

HuanHusted_TSA_Competition

Kelsey Husted & Yu Huan

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Time Series Competition

```
knitr::opts_chunk$set(echo = TRUE, tidy.opts=list(width.cutoff=80), tidy=FALSE)
```

```
##Load packages
```

```
library(readxl)
library(dplyr)
library(lubridate)
library(openxlsx)
library(ggplot2)
library(forecast)
library(Kendall)
library(tseries)
library(outliers)
library(tidyverse)
library(smooth)
library(zoo)
library(kableExtra)
```

Data wrangling and processing from 2005-2009

Hourly data was transformed into daily data with aggregate functions and pipes (i.e., tidyverse).

```
#Import data
df <- read_xlsx("./Competition/Data/load.xlsx")

#Wrangle data from hourly to daily
#Wrangling date column 2005 to 2009
df_daily <- df %>%
  mutate( Date = ymd(date)) %>%
  filter(Date < '2010-01-01')

#removing no numeric columns so rowMeans() functino will work
df_dailyV2 <- df %>%
  mutate( Date = ymd(date)) %>%
  filter(Date < '2010-01-01') %>%
  select(3:26)

#Creating daily data
df_processed <- df_dailyV2 %>%
  mutate(rowMeans(df_dailyV2)) %>%
  rename(Daily_data = "rowMeans(df_dailyV2)") %>%
```

```

select(25)

#Combining date and daily data
date <- df_daily[,2]
df_processed <- cbind(date, df_processed)

nobs = nrow(df_daily)

```

Data wrangling and processing from 2005-2010

The data needs to be formatted to include 2010 as well since the objective is to forecast for 2011. Instead of making two separate datasets, I should use the `window()` function for future reference.

```

#Wrangle data from hourly to daily
#Wrangling date column 2005 to 2010
#removing no numeric columns so rowMeans() function will work
df_daily2010 <- df %>%
  mutate( Date = ymd(date)) %>%
  select(3:26)

#Creating daily data
df_processed2010 <- df_daily2010 %>%
  mutate(rowMeans(df_daily2010)) %>%
  rename(Daily_data = "rowMeans(df_daily2010)") %>%
  select(25)

#Combining data and daily data
date <- df[,2]
df_processed2010 <- cbind(date, df_processed2010)

nobs2010 = nrow(df_processed2010)

```

Time series object transformation

```

#ts transformation 2005 to 2009
ts_daily <- msts(df_processed$Daily_data,
  seasonal.periods=c(7,365.25),
  start=c(2005, 01, 01))

#ts transformation 2005 to 2010
ts_daily2010 <- msts(df_processed2010$Daily_data,
  seasonal.periods=c(7,365.25),
  start=c(2005, 01, 01))

```

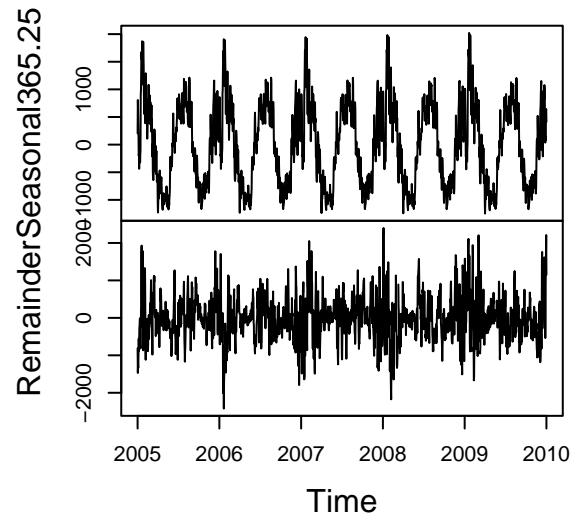
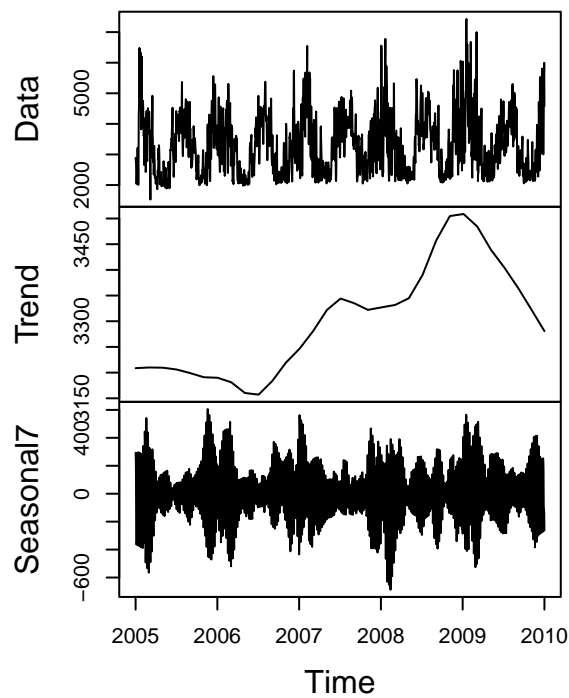
Time series decomposition and plot

```

#Decompose time series
ts_decompose <- ts_daily %>%
  mstl()
plot(ts_decompose)

```

ts_decompose



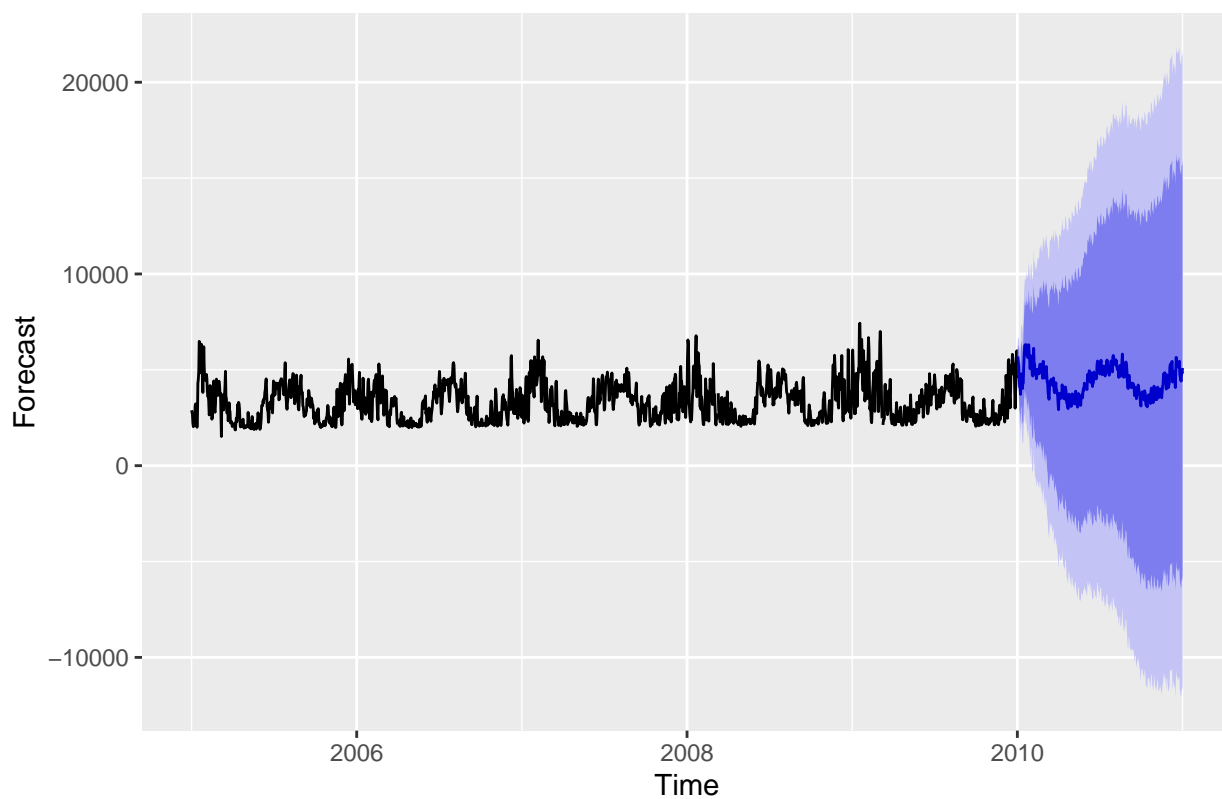
##

Model 1 STL + ETS: Forecast 2010

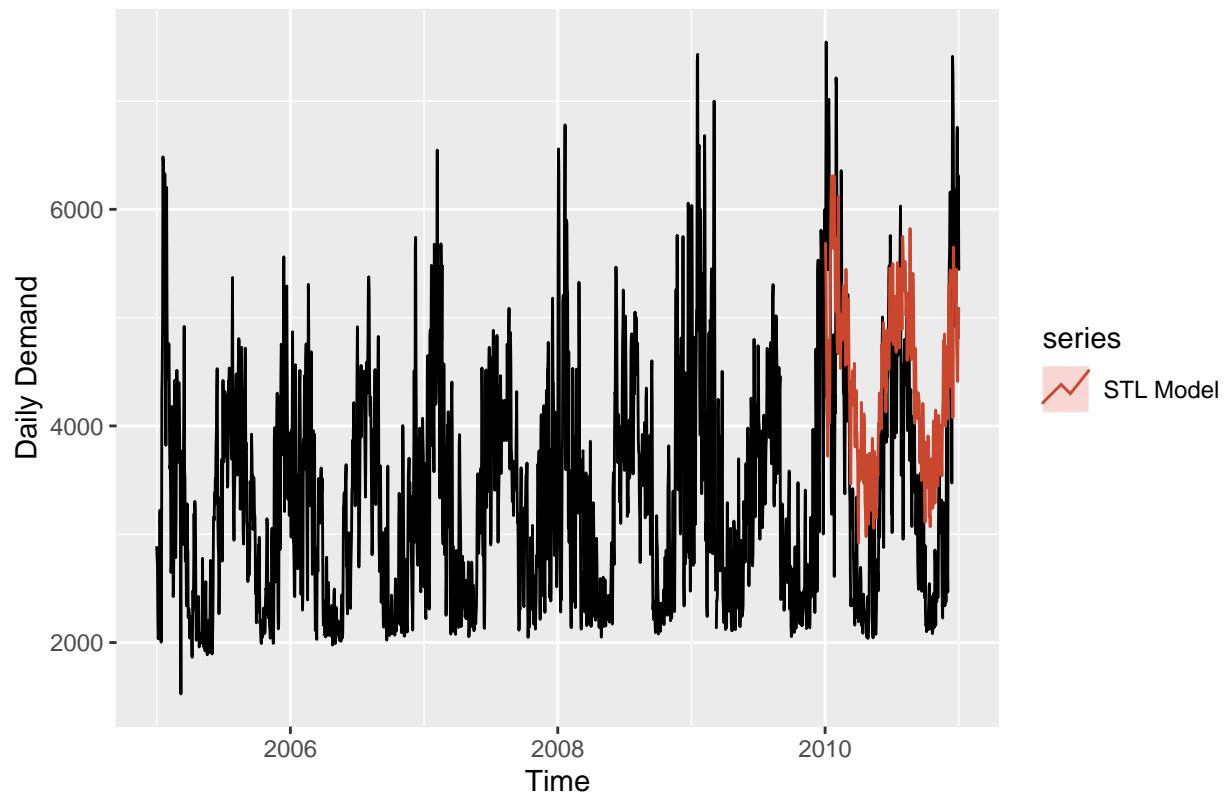
```
#Fit and forecast STL model
ETS_model <- stlf(ts_daily,h=365)

#Plot forecasting
autoplot(ETS_model) + ylab("Forecast")
```

Forecasts from STL + ETS(A,N,N)

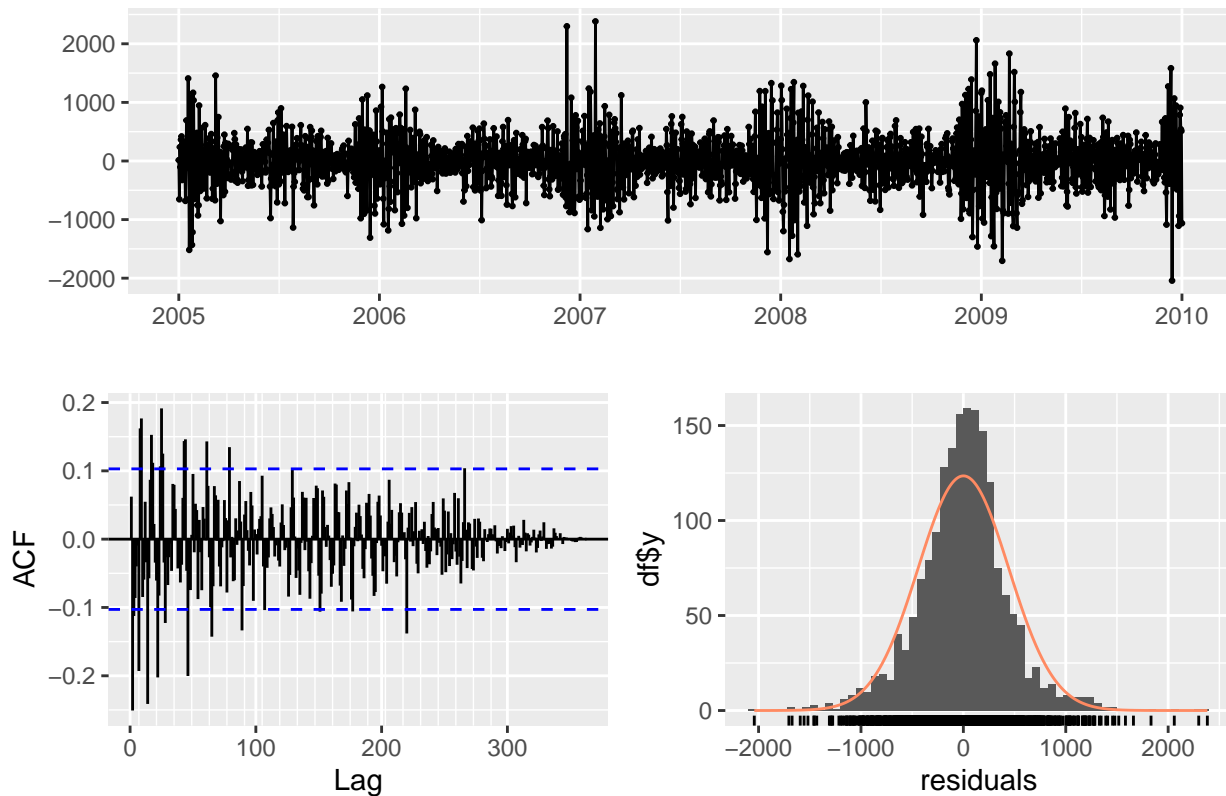


```
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(ETS_model, series="STL Model",PI=FALSE) +
  ylab("Daily Demand")
```



```
#Plot the residuals  
checkresiduals(ETS_model)
```

Residuals from STL + ETS(A,N,N)



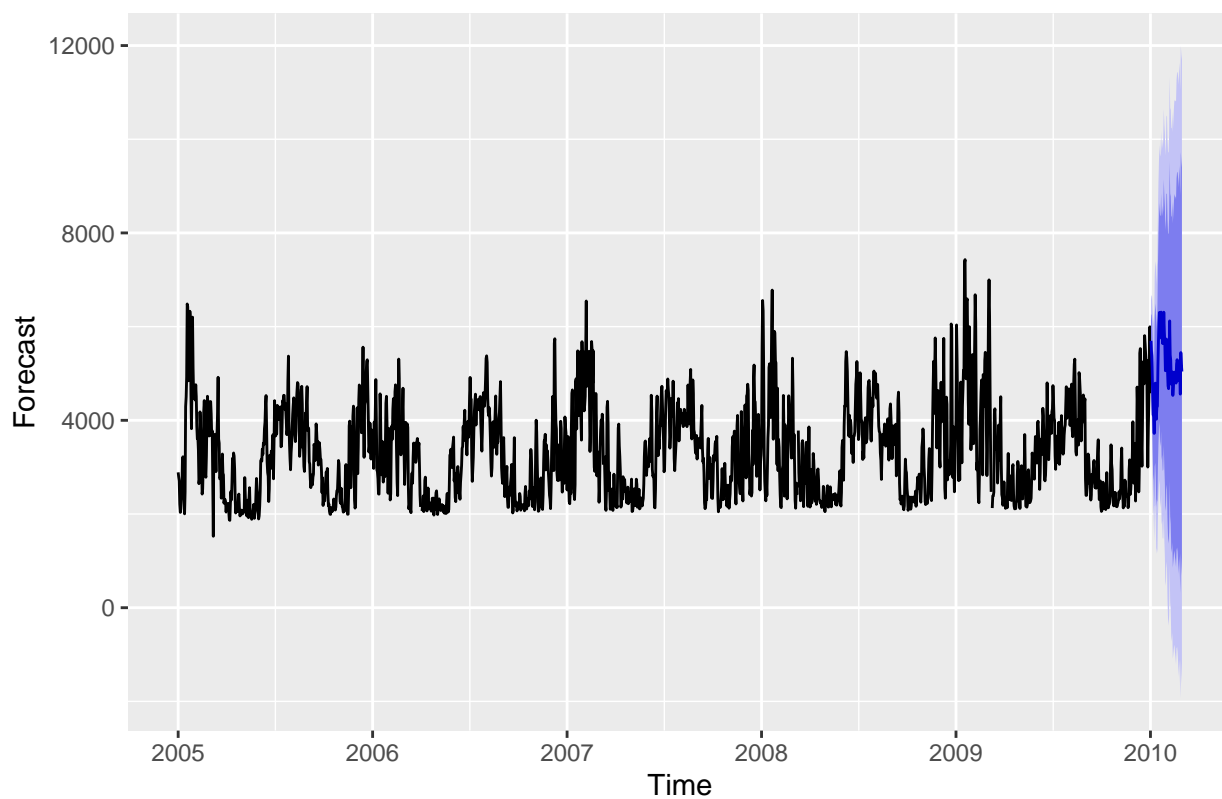
```
##
##  Ljung-Box test
##
## data:  Residuals from STL +  ETS(A,N,N)
## Q* = 1309.7, df = 363, p-value < 2.2e-16
##
## Model df: 2.    Total lags used: 365
#Check accuracy of model
n_for <- 365
observed <- df_processed[(nobs-n_for+1):nobs, "Daily_data"]
ETS_scores <- accuracy(ETS_model$mean,observed)
print(ETS_scores)

##              ME      RMSE      MAE      MPE      MAPE
## Test set -984.5201 1210.625 1079.332 -35.24753 36.80666
# Changed forecast

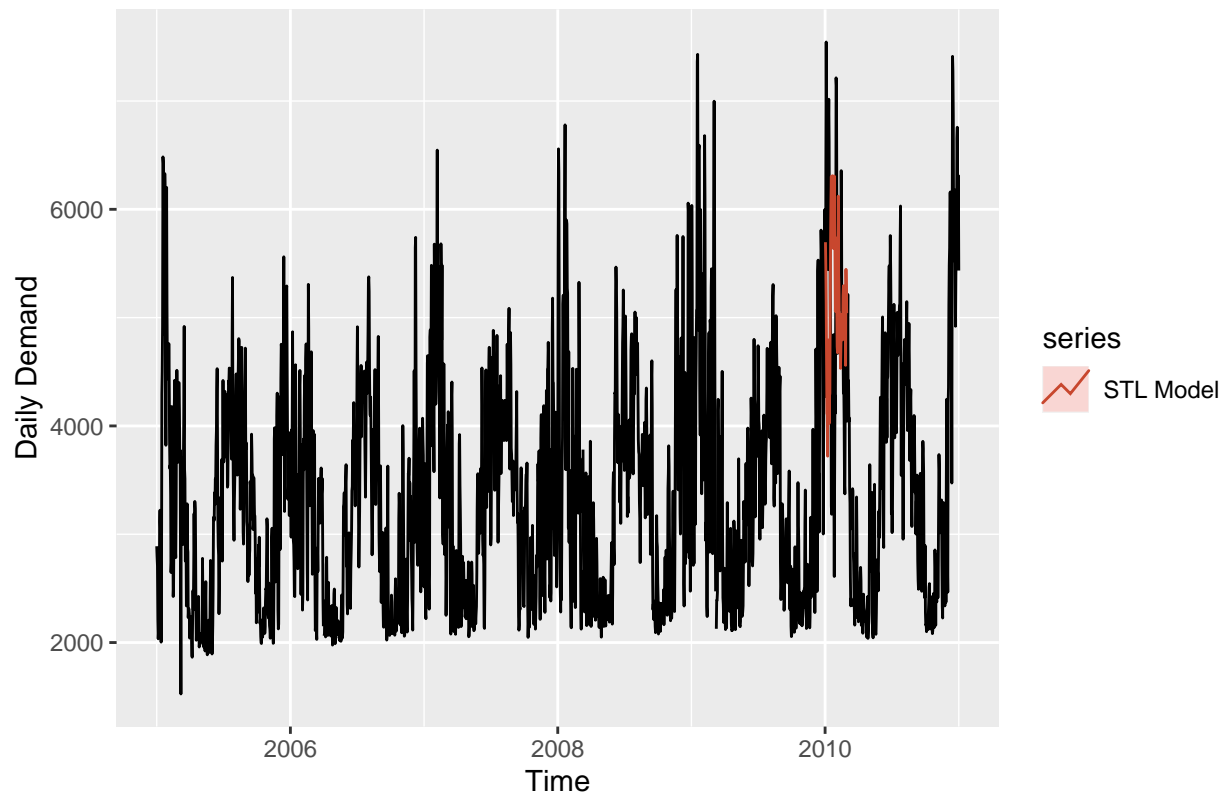
#Fit and forecast STL model
ETS_model <- stlf(ts_daily,h=59)

#Plot forecasting
autoplot(ETS_model) + ylab("Forecast")
```

Forecasts from STL + ETS(A,N,N)

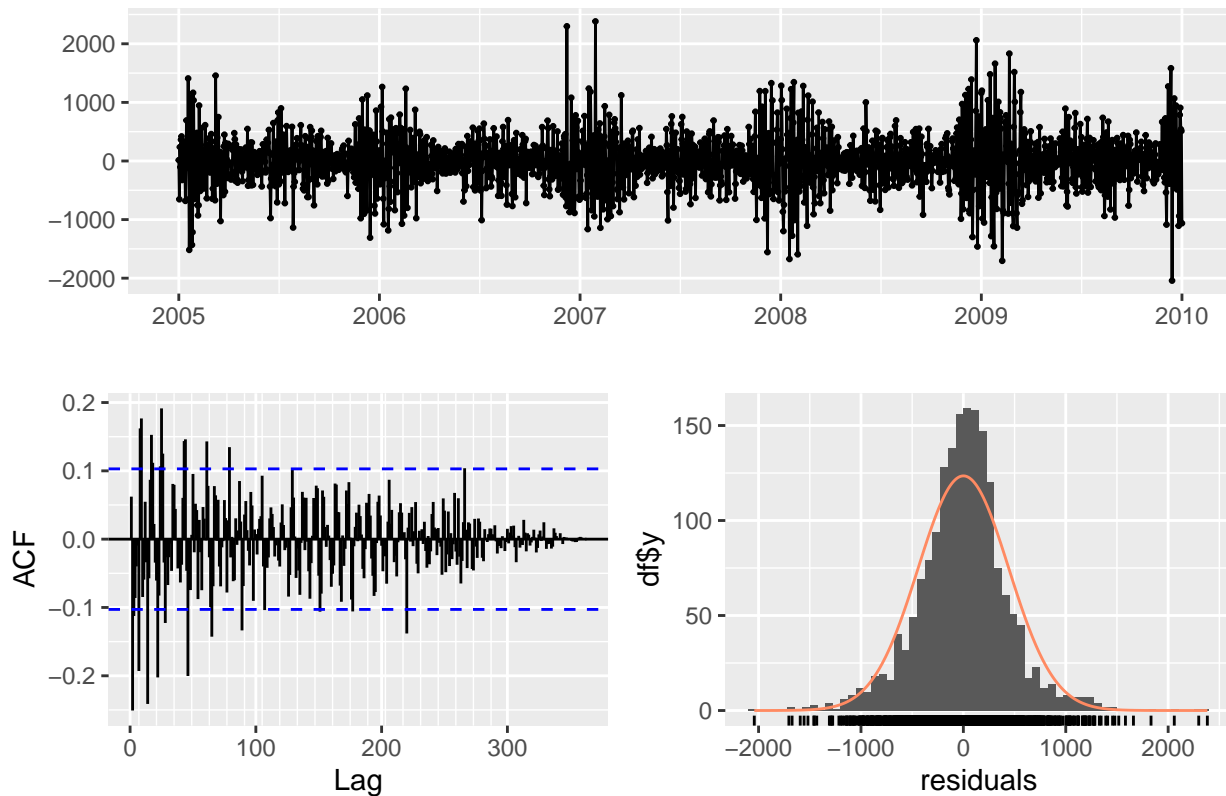


```
#Plot model + observed data  
autoplot(ts_daily2010) +  
  autolayer(ETS_model, series="STL Model",PI=FALSE) +  
  ylab("Daily Demand")
```



```
#Plot the residuals  
checkresiduals(ETS_model)
```


Residuals from STL + ETS(A,N,N)



```
##
##  Ljung-Box test
##
## data:  Residuals from STL +  ETS(A,N,N)
## Q* = 1309.7, df = 363, p-value < 2.2e-16
##
## Model df: 2.    Total lags used: 365
#Check accuracy of model
n_for <- 59
observed <- df_processed2010[1827:1885, "Daily_data"]
ETS_scores <- accuracy(ETS_model$mean,observed)
print(ETS_scores)

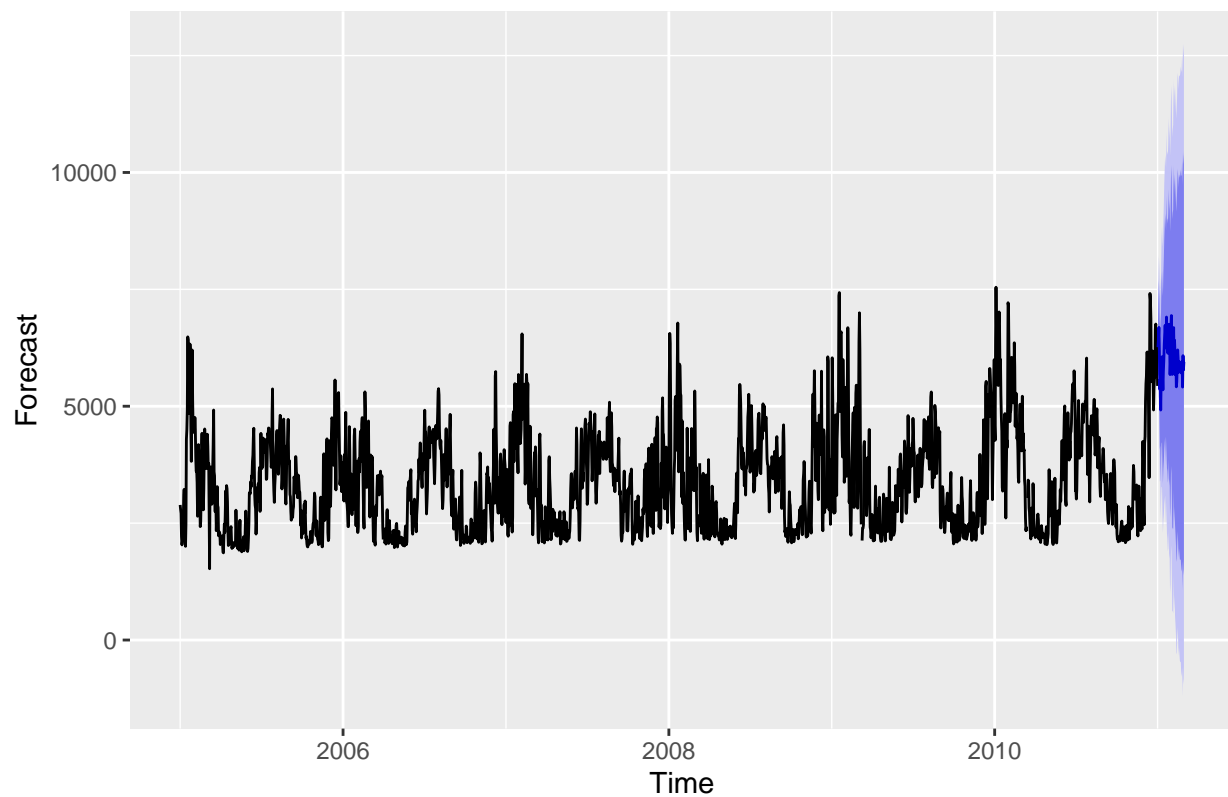
##              ME      RMSE      MAE      MPE      MAPE
## Test set -103.0303 1547.348 1280.656 -9.574082 28.27524
```

Model 1 STL + ETS: Forecast 2011

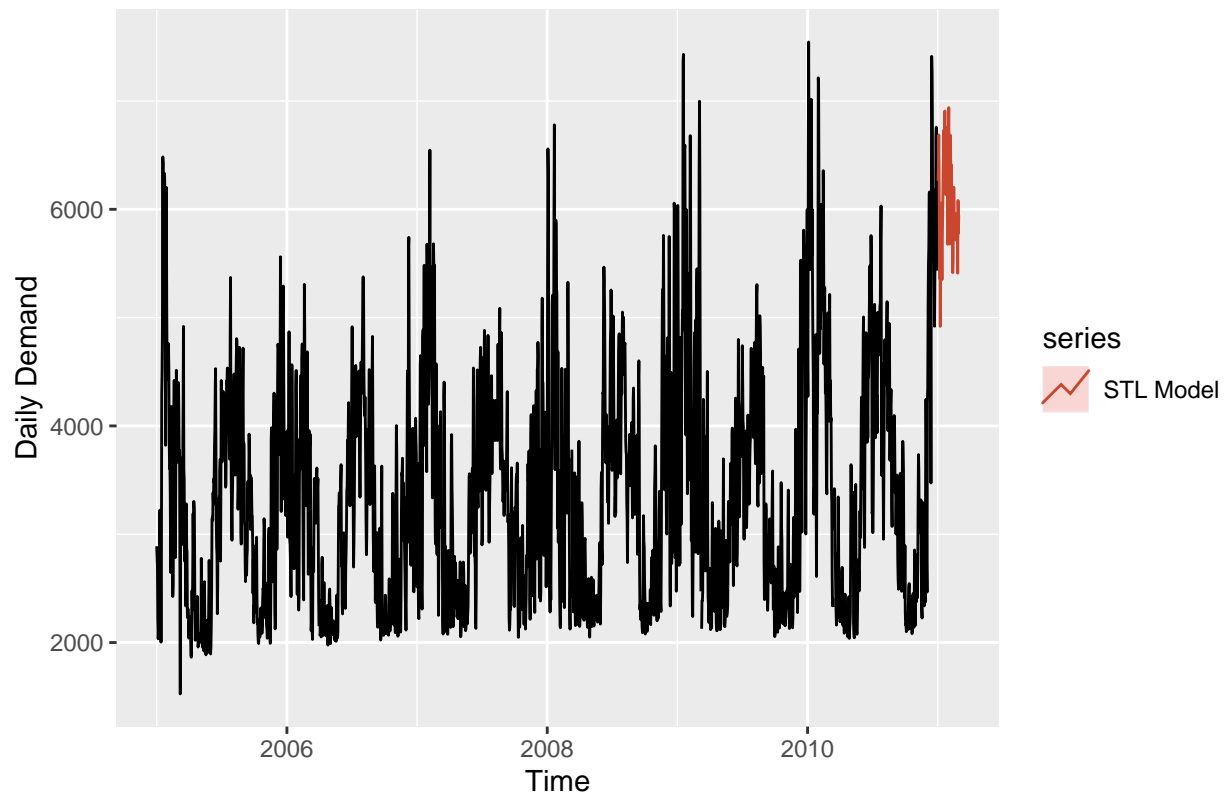
```
#Fit and forecast STL model January 1st to February 28th 2011
ETS_model2011 <- stlf(ts_daily2010,h=59)

#Plot forecasting
autoplot(ETS_model2011) + ylab("Forecast")
```

Forecasts from STL + ETS(A,N,N)



```
#Plot model + observed data  
autoplot(ts_daily2010) +  
  autolayer(ETS_model2011, series="STL Model",PI=FALSE) +  
  ylab("Daily Demand")
```



```
#Check accuracy of model
n_for <- 59
observed <- df_processed2010[(nobs-n_for+1):nobs, "Daily_data"]
ETS_scores_for <- accuracy(ETS_model2011$mean,observed)
print(ETS_scores_for)
```

```
##           ME      RMSE      MAE      MPE      MAPE
## Test set -2528.13 2846.706 2535.511 -90.47756 90.60064
```

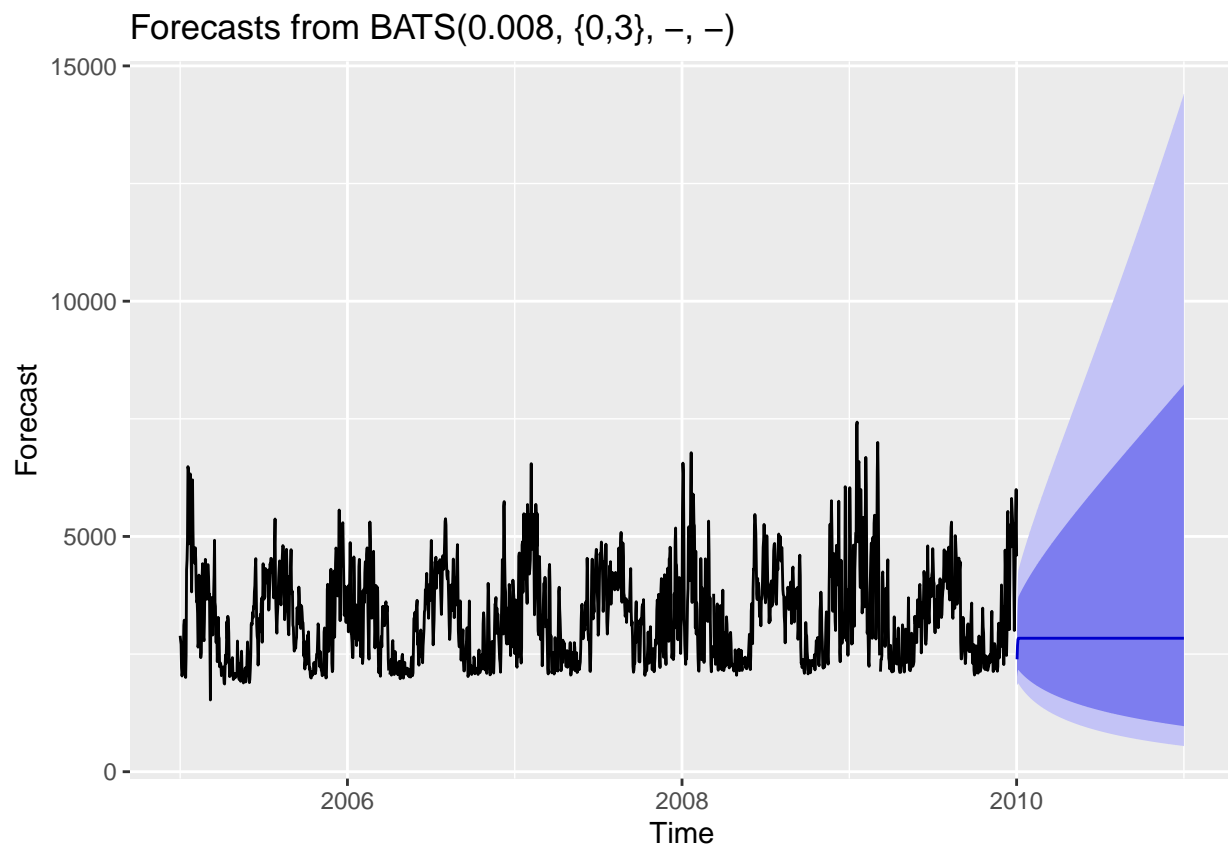
Model 2 TBATS: Forecast 2010

The model looks like a really bad fit visually and will not be used to forecast for 2011.

```
#Fit and forecast TBATS model
TBATS_model <- tbats(ts_daily)

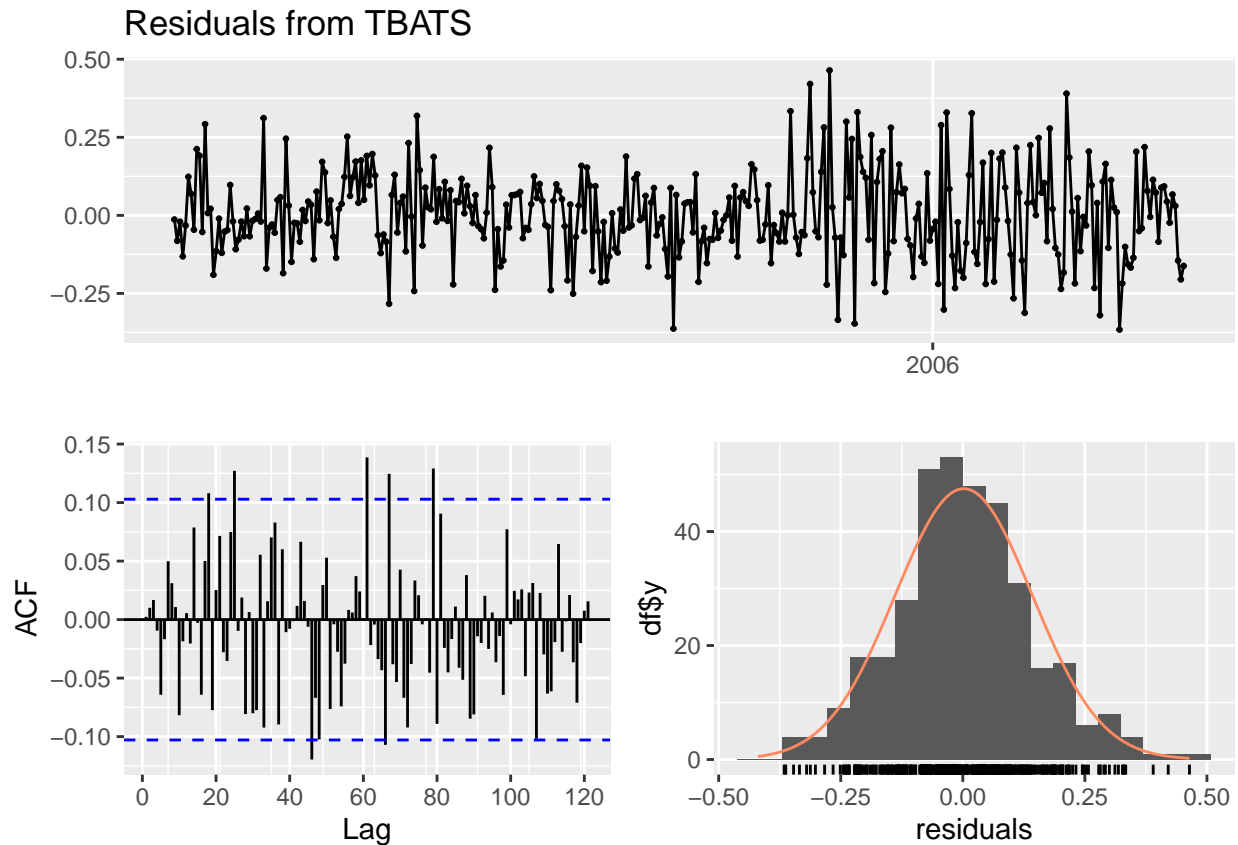
#forecast
TBATS_for <- forecast(TBATS_model,h=365)

#Plot forecasting
autoplot(TBATS_for) + ylab("Forecast")
```

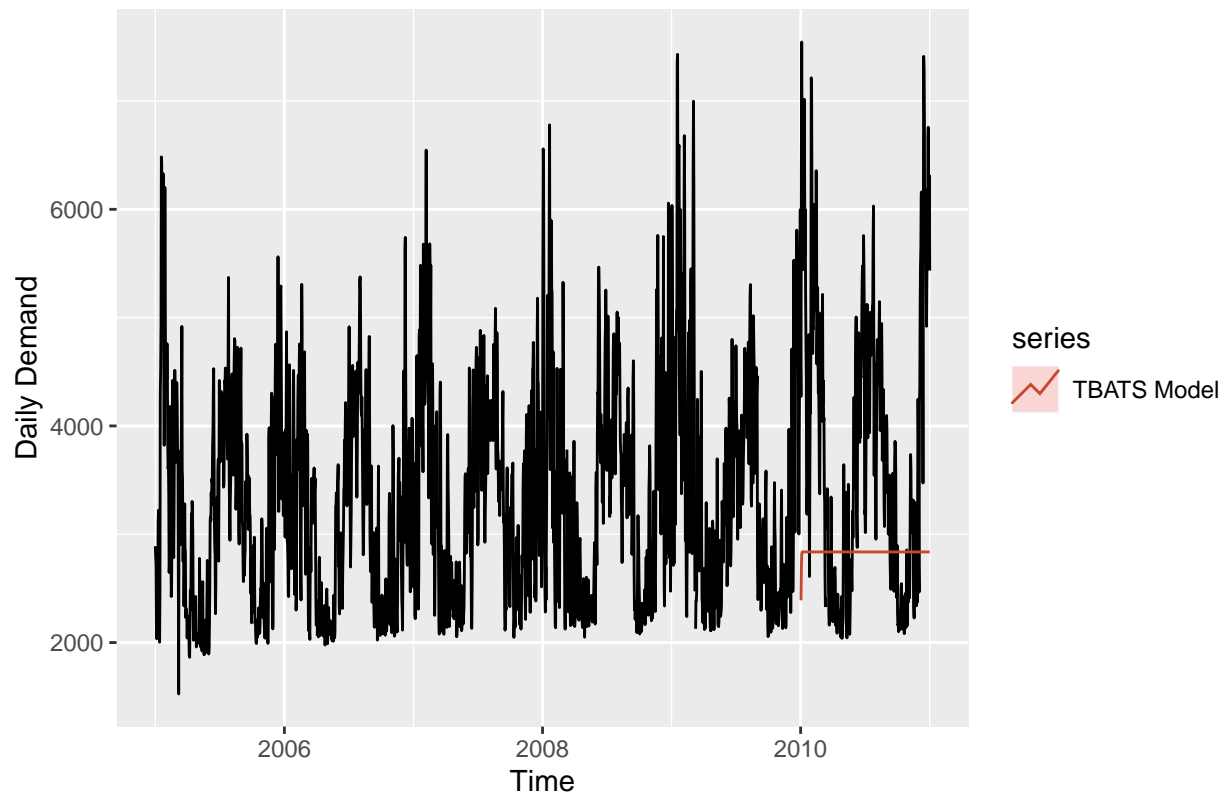


```
#Plot the residuals
```

```
checkresiduals(TBATS_model)
```



```
##
##  Ljung-Box test
##
## data:  Residuals from TBATS
## Q* = 105.04, df = 68, p-value = 0.002646
##
## Model df: 5.    Total lags used: 73
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(TBATS_for, series="TBATS Model",PI=FALSE) +
  ylab("Daily Demand")
```



```
#Check accuracy of model
n_for <- 365
observed <- df_processed[(nobs-n_for+1):nobs, "Daily_data"]
TBATS_scores <- accuracy(TBATS_for$mean,observed)
print(TBATS_scores)
```

```
##           ME      RMSE      MAE      MPE      MAPE
## Test set 613.9492 1258.164 921.0355 10.07795 23.5087
```

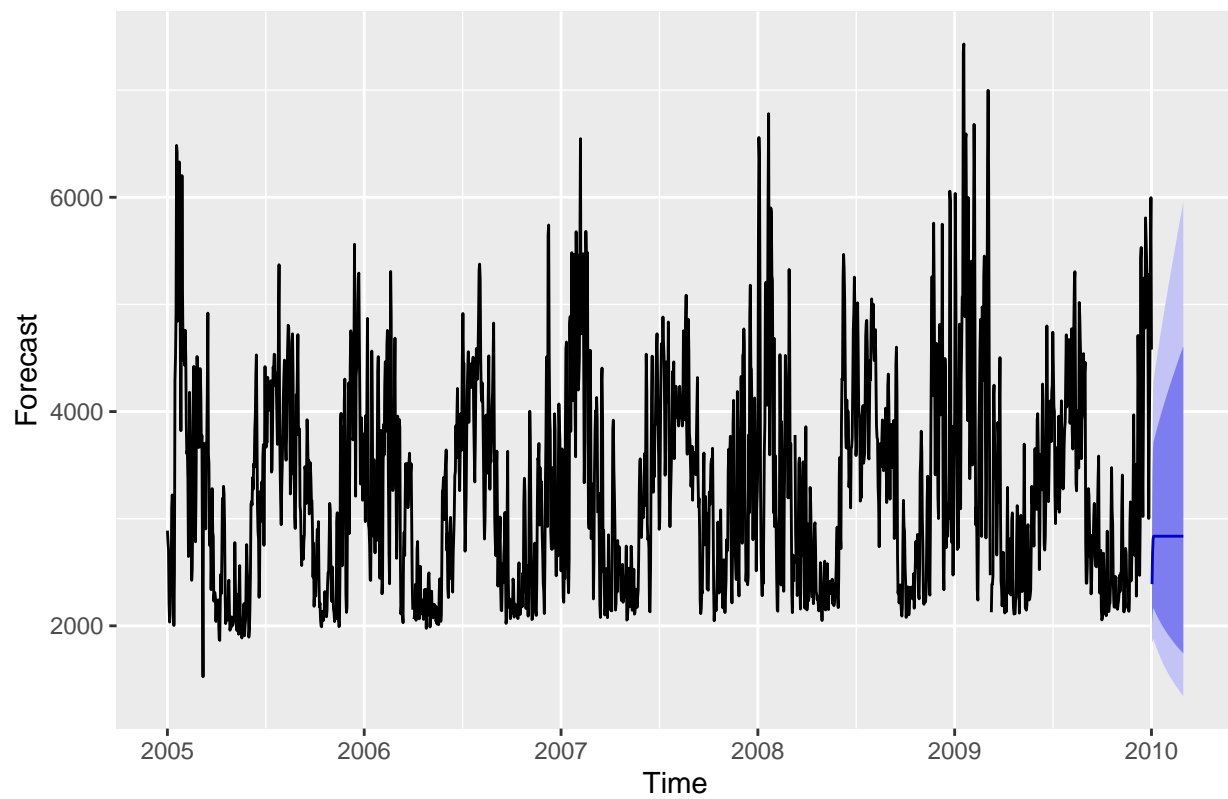
```
# Changed version
```

```
#Fit and forecast TBATS model
TBATS_model <- tbats(ts_daily)
```

```
#forecast
TBATS_for <- forecast(TBATS_model,h=59)
```

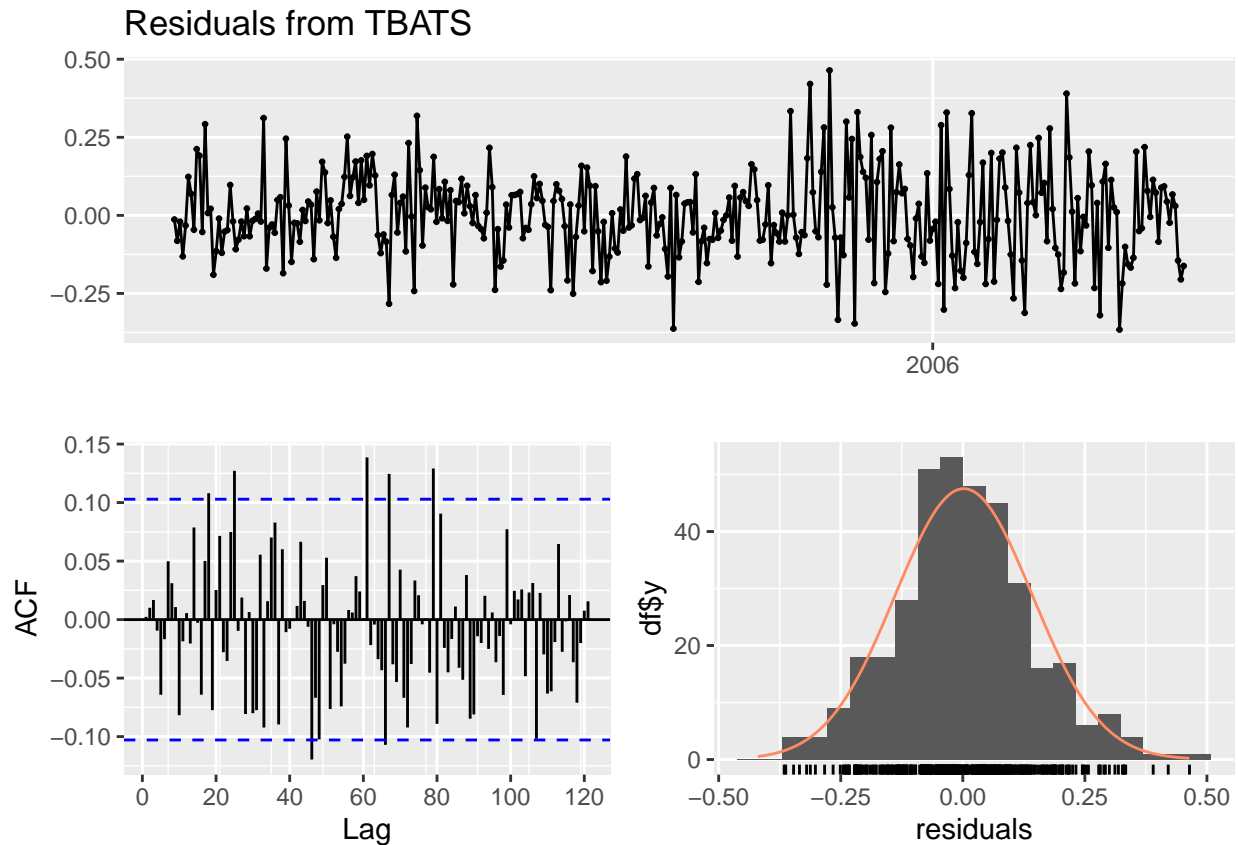
```
#Plot forecasting
autoplot(TBATS_for) + ylab("Forecast")
```

Forecasts from BATS(0.008, {0,3}, -, -)

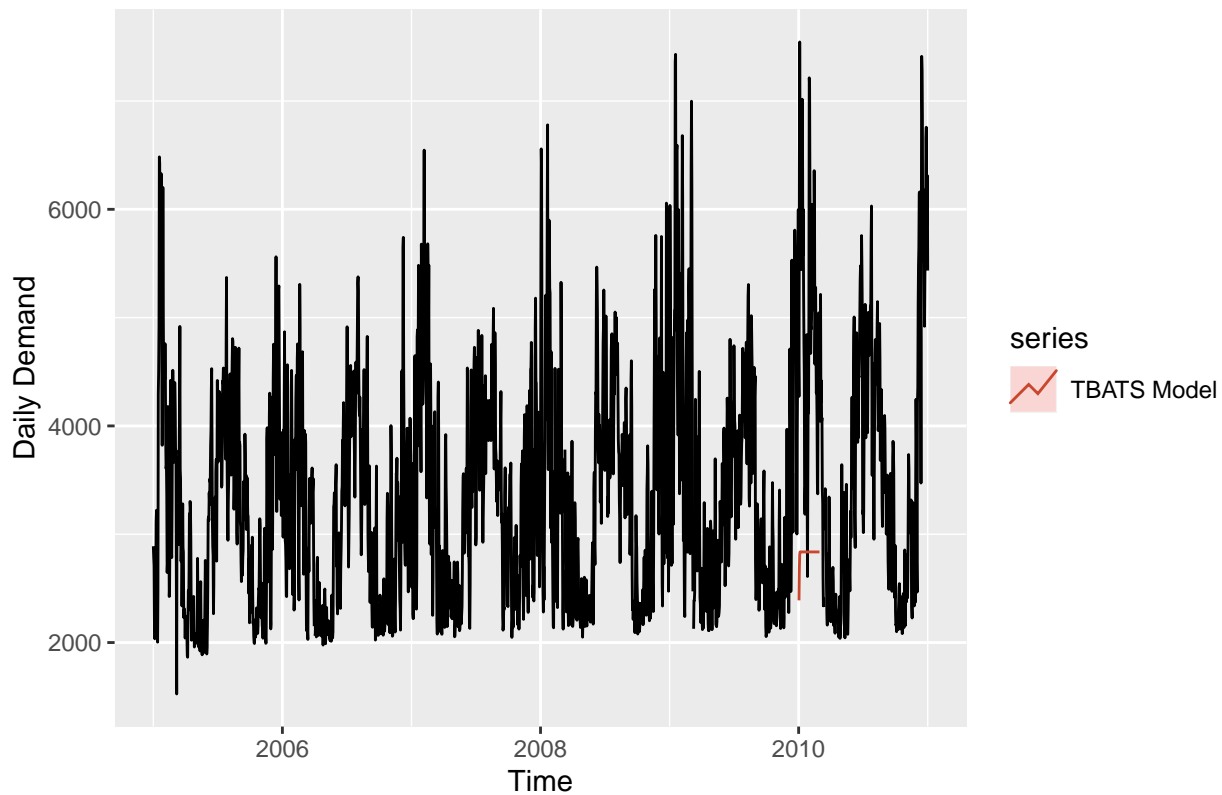


```
#Plot the residuals
```

```
checkresiduals(TBATS_model)
```



```
##
##  Ljung-Box test
##
## data:  Residuals from TBATS
## Q* = 105.04, df = 68, p-value = 0.002646
##
## Model df: 5.    Total lags used: 73
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(TBATS_for, series="TBATS Model",PI=FALSE) +
  ylab("Daily Demand")
```

```
#Check accuracy of model
n_for <- 59
observed <- df_processed2010[1827:1885, "Daily_data"]
TBATS_scores <- accuracy(TBATS_for$mean,observed)
print(TBATS_scores)
```

```
##              ME      RMSE      MAE      MPE      MAPE
## Test set 2226.34 2499.097 2234.019 40.94677 41.24095
```

Model 2 TBATS: Forecast 2011

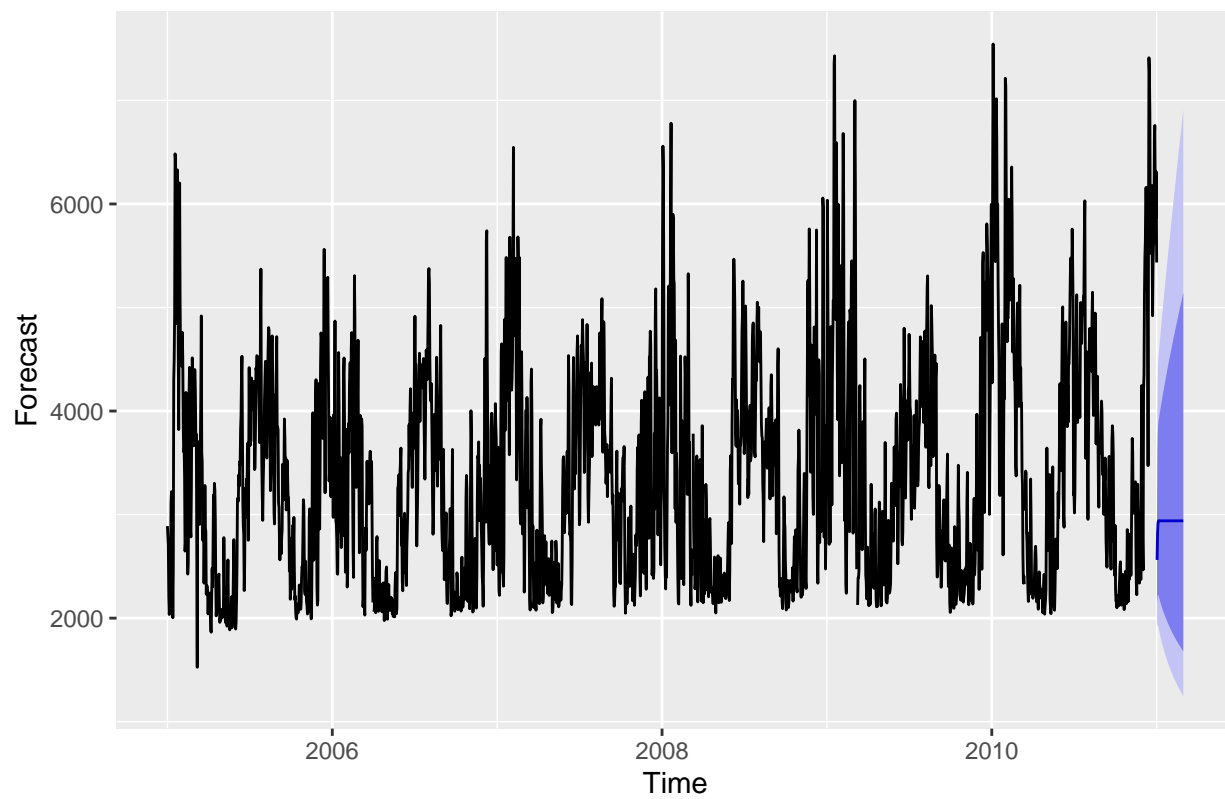
```
#Fit and forecast TBATS model
TBATS_model2011 <- tbats(ts_daily2010)

## Warning in tbats(ts_daily2010): Missing values encountered. Using longest
## contiguous portion of time series

#forecast
TBATS_for2011 <- forecast(TBATS_model2011,h=59)

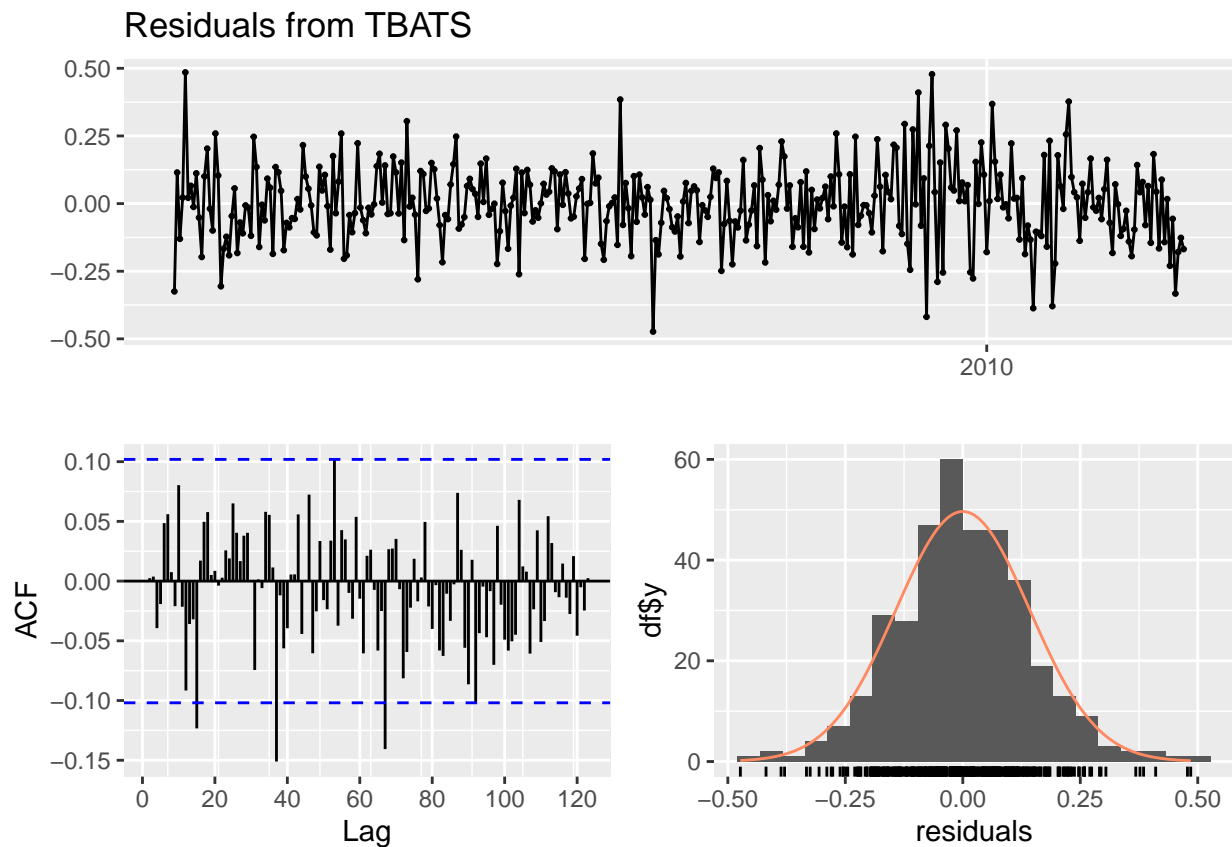
#Plot forecasting
autoplot(TBATS_for2011) + ylab("Forecast")
```

Forecasts from BATS(0.003, {2,1}, -, -)

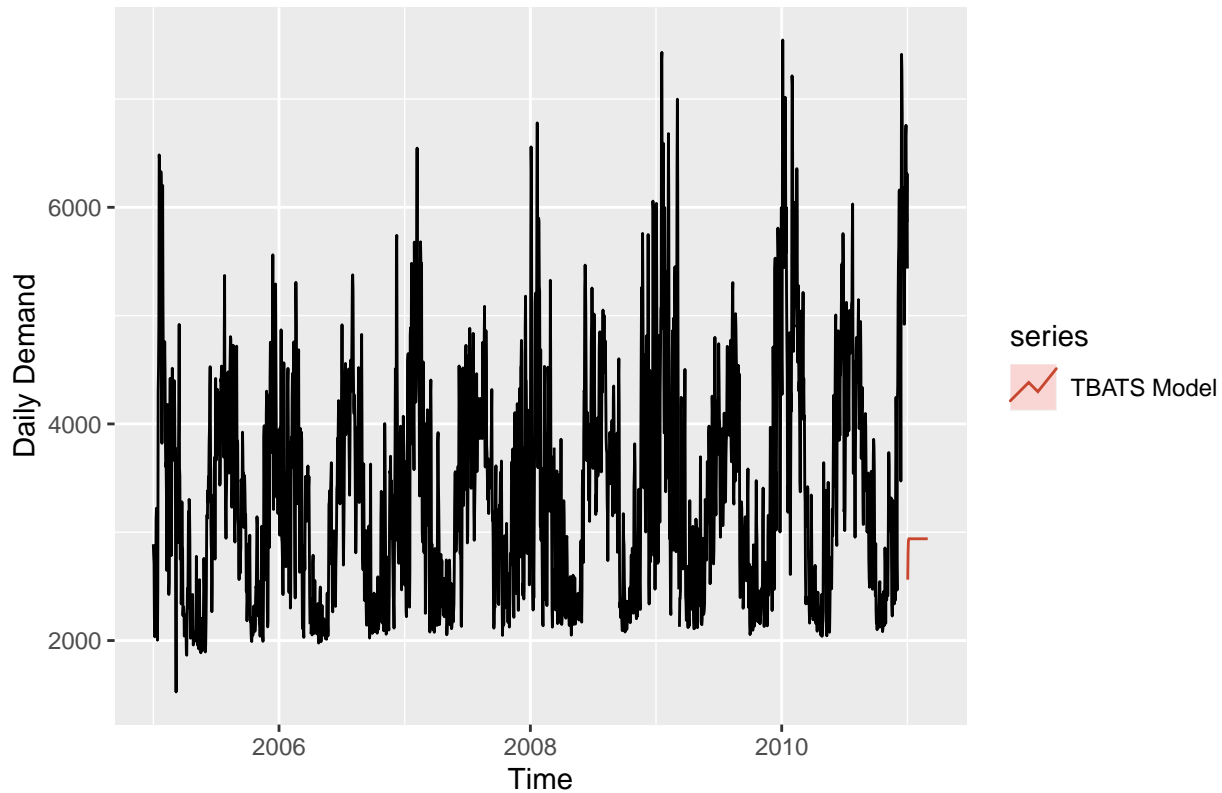


#Plot the residuals

```
checkresiduals(TBATS_model2011)
```



```
##
##  Ljung-Box test
##
## data:  Residuals from TBATS
## Q* = 73.551, df = 69, p-value = 0.3315
##
## Model df: 5.    Total lags used: 74
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(TBATS_for2011, series="TBATS Model",PI=FALSE) +
  ylab("Daily Demand")
```



```
#Check accuracy of model
n_for <- 59
observed <- df_processed2010[(nobs-n_for+1):nobs, "Daily_data"]
TBATS_scores_for <- accuracy(TBATS_for$mean,observed)
print(TBATS_scores_for)
```

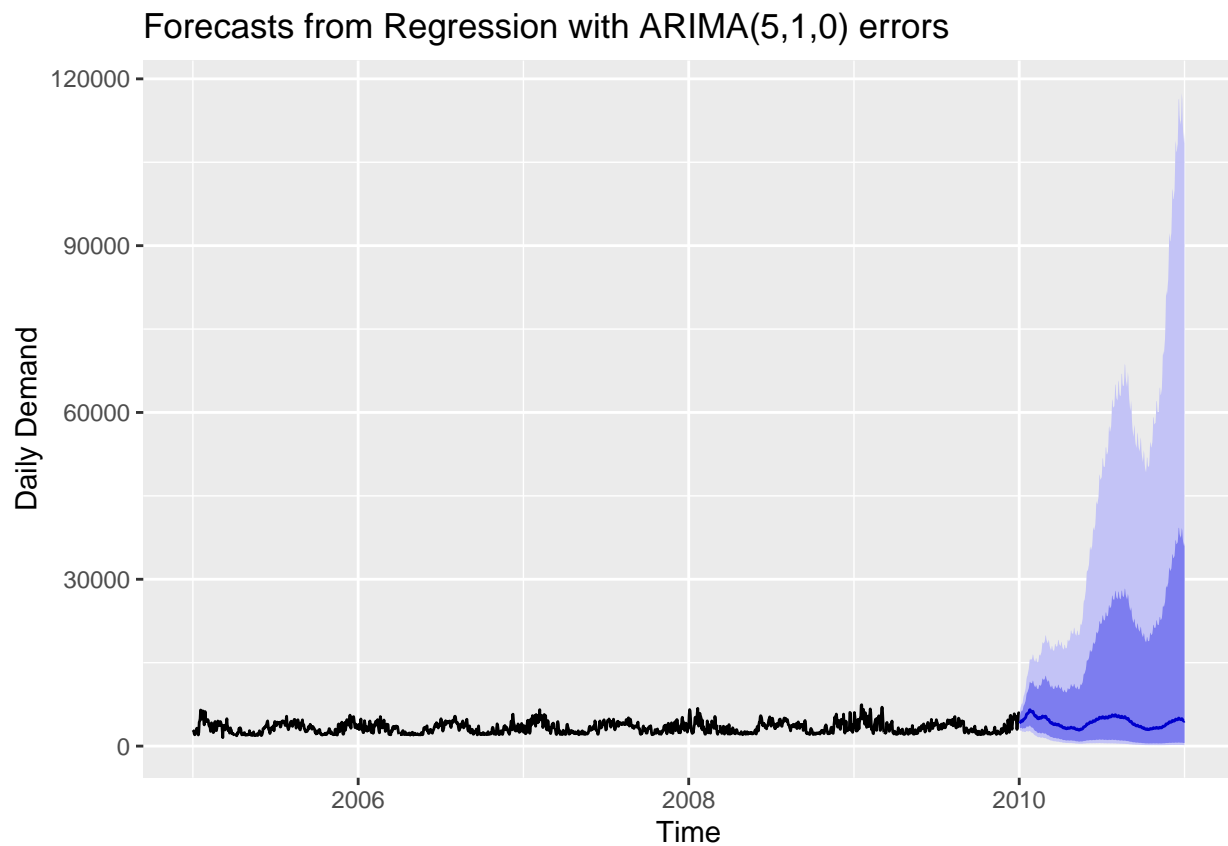
```
##              ME      RMSE      MAE      MPE      MAPE
## Test set 681.5893 1327.303 964.6684 11.34867 23.42342
```

Model 3 ARIMA + FOURIER terms: Forecast 2010

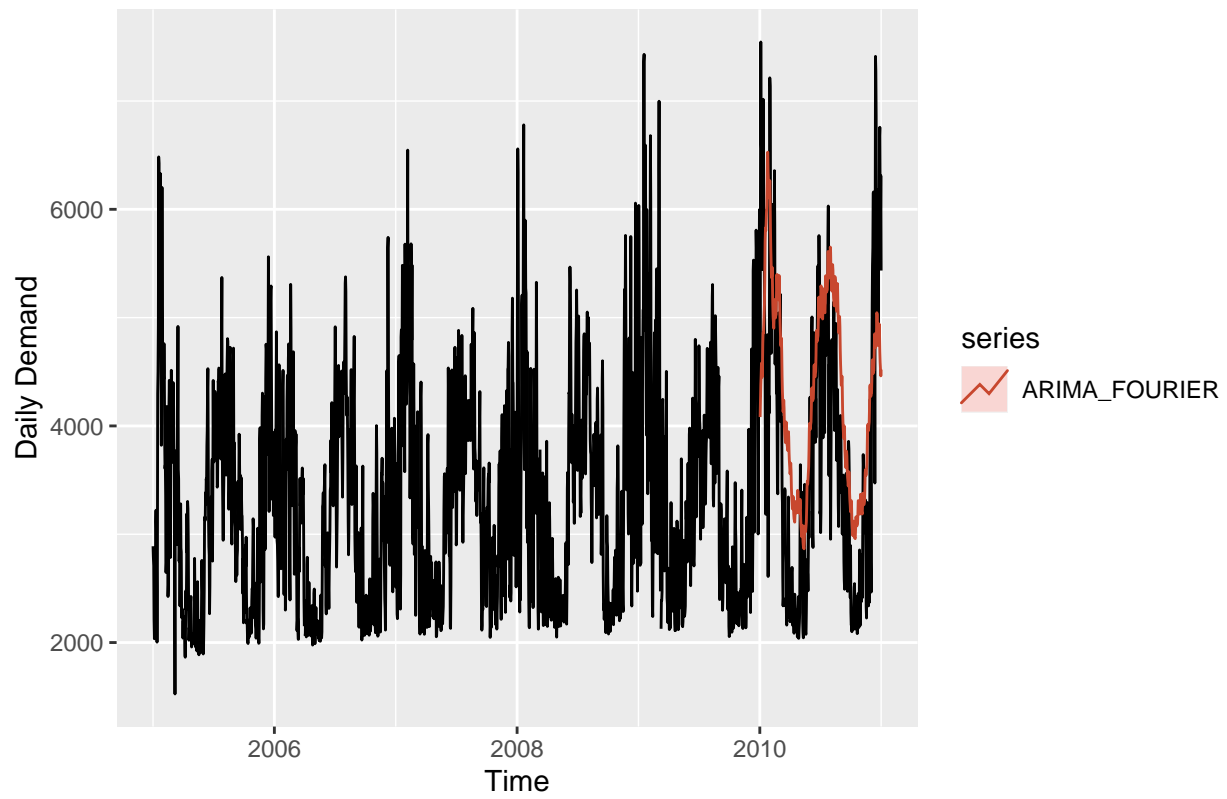
```
#Fit and forecast TBATS model
ARIMA_Four_model <- auto.arima(ts_daily,
                               seasonal=FALSE,
                               lambda=0,
                               xreg=fourier(ts_daily,
                                             K=c(2,12))
                               )

#Forecast
ARIMA_Four_for <- forecast(ARIMA_Four_model,
                           xreg=fourier(ts_daily,
                                         K=c(2,12),
                                         h=365),
                           h=365
                           )

#Plot forecasting results
autoplot(ARIMA_Four_for) + ylab("Daily Demand")
```

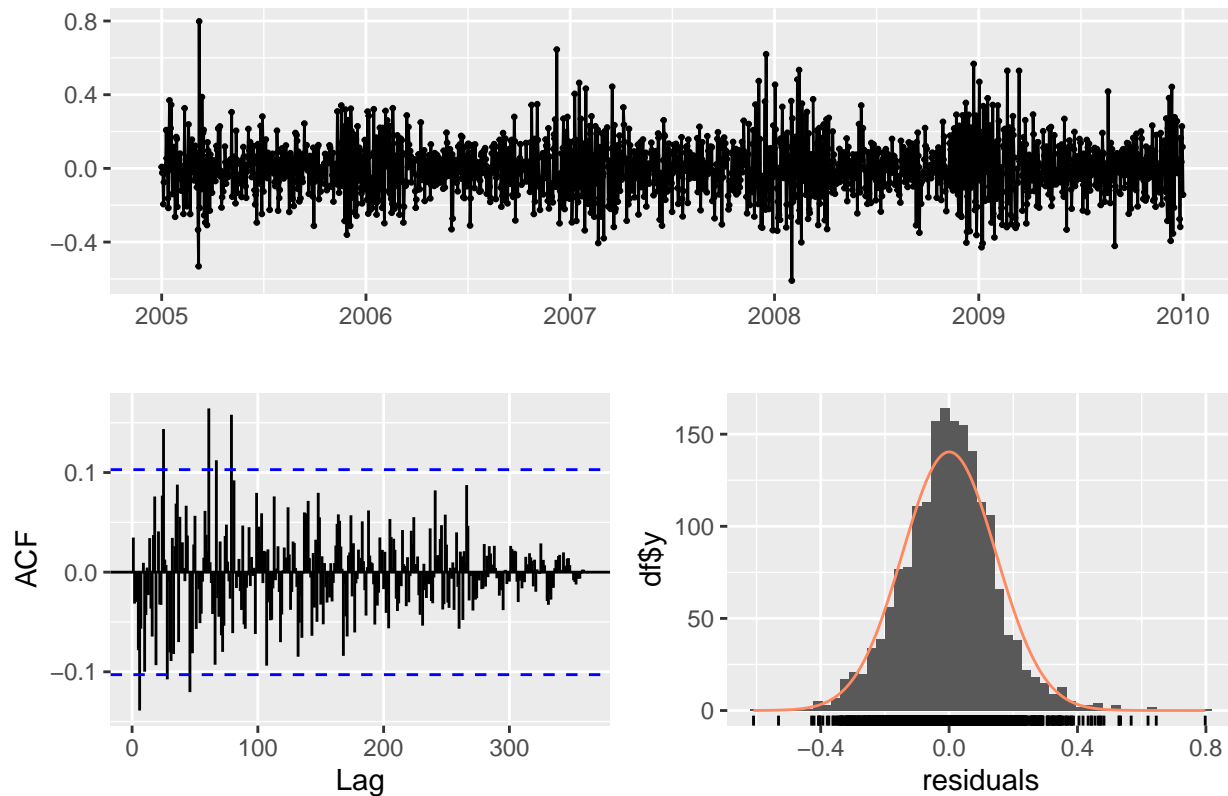


```
#Plot model + observed data  
autoplot(ts_daily2010) +  
  autolayer(ARIMA_Four_for, series="ARIMA_FOURIER",PI=FALSE) +  
  ylab("Daily Demand")
```



```
# Plot the residuals  
checkresiduals(ARIMA_Four_model)
```

Residuals from Regression with ARIMA(5,1,0) errors



```
##
##  Ljung-Box test
##
## data:  Residuals from Regression with ARIMA(5,1,0) errors
## Q* = 462.43, df = 360, p-value = 0.0002078
##
## Model df: 5.    Total lags used: 365
#Check accuracy of model
n_for <- 365
observed <- df_processed[(nobs-n_for+1):nobs, "Daily_data"]
ARIMA_Four_scores <- accuracy(ARIMA_Four_for$mean,observed)
print(ARIMA_Four_scores)
```

```
##              ME      RMSE      MAE      MPE      MAPE
## Test set -853.8232 1158.956 991.685 -30.4006 32.76586
```

Changed version

```
ARIMA_Four_model <- auto.arima(ts_daily,
                               seasonal=FALSE,
                               lambda=0,
                               xreg=fourier(ts_daily,
                                             K=c(2,12))
                               )
```

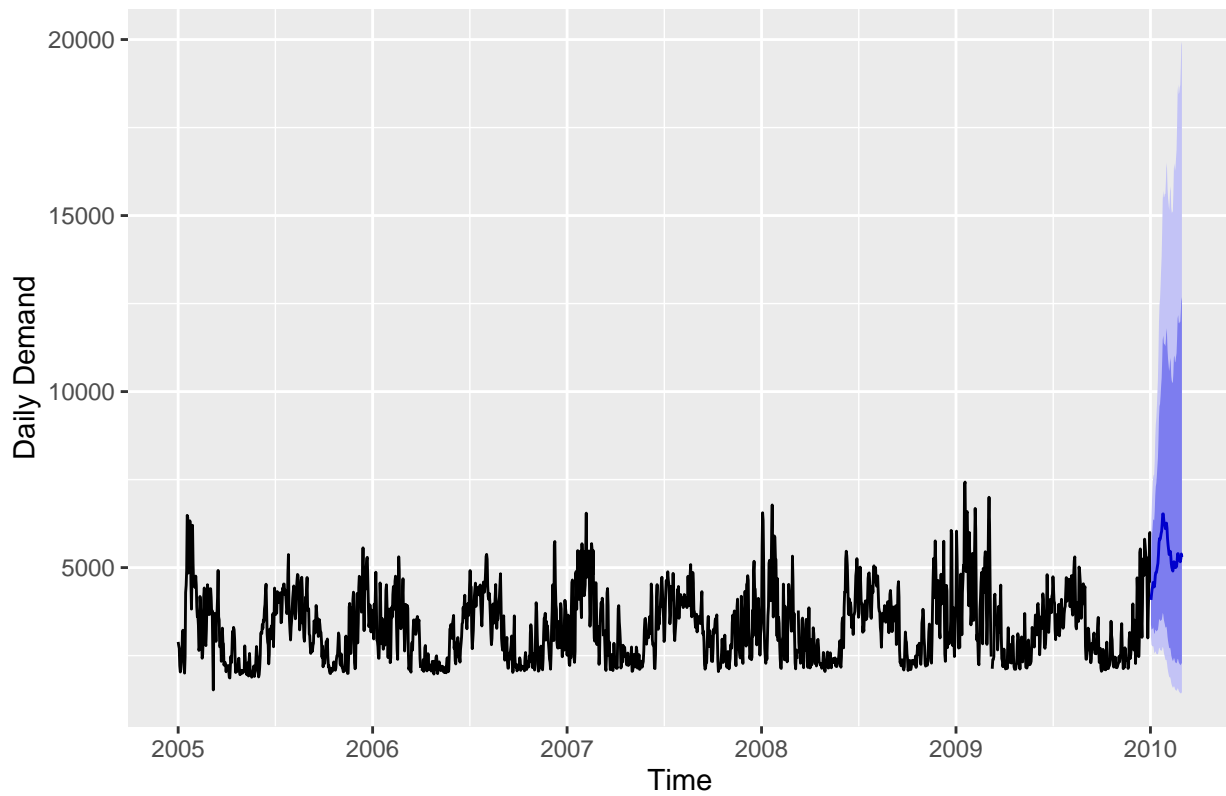
#Forecast

```
ARIMA_Four_for <- forecast(ARIMA_Four_model,
```

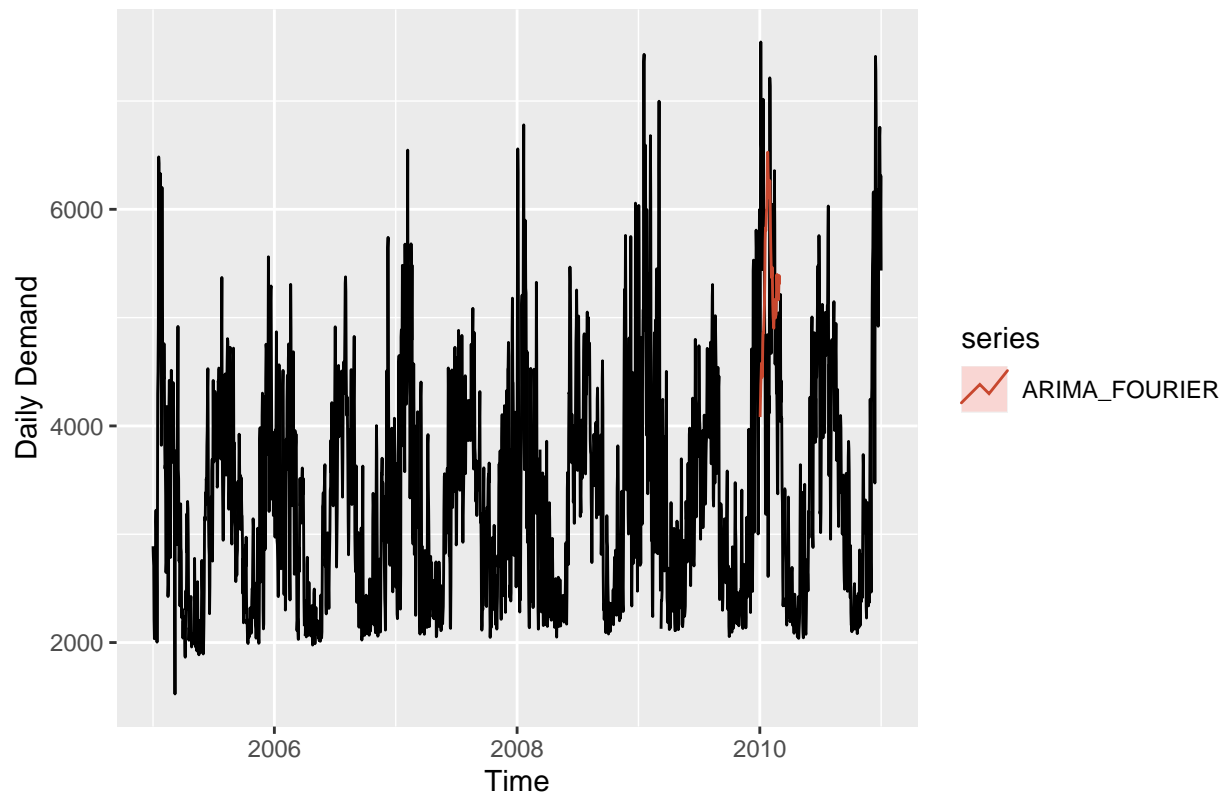
```
xreg=fourier(ts_daily,
              K=c(2,12),
              h=59),
)
```

```
#Plot forecasting results
autoplot(ARIMA_Four_for) + ylab("Daily Demand")
```

Forecasts from Regression with ARIMA(5,1,0) errors

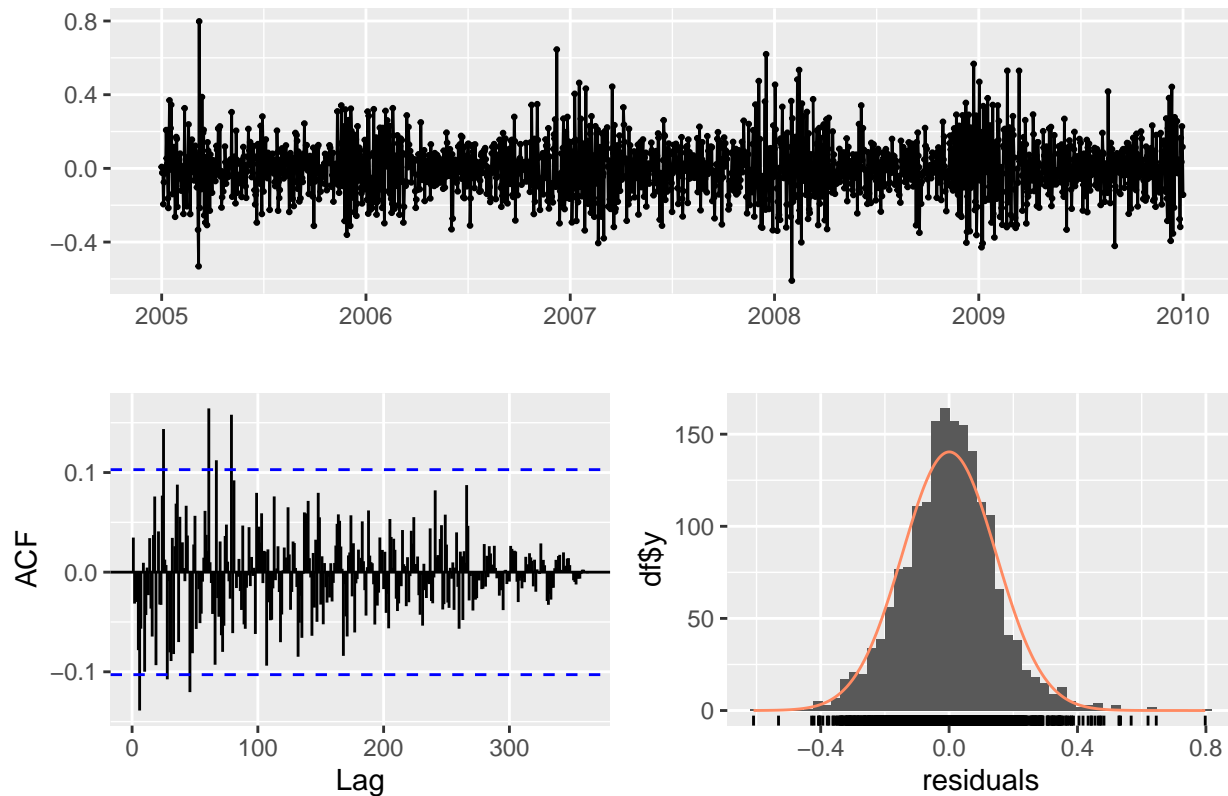


```
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(ARIMA_Four_for, series="ARIMA_FOURIER", PI=FALSE) +
  ylab("Daily Demand")
```

```
# Plot the residuals  
checkresiduals(ARIMA_Four_model)
```

Residuals from Regression with ARIMA(5,1,0) errors



```
##
##  Ljung-Box test
##
## data:  Residuals from Regression with ARIMA(5,1,0) errors
## Q* = 462.43, df = 360, p-value = 0.0002078
##
## Model df: 5.    Total lags used: 365
#Check accuracy of model
n_for <- 59
observed <- df_processed2010[1827:1885, "Daily_data"]
ARIMA_Four_scores <- accuracy(ARIMA_Four_for$mean,observed)
print(ARIMA_Four_scores)
```

```
##              ME      RMSE      MAE      MPE      MAPE
## Test set -284.3608 1536.398 1243.755 -13.07091 28.0451
```

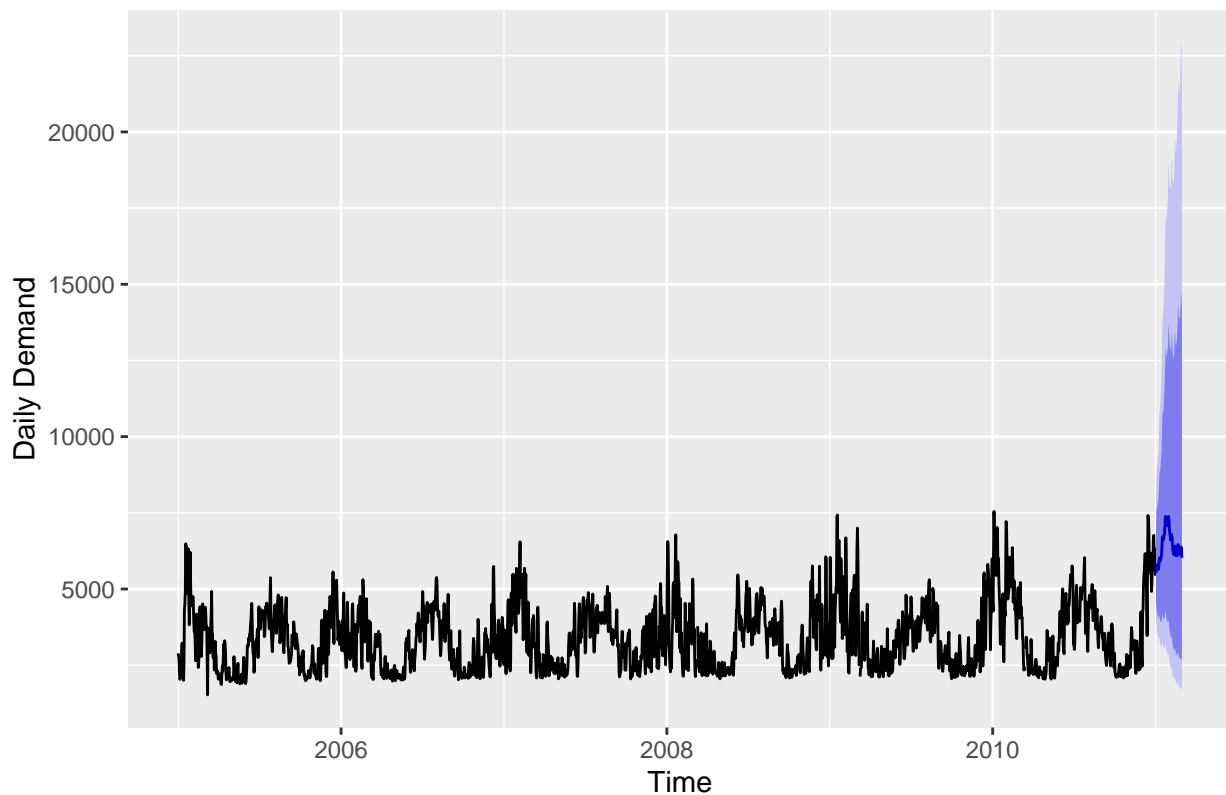
Model 3 ARIMA + FOURIER terms: Forecast 2011

```
#Fit and forecast TBATS model
ARIMA_Four_model2011 <- auto.arima(ts_daily2010,
                                   seasonal=FALSE,
                                   lambda=0,
                                   xreg=fourier(ts_daily2010,
                                                K=c(2,12))
                                   )
```

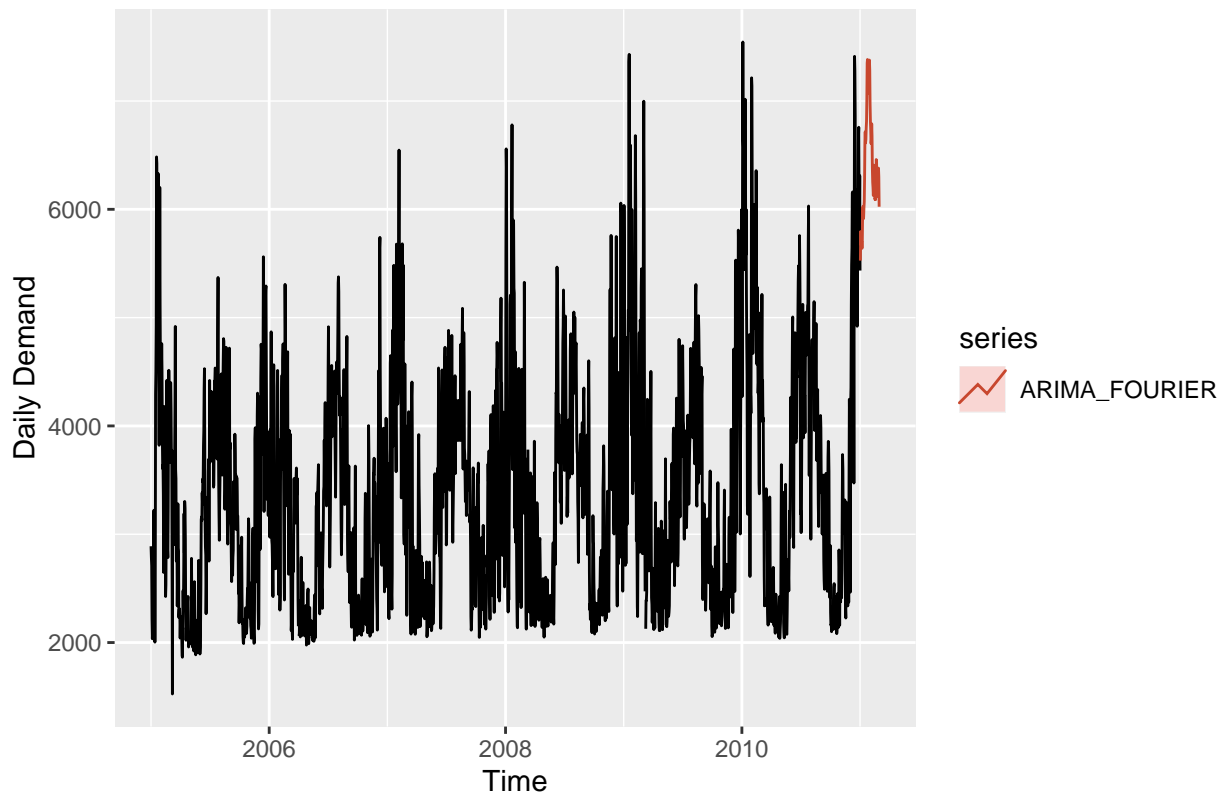
```
#Forecast
ARIMA_Four_for2011 <- forecast(ARIMA_Four_model2011,
                               xreg=fourier(ts_daily2010,
                                             K=c(2,12),
                                             h=59),
                               h=59
                               )

#Plot forecasting results
autoplot(ARIMA_Four_for2011) + ylab("Daily Demand")
```

Forecasts from Regression with ARIMA(5,1,0) errors



```
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(ARIMA_Four_for2011, series="ARIMA_FOURIER", PI=FALSE) +
  ylab("Daily Demand")
```



```
#Check accuracy of model
n_for <- 59
observed <- df_processed2010[(nobs-n_for+1):nobs, "Daily_data"]
ARIMA_Four_scores_for <- accuracy(ARIMA_Four_for$mean,observed)
print(ARIMA_Four_scores_for)
```

```
##                ME    RMSE    MAE    MPE    MAPE
## Test set -1829.112 2256.61 1946.548 -67.636 69.71813
```

```
#print(ARIMA_Four_for2011$mean)
```

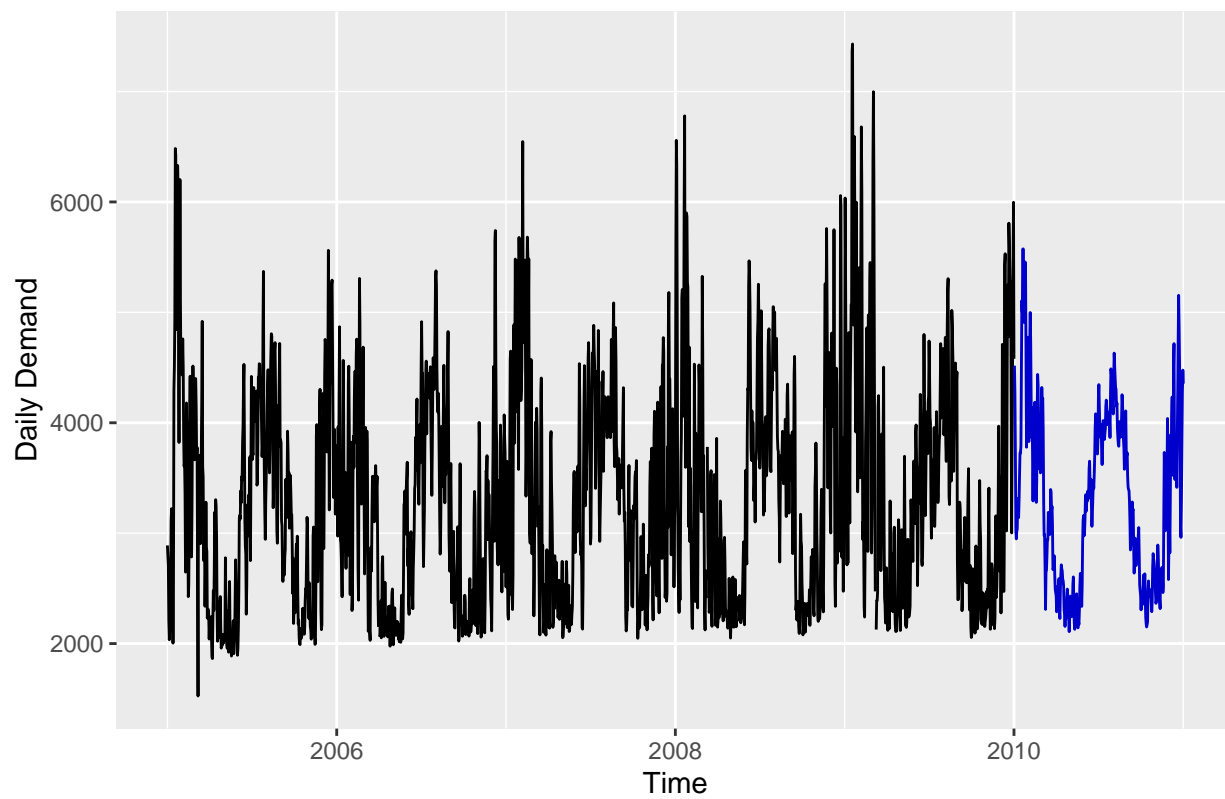
Model 4 Neural Network Time Series: Forecasts 2010

```
#NN_fit <- nnetar(ts_act_power_daily_train,p=1,P=1)
NN_model <- nnetar(ts_daily,decay=0.5, maxit=150, p=1,P=0,xreg=fourier(ts_daily, K=c(2,12)))

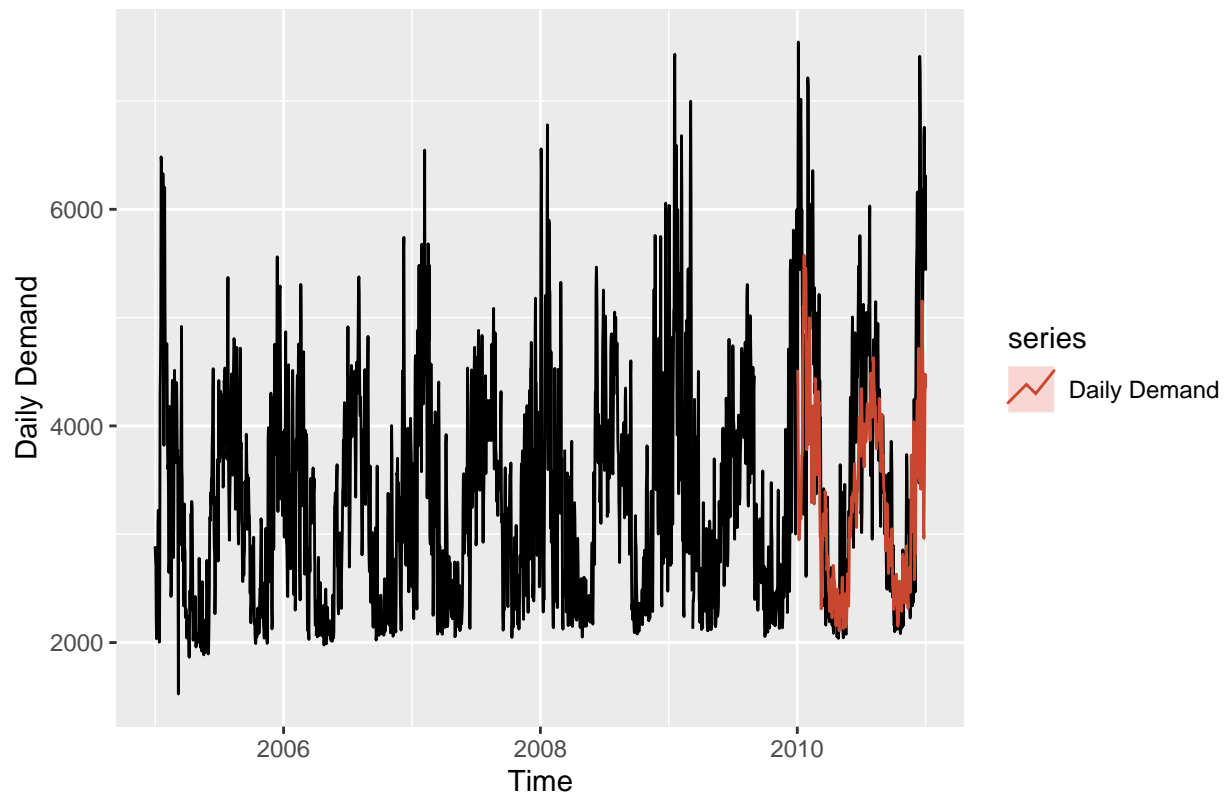
#NN_for <- forecast(NN_fit, h=365)
NN_for <- forecast(NN_model, h=365,xreg=fourier(ts_daily,
                                                K=c(2,12),h=365))

#Plot foresting results
autoplot(NN_for) +
  ylab("Daily Demand")
```

Forecasts from NNAR(1,15)

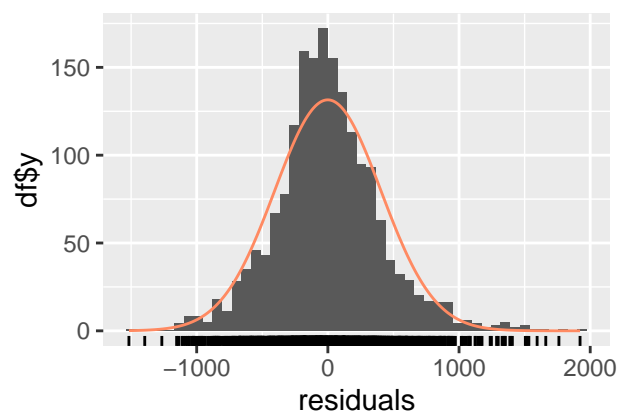
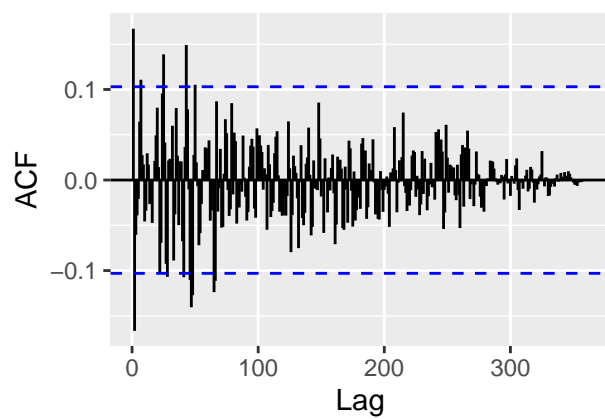
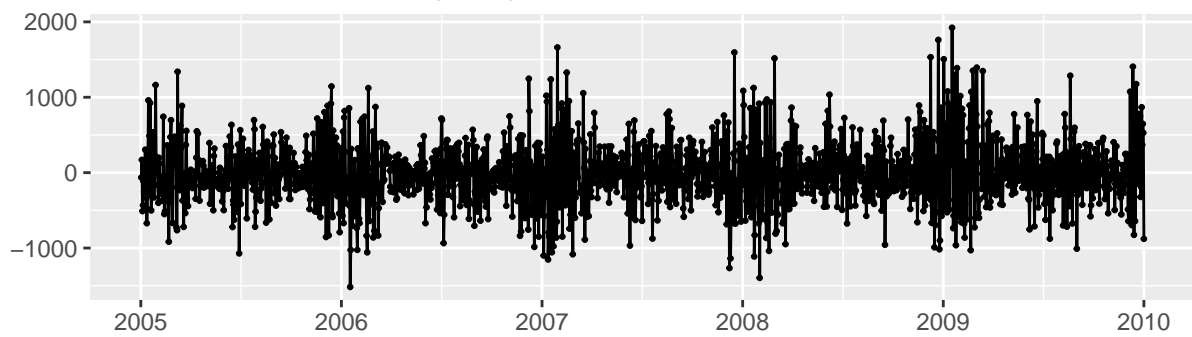


```
#Plot model + observed data  
autoplot(ts_daily2010) +  
  autolayer(NN_for, series="Daily Demand",PI=FALSE)+  
  ylab("Daily Demand")
```



```
checkresiduals(NN_model)
```

Residuals from NNAR(1,15)



```

#Checking error variables to decide which model fits the data the best
n_for <- 365
observed <- df_processed[(nobs-n_for+1):nobs, "Daily_data"]
NN_scores1 <- accuracy(NN_for$mean,observed)
print(NN_scores1)

##           ME      RMSE      MAE      MPE      MAPE
## Test set 127.3959 718.8671 536.2577 0.1572307 14.9895

# Changed version

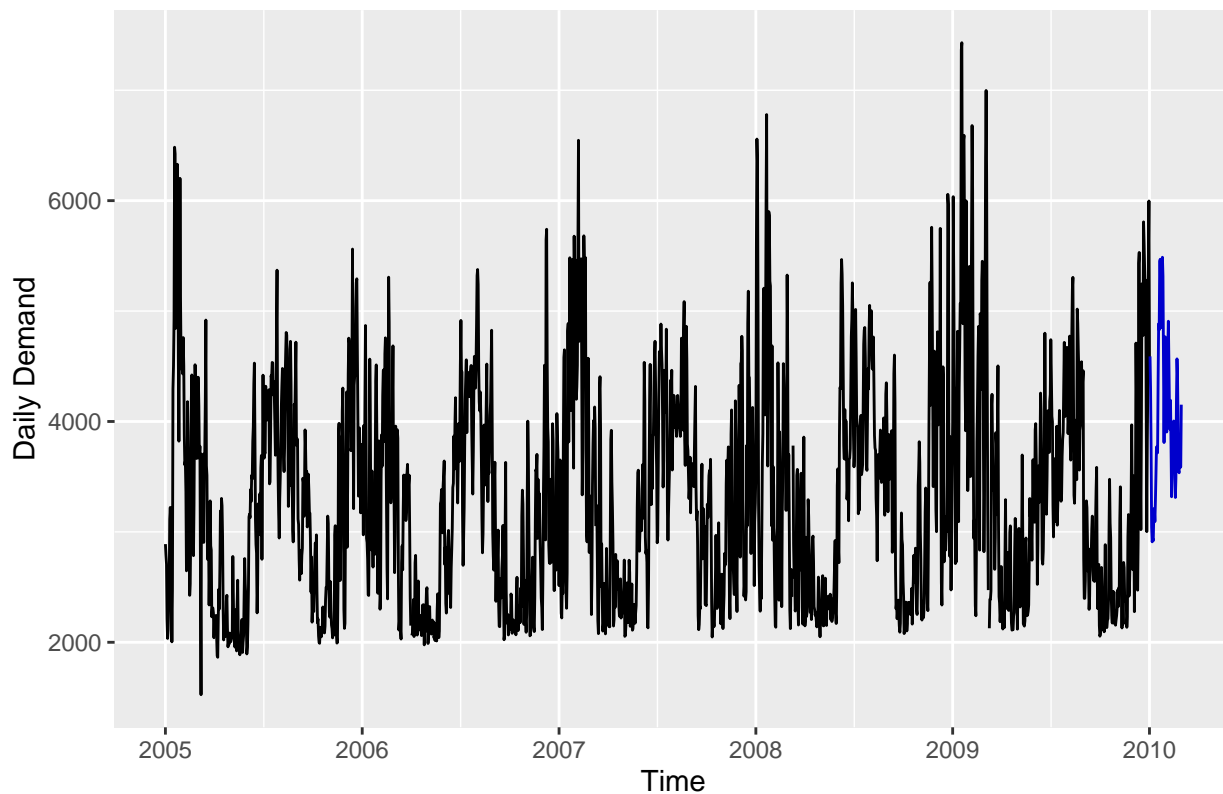
NN_model <- nnetar(ts_daily,decay=0.5, maxit=150, p=1,P=0,xreg=fourier(ts_daily, K=c(2,12)))

#NN_for <- forecast(NN_fit, h=365)
NN_for <- forecast(NN_model, h=59,xreg=fourier(ts_daily,
                                              K=c(2,12),h=59))

#Plot forecasting results
autoplot(NN_for) +
  ylab("Daily Demand")

```

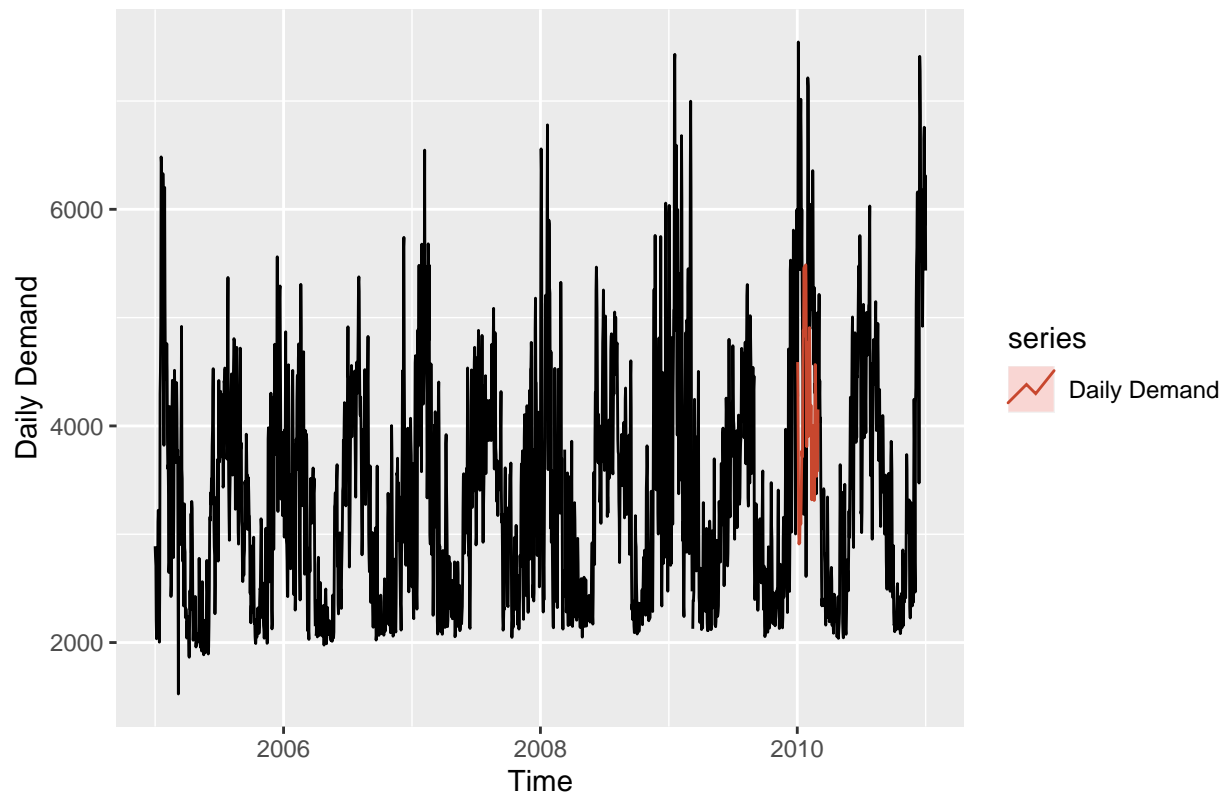
Forecasts from NNAR(1,15)



```

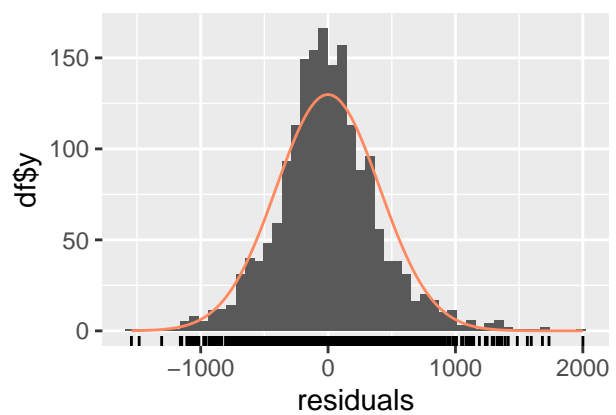
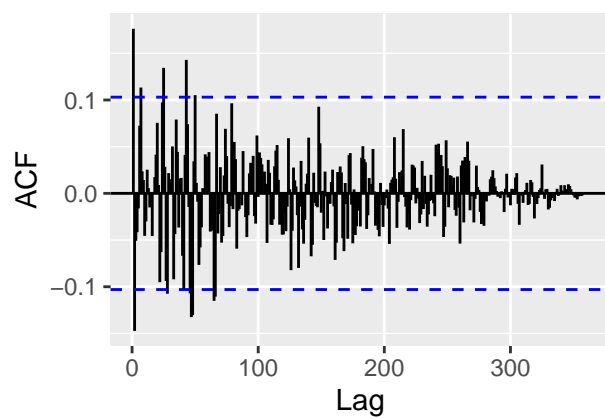
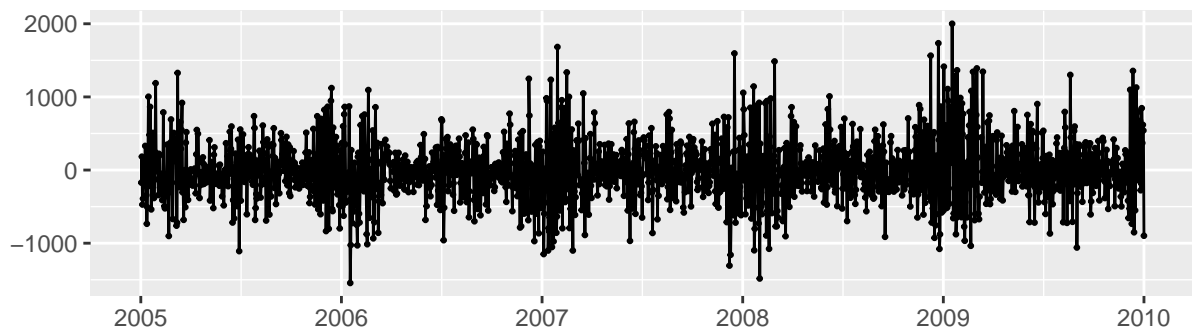
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(NN_for, series="Daily Demand",PI=FALSE)+
  ylab("Daily Demand")

```



```
checkresiduals(NN_model)
```

Residuals from NNAR(1,15)




```
#Checking error variables to decide which model fits the data the best
n_for <- 59
observed <- df_processed2010[1827:1885, "Daily_data"]
NN_scores1 <- accuracy(NN_for$mean,observed)
print(NN_scores1)
```

```
##           ME      RMSE      MAE      MPE      MAPE
## Test set 997.2496 1904.559 1558.008 13.12065 29.98057
```

Model 4 Neural Network Time Series: Forecasts 2011

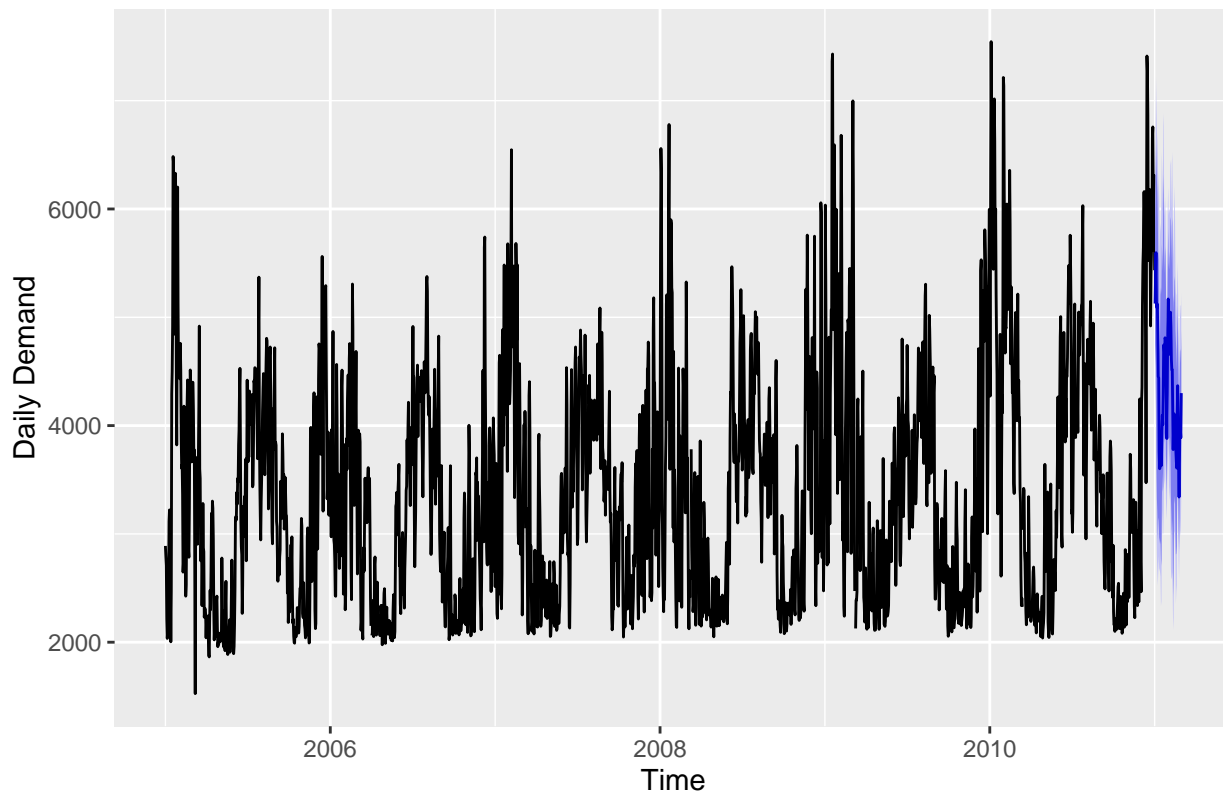
Note: Based on the error variables calculated with the accuracy() function, the Neural Network model seems to fit the data the best.

```
#NN_fit <- nnetar(ts_act_power_daily_train,p=1,P=1)
NN_model2010 <- nnetar(ts_daily2010,lambda = 0.5,p=1,P=0,xreg=fourier(ts_daily2010, K=c(2,12)))

#NN_for <- forecast(NN_fit, h=365)
NN_for2010 <- forecast(NN_model2010,PI=TRUE, h=59,xreg=fourier(ts_daily,
                                                              K=c(2,12),h=59))

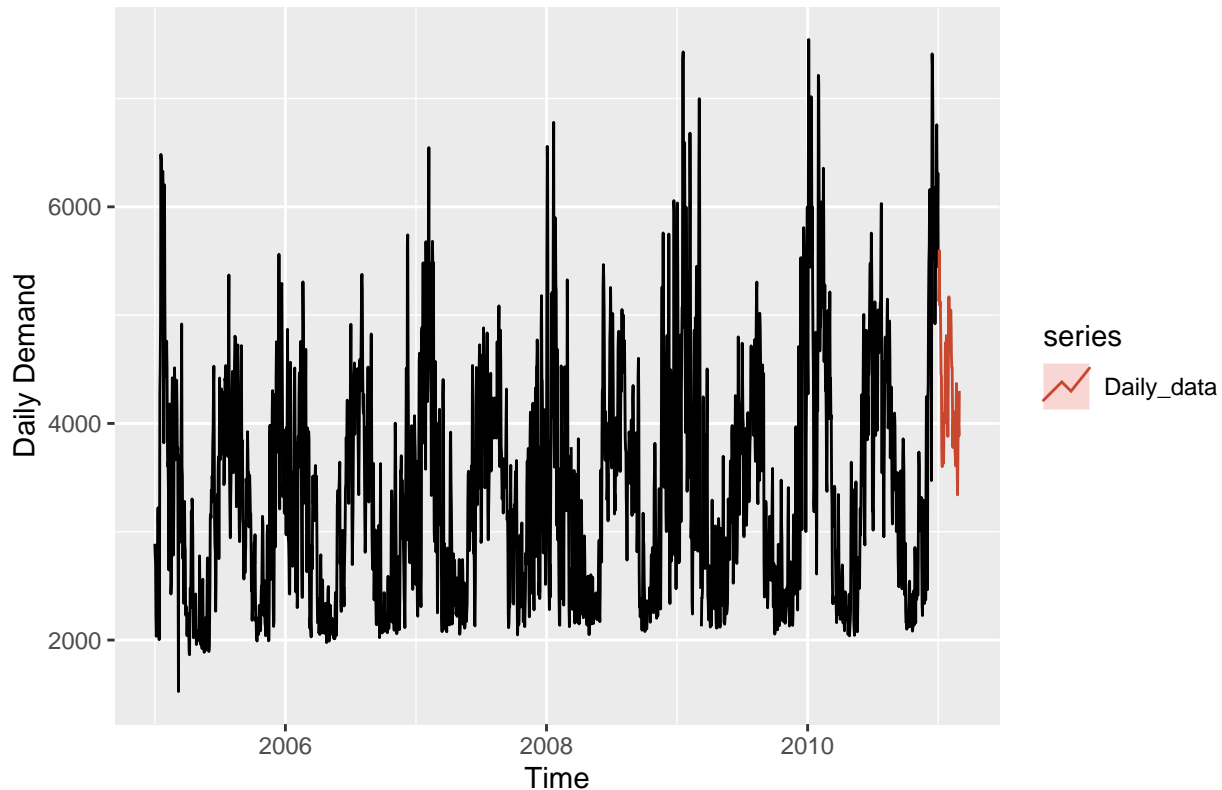
#Plot forecasting results
autoplot(NN_for2010) +
  ylab("Daily Demand")
```

Forecasts from NNAR(1,15)



```
#Plot model + observed data
autoplot(ts_daily2010) +
  autolayer(NN_for2010, series="Daily_data",PI=FALSE)+
```

```
ylab("Daily Demand")
```



```
n_for <- 59
observed <- df_processed2010[(nobs-n_for+1):nobs, "Daily_data"]
NN_scores1_for <- accuracy(NN_for2010$mean,observed)
print(NN_scores1_for)
```

```
##           ME      RMSE      MAE      MPE      MAPE
## Test set -826.2641 1617.556 1436.362 -37.20911 48.58572
```

```
print(NN_for2010$mean)
```

```
## Multi-Seasonal Time Series:
```

```
## Start: 2011 2
```

```
## Seasonal Periods: 7 365.25
```

```
## Data:
```

```
## [1] 5126.954 5373.144 5596.523 5140.610 5087.942 5121.933 4835.299 4453.675
## [9] 4440.413 3758.617 3601.665 3610.857 3868.796 3802.063 3632.335 3950.547
## [17] 4093.632 4008.631 4285.970 4743.872 4734.358 4647.106 4810.932 4790.960
## [25] 4545.453 4232.877 3880.950 4359.404 4902.073 5169.138 4776.518 4658.043
## [33] 4746.998 4820.472 5047.013 4910.971 4613.401 4515.395 4516.333 4139.741
## [41] 3778.768 3994.564 4108.807 4046.701 4026.268 3902.232 3767.947 3668.704
## [49] 3607.980 4109.539 4368.426 4096.203 3634.835 3340.556 3682.422 4051.544
## [57] 3972.925 3888.103 4300.028
```

Compare performance matrix

```
#create data frame
```

```
seas_scores <- as.data.frame(rbind(ETS_scores, TBATS_scores, ARIMA_Four_scores, NN_scores1))
```

Table 1: Forecast Accuracy for Seasonal Data

| | ME | RMSE | MAE | MPE | MAPE |
|-------------|-----------|----------|----------|-----------|----------|
| STL-ETS | -103.0303 | 1547.348 | 1280.656 | -9.57408 | 28.27524 |
| TBATS | 2226.3400 | 2499.097 | 2234.019 | 40.94677 | 41.24095 |
| ARIMA_FOUR | -284.3608 | 1536.398 | 1243.755 | -13.07091 | 28.04510 |
| NEU-NETWORK | 997.2496 | 1904.559 | 1558.008 | 13.12065 | 29.98057 |

```

row.names(seas_scores) <- c("STL-ETS", "TBATS", "ARIMA_FOUR", "NEU-NETWORK")

#choose model with lowest RMSE
best_model_index <- which.min(seas_scores[, "RMSE"])
cat("The best model by RMSE is:", row.names(seas_scores[best_model_index,]))

## The best model by RMSE is: ARIMA_FOUR

kbl(seas_scores,
     caption = "Forecast Accuracy for Seasonal Data",
     digits = array(5, ncol(seas_scores))) %>%
  kable_styling(full_width = FALSE, position = "center") %>%
  #highlight model with lowest RMSE
  kable_styling(latex_options="striped", stripe_index = which.min(seas_scores[, "RMSE"]))

```