# Estimating population average treatment effects from experiments with noncompliance

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### Motivation

- RCTs are the "gold standard" for estimating the causal effect of a treatment
  - External validity is an issue when RCT participants don't reflect the target population
  - Non-compliance to treatment assignment biases estimates of the sample average treatment effect (SATE) towards 0
- ▶ Idea: reweight responses in the treatment group of RCT compliers to estimate population average treatment effect on the treated (PATT)
  - Hartman et al. [to appear] develop a nonparametric reweighting method to extend SATE to PATT
  - ▶ We extend this method to the case of one-way crossover

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### Overview of experiment

▶ Oregon Health Insurance Experiment

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### Estimating treatment effects

- Neyman-Rubin framework: each  $i = \{1, ..., N\}$  participants have four potential outcomes,  $Y_{ist}$  for s = 0, 1 and t = 0, 1
- ▶ Define W, S, T, C, D, Y

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### Estimating treatment effects

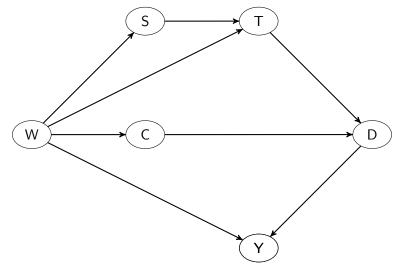


Figure: Causal diagram indicating the conditional independence assumptions needed to estimate the PATT.

### Assumption 1

Consistency under parallel studies: for all i and for t = 0, 1,

$$Y_{i0t} = Y_{i1t}$$

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#### Assumption 2

Strong ignorability of sample assignment for treated:

$$(Y_{01}, Y_{11}) \perp S \mid (W, T = 1, C = 1), 0 < \mathbb{P}(S = 1 \mid W, T = 1, C = 1) < 1$$

Potential outcomes for treatment are independent of sample assignment for individuals with the same covariates W and assignment to treatment.

#### Assumption 3

Strong ignorability of sample assignment for controls:

$$(\textit{Y}_{00},\textit{Y}_{10}) \perp \!\!\! \perp \textit{S} \mid (\textit{W},\textit{T}=1,\textit{C}=1), 0 < \mathbb{P}(\textit{S}=1 \mid \textit{W},\textit{T}=1,\textit{C}=1) < 1$$

Potential outcomes for control are independent of sample assignment for individuals with the same covariates W and assignment to treatment.

#### Assumption 4

Stable unit treatment value assumption (SUTVA):

$$Y_{ist}^{L_i} = Y_{ist}^{L_j}, \forall i \neq j$$

where  $L_i$  is the treatment and sample assignment vector for unit j.

#### Assumption 5

Conditional independence of compliance and assignment:

$$C \perp \!\!\! \perp T = 1 \mid W, 0 < \mathbb{P}(C = 1 \mid W) < 1$$

#### Assumption 6

Monotonicity:

$$T_i \geq D_i, \forall i$$

This assumption implies that there are no defiers and that crossover is only possible from treatment to control.

#### Assumption 7

Exclusion restriction: For non-compliers

$$Y_{11}=Y_{10}$$

The treatment assignment affects the response only through the treatment received. In particular, the treatment effect may only be non-zero for compliers.

#### **Theorem**

Under assumptions (1) - (7),

$$au_{PATT} = \mathbb{E}_{01}\left[\mathbb{E}\left(Y_{11} \mid S = 1, D = 1, W\right)\right] - \mathbb{E}_{01}\left[\mathbb{E}\left(Y_{10} \mid S = 1, T = 0, C = 1, W\right)\right]$$

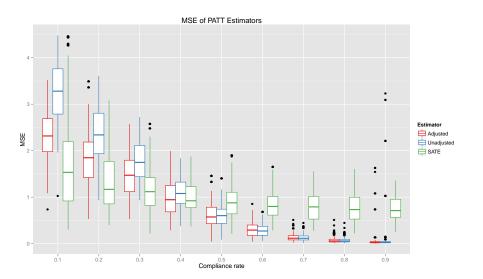
where  $\mathbb{E}_{01}[\mathbb{E}(\cdot \mid ..., W)]$  denotes the expectation with respect to the distribution of W in the treated individuals in the target population.

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### Simulation

describe simulation design?

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### Data

- ► OHIE data
- ► NHIS data

### **Checking Assumptions**

- Monotonicity is violated. There is some 2-way cross-over
- Key assumption is strong ignorability: model of response given covariates is the same in the RCT and in the population
  - ▶ No way to check that we've included all possible confounders
  - We have included all the confounders we have data on

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### Checking Assumptions (cont.)

table of covariates, in OHIE and NHIS

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#### Estimation Procedure

- 1. Using the Medicaid lottery winners in the OHIE (S = 1, T = 1), train a model to predict complier status using observed covariates.
- 2. Predict which lottery losers in the OHIE would have signed up for Medicaid had they been eligible.
- 3. For the group of observed compliers to treatment and predicted compliers in the control group, train a model to predict hospital use using the covariates and Medicaid enrollment as features.
- 4. For all individuals who enrolled in Medicaid in the NHIS, estimate their potential outcomes  $Y_{10}$  and  $Y_{11}$  using the model from step 3. The mean counterfactual  $Y_{11}$  minus the mean counterfactual  $Y_{10}$  is the estimate of  $\tau_{PATT}$ .

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Figure: Heterogeneous effects of Medicaid enrollment on hospital visits.

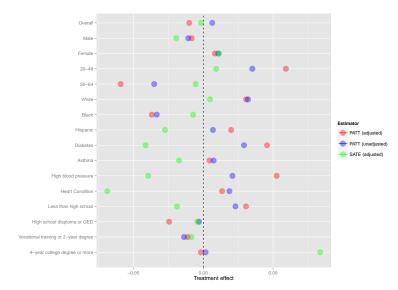
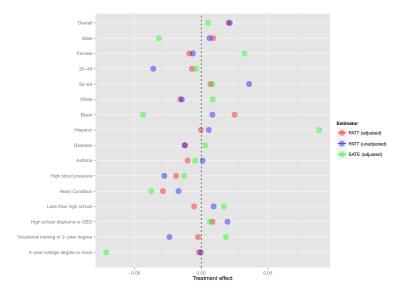


Figure: Heterogeneous effects of Medicaid enrollment on outpatient visits.



#### Conclusions

- ▶ If the compliance rate is moderate and compliance is predictable by observed covariates, then it makes sense to use the proposed estimator
- ▶ statement or two about the OHIE/NHIS conclusions

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#### References

Erin Hartman, Richard Grieve, Roland Ramsahai, and Jasjeet S. Sekhon. From sate to patt: Combining experimental with observational studies to estimate population treatment effects. *Journal of the Royal Statistical Society, Series A*, to appear.