

# Rational Function Proper Form

The ratio of Polynomials,  $P(x)/Q(x)$  is rational Function

where

$$P(X) = a_n X^n + a_{n-1} X^{n-1} + \dots a_0$$

$$= a_n (X - b_1)(X - b_2)(X - b_3) \dots (X - b_n)$$

$$Q(X) = a_m X^m + a_{m-1} X^{m-1} + \dots a_0$$

$$= a_m (X - c_1)(X - c_2)(X - c_3) \dots (X - c_m)$$

$$F(x) = \frac{P(x)}{Q(x)}$$

$F(x)$  is proper form when  $n < m$

$$F(x) = F_{\text{proper}}(x) + D(x)$$

$F(x)$  can be changed to proper form plus  $D(x)$ , a polynomial function