Assignment 1

Kelvin Xu
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Problem 1. (a). See function load_data

Problem 1. (b). With each datacase as a row

$$Xw = Y$$

By doing this, we can see that we are not changing any of the decision boundaries. We are just are only effecting the regression coefficients, and their corresponding intepretation. This approach also has the added advantage that it can help avoid numerical instabilities.

Finally, normalization of this type, and other similar normalization schemes helps make the model invariant to parameterization. For example, the ridge regression classifier will have very different weights for the same data shifted around because the penalty will shrink the weight matrix often at the expense of accuracy.

Problem 1. (c). See function polyRegress

Problem 1. (d). See function cross_valid_regress

Problem 1. (e).

Problem 1. (f).

Problem 2.. Writing out the log-likelihood:

$$L = \prod_{i=1}^{m} P(y_i \mid x_i; h) P(x_i)$$

We are interested in the argmax of this value, we also take a log which doesn't change the argmax since it is a monotonically increasing function.

$$\arg\max_{w} L = \arg\max \log l$$

$$l = \sum_{i=1}^{m} \log P(y_i \mid x_i; w) + \log P(x_i)$$

Discarding the $P(x_i)$ term since it does not depend on w.

$$
\begin{aligned}
l &= \sum_{i=1}^{m} \log P(y_i \mid x_i; w) \\
&= \sum_{i=1}^{m} \log \left(\frac{1}{\sqrt{2\pi\sigma_i^2}} \exp\Big(-\frac{1}{2} \frac{(y_i - h_w(x_i))^2}{\sigma_i^2} \Big) \right) \\
&= \sum_{i=1}^{m} \log \Big(\frac{1}{\sqrt{2\pi\sigma_i^2}} \Big) - \sum_{i=1}^{m} \Big(\frac{1}{2} \frac{(y_i - h_w(x_i))^2}{\sigma_i^2} \Big)
\end{aligned}
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Problem 3. (a).

Problem 3. (b).

Problem 3. (c).

Problem 4..