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CALIFICACIÓN
100 %

Practice quiz on Sets

PUNTOS TOTALES DE 3

1. Let $A = \{1, 3, 5\}$. Is the following statement: $3 \in A$. True or false?

1 / 1 puntos

- False
 True

 Correcto

The symbol \in stands for "is an element of" and it is true that 3 is an element of A . The other two elements of A are 1 and 5.

2. Let $E = \{-1, -2, -3\}$. Compute the cardinality $|E|$ of E :

1 / 1 puntos

- 3
 0
 -3
 E

 Correcto

Recall that the cardinality of a set is the number of elements in it. Since E has three elements (which are $-1, -2, -3$), the cardinality of E is $|E| = 3$.

3. Let $A = \{1, 3, 5\}$ and $B = \{3, 5, 10, 11, 14\}$.

1 / 1 puntos

Which of the following sets is equal to the intersection $A \cap B$?

- $\{1, 3, 5\}$
 $\{3\}$
 $\{3, 5\}$
 $\{3, 5, 10\}$

 Correcto

The intersection of two sets consists precisely of the elements they share in common. The elements 3 and 5 are in both A and B .

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87,50 %

Practice quiz on the Number Line, including Inequalities

PUNTOS TOTALES DE 8

1. Which of the following real numbers is not an integer?

1 / 1 puntos

- 4.3
- 0
- 3
- 7

2. Which of the following is the absolute value $| -7 |$ of the number -7?

1 / 1 puntos

- 1
- 0
- 7
- 7

Correcto

The absolute value of a number x is the distance along the number line from x to 0. In this case, -7 is 7 units away from 0, and so $| -7 | = 7$.

3. Suppose I tell you that x and y are two real numbers which make the statement $x < y$ true. Which pair of numbers cannot be values for x and y ?

1 / 1 puntos

- $x = 1$ and $y = 7.3$
- $x = -17.3$ and $y = -17.1$
- $x = -1$ and $y = 0$
- $x = 5$ and $y = 3.3$

Correcto

The statement $x < y$ means that x is to the left of y on the real number line. Since 5 is to the right of 3.3, these cannot be values for x and y .

4. Suppose I tell you that w is a real number which makes both of the following statements true: $w > 1$ and $w < 1.2$. Which of the following numbers could be w ?

0 / 1 puntos

- $w = 1.05$
- $w = 11$
- $w = 0$
- $w = 1.2$

Incorrecto

Note that $11 > 1$ is true since 11 is to the right of 1 on the real number line, but $11 < 1.2$ is false, since 11 is not to the left of 1.2 on the real number line.

5. Suppose that x and y are two real numbers which satisfy $x + 3 = 4y + 1$. Which of the following statements are false?

1 / 1 puntos

- $x = 4y - 2$
- $x + 2 = 4y$
- $x = 4y$
- $2x + 6 = 8y + 2$

 Correcto

The equation $x = 4y$ cannot be derived from the given equation.

6. Which of the following real numbers is in the open interval $(2, 3)$?

1 / 1 puntos

- 2
- 2.1
- 1
- 3

 Correcto

Recall that the open interval $(2, 3)$ consists of all real numbers x which satisfy $2 < x < 3$. Since $2.1 > 2$ and $2.1 < 3$, the number 2.1 is in this open interval.

7. Which of the following real numbers are in the open ray $(3.1, \infty)$?

1 / 1 puntos

- 0
- 3.1
- 4.75
- 5

 Correcto

Recall that $(3.1, \infty) = \{x \in \mathbb{R} \mid x > 3.1\}$. Since $4.75 > 3.1$ is true, $4.75 \in (3.1, \infty)$.

8. Which of the following values for x solves the equation $-3x + 2 = -4$

1 / 1 puntos

- $x = 2$
- $x = \frac{2}{3}$
- $x = -2$
- All values of x such that $x \leq 2$

 Correcto

First we subtract 2 from both sides of the given equation, to obtain $-3x = -6$. Finally, to isolate x we divide both sides of the equation by -3 to obtain $x = 2$.

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Practice quiz on Simplification Rules and Sigma Notation

PUNTOS TOTALES DE 6

1. Which of the numbers below is equal to the following summation: $\sum_{i=1}^3 i^2$? 1 / 1 puntos

- 30
- 14
- 1
- 9

2. Suppose that $A = \sum_{k=1}^{100} k^4$ and $B = \sum_{j=1}^{100} j^4$ 1 / 1 puntos

- Which of the following statements is true?
- $A = B$
 - $A > B$
 - $B > A$
 - There is not enough information to do the problem

✓ Correcto

$A = B$. Both summations evaluate to the same number, since k and j are just dummy indices.

3. Which of the numbers below is equal to the summation $\sum_{i=1}^{10} 7$? 1 / 1 puntos

- 70
- 7
- 55
- 0

✓ Correcto

According to one of our Sigma notation simplification rules, this summation is just equal to 10 copies of the number 7 all added together, and so we get $10 \times 7 = 70$.

4. Suppose that $X = \sum_{i=1}^5 i^3$ and $Y = \sum_{i=1}^5 i^4$.

1 / 1 puntos

Which of the following expressions is equal to the summation $\sum_{i=1}^5 (2i^3 + 5i^4)$?

- $X + Y$
- $2X + 5Y$
- 3375
- 7



To get here, you apply two of our Sigma notation simplification rules $\sum_{i=1}^5 2i^3 + 5i^4 = 2(\sum_{i=1}^5 i^3) + 5(\sum_{i=1}^5 i^4) = 2X + 5Y$.

5. Which of the following numbers is the mean μ_Z of the set $Z = \{-2, 4, 7\}$?

1 / 1 puntos

- 4
- 3
- $\frac{13}{3}$
- 9



To get the mean of a set of numbers, you need to perform two steps: first add them all up (in this case getting $-2 + 4 + 7 = 9$), and then divide by the number of elements in the set (in this case that number is 3).

So you should obtain $\mu_Z = \frac{9}{3} = 3$, which you did!

6. Suppose the set X has five numbers in it: $X = \{x_1, x_2, x_3, x_4, x_5\}$. Which of the following expression 1 / 1 puntos represents the mean of the set X ?

- $\frac{1}{5} [\sum_{i=1}^5 x_i]$
- $\frac{1}{5} [\sum_{i=1}^5 (x_i - \mu_X)^2]$
- $\sum_{i=1}^5 x_i$
- $\frac{1}{N} [\sum_{i=1}^N x_i]$



To obtain the mean of a set of numbers, you first add them all up (which is expressed here by the sigma operation inside the square brackets) and then you divide by the number of numbers in the set (which is expressed here by the $\frac{1}{n}$ outside the square brackets).

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Practice quiz on the Cartesian Plane

PUNTOS TOTALES DE 5

1. Which of the following points in the Cartesian Plane is on the y -axis?

1 / 1 puntos

- (0, -5)
- (-5, 0)
- (5, 0)
- (1, 1)

Correcto

2. Find the distance between the points $A = (2, 2)$ and $C = (3, 3)$:

1 / 1 puntos

- 0
- 1
- 2
- $\sqrt{2}$

Correcto

Recall that the distance between points (a, b) and (c, d) is $\sqrt{(c - a)^2 + (d - b)^2}$.

In this case $(a, b) = (2, 2)$ and $(c, d) = (3, 3)$, so the distance is $\sqrt{(3 - 2)^2 + (3 - 2)^2} = \sqrt{2}$.

3. Find the point-slope form of the equation of the line that goes between $A = (1, 1)$ and $B = (5, 3)$:

1 / 1 puntos

- $y - 3 = \frac{1}{2}(x - 1)$
- $y - 1 = \frac{1}{2}(x - 5)$
- $y - 1 = \frac{1}{2}(x - 1)$
- $y = \frac{1}{2}x$

Correcto

The point-slope form for the equation of a line with slope m that goes through the point (x_0, y_0) is $y - y_0 = m(x - x_0)$

In this case, the slope $m = \frac{3 - 1}{5 - 1} = \frac{1}{2}$

4. Which of the following points is on the line with equation:

1 / 1 puntos

$$y - 1 = 2(x - 2)?$$

- (2, 3)
- (0, 0)
- (3, 2)
- (2, 1)

 Correcto

If we plug in 1 for y and 2 for x in the equation of the line, we make a true statement, $0 = 0$, so this point lies on the line.

5. Suppose that a line ℓ has slope 2 and goes through the point $(-1, 0)$. What is the y -intercept of ℓ ?

1 / 1 puntos

- 2
- 1
- 0
- 1

 Correcto

Recall that the y -intercept of ℓ is the y -coordinate of where ℓ hits the y -axis.

Since $(-1, 0) \in \ell$, the point on ℓ with $x = 0$ is obtained by running one unit from $(-1, 0)$ while rising two units.

This gives $y = 2$ as the y -intercept.

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CALIFICACIÓN
100 %

Practice quiz on Types of Functions

PUNTOS TOTALES DE 6

1. Suppose that $A = \{1, 2, 10\}$ and $B = \{4, 8, 40\}$. Which of the following formulae do *not* define a function $f : A \rightarrow B$?

1 / 1 puntos

- $f(a) = 4a$, for each $a \in A$
- $f(1) = 4, f(2) = 40$, and $f(10) = 8$.
- $f(1) = 4, f(2) = 4$, and $f(10) = 4$.
- $f(1) = 5, f(2) = 8$, and $f(10) = 40$.

2. Suppose that A contains every person in the VBS study (see the second video in the course if you're confused here!). Suppose that $Y = \{+, -\}$ and $Z = \{H, S\}$

1 / 1 puntos

Suppose that $T : A \rightarrow Y$ is the function which gives $T(a) = +$ if person a tests positive and $T(a) = -$ if they test negative.

Suppose that $D : A \rightarrow Z$ is the function which gives $D(a) = H$ does not actually have VBS and $D(a) = S$ if the person actually has VBS.

Which of the following must be true of person a if we have a false positive?

- $T(a) = -$ and $D(a) = S$
- $T(a) = +$ and $D(a) = H$
- $T(a) = -$ and $D(a) = H$
- $T(a) = +$ and $D(a) = S$

 Correcto

Recall that a false positive is a positive test result (so $T(a) = +$) which is misleading because the person actually does not have the disease ($D(a) = H$)

3. Consider the function $g : \mathbb{R} \rightarrow \mathbb{R}$ defined by $g(x) = x^2 - 1$. Which of the following points are *not* on the graph of g ?

1 / 1 puntos

- $(0, -1)$
- $(-1, 0)$
- $(2, -1)$
- $(1, 0)$

 Correcto

Recall that the graph of g consists of all points (x, y) such that $y = g(x)$. Here $g(2) = 3 \neq -1$, so the point $(2, -1)$ is *not* on the graph of g .

4. Let the point $A = (2, 4)$. Which of the following graphs does *not* contain the point A ?

1 / 1 puntos

- The graph of $h(x) = x - 1$
- The graph of $s(x) = x^2$
- The graph of $f(x) = 2x$
- The graph of $g(x) = x + 2$

 Correcto

The graph of h consists of all points (x, y) such that $y = h(x)$. Here $h(2) = 1 \neq 4$, so the point $(2, 4)$ is *not* on the graph of h .

5. Suppose that $h(x) = -3x + 4$. Which of the following statements is true?

1 / 1 puntos

- h is a strictly decreasing function
- h is a strictly increasing function
- h is neither a strictly increasing function nor a strictly decreasing function.
- All statements are correct

 Correcto

A function h is called strictly decreasing if whenever $a < b$, then $h(a) > h(b)$

Since the graph of h is a line with negative slope, this is in fact true!

6. Suppose that $f : \mathbb{R} \rightarrow \mathbb{R}$ is a strictly increasing function, with $f(3) = 15$

1 / 1 puntos

Which of the following is a possible value for $f(3.7)$?

- 3
- 14.7
- 17
- 3

 Correcto

A function f is called strictly increasing if whenever $a < b$, then $f(a) < f(b)$.

Since $f(3) = 15$ is given and $3 < 3.7$, it must be that $15 < f(3.7)$, and this answer satisfies that.

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CALIFICACIÓN
92,30 %

Graded quiz on Cartesian Plane and Types of Function

CALIFICACIÓN DEL ÚLTIMO ENVÍO

92.3%

1. Which of the following points in the Cartesian Plane have positive x -coordinate and negative y -coordinate? 1 / 1 puntos

- (7, -1)
- (0, 0)
- (5, 7)
- (-4, 5)

Correcto

The x -coordinate, 7, is positive, and the y -coordinate, -1, is negative.

2. Which of the following points is in the first quadrant of the Cartesian Plane? 1 / 1 puntos

- (7, 11)
- (-4, -7)
- (5, -1)
- (-5, 1)

Correcto

The first quadrant is defined to be all points in the Cartesian plane whose coordinates are both positive.

3. Let A, B, C, D be points in the Cartesian Plane, and let the set $S = \{B, C, D\}$ 1 / 1 puntos

Suppose that the distances from A to B, C, D are 5.3, 2.1, and 11.75, respectively.

Which of the following points is the nearest neighbor to the point A in the set S ?

- D
- A
- B
- C

Correcto

The distance from A to C is 2.1 and that is smaller than the distance from A to any other element of S .

4. Find the distance between the points $A = (2, 2)$ and $B = (-1, -2)$.

0 / 1 puntos

- 25
- 5
- 25
- 1



If you got here, you probably got confused between negative and positive numbers in arithmetic.

5. Find the slope of the line segment between the points $A = (0, 1)$ and $B = (1, 0)$.

1 / 1 puntos

- 1
- 1
- $\sqrt{2}$
- 0



The slope of this line segment is $\frac{0 - 1}{1 - 0} = -1$

6. Find the point-slope form of the equation of the line with slope -2 that goes through the point $(5, 4)$.

1 / 1 puntos

- $y - 5 = -2(x - 4)$
- $(5, 4)$
- $y - 4 = 2(x - 5)$
- $y - 4 = -2(x - 5)$



The point-slope form for the equation of a line with slope m that goes through the point (x_0, y_0) is $y - y_0 = m(x - x_0)$.

In this case, the slope $m = -2$ is given and the point $(5, 4)$ on the line is given.

7. Which of the following equations is for a line with the same slope as $y = -3x + 2$?

1 / 1 puntos

- $y = -3x - 8$
- $y = 5x + 2$
- $y = 5x$
- $y = 8x - 3$

 Correcto

The slope-intercept formula for a line is $y = mx + b$, where m is the slope and b is the y -coordinate of the point where the line hits the y -axis.

This line has slope $m = -3$ which is the same slope as the given line.

8. Which of the following equations is for a line with the same y -intercept as $y = -3x + 2$?

1 / 1 puntos

- $y = 5x + 2$
- $y = -3x - 8$
- $y = 8x - 3$
- $y = 5x$

 Correcto

The slope-intercept formula for a line is $y = mx + b$, where m is the slope and b is the y -coordinate of the point where the line hits the y -axis. This line has a y -intercept of 2 which is the same as the given line.

9. How many lines contain both the point $A = (1, 1)$ and the point $B = (2, 2)$?

1 / 1 puntos

- None
- infinitely many
- 1
- 2

 Correcto

The line with equation $y = x$ is the one and only line that meets the stated requirements.

10. Suppose that we have two sets, $A = \{a, b\}$ and $Z = \{x, y\}$. How many different functions $F : A \rightarrow Z$ are possible?

1 / 1 puntos

- 4
- There are none
- 1
- There are infinitely many

 Correcto

A function $F : A \rightarrow Z$ is a rule which assigns an element $F(a) \in Z$ to each element $a \in A$.

There are two elements in A ; namely, a and b . For each of these elements, there are two assignment choices we could make: x and y .

Here are the four possible functions:

$$F(a) = x, F(b) = y, \text{ OR}$$

$$F(a) = y, F(b) = x, \text{ OR}$$

$$F(a) = x, F(b) = x, \text{ OR}$$

$$F(a) = y, F(b) = y.$$

11. How many graphs contain both the point $A = (0, 0)$ and the point $B = (1, 1)$

1 / 1 puntos

- 2
- 1
- Infinitely many
- None

 Correcto

The graphs of $f(x) = x, g(x) = x^2, h(x) = x^3, s(x) = x^4, \dots$ all contain both A and B

12. Suppose that $g : \mathbb{R} \rightarrow \mathbb{R}$ is a continuous function whose graph intersects the x -axis more than once.
Which of the following statements is true?

1 / 1 puntos

- g is strictly increasing.
- All of the above.
- g is strictly decreasing.
- g is neither strictly increasing nor strictly decreasing.

✓ Correcto

The function g fails the horizontal line test, so it can neither be strictly increasing nor strictly decreasing.

13. Find the slope of the line segment between the points $A = (1, 1)$ and $B = (5, 3)$.

1 / 1 puntos

- 2
- $\sqrt{20}$
- 4
- $\frac{1}{2}$

✓ Correcto

The slope of this line segment is $\frac{3 - 1}{5 - 1} = \frac{1}{2}$, where $3 - 1$ is the rise and $5 - 1$ is the run.

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CALIFICACIÓN
100 %

Practice quiz on Tangent Lines to Functions

PUNTOS TOTALES DE 2

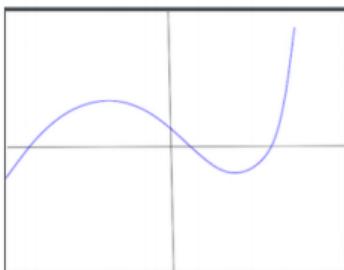
1. Suppose that $f : \mathbb{R} \rightarrow \mathbb{R}$ is a function. Which of the following expressions corresponds to $f'(2)$, the slope of the tangent line to the graph of $f(x)$ at $x = 2$? 1 / 1 puntos

- $f'(2) = mx + b$
- $f'(2) = 2$
- $f'(2) = \lim_{h \rightarrow 0} \frac{f(2+h)-f(2)}{h}$
- $f'(2) = \lim_{h \rightarrow 0} \frac{f(a+h)-f(a)}{h}$

 Correcto

This expression can be obtained from the first screen of our video by plugging in 2 for a .

2. Suppose that $h : \mathbb{R} \rightarrow \mathbb{R}$ is a function whose graph is shown as the blue curve in the figure. For how many values of a is $h'(a) = 0$? 1 / 1 puntos



- 3
- Never
- Always
- 2

 Correcto

$h'(a)$ gives the slope of the tangent line to the graph of h at the point $x = a$.

When $h'(a) = 0$, this means that the tangent line is horizontal.

There are two places (one on each side of the y -axis) where this tangent line is horizontal, so this answer is correct.

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CALIFICACIÓN

75 %

Practice quiz on Exponents and Logarithms

PUNTOS TOTALES DE 12

1. Re write the number $784 = 2 \times 2 \times 2 \times 2 \times 7 \times 7$ using exponents.

1 / 1 puntos

- $(16^4)(49^2)$
- $(2^6)(7^6)$
- $(2 \times 7)^6$
- $(2^4)(7^2)$

Correcto

For this type of problem, count the number of times each relevant factor appears in the product. That number is the exponent for that factor.

2. What is $(x^2 - 5)^0$?

1 / 1 puntos

- 1
- 4
- (x^2)
- $(x^2) - 5$

Correcto

Any real number (except zero) raised to the "zeroith" power = 1.

3. Simplify $((x - 5)^2)^{-3}$

1 / 1 puntos

- $(x - 5)^{-6}$
- $(x - 5)$
- $(x - 5)^{-5}$
- $(x - 5)^{-1}$

Correcto

By Rule 2, "Power to a Power," multiply the exponents and get:

$$(x - 5)^{(2 \times -3)} = (x - 5)^{-6}$$

By the definition of negative exponents, this is equal to $\frac{1}{(x - 5)^6}$

4. Simplify $(\frac{8^2}{8^7})^2$

1 / 1 puntos

- 8^{-5}
- 8^{-10}
- 8^{-4}
- 8^{-1}

 Correcto

We can first simplify what is inside the parenthesis to 8^{-5} using the Division and Negative Powers Rule.

Then apply division and negative powers-- the result is the same. $\frac{8^4}{8^{14}} = 8^{-10}$

5. $\log 35 = \log 7 + \log x$

1 / 1 puntos

Solve for x

- 5
- 4
- 7
- 28

 Correcto

$$\log(x) = \log 35 - \log 7$$

$$\log(x) = \log \left(\frac{35}{7} \right)$$

$$\text{By the Quotient Rule } \log x = \log 5$$

6. $\log_2(x^2 + 5x + 7) = 0$

1 / 1 puntos

Solve for x

- $x = 2$
- $x = 2$ or $x = 3$
- $x = -2$ or $x = -3$
- $x = 3$



We use the property that $b^{\log_b a} = a$

Use both sides as exponent for 2.

$$2^{\log_2 x^2 + 5x + 7} = 2^0$$

$$x^2 + 5x + 7 = 1$$

$$x^2 + 5x + 6 = 0$$

$$(x + 3)(x + 2) = 0$$

$$x = -3 \quad \text{OR}$$

$$x = -2$$

7. Simplify $\log_2 72 - \log_2 9$

1 / 1 puntos

- 4
- $\log_2 4$
- 3
- $\log_2 63$



By the quotient rule, this is $\log_2 \frac{72}{9} = \log_2 2^3 = 3$

8. Simplify $\log_3 9 - \log_3 3 + \log_3 5$

0 / 1 puntos

- $\log_3 15$
- 8
- $\log_3 8$
- 15

! Incorrecto

By the Quotient and Product Rules, this is $\log_3 \frac{9 \times 5}{3} = \log_3 15$

9. Simplify $\log_2(3^8 \times 5^7)$

1 / 1 puntos

- $15 \times \log_2 56$
- $56 \times \log_2 15$
- $(5 \times \log_2 3) + (8 \times \log_2 5)$
- $(8 \times \log_2 3) + (7 \times \log_2 5)$

✓ Correcto

We first apply the Product Rule to convert to the sum: $\log_2(3^8) + \log_2(5^7)$. Then apply the power and root rule.

10. If $\log_{10} y = 100$, what is $\log_2 y = ?$

0 / 1 puntos

- 20
- 332.19
- 301.03
- 500

! Incorrecto

Use the change of base formula, $\log_a b = \frac{\log_x b}{\log_x a}$

Where the "old" base is x and the "new" base is a .

$$\text{So } \frac{100}{\log_{10}(2)} = \frac{100}{0.30103} = 332.19$$

11. A tree is growing taller at a continuous rate. In the past 12 years it has grown from 3 meters to 15 meters. 1 / 1 puntos
- What is its rate of growth per year?

- 11.41%
- 13.41%
- 10.41%
- 12.41%

Correcto

$$\frac{\ln \frac{15}{3}}{12} = 0.1341$$

12. Bacteria can reproduce exponentially if not constrained. Assume a colony grows at a continually compounded rate of 400% per day. How many days before a colony with initial mass of 6.25×10^{-10} grams weights 1000 Kilograms? 0 / 1 puntos

- 8.75 days
- 87.5 days
- 875 days
- 0.875 days

Incorrecto

$$6.25 \times 10^{-10} \times e^{4t} = 10^6$$

$$4t = \ln \left(\frac{10^6}{(6.25 \times 10^{-10})} \right) = 35.00878$$

$$t = \ln \frac{10^6}{6.25 \times 10^{-10}} = 8.752195$$

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CALIFICACIÓN
100 %

Graded quiz on Tangent Lines to Functions, Exponents and Logarithms

CALIFICACIÓN DEL ÚLTIMO ENVÍO

100%

1. Convert $\frac{1}{49}$ to exponential form, using 7 as the factor.

1 / 1 puntos

- (7^2)
- $\frac{7}{7^3}$
- 49^{-1}
- 7^{-2}

 Correcto

The rule for a factor to a Negative exponent is to divide by the same factor to a positive exponent with the same absolute value.

2. A light-year (the distance light travels in a vacuum in one year) is 9,460 trillion meters. Express in scientific notation.

1 / 1 puntos

- 9460×10^{12} meters
- 9.46×10^{15} kilometers
- 0.946×10^{16}
- 9.46×10^{15} meters.

 Correcto

9,460 is (9.4×10^3) meters and one trillion meters is 10^{12} meters. $(9.4 \times 10^3)(10^{12}) = 9.4 \times 10^{15}$. A kilometer is 1000 meters.

3. Simplify $(x^8)(y^3)(x^{-10})(y^{-2})$

1 / 1 puntos

$(x^{-80})(y^{-6})$

$(x^2)(y)$

$(x^{-2})(y)$

$(x)(y^{-2})$

Correcto

By the Division and Negative Powers Rule, this is $(x^{(8-10)})(y^{(3-2)})$

4. Simplify $[(x^4)(y^{-6})]^{-1}$

1 / 1 puntos

$\frac{(x^{-4})}{(y^6)}$

$(x^{-4})(y^6)$

$(x^3)(y^{-7})$

$\frac{(x^4)}{(y^{-6})}$

Correcto

By the Power to a Power Rule, each of the exponents is multiplied by (-1)

5. Solve for x :

1 / 1 puntos

$$\log_2(39x) - \log_2(x - 5) = 4$$

$\frac{80}{38}$

$\frac{39}{23}$

$\frac{23}{80}$

$\frac{-80}{23}$

 Correcto

$$\log_2 \frac{39x}{(x-5)} = 4 \text{ by the Quotient Rule.}$$

Since both sides are equal, we can use them as exponents in an equation.

$$2^{\log_2 \frac{39x}{(x-5)}} = 2^4$$

$$\frac{39x}{(x-5)} = 16$$

$$39x = 16 \times (x - 5)$$

$$39x = 16x - 80$$

$$23x = -80$$

$$x = \frac{-80}{23}$$

6. Simplify this expression:

1 / 1 puntos

$$(x^{\frac{1}{2}})^{\frac{-3}{2}}$$

$x^{-\frac{3}{4}}$

$x^{\frac{1}{3}}$

$x^{\frac{4}{3}}$

x^{-1}

7. Simplify $\log_{10} 1000 + \log_{10} \frac{1}{10000}$

1 / 1 puntos

$\frac{1}{10}$

-1

1

$\log_{10} -10$

 Correcto

By the Product Rule, this is:

$$\log_{10} \left(\frac{1000}{10000} \right) = \log_{10} \left(\frac{1}{10} \right) = -1$$

8. If $\log_3 19 = 2.680$, what is $\log_9 19$?

1 / 1 puntos

- 1.304
- 5.216
- 0.4347
- 0.8934

✓ Correcto

To convert from \log_3 to \log_9 , divide by $\log_3 9$. Which is equal to 2, so the answer is 1.34

9. If $\log_{10} b = 1.8$ and $\log_a b = 2.5752$, what is a ?

1 / 1 puntos

- 5
- 3
- 6
- 4

✓ Correcto

To solve for a in the formula;

$$\log_a b = \frac{\log_x b}{\log_x a}$$

$$\log_a b = 2.5752 \text{ and } \log_{10} b = 1.8$$

$$\text{Therefore, } \log_{10} a \text{ must equal to } \frac{1.8}{2.5752} = 0.69897$$

Treating both sides of equation $\log_{10} a = 0.69897$ as exponents of 10 gives $a = 10^{0.69897} = 5$

10. An investment of 1,600 is worth 7,400 after 8.5 years. What is the continuously compounded rate of return of this investment?

1 / 1 puntos

- 20.01
- 19.01%
- 17.01%
- 18.02%

✓ Correcto

$$\frac{\ln \frac{7400}{1600}}{8.5} = 0.18017$$

11. A pearl grows in an oyster at a continuously compounded rate of .24 per year. If a 25-year old pearl weighs 1 gram, what did it weigh when it began to form?

1 / 1 puntos

- 0.2478
- 0.0002478
- 0.02478
- 0.002478

✓ Correcto

$$e^{(0.24 \times 25)} = \frac{1}{x}$$

$$x = \frac{1}{(e^{0.24 \times 25})}$$

$$x = \frac{1}{403.4288}$$

$$x = 0.002478$$

12. $\log_2 z = 6.754$. What is $\log_{10}(z)$?

1 / 1 puntos

- 0.49185
- 1.3508
- 0.82956
- 2.03316

✓ Correcto

$$\frac{\log_2 z}{\log_2 10} =$$

$$(\log_{10} z) \times (\log_2 10) = 3.321928$$

$$\text{Therefore, } \log_{10} z = \frac{6.754}{3.321928} = 2.03316$$

13. Suppose that $g : \mathbb{R} \rightarrow \mathbb{R}$ is a function, and that $g(1) = 10$. Suppose that $g'(a)$ is negative for every single value of a . Which of the following could possibly be $g(1.5)$?

1 / 1 puntos

- $g(1.5) = 103.4$
- $g(1.5) = 11$
- $g(1.5) = 9.7$
- $g(1.5) = 10.1$

✓ Correcto

Since the slope of the tangent line to the graph of g is negative everywhere on the graph, we know that g is *decreasing* function! And therefore we must have $g(1.5) < g(1)$. That is the case here, so this value is at least possible.

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

Continúa aprendiendo

CALIFICACIÓN
88,88 %

Practice quiz on Probability Concepts

PUNTOS TOTALES DE 9

1. If $x = \text{"It is raining,"}$ what is $\sim (\sim x)$?

0 / 1 puntos

- "It is not raining"
- "It is raining"
- "It is always raining"
- "It is never raining"

Incorrecto

The second negation cancels out the first one.

Similarly $\sim (\sim (\sim x)) = \sim x$

2. If the statement "I am 25 years old" is assigned probability 0, what probability is assigned to the statement "I am not 25 years old?"

1 / 1 puntos

- 0
- Unknown
- 1
- 1

Correcto

It is always the case that $p(x) + p(\sim x) = 1$.

3. If I assign to the statement $x = \text{"it will rain today"}$ a probability of $p(x) = 0.35$, what probability must I assign to the statement "it will not rain today?"

1 / 1 puntos

- .5
- 0
- .35
- .65

Correcto

$p(x) + p(\sim x) = 1$

4. Is the following collection of statements a probability distribution?

1 / 1 puntos

1. I own a Toyota pickup truck
2. I do not own a Toyota pickup truck
3. I own a non-Toyota pickup truck
4. I do not own a non-Toyota pickup truck

- Yes
 No

 Correcto

The statements are not *exclusive*: 1 and 4 could both be true, 2 and 3 could both be true, 2 and 4 could both be true, and even (1) and (3) could both be true (if I owned more than one pickup truck).

5. I don't know what it means to be "ingenuous." What probability would I assign to the statement, "I am ingenuous OR I am not ingenuous"?

1 / 1 puntos

- 1
 1
 0
 .5

 Correcto

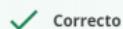
It is always the case, regardless of the content of the statement x , that $p(x \text{ or } \sim x) = 1$

6. A friend of mine circumscribes a circle inside a square, so that the diameter of the circle and the edge of the square are the same length. He asks me to close my eyes and pick a point at random inside the square. He says the probability that my point will also be inside the circle is $\frac{\pi}{4}$

1 / 1 puntos

Is this correct?

- Yes
 No



Probabilities can be any real number between 0 and 1. They do not need to be rational numbers – a numerator that is a transcendental number like Pi is acceptable.

Note that

the correct probability does not depend on the length r of the circle's radius. For a circle with any radius r to be circumscribed inside a square, the square must have sides each of length $2r$. The area of the circle is πr^2 and the area of the square is $(2r)^2 = 4r^2$. The probability of landing in a circle of area πr^2 when it is known that one is in the area of the square is equal to the ratio of the area of the circle to the area of the square in which it is circumscribed, or $\pi r^2 / 4r^2$, which equals $\pi/4$.

7. The probability of drawing a straight flush (including a Royal Flush) in a five-card poker hand is 0.0000153908

What is
the probability of **not** drawing a
straight flush?

- .9996582672
 .9999846092
 .9999745688
 .9967253809



$$p(\sim x) = 1 - p(x)$$

8. What is the probability that a fair, six-sided die will come up with a prime number? (Recall that prime numbers are positive integers other than 1 that are divisible only by themselves and 1)
- 1 / 1 puntos

- $\frac{2}{3}$
- $\frac{1}{2}$
- $\frac{1}{6}$
- $\frac{1}{3}$

✓ Correcto

The faces with 2, 3 and 5 satisfy the condition – which makes 3 relevant outcomes out of the “universe” of 6 outcomes = $\frac{3}{6} = \frac{1}{2}$

9. The joint probability p (the die will come up 5, the next card will be a heart) is equal to the joint probability:
- 1 / 1 puntos

- p (the die will **not** come up 5,
the next card will **not** be a heart)
- p (the
next card will **not** come up 5, the
next card will be a heart)
- p (the
next card will be a heart, the die will **not**
come up 5)
- p (the next card will be a heart, the die will
come up 5)

✓ Correcto

In joint probabilities, the order does not change the probability: $p(A, B) = p(B, A)$

 ¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

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CALIFICACIÓN
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Practice quiz on Problem Solving

PUNTOS TOTALES DE 9

1. I am given the following 3 joint probabilities:

1 / 1 puntos

$p(\text{I am leaving work early, there is a football game that I want to watch this afternoon}) = .1$

$p(\text{I am leaving work early, there is not a football game that I want to watch this afternoon}) = .05$

$p(\text{I am not leaving work early, there is not a football game that I want to watch this afternoon}) = .65$

What is the probability that there is a football game that I want to watch this afternoon?

- .3
- .35
- .2
- .1

 Correcto

Getting the answer is a two-step process. First, recall that the sum of probabilities for a probability distribution must sum to 1. So the “missing” joint distribution

$p(\text{I am not leaving work early, there is a football game I want to watch this afternoon})$ must be $1 - (0.1 + 0.05 + 0.65) = 0.2$

By the sum rule, the marginal probability $p(\text{there is a football game that I want to watch this afternoon})$ = the sum of the joint probabilities

$P(\text{I am leaving work early, there is a football game that I want to watch this afternoon}) + P(\text{I am not leaving work early, there is a football game I want to watch this afternoon}) = .1 + .2 = .3$

2. The

1 / 1 puntos

Joint probability of my summiting Mt. Baker in the next two years AND publishing a best-selling book in the next two years is .05. If the probability of my publishing a best-selling book in the next two years is 10%, and the probability of my summing Mt. Baker in the next two years is 30%, are these two events dependent or independent?

- Dependent
 Independent

✓ Correcto

We know this because the joint distribution of 5% does not equal the product distribution of $(0.1) \times (0.3) = 3\%$. If I summit Mt. Baker, I am more likely to publish a best-selling book, and vice versa.

3. The

1 / 1 puntos

Joint probability of my summiting Mt. Baker in the next two years AND my publishing a best-selling book in the next two years is .05.

If the probability of my publishing a best-selling book in the next two years is 10%, and the probability of my summing Mt. Baker in the next two years is 30%, what is the probability that (sadly) in the next two years I will neither summit Mt. Baker nor publish a best-selling book?

- .95
 .25
 .65
 .9

✓ Correcto

Set A = I will summit Mt. Baker in the next two years

Set B = I will publish a best-selling book in the next two years.

Since $p(A) = 0.3$ and $p(A, B) = 0.05$, by the SUM RULE we know that $p(A, \sim B) = (0.3 - 0.05) = 0.25$

Since $p(B) = 0.1, p(\sim B) = 0.9$

Since $p(\sim B) = 0.9$ and $p(A, \sim B) = 0.25$ and again by the SUM RULE, $p(\sim A, \sim B) = 0.9 - 0.25 = .65$

4. |

1 / 1 puntos

have two coins. One is fair, and has a probability of coming up heads of .5. The second is bent, and has a probability of coming up heads of .75. If I toss each coin once, what is the probability that *at least* one of the coins will come up heads?

- .375
- .875
- 1.0
- .625

 Correcto

We apply the rule $p(A \text{ or } B \text{ or both})$

$$= 1 - (p(\sim A)p(\sim B))$$

$$= 1 - ((1 - .5)(1 - .75))$$

$$= 1 - .125$$

$$=.875$$

5. What is $\frac{11!}{9!}$?

1 / 1 puntos

- 4,435,200
- 110,000
- 554,400
- 110

 Correcto

$$\frac{11!}{9!} = 11 \times 10 = 110$$

6. What is the probability that, in six throws of a die, there will be exactly one each of “1” “2” “3” “4” “5” and “6”?

0 / 1 puntos

- .01176210
- .00187220
- .01432110
- .01543210

! Incorrecto

There are $6! = 720$ permutations where each face occurs exactly once.

There are $6 \times 6 \times 6 \times 6 \times 6 \times 6 = 46656$ total permutations of 6 throws.

The probability is therefore $\frac{720}{46656} = 0.01543210$

7. On 1 day in 1000, there is a fire and the fire alarm rings.

1 / 1 puntos

On 1 day in 100, there is no fire and the fire alarm rings (false alarm)

On 1 day in 10,000, there is a fire and the fire alarm does not ring (defective alarm).

On 9,889 days out of 10,000, there is no fire and the fire alarm does not ring.

If the fire alarm rings, what is the (conditional) probability that there is a fire?

Written $p(\text{there is a fire} \mid \text{fire alarm rings})$

- 1.1%
- 9.09%
- 1.12%
- 90.9%

✓ Correcto

10 days out of every 10,000 there is fire and the fire alarm rings.

100 days out of every 10,000 there is no fire and the fire alarm rings.

110 days out of every 10,000 the fire alarm rings.

The probability that there is a fire, given that the fire alarm rings, is $\frac{10}{110} = 9.09\%$

8. On 1 day in 1000, there is a fire and the fire alarm rings.

1 / 1 puntos

On 1 day in 100, there is no fire and the fire alarm rings
(false alarm)

On 1 day in 10,000, there is a fire and the fire alarm does not ring (defective alarm).

On 9,889 days out of 10,000, there is no fire and the fire alarm does not ring.

If the fire alarm does not ring, what is the (conditional) probability that there is a fire?

- .10011%
- 1.0001%
- .01000%
- 0.01011%



Correcto

On $(1 + 9,889) = 9,890$ days out of every 10,000 the fire alarm does not ring.

On 1 of those 10,000 days there is a fire.

$$\frac{1}{9890} = 0.01011\%$$

9. A group of 45 civil servants at the State Department are newly qualified to serve as Ambassadors to foreign governments. There are 22 countries that currently need Ambassadors. How many distinct groups of 22 people can the President promote to fill these jobs?

1 / 1 puntos

- $\$\$4.1167 \times (10^{12})$
- $8.2334 \times (10^{12})$
- $=1.06 \times (10^{35})$
- $=2.429 \times (10^{-13})$



Correcto

$$\binom{45}{22}$$

$$= 45!/(23!)(22!)$$

$$= \frac{45!}{23! \times 22!}$$

¡Felicitaciones! ¡Aprobaste!

PARA APROBAR 75 % o más

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CALIFICACIÓN
88,88 %

Practice quiz on Bayes Theorem and the Binomial Theorem

PUNTOS TOTALES DE 9

1. A jewelry store that serves just one customer at a time is concerned about the safety of its isolated customers.

0 / 1 puntos

The store does some research and learns that:

- 10% of the times that a jewelry store is robbed, a customer is in the store.
- A jewelry store has a customer on average 20% of each 24-hour day.
- The probability that a jewelry store is being robbed (anywhere in the world) is 1 in 2 million.

What is the probability that a robbery will occur while a customer is in the store?

- $\frac{1}{500000}$
- $\frac{1}{2000000}$
- $\frac{1}{4000000}$
- $\frac{1}{5000000}$

Incorrecto

What is known is:

A: "a customer is in the store," $P(A) = 0.2$

B: "a robbery is occurring," $P(B) = \frac{1}{2,000,000}$

$P(\text{a customer is in the store} \mid \text{a robbery occurs}) = P(A \mid B)$

$P(A \mid B) = 10\%$

What is wanted:

$P(\text{a robbery occurs} \mid \text{a customer is in the store}) = P(B \mid A)$

By the product rule:

$$P(B \mid A) = \frac{P(A, B)}{P(A)}$$

and $P(A, B) = P(A \mid B)P(B)$

Therefore:

$$P(B \mid A) = \frac{P(A \mid B)P(B)}{P(A)} = \frac{(0.1)\left(\frac{1}{2000000}\right)}{0.2} = \frac{1}{4000000}$$

2. If I flip a fair coin, with heads and tails, ten times in a row, what is the probability that I will get exactly six heads?

1 / 1 puntos

- 0.021
- 0.187
- 0.2051
- 0.305

 Correcto

By Binomial Theorem, equals

$$\begin{aligned} & \binom{10}{6} (0.5^{10}) \\ &= \left(\frac{10!}{4! \times 6!} \right) \left(\frac{1}{1024} \right) \\ &= 0.2051 \end{aligned}$$

3. If a coin is bent so that it has a 40% probability of coming up heads, what is the probability of getting *exactly* 6 heads in 10 throws?

1 / 1 puntos

- 0.0974
- 0.1045
- 0.1115
- 0.1219

 Correcto

$$\binom{10}{6} \times 0.4^6 \times 0.6^4 = 0.1115$$

4. A bent coin has 40% probability of coming up heads on each independent toss. If I toss the coin ten times, 1 / 1 puntos what is the probability that I get at least 8 heads?

- 0.0213
- 0.0312
- 0.0132
- 0.0123

 Correcto

The answer is the sum of three binomial probabilities:

$$\begin{aligned} & \left(\binom{10}{8} \times (0.4^8) \times (0.6^2) \right) + \left(\binom{10}{9} \times (0.4^9) \times (0.6^1) \right) + \\ & \left(\binom{10}{10} \times (0.4^{10}) \times (0.6^0) \right) \end{aligned}$$

5. Suppose I have a bent coin with
a 60% probability of coming up heads. I throw the coin ten times and
it comes up heads 8 times.

1 / 1 puntos

What is the value of the “likelihood” term in Bayes’ Theorem
-- the conditional probability of the data given the parameter.

- 0.168835
- 0.043945
- 0.122885
- 0.120932

 Correcto

Bayesian “likelihood” --- the
 $p(\text{observed data} \mid \text{parameter})$ is

$p(8 \text{ of } 10 \text{ heads} \mid \text{coin has } p = .6 \text{ of coming up heads})$

$$\binom{10}{8} \times (0.6^8) \times (0.4^2) = 0.120932$$

6. We have the following information about a new medical test for diagnosing cancer.

1 / 1 puntos

Before any data are observed, we know that 5% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer. The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 90% of them get an accurate test result of "Negative" for cancer. The other 10% get a false test result of "Positive" for cancer.

What is the conditional probability that I have Cancer, if I get a "Positive" test result for Cancer?

**Formulas in the feedback section are very long, and do not fit within the standard viewing window. Therefore, the font is a bit smaller and the word "positive test" has been abbreviated as PT.

- 9.5%
- 32.1% probability that I have cancer
- 4.5%
- 67.9%

 Correcto

I still have a more than $\frac{2}{3}$ probability of not having cancer

Posterior probability:

$p(\text{I actually have cancer} \mid \text{receive a "positive" Test})$

By Bayes Theorem:

$$= \frac{(\text{chance of observing a PT if I have cancer})(\text{prior probability of having cancer})}{(\text{marginal likelihood of the observation of a PT})}$$

$$= \frac{p(\text{receiving positive test} \mid \text{has cancer})p(\text{has cancer} \mid \text{before data is observed})}{p(\text{positive} \mid \text{has cancer})p(\text{has cancer}) + p(\text{positive} \mid \text{no cancer})p(\text{no cancer})}$$

$$= (90\%)(5\%) / ((90\%)(5\%) + (10\%)(95\%))$$

$$= 32.1\%$$

7. We have the following information about a new medical test for diagnosing cancer.

1 / 1 puntos

Before any data are observed, we know that 8% of the population to be tested actually have Cancer.

Of those tested who do have cancer, 90% of them get an accurate test result of "Positive" for cancer.

The other 10% get a false test result of "Negative" for Cancer.

Of the people who do not have cancer, 95% of them get an accurate test result of "Negative" for cancer.

The other 5% get a false test result of "Positive" for cancer.

What is the conditional probability that I have cancer, if I get a "Negative" test result for Cancer?

- 0.9%
- 88.2%
- .80%
- 99.1%

 Correcto

$$p(\text{cancer} \mid \text{negative test}) =$$

$$\frac{p(\text{negative test} \mid \text{Cancer}) p(\text{Cancer})}{p(\text{negative test} \mid \text{cancer}) p(\text{cancer}) + p(\text{negative test} \mid \text{no cancer}) p(\text{no cancer})}$$

$$\frac{(10\%)(8\%)}{(10\%)(8\%) + (95\%)(92\%)}$$

$$\frac{0.8\%}{0.8\% + 87.4\%}$$

$$\frac{0.8\%}{88.2\%}$$

$$= 0.9\%$$

8. An urn contains 50 marbles – 40 blue and 10 white. After 50 draws, exactly 40 blue and 10 white are observed.

1 / 1 puntos

You are not told whether the draw was done “with replacement” or “without replacement.”

What is the probability that the draw was done with replacement?

- 1
- 13.98%
- 12.27%
- 87.73%

 Correcto

$p(40 \text{ blue and } 10 \text{ white} \mid \text{draws without replacement}) = 1$ [this is the only possible outcome when 50 draws are made without replacement]

$p(40 \text{ blue and } 10 \text{ white} \mid \text{draws with replacement})$

$$S = 40$$

$$N = 50$$

$P = .8$ [for draws with replacement] because 40 blue of 50 total means $p(\text{blue}) = 40/50 = .8$

$$\left(\frac{50}{40}\right)(0.8^{40})(0.2^{10})$$

$$= 13.98\%$$

By Bayes' Theorem:

$$p(\text{draws with replacement} \mid \text{observed data}) =$$

$$\frac{13.98\%(.5)}{(13.98\%)(.5)+(1)(.5)}$$

$$= \frac{0.1398}{1.1398}$$

$$= 12.27\%$$

9. According to Department of Customs Enforcement Research: 99% of people crossing into the United States are not smugglers.

1 / 1 puntos

The majority of all Smugglers at the border (65%) appear nervous and sweaty.

Only 8% of innocent people at the border appear nervous and sweaty.

If someone at the border appears nervous and sweaty, what is the probability that they are a Smuggler?

- 8.57%
- 7.92%
- 7.58%
- 92.42%

 Correcto

By
Bayes' Theorem, the answer is

$$\frac{(.65)(.01)}{((.65)(.01) + (.08)(.99))}$$

$$= 7.58\%$$

 ¡Felicitaciones! ¡Aprobaste!

PARA APROBAR: 80 % o más

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CALIFICACIÓN
91,66 %

Probability (basic and Intermediate) Graded Quiz

CALIFICACIÓN DEL ÚLTIMO ENVÍO

91.66%

1. What additional statement, added to the three below, forms a probability distribution?

1 / 1 puntos

- (1) I missed only my first class today
- (2) I missed only my second class today
- (3) I missed both my first and second class today

 Correcto

2. My friend takes 10 cards at random from a 52-card deck, and places them in a box. Then he puts the other 42 cards in a second, identical box. He hands me one of the two boxes and asks me to draw out the top card. What is the probability that the first card I draw will be the Ace of Spades?

1 / 1 puntos

 Correcto

3. I will go sailing today if it does not rain. Are the following two statements Independent or dependent?

1 / 1 puntos

- (1) "I will go sailing today"
- (2) "It will not rain today"

 Correcto

4. The probability that I will go sailing today AND the fair six-sided die will come up even on the next roll is .3.

1 / 1 puntos

If these events are independent, what is the probability that I will go sailing today?

 Correcto

5. I have two coins. One is fair, and has a probability of coming up heads of .5. The second is bent, and has a probability of coming up heads of .75. If I toss each coin once, what is the probability that at least one of the coins will come up tails?

1 / 1 puntos

✓ Correcto

6. What is the probability, when drawing 5 cards from a fair 52-card deck, of drawing a "full house" (three of a kind and a pair) in the form AAABB?

0 / 1 puntos

! Incorrecto

7. If it rains, I do not go sailing. It rains 10% of days; I go sailing 3% of days.

1 / 1 puntos

If it does not rain, what is the (conditional) probability that I go sailing?

Written " $p(\text{I go sailing} \mid \text{it does not rain})$ "?

✓ Correcto

8. I am at my office AND not working 2% of the time. I am at my office 10% of the time. What is the conditional probability that I am not working, if I am at my office?

1 / 1 puntos

✓ Correcto

9. The factory quality control department discovers that the conditional probability of making a manufacturing mistake in its precision ball bearing production is 4% on Tuesday, 4% on Wednesday, 4% on Thursday, 8% on Monday, and 12% on Friday.

1 / 1 puntos

The Company manufactures an equal amount of ball bearings (20%) on each weekday. What is the probability that a defective ball bearing was manufactured on a Friday?

✓ Correcto

10. An Urn contains two white marbles and one black marble. A marble is drawn from the Urn without replacement and put aside without my seeing it. Then a second marble is drawn, and it is white.

1 / 1 puntos

What is the probability that the unknown removed marble is white, and what is the probability that it is black?

✓ Correcto

11. What is the probability, if I flip a fair coin with heads and tails ten times in a row, that I get at least 8 heads? **1 / 1 puntos**

 Correcto

12. Suppose I have either a fair coin or a bent coin, and I don't know which. The bent coin has a 60% probability of coming up heads. **1 / 1 puntos**

I throw the coin ten times and it comes up heads 8 times. What is the probability I have the fair coin vs. the probability I have the bent coin?

Assume at the outset there is an equal (.5,.5) prior probability of either coin.

*Please note that in order to fit the entire formula in the feedback, probability has been abbreviated to "prob."

 Correcto