MATHSEMANTICS.STY - SEMANTIC MATH COMMANDS

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1 Introduction

This package aims to provide semantic commands for ease of use in mathematics to see better *what* you semantically mean which should be distinct/split from *how* it is realised in Lagran.

The package is a spin-off and developed in the suite of packages from the former numapde-group in Chemnitz, see the original repository at https://gitlab.hrz.tu-chemnitz.de/numapde-public/numapde-latex.

Throughout this documentation most commands are directly illustrated by examples, which are both displayed as code (or for math examples) and its rendered result in Lagrange (). Two examples are

$$\$$
 \bbR $\$ \B \\ and \\\ \eg \\ \eg \\ e. g.

The aim is to first ease the use of some often used letters and low-level formats like bold face letters $\$ \bbR \Delta \R , but also to provide high level commands that make typing mathematics easier, for example using \As\frac{1}{2} \abs\frac{1}{2}| and \As\sigma\frac{1}{2}| abs\[Big]{\frac{1}{2}| This is the main goal in Section 4 about syntactical commands for mathematics. A next more support/helping section about abbreviations and names is Section 5.

The first main part on general semantic commands is Section 7.

While all these are loaded by default. The next part, Section 8, introduces semantic commands for specific topics. These are given in separate sub-packages and can be loaded if you work in this area and want to use the commands.

The package should be loaded late, since it might overwrite a few commands, currently most prominently \d which is overwritten by cleveref in case minted is loaded. So for more flexibility, there is the alternative command \dInt.

2 PACKAGE OPTIONS

shortbb

use shorter notations for the blackboard-bold math letters \C, \K, \N, \Q, \R, \Z

3 REQUIRED PACKAGES

amssymb.sty defines mathematical symbol fonts

ifthen.sty facilitates the definition of conditional commands

ifxetex.sty provides a way to check if a document is being processed by XATeX and company

mathtools.sty provides lots of improvements for math typesetting (includes amsmath.sty)

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xifthen.sty extends if then.sty by adding new boolean conditions

xparse.sty provides a high-level interface to define new commands

xspace.sty adds space depending on context

4 SYNTAX

The mathsemantics-syntax.sty package provides mainly symbols and short commands, which can be used in semantic definitions for ease of notation. They usually are rather simple commands without too many parameters.

4.1 LETTERS

babz	lower-case b old-face letters \P \br, \bf $ extstyle r, f$
bAbZ	upper-case b old-face letters $\langle l \rangle$ \bR, \bF \bigcirc R, F
balpha bomega	lower-case bold-face Greek letters $\$ \balpha, \boldeta $\$ α, η (the latter being an exception)
bAlphabOmega	upper-case b old-face Greek letters \P \bGamma, \bDelta \P Γ , Δ
bnull	bold-face zero 📏 \bnull 💿 0
bone	bold-face one 📏 \bone 🌑 1
cAcZ	upper-case c alligraphic letters $\langle 1 \rangle$ \cM, \cN \otimes \mathcal{M} , \mathcal{N}
fAfZ	upper-case fraktur letters \P \fM, \fN, \fX $ extstyle exttt{M}, exttt{N}, \fX extstyle exttt{M}, extt$
sAsZ	upper-case script letters $\P \$ \sM, \sN, \sX $\$ $\$ $\mathscr{M}, \mathcal{N}, \mathcal{X}$
vavz	lower-case letters with a vector accent $\langle \rangle$ \va,\vb \vec{a},\vec{b}
vA vZ	upper-case letters with a vector accent $\checkmark \$ $\$ $\$ $\$ $\$ $\$ $\$ $\$ $\$ $\$
valphavomega	lower-case Greek letters with a vector accent $\$ \valpha, \vbeta $\vec{\alpha}, \vec{\beta}$

 $\odot \vec{0}$

1, 🗅

vector zero **//** \vnull

vone vector one 🔖 \vone • 1

bbA,...,bbZ blackboard-bold uppercase letters

 $\begin{picture}(100,0) \put(0,0){\line(0,0){100}} \put(0,0){\line(0,0){1$

use the package option shortbb to introduce

 $\$ \C,\K,\N,\Q,\R,\Z $\$ $\$ $\$ \mathbb{C} , \mathbb{K} , \mathbb{N} , \mathbb{Q} , \mathbb{R} , \mathbb{Z} if not already defined elsewhere (i. e. they are not redefined, only *provided*.

4.2 SYNTAX HELPERS

enclspacing

provides spacing after the opening and before the closing delimiters for \enclose. This is by default set to be empty.

enclose

vnull

is a command which encloses some content in scaled delimiters. It is meant as a helper to facilitate the definition of other commands. Its syntax is \enclose[#1]{#2}{#3}{#4}. The first (optional) argument is used to scale the delimiters to the standard amsmath sizes. The second and fourth arguments specify the opening and closing delimiters, respectively. The third argument is the content to be enclosed.

$$\$$
 \enclose{[}{\dfrac{1}{2}}{]} $\$ \enclose{[}

$$\$$
 \enclose[Big][{\dfrac{1}{2}}] $\$ \enclose[Big][\dfrac{1}{2}]

$$4$$
 \enclose[auto]{[}{\dfrac{1}{2}}{]} \bullet $\left[\frac{1}{2}\right]$

$$4$$
 \enclose[none]{[}{\dfrac{1}{2}}{]} \bullet $\frac{1}{2}$

Note 1. none is merely meant for testing when having arguments in brackets whether it is useful to omit them. You can also deactivate the absolute value vertical lines this way, so *use this option with care*.

Note 2. This command should normally be used only in the definition of other commands. For instance, \abs is using it internally. See \paren for the

¹big, Big, bigg, Bigg or auto, which uses left and right as well as none to easily deactivate brackets.

nicer command to use

enclspacingSet

provides spacing before and after the center delimiter \encloseSet. This is by default set to \,.

encloseSet

is a command which encloses some content in scaled delimiters. It is meant as a helper to facilitate the definition of other commands. Its syntax is \encloseSet#1]{#2}{#3}{#4}{#5}{#6}. The first (optional) argument is used to scale the delimiters including the center one to the standard amsmath sizes.¹ The second and sixth arguments specify the opening and closing delimiters, respectively. The fourth argument specifies the center delimiter and The third and fifth argument are the content to be enclosed.

Note. This command should normally be used only in the definition of other commands. For instance, \setDef is using it internally.

paren

is an alternative to \enclose, with a different ordering of arguments. Its syntax is \paren[#1]{#2}{#3}{#4}, which is simply mapped to \enclose[#1]{#2}{#4}{#3}.

$$\label{eq:paren} \$$
 \paren[Big]{[]}{\dfrac{1}{2}} \ \emptyset{\lefta} \left[\frac{1}{2}\right]

$$\$$
 \paren[Big][]{\dfrac{1}{2}} $\$ \(\Phi\)

$$\$$
 \paren[auto]{[}{]}{\dfrac{1}{2}} $\$ $\$

4.3 SPACING HELPERS

clap

complements the standard LaTeX commands \lap and \rlap. These commands horizontally smash their arguments.

mathllap

corresponds to \llap in math mode.

$$\$$
 \sum_{\mathbb{1}i = i = j = n} X_{ij} $\sum_{1 \leq i \leq j \leq n} X_{ij}$

mathclap corresponds to \clap in math mode.

$$\$$
 \sum_{\mathbb{1}\in \mathbb{1}\in \mathbb{1}} X_{ij}

mathrlap corresponds to \rlap in math mode.

$$\$$
 \sum_{\mathbb{1}}e i\le i\le j\le n} $\$ \sum_{ij} $\$ $\sum_{1 \le i \le j \le n} X_{ij}$

stands for *math replace* and it typesets an argument while reserving the space for another. Its syntax is $\mbox{mrep}[\#1]\{\#2\}\{\#3\}$ The first (optional) argument is one of $\{l,c,r\}$ and it is used to define the alignment. c is the default.

5 ABBREVIATIONS

Abbreviations and their spacing might be diifcult to genannt

abrv write the letters provided as an abbreviation

And we introduce a few of them specifically also a few that are not following this scheme.

5.1 ENGLISH

ale almost everywhere
$$\langle \rangle$$
 \ale • a. e.

```
exempli gratia (for example) //> \eg • e. g.
eg
                   Exempli gratia (for example, at beginning of a sentence) \
                                                                        ● E.g.
Eg
                   etc
                   id est (id est) /> \ie  i.e.
ie
                   iid
                   symmetric positive definite \P \spd 	ext{ } 	ext{spd} 	ext{ } 	ext{ } 	ext{s. p. d.}
spd
                   such that or subject to \> \suth  suth  s.t.
suth
                   with respect to \checkmark \wrt \odot w.r.t.
wrt
```

beispielsweise (for example) **\forall \bspw \log bspw**.

5.2 GERMAN

bspw

bzgl	bezüglich (with regard to) //> \bzgl ③ bzgl.
bzw	beziehungsweise (respectively) bzw.
Dah	Das heißt (That is, beginning of phrase) 🔷 \Dah 💿 D. h.
dah	das heißt (that is) 🕩 \dah 🌑 d.h.
evtl	eventuell (possibly) 🕩 \evtl 🌑 evtl.
fs	fast sicher \f \fs
fue	fast überall 🕩 \fue 🍑 f. ü.
IA	Im Allgemeinen (beginning of phrase) 🕩 🕦 🕒 I. A.
iA	im Allgemeinen 🎶 🔰 i. A.
idR	in der Regel ⟨/> \id R
IdR	In der Regel (beginning of phrase) 🌗 \IdR 💿 I. d. R.
iW	im Wesentlichen 🕩 \iW . i. W.

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Im Wesentlichen (beginning of phrase) </br> ● I.W. IW meines Erachtens **\>** \mE • m.E. mΕ ohne Beschränkung der Allgemeinheit **\>** \oBdA • o. B. d. A. oBdA ohne Beschränkung der Allgemeinheit (beginning of phrase) **OBdA** </>
</>
</body> ① O.b.d.A. oben genannt **⟨/>** \oge oge oder ähnliche **//>** \oae • o. ä. oae siehe oben **\>** \sio sio unter anderem **</>>/>** \ua • u.a. ua Unter anderem (beginning of phrase) 🕩 \Ua 💿 U. a. Ua unten genannt **//>** \ug ug und so weiter (and so on) • usw. usw unter Umständen 💔 👊 uU • u. U. Unter Umständen (beginning of phrase) UnU vergleiche (compare) **//>** \vgl vgl zum Beisiel **</>> \z**B zΒ Zum Beispiel (beginning of phrase) </>
\ZB ΖB **②** Z.B. zu Händen 💔 🗎 🗎 zHd 6 Names ADIMAT adimat AMPL ampl

BibTeX

BIBTEX

● BIBLATEX BibLaTeX **●** CG cg **●** C++ срр CPPMAT cppmat ODLFIN dolfin dolfinplot ODLFIN-PLOT dolfinadjoint ODLFIN-ADJOINT O Doxygen doxygen FEMORPH femorph FENICS fenics ffc FFC FMG fmg FORTRAN fortran GITLAB gitlab • GMRES gmres GMSH gmsh IPOPT ipopt LIBSVM libsvm • LIBLINEAR liblinear macmpec MACMPEC manifoldsjl MANIFOLDS.JL MANOPT manopt

manoptjl

mathematica

MANOPT.JL

MATHEMATICA

MATLAB matlab maple MAPLE maxima MAXIMA metis METIS MINRES minres mshr MSHR MVIRT mvirt NumPy numpy PARAVIEW paraview ● PDF⊮TEX pdflatex PERL perl PETSc petsc PYMAT pymat PYTHON python scikit SciKit scikitlearn SciKit-learn SciPy scipy SPHINX sphinx SUBGMRES subgmres subminres SubMinres superlu SUPERLU \odot SVM^{LIGHT} svmlight tritetmesh TRITETMESH

• UFL

ufl

uqlab	UQLAB
viper	• VIPER
xml	XML

7 SEMANTIC COMMANDS

Build upon Syntax from Section 4 this part provides semantic mathematical commands.

abs absolute value. Its syntax is \abs[#1]{#2}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes.¹ The second argument denotes the argument.

$$4$$
 \abs[auto]{\\dfrac{1}{2}} \bullet $\frac{1}{2}$

Argmin set of minimizers of a function
$$\mbox{\sc Argmin}_{\{x \in \mathbb{R}\}} f(x)$$

 $Argmin_{\{x \in \mathbb{R}\}} f(x)$

bdiv	bold (meaning: vector) divergence of a matrix-valued function / \bdiv @ div
ceil	integer larger or equal to input. Its syntax is \ceil[#1]{#2}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes.¹ The second argument denotes the argument.
	√/ § \ceil{a}
	$\langle \rangle \ Big \dfrac{1}{2} $ $\bigcirc \left[\frac{1}{2}\right]$
clconv	closure of the convex hull of a set $\langle \rangle$ \closure M
closure	closure of a set $\langle \rangle$ \closure M \odot cl M
cofac	cofactor matrix $\langle A \rangle \setminus \operatorname{cofac}(A)$ $\odot \operatorname{cof}(A)$
compactly	compact embedding of topological spaces $\$ \compactly $\$ $\$ $\$ $\$ $\$
cone	conic hull 🔥 \cone 💿 cone
conv	convex hull of a set $\langle \rangle$ \conv M \odot conv M
corresponds	binary operator for correspondence $\ \ \ \ \ \ \ \ \ \ \ \ \ $
cov	covariance 🔥 \cov 💿 Cov
curl	the curl operator 🐴 \curl 💿 curl
d, dInt	integral symbol with prepended space, as in
	\\ \int_\bbR \exp(-x^2) \d x \\ \int_\\ \gerp(-x^2) \dx \] Since \\ \d \text{is often overridden, \dInt is the safe alternative}
dev	deviator of a matrix ⟨/ § \dev A
diag	diagonal matrix composed of entries in a vector, or diagonal of a matrix
	$\label{eq:diag} \$ \diag(a) $\$ diag(a)
	$\label{eq:diag} \$ \diag(A) $\$ diag(A)
diam	diameter $\langle \rangle \operatorname{diam}(M)$ \odot diam (M)

dist0p the mathematical operator denoting the distance </k> dist dist distance from a point to a set. Its syntax is $\dist[#1]{#2}{#3}$ or $\dist[#1]{#2}$. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.1 The second argument denotes the set. The third argument denotes the point; it can be omitted. The command \distOp is used to typeset the operator. $\sqrt{\frac{x}{2}} \det[Big]{\cC}{\dfrac{x}{2}}$ $\odot \operatorname{dist}_{C}(\frac{x}{2})$ </i>
√ dist div (row-wise) divergence **⟨/**⟩ \Div Div Div domain 🗸 \dom dom dom dotcup double contraction of matrices $A : B = \sum_{i,j} A_{ij} B_{ij} = \operatorname{trace}(A^{\mathsf{T}}B)$ dprod $A \cdot A \cdot A \cdot B$ dual duality pairing. Its syntax is \dual[#1]{#2}{#3}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes.1 The second argument denotes the first factor. The third argument denotes the second factor. $\langle x^* \rangle \langle x^* \rangle \langle x^* \rangle$ $\langle x^*, \frac{1}{2} \rangle$ \\dual[Big]{x^*}{\dfrac{1}{2}} \end{array} Euler's number 🕢 \e е embed synonym of $\mbox{\em bed }\mbox{\em }\mbox{\em beds}$ embeds epigraph 🖊 \epi 🗼 epi epi

```
extended real line 
\eR = \bbR \cup \{\pm \infty\}
                                                                                 \odot \overline{\mathbb{R}} = \mathbb{R} \cup
eR
                       \{\pm\infty\}
                       essential infimum
essinf
                        \displaystyle\essinf_{x \in \bbR} f(x)
                                                                      \bullet \operatorname{ess\,inf}_{x\in\mathbb{R}} f(x)
esssup
                       essential supremum
                        \displaystyle\esssup_{x \in \bbR} f(x)
                                                                        file
                       typesets a file name (using nolinkurl)
                       </> \file{test.txt}
                                               test.txt
floor
                       integer less or equal to input. Its syntax is \floor[#1]{#2}. The first (op-
                       tional) argument is used to scale the delimiters enclosing the arguments to
                       the standard amsmath sizes.1 The second argument denotes the argument.
                       4 \floor[Big]{\\dfrac{1}{2}} \bigcirc \left|\frac{1}{2}\right|
                       gradient (of a function) 👍 \grad F
                                                             \odot grad F
grad
                       graph of a function \\strack \Graph
Graph
                       identity operator 🐴 \id 💿 id
id
                       image of a function </ >
                                                        image
image
                       injectivity (radius) 🐴 \inj 🌑 inj
inj
inner
                       inner product. Its syntax is \inner[#1]{#2}{#3}. The first (optional) ar-
                       gument is used to scale the parentheses enclosing the arguments to the
                       standard amsmath sizes.1 The second argument denotes the first factor. The
                       third argument denotes the second factor.
                       \langle a \rangle  \inner{a}{b} \bullet (a, b)
                       interior
```

jump

jump of a quantity, e. g., across a finite element facet. Its syntax is \jump[#1]{#2}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes. The second argument denotes the argument.

$$\langle \mathbf{/} \mathbf{\rangle} \setminus \text{jump}\{a\}$$
 \bullet $[a]$

$$\sqrt{\ \ \ \ }$$
 \jump[Big]{\\dfrac{1}{2}} \bigcirc $\boxed{\frac{1}{2}}$

laplace

the Laplace operator $\langle \rangle$ \laplace u $\odot \Delta u$

lin

linear hull of a set of vectors $\langle v_1, v_2 \rangle$ $\langle v_1, v_2 \rangle$

norm

norm of a vector. Its syntax is \norm[#1]{#2}. The first (optional) argument is used to scale the delimiters enclosing the arguments to the standard amsmath sizes.¹ The second argument denotes the argument.

$$\langle \mathbf{/} \mathbf{>} \setminus \mathbf{norm} \{a\}$$
 $\bullet \|a\|$

$$\langle \rangle \setminus \text{norm[Big]} \{ \langle c \rangle \}$$

proj0p

the mathematical operator denoting the projection 🔥 \projOp 🕟 proj

proj

projection onto a set. Its syntax is \proj[#1]{#2}(#3) or \proj[#1]{#2}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes. The second argument denotes the set and can also be left out. The third argument denotes the point; it can be omitted. The command \proj0p is used to typeset the operator.

$$\proj(x)$$
 $\proj(x)$

$$\$$
 \proj{\cC} $\$ proj_C

$$\$$
 \proj{\cC}(x) \bullet proj $_C(x)$

$$\sqrt{\frac{x}{2}} \operatorname{proj}[\operatorname{Big}](\operatorname{dfrac}\{x\}\{2\})$$
 \bullet proj $\left(\frac{x}{2}\right)$

 $\langle x \rangle \text{proj[Big]}(\cC)(\dfrac\{x\}\{2\})$ $\bullet \text{proj}_{C}(\frac{x}{2})$

the mathematical operator denoting the proximal map prox0p

> **⟨/**≽ \prox0p prox

the proximal operator of a function. Its syntax is \prox[#1]{#2}(#3) or prox \prox[#1]{#2}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the point; it can be omitted. The command \prox0p is used to typeset the operator.

⟨/≽ \prox
● prox

 $\$ \prox{\lambda F}(x) $\$ prox $_{\lambda F}(x)$

rank (of a matrix) 🔥 \rank 💿 rank rank

range of some operator **** \range \range range

> restriction/evaluation. Its syntax is \restr[#1]{#2}{#3}. The first (optional) argument is used to scale the deliminters enclosing the arguments to the standard amsmath sizes.1 The second argument denotes the argument to be restricted/evaluated. The third argument denotes the restriction set/evaluation point.

relative interior 🐴 \ri 💿 ri ri

restr

define a set, where \setMid serves as the center divider. Its syntax is \setDef[#1]{#2}{#3}. setDef The first (optional) argument is used to scale the parentheses enclosing the argument and the center divider to the standard amsmath sizes.1 The second argument denotes the left part of the definition, naming the potential elements of the set being defined. The third argument denotes the condition to include the elements in the set.

8 Additional Semantics by Topic

While semantic commands might be suitable for all mathematical topics, the following subsections collect commands which are most useful in one particular mathematical area and hence might clutter the general semantic file. Any semantic topic files should always build on mathsemantics-semantic. sty.

8.1 Manifolds: mathsemantics-manifolds.sty

The semantic file mathsemantics-manifolds.sty collects definitions and notations for Riemannian manifolds.

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bitangentSpace

the bi tangent space. Its syntax is $\bitangent{#1}[#2]$. The first argument denotes the base point. The second (optional) argument denotes the manifold, which defaults to \mathcal{M} .



 $\label{eq:local_problem} \$ \bitangentSpace{q}[\cN] $\$ $\mathcal{T}_q^{**}\mathcal{N}$

bitangentSpaceSymbol the symbol used within \bitangentSpace.

 $\label{eq:theorem} \begin{picture}(4)\put(0,0){\line(1,0){100}} \put(0,0){\line(1,0){100}} \put(0,0)$

cotangentSpace

the cotangent space. Its syntax is $\operatorname{cotangentSpace}\{\#1\}[\#2]$. The first argument denotes the base point. The second (optional) argument denotes the manifold, which defaults to \mathcal{M} .

cotangentBundle

the cotangent bundle. Its syntax is $\operatorname{LotangentBundle}[\#1]$. The (optional) argument denotes the manifold, which defaults to \mathcal{M} .

cotangentSpaceSymbol the symbol used within \cotangent.

 \checkmark \cotangentSpaceSymbol $\odot \mathcal{T}^*$

covariantDerivative

is the covariant derivative. Its syntax is \covariantDerivative{#1}[#2]. The first argument is the vector (or vector field) determining the direction of differentiation. The second (optional) argument denotes the tensor field being differentiated.

 $\langle Y \rangle \sim D_X Y$

covariantDerivativeSymbtolle symbol used for the covariant derivative \covariantDerivative.

 $\begin{tabular}{ll} \begin{tabular}{ll} \beg$

exponential

the exponential map. Its syntax is \exponential[#1]{#2}(#3). The first argument can be used to scale the third. The second argument denotes the base point and is mandatory. The third argument denotes the tangent vector,

which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

$$\langle \rangle \times \exp(n \pi i \pi i) = \exp_p X$$

$$\langle X \rangle = \exp_p(\frac{X}{2})$$

the symbol used within the \exponential.

geodesic

exp0p

a geodesic. Its syntax is $\ensuremath{\mbox{\mbox{$\setminus$geodesic#}1$-$_i$#2}[\#3]$-$\#4"-$\#5"(\#6)$-.The first argument can be used to use a different symbol (locally) for the geodesic The second (optional) argument is used to modify the style of the geodesic (symbol, long, arc or plain, where the last is the default) The third (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.\(^1\) It is ignored when the sixth argument is not given. The fourth argument denotes the initial point (at <math>t=0$). The fifth argument denotes either the final point (at t=1) for types \(^1\) and \(^2\), or the initial tangent vector for type \(^1\). The sixth (optional) argument denotes the evaluation point. The command $\ensuremath{\mbox{\mbox{$\setminus$geodesicSymbol}$}}$ is used to typeset the geodesic symbol default (i.e. globally)

$$\$$
 \geodesic~~(t) $\$ $\gamma(t)$~~

$$\protect\$$
 \geodesic<\p\{q\} $\protect\$ \geodesic<

$$\fint{$\ll} \$$
 \geodesic{p}{q}(t) $\fint{$\ll} \ \ \gamma(t;p,q)$

$$\langle \rangle$$
 \geodesic{p}{q} \$\bigcirc\$ \$\gamma_{\widehat{p,q}}\$

$$\P$$
 \geodesic\[Big\]{p}{q}\(\dfrac{t}{2}\) \$\P\$ \$\gamma_{\widehat{p,q}}\(\frac{t}{2}\)\$

$$\$$
 \geodesic|\dot\gamma|{p}{X}(t) $\$ $\dot{\gamma}_{p,X}(t)$

geodesicSymbol symbol to use for the geodesic in \geodesic

$$\label{eq:pq}$$
 \inverseRetract{p}q $\ \odot \ \mathrm{retr}_p^{-1}q$

$$\$$
 \inverseRetract{p}(q) $\$ retr $_p^{-1}(q)$

$$\$$
 \inverseRetract[Big]{p}(q) $\$ retr $_p^{-1}(q)$

logarithm

the logarithmic map. Its syntax is \logarithm[#1]{#2}(#3). The first argument can be used to scale the third. The second argument denotes the base point and is mandatory. The third argument denotes another point, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

logOp the symbol used within the \logarithm.

parallelTransport

the parallel transport.

Its syntax is \parallelTransport[#1]{#2}{#3}(#4){5}. The first (optional) argument is used to scale the parentheses enclosing the argument #4. The second argument is the start point of parallel transport on a manifold. The third argument is the end point of parallel transport on a manifold. The fourth (optional) argument is the tangent vector that is transported. Putting it in brackets enables the scaling by the first argument. The fifth (optional) argument specifies an exponent, for example to parallel transport along a curve c

$$\protect\$$
 \parallelTransport[big]{p}{q}(X) $\protect\$ P $_{q\leftarrow p}(X)$

$$\protect\$$
 \parallelTransport{p}{q}[c] $\protect\$ $\protect\$

parallelTransportDir

similar to \parallelTransport, but the third argument is a direction to transport into. This can be rewritten to the classical notation applying an exponential map from the base point (#2) to th direction (#3). The fifth (optional) argument specifies an exponent, for example to parallel transport along a curve c

$$\begin{tabular}{ll} $\parallelTransportDir{p}{Y}X & \begin{tabular}{ll} $\Phi_{p,Y}X$ \\ \end{tabular}$$

$$\protect\$$
 \parallelTransportDir{p}{Y}(X) $\protect\$ $\protect\$

parallelTransportSymbol the symbol to use within \parallelTransport and \parallelTransportDir

retract

a retraction.

Its syntax is \retract[#1]{#2}{#3}. The first argument can be used to scale the third. The second argument denotes the base point. The third argument denotes the tangent vector, which is optional, but if provided, the argument is put in brackets. The first following example illustrates the case, where no brackets are put. Note that the space is mandatory.

$$\five \text{retract}(p)(X)$$
 $\five \text{retr}_p(X)$

$$\$$
 \retract[Big]{p}(\frac{X}{2}) • retr_p($\frac{X}{2}$)

retractionSymbol

symbol to use for a retraction and an inverse retraction, see \retract and

\inverseRetract.

riemannian

the Riemannian metric (family of inner products on the tangent spaces). Its syntax is \riemannian[#1]{#2}{#3}[#4]. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the first factor. The third argument denotes the second factor. The fourth (optional) argument denotes the base point of the tangent space.

$$\$$
 \riemannian[Big]{\dfrac{1}{2}X_1}{X_2}[p] $\$ $\left(\frac{1}{2}X_1, X_2\right)_p$

riemanniannorm

the norm induced by the Riemannian metric.

Its syntax is \riemanniannorm[#1]{#2}[#3]. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the argument. The third (optional) argument denotes the base point of the tangent space.

secondCovariantDerivative is the second-order covariant derivative.

Its syntax is \secondCovariantDerivative{#1}{#2}[#3]. The first argument is the vector (or vector field) determining the first direction of differentiation. The second argument is the vector (or vector field) determining the second direction of differentiation. The third (optional) argument denotes the tensor field being differentiated.

secondCovariantDerivativeSymbol the symbol used for the second covariant derivative.

This is used within \secondCovariantDerivative.

tangentSpace the tangent space. Its syntax is \tangentSpace{#1}[#2]. The first argument

denotes the base point. The second (optional) argument denotes the manifold, which defaults to \mathcal{M} .

 $\$ \tangentSpace{p} $\$ $\mathcal{T}_p\mathcal{M}$

 $\$ \tangentSpace{q}[\cN] $\$ $\mathcal{T}_q\mathcal{N}$

tangentBundle

the tangent bundle. Its syntax is \tangentBundle[#1]. The (optional) argument denotes the manifold, which defaults to \mathcal{M} .

⟨/≥ \tangentBundle
● TM

⟨**/**⟩ \tangentBundle[\cN]
● TN

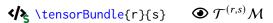
tangentSpaceSymbol

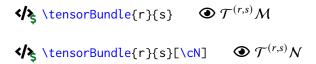
the symbol used within \tangent.

 $\$ \tangentSpaceSymbol $\odot \mathcal{T}$

tensorBundle

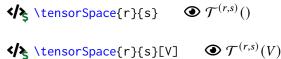
the tensor bundle. Its syntax is \tensorBundle{#1}{#2}[#3]. The first argument denotes the number *r* of elements of the cotangent space the tensors accept. The second argument denotes the number s of elements of the tangent space the tensors accept. The third (optional) argument denotes the manifold, which defaults to \mathcal{M} .





tensorSpace

a tensor space over a vector space V. Its syntax is $\tensorSpace{#1}{#2}[#3]$. The first argument denotes the number r of elements of the dual space V^* the tensors accept. The second argument denotes the number s of elements of the space *V* the tensors accept. The third (optional) argument denotes the vector space, which defaults to empty.



tensorSpaceSymbol

the symbol used within \tensorSpace and \tensorBundle.



vectorTransport

a vector transport.

Its syntax is \vectorTransport[#1]{#2}{#3}(#4)[#5]. The first (optional) argument is used to scale the parentheses enclosing the argument #4.1 The second argument is the start point of vector transport on a manifold. The third argument is the end point of vector transport on a manifold. The fourth (optional) argument is the tangent vector that is transported. Putting it in brackets enables the scaling by the first argument. Finally a retraction symbol can be added in the exponent to distinguish vector transports as #5.

 $\ensuremath{\checkmark}\$ \vectorTransport{p}{q}X $\ensuremath{\bullet}$ $\ensuremath{\mathsf{T}}_{q\leftarrow p}X$

 $\protect\$ \vectorTransport[big]{p}{q}(X) $\protect\$ $\protect\$

 $\P \$ \vectorTransport{p}{q}(X)[\retractionSymbol] $\P \$ $\P \$

vectorTransportDir

similar to \vectorTransport, but the third argument is a direction to transport into. This can be rewritten to the classical notation applying an retraction from the base point (#2) to th direction (#3).

 $\$ \vectorTransportDir[big]{p}{Y}(X) \bullet $T_{p,Y}(X)$

 $\five T_{p,Y}^{\text{retr}}(X)$ \vectorTransportDir $\{p\}\{Y\}(X)$ [\retractionSymbol] $\five T_{p,Y}^{\text{retr}}(X)$

vectorTransportSymbol

the symbol to use within \vectorTransport and \vectorTransportDir

⟨**/**§ \vectorTransportSymbol
▼ T

8.2 Optimization: mathsemantics-optimization.sty

The semantic file mathsemantics-optimization.sty collects definitions and notations related to optimization.

linearizingcone

the linearizing cone. Its syntax is \linearizingcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

normalcone

radialcone

the normal cone. Its syntax is \normalcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes. The second argument denotes the set. The third argument denotes the base point.

polarcone the polar cone of a set $\langle \rangle$ \polarcone{A} \bigcirc A°

the radial cone. Its syntax is \radialcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

 $\$ \radialcone[big]{A}{x^2} $\$ $\$ $\mathcal{K}_A(x^2)$

the tangent cone. Its syntax is \tangentcone[#1]{#2}{#3}. The first (optional) argument is used to scale the parentheses enclosing the argument to the standard amsmath sizes.¹ The second argument denotes the set. The third argument denotes the base point.

 $\$ \tangentcone[big]{A}{x^2} $\$ $\mathcal{T}_A(x^2)$