,Y}(X)$

$\backslash\text{vectorTransportDir}[\text{big}]\{p\}\{Y\}(X)$ $\mathcal{T}_{p,Y}(X)$

$\backslash\text{vectorTransportDir}\{p\}\{Y\}(X)[\text{retractionSymbol}]$ $\mathcal{T}_{p,Y}^{\text{retr}}(X)$

`vectorTransportSymbol` the symbol to use within `\vectorTransport` and `\vectorTransportDir`

$\backslash\text{vectorTransportSymbol}$ T

8.2 OPTIMIZATION: numapde-optimization.sty

The semantic file `mathsemantics-optimization.sty` collects definitions and notations related to optimization.

`linearizingcone` the linearizing cone. Its syntax is `\linearizingcone[#1]{#2}{#3}`. The first (optional) argument is used to scale the parantheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

$\backslash\text{linearizingcone}\{A\}\{x\}$ $\mathcal{T}_A^{\text{lin}}(x)$

$\backslash\text{linearizingcone}\{A\}\{x^2\}$ $\mathcal{T}_A^{\text{lin}}(x^2)$

$\backslash\text{linearizingcone}[\text{big}]\{A\}\{x^2\}$ $\mathcal{T}_A^{\text{lin}}(x^2)$

`normalcone` the normal cone. Its syntax is `\normalcone[#1]{#2}{#3}`. The first (optional) argument is used to scale the parantheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

$\backslash\text{normalcone}\{A\}\{x\}$ $\mathcal{N}_A(x)$

$\backslash\text{normalcone}\{A\}\{x^2\}$ $\mathcal{N}_A(x^2)$

$\backslash\text{normalcone}[\text{big}]\{A\}\{x^2\}$ $\mathcal{N}_A(x^2)$

`polarcone` the polar cone of a set $\backslash\text{polarcone}\{A\}$ A°

`radialcone` the radial cone. Its syntax is `\radialcone[#1]{#2}{#3}`. The first (optional) argument is used to scale the parantheses enclosing the argument to the

standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

$\backslash\text{radialcone}\{A\}\{x\}$ $\mathcal{K}_A(x)$

$\backslash\text{radialcone}\{A\}\{x^2\}$ $\mathcal{K}_A(x^2)$

$\backslash\text{radialcone}[\text{big}]\{A\}\{x^2\}$ $\mathcal{K}_A(x^2)$

tangentcone

the tangent cone. Its syntax is $\backslash\text{tangentcone}[\#1]\{\#2\}\{\#3\}$. The first (optional) argument is used to scale the parantheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

$\backslash\text{tangentcone}\{A\}\{x\}$ $\mathcal{T}_A(x)$

$\backslash\text{tangentcone}\{A\}\{x^2\}$ $\mathcal{T}_A(x^2)$

$\backslash\text{tangentcone}[\text{big}]\{A\}\{x^2\}$ $\mathcal{T}_A(x^2)$