

### Procedure for 3D migration of RFs in spherical coordinates for the AlpArray RF group (version 6.7.2020. GH)

- select station
- select earthquake
- calculate back-azimuth at start  $baz_0$  (ray will remain in plane but this will need to be updated at each step)
- calculate P wave ray parameter  $p_{OP}$
- correct ray parameter  $p$  for P-to-S wave at assumed Moho (Leonardo's step)
- **migration itself**, from station  $[phy_0, lambda_0, z_0+elev.]$  downwards (loop on  $_i$ ,  $_i$  being index of next level)
  - step down  $\Delta Z$  from current  $z_{i-1}$  to next  $z_i$  ( $_i=1$  in the figure below)
  - use departing level's velocity, interpolated from 3D model (ideally: in that plane only)  $v_{i-1}$
  - calculate departing incidence angle  $id_{i-1}$  from spherical ray param. def.  $p = ([R_{Earth} - (i-1) * \Delta Z + elev] * \sin(id_{i-1})) / v_{i-1}$
  - calculate great-circle distance travelled  $\Delta_i$ 
    - from sine law the arrival angle at layer  $_i$  is:  $ia_i = \arcsin \{ \sin(id_{i-1}) / (R_{Earth} - i * \Delta Z) * (R_{Earth} - (i-1) * \Delta Z) \}$   
(NB: verify that  $ia_i > 90^\circ$  !)
    - from simple triangle angle sum:  $\Delta_{i-1} = 180^\circ - id_{i-1} - ia_i$
  - calculate new position  $[phy_i, lambda_i]$  using original position,  $\Delta_{i-1}$  and  $baz_{i-1}$
  - update local back-azimuth  $baz_i$  for next step using  $[phy_i, lambda_i]$  and earthquake coordinates
- assign RF time samples to depth mesh
- stack, mean, etc. (as usual, using neighbouring cells)
- change representation to spherical (paraview?)

Below is a tentative sketch accompanying the text, top part refers to the step from level 0 to 1, the bottom part is generic (with index  $_i$ ).

