

LAB 7

by

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Abstract

blah blah blah

1 Introduction

2 Methods and Materials

By using a National Instrument VirtualBench VB-8012 (VBench) to control input signals and a National Instrument data acquisition (NI-DAQ) system with a custom virtual interface to collect data, various signals were able to be processed in the frequency and time domain. The experiment focused on three primary modes; analyzing a well known signal in the frequency domain, examining the response for a signal being aliased in the frequency domain and time domain, and determining the characteristics of an unknown signal in the frequency and time domain.

2.1 Sine and Square Waves

To establish a foundational understanding for interpreting signals in the frequency domain, the VBench function generator was used to create a sine and square wave. Both of these signals were created parameters using the parameters, $2 V_{rms}$ amplitude and a f of 100 Hz. For the sine wave, a sampling rate of 400Hz was chosen to ensure the no aliasing of the signal occurred. Collecting enough data for the square wave, however, required a higher sampling frequency of 10 kHz due to the harmonics expressed in Equation ??.

2.2 Aliasing of a Known Signal

To properly demonstrate the *fold back* type of behavior associated with aliasing a sine wave signal requires a proper measurement, therefore, a sampling frequency of 10 kHz was chosen to measure a 1500 Hz signal. This ensured that the maximum observable frequency was well beyond the Nyquist frequency described in Equation ??. Additionally, the same signal was analyzed using the sampling frequency of 2.5 kHz. These two sampling frequencies ensured that data was collected under aliased and non-aliased conditions.

To further analyze a sine wave under aliasing conditions, the signal was analyzed in time domain of the virtual interface using sampling frequencies of 2.5 kHz and 1.5 kHz. To conclude the experimental observations of an aliased sine wave in the time domain, the frequency on the function generator was changed in increments of 1 Hz on the interval from 1,500 Hz to 1,490 Hz.

2.3 Characterizing an Unknown Signal

Characterizing the unknown signal was done by setting the sampling rate to 20 kHz and examining the time trace for continuity and a well defined shaped, thus ensuring the signal was not being aliased. Lastly, the sampling frequency was set to 2,000 kHz and than 1,000 kHz and data sets were collected using the NI-DAQ in the frequency domain.

3 Results

Figure 1 shows the results for sine wave and square generated with the VBench in the frequency domain. Both signals satisfy the condition $f_s > f_{Ny}$ and thus ensure no aliasing is occurring. Furthermore, the peak values in Figure 1(a) corresponds to same frequency on the function generator and harmonic frequencies in Figure 1(b) match the values associated with the Fourier transformation depicted in the Equation ??

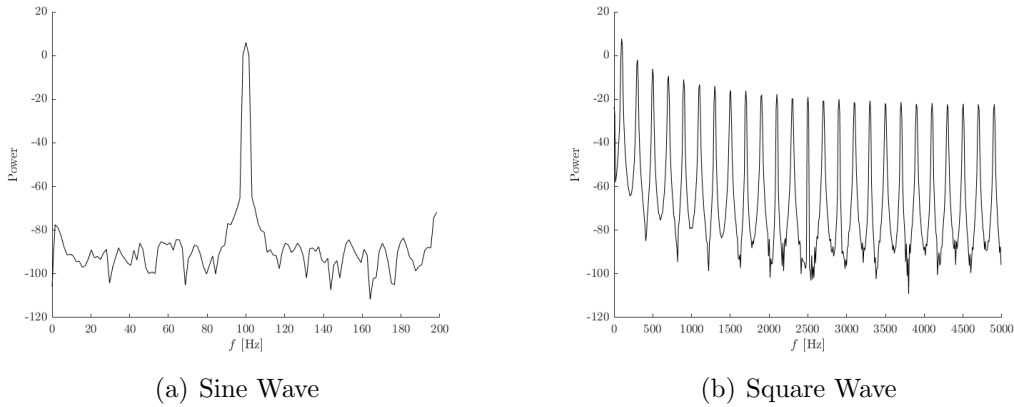
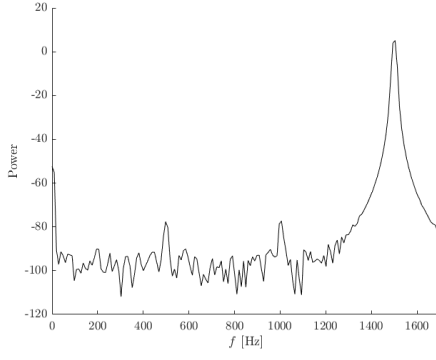


Figure 1: Sine and square waves with V_{rms} of 2 V at 100Hz shown in the frequency domain

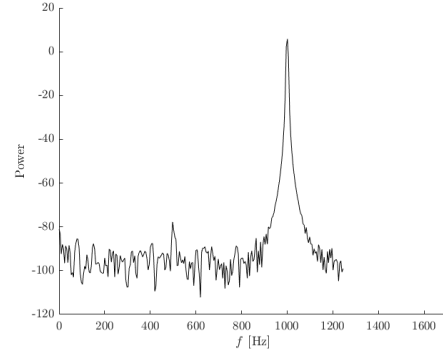
On the contrary, Figure 2 shows a 1.5 kHz sine wave purposely being aliased by setting the sampling frequency to 10 kHz and reducing it to 2.5 kHz. Since the Nyquis frequency is less than the measured frequency, these results reflect the observed frequency expressed in Equation ?? and illustrate the *fold back* type of behavior expected in a aliased signal.

Figure 3 illustrates the same signal in the time domain. This analysis indicated that using a sample frequency of 2.5 kHz is not sufficient enough to return the amplitude or shape of the signal, rather it only returns the frequency of the signal. Furthermore, Figure 3(b) illustrates the scenario $f_s = f_{signal}$. In this situation, the sampling rate is no longer sufficient enough to collect any sort of data from the signal(i.e., shape, offset, frequency, or amplitude). However, incrementally reducing or increasing the sample frequency, as shown in Figure 3(c), seemed to restore the characteristics of the graph in the time domain.

Plotting the time trace for the unknown signal revealed a high frequency component

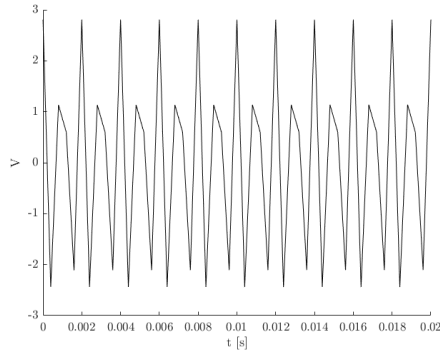


(a) $f_s = 10$ kHz

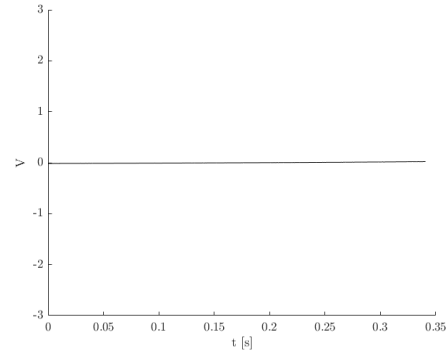


(b) $f_s = 2.5$ kHz

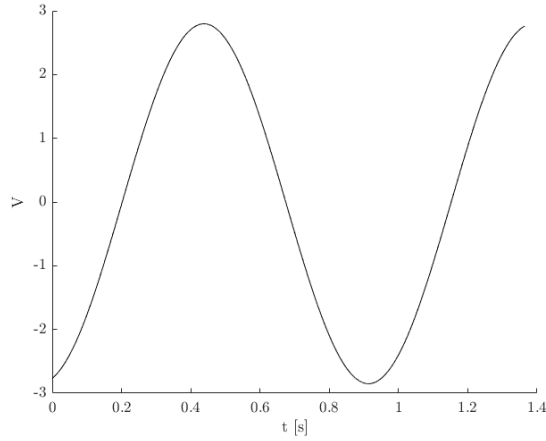
Figure 2: Sine and square waves with V_{rms} of 2V at 100Hz shown in the frequency domain



(a) $f_s > f$



(b) $f_s = f$



(c) $f_s < f$

Figure 3: Sine and square waves with V_{rms} of 2V at 100Hz shown in the frequency domain embedded in a low frequency signal.

The power spectra of the unknown signal was examined at sampling frequencies of 1 kHz

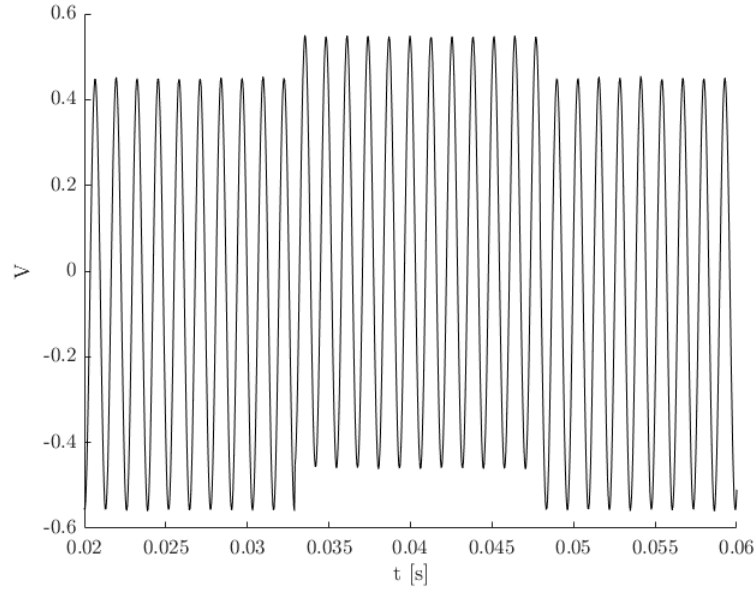


Figure 4: Time trace of unknown signal

and 2 kHz. Comparing the two samples reveals that the former of the sampling frequencies aliases the signal and is most apparent by the shift in the largest peak.

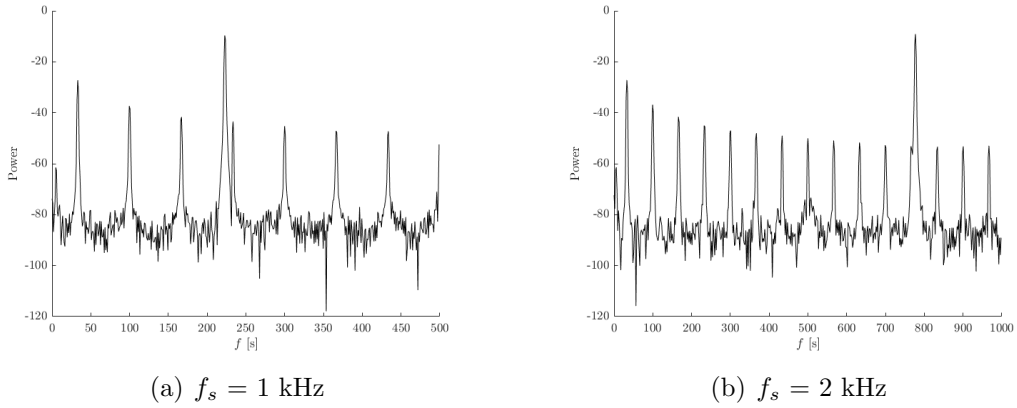


Figure 5: Power Spectrum for unknown signal

4 Discussion

4.1 Analysis of Known Signal

Examining key characteristics of graphs shown in Figure 1 and Figure 2 reveals an agreement between theoretical predictions and experimental results for signals represented on a power spectra. In both parts experiment, signals generated via the VBench function generator were shown to have either single peaks or harmonics for sine and square waves, respectively. Additionally, in the square wave power spectra, the harmonic frequencies matched the corresponding multiples of the initial frequency (i.e., peaks at f , $3f$, $5f$, ...).

Analysis of known signals in the time domain also qualitative matched theoretical predictions. From Figure 3(a), it shown that the observable frequency is equivalent to the signal via the function generator. The shape and amplitude, however, cannot be recovered and is a consequence of the Nyquins frequency being insufficient to properly measure the incoming signal. When adjusting the sampling rate to match the signal frequency, it is shown in Figure 3(b) that the time trace will consist of a straight line. This phenomenon was due to the NI-DAQ measuring the same point on the curve every cycle, and in this experiment, the measured point also aligned to the point where the amplitude of the sine wave was equal to zero. Adjusting the sampling frequency such that $f_s < f$, however, did not align with the anticipated results in the time domain. The anticipated result was a time trace with no particular shape, amplitude, nor frequency but the results shown in Figure 3(c) shows an entirely different outcome. Experimental data showed a sinusoidal wave with a frequency of approximately 1 Hz.

4.2 Analysis of Unknown Signal

The time trace shown in Figure 4 shows a minimum of two combined signal patterns, with one at greater frequency than the other. Viewing the signal in the power spectra confirmed the existence of a low frequency signal with harmonics (i.e., square or triangle) and a high frequency signal with no harmonics (i.e., sinusoidal wave). Measuring the signal at a sampling rate of 1 kHz and 2 kHz showed that the signal was being aliased at 1 kHz and matched the *fold back* behavior for a sine wave at 777Hz and a Nyquist frequency of 500 Hz. In Figure 5(a), the observed frequency of the sine wave occurs at $223 \text{ Hz} \pm df$ and this observation matches the theoretical outcome described in Equation ??.

The harmonics observed in the unknown signal matched to known signals via trial and error. It was assumed that either a triangle or square wave were the underlying type of wave associated with the measurements obtained in the power spectra. Figure 6 shows the measured signal in blue and a replicated signal in black. The replicated signal was created using the function generated and combining two sets of data. The first set of data was obtained by creating a sine wave with a frequency of 777 Hz and the second data set

was obtained by generating a triangle wave at 33 Hz and 50% symmetry. A side by side qualitatively shows that replicated signal matches harmonic frequency of the unknown signal. The amplitude of the signals, however, differ in magnitude and the replicated signal carries more energy than the unknown signal.

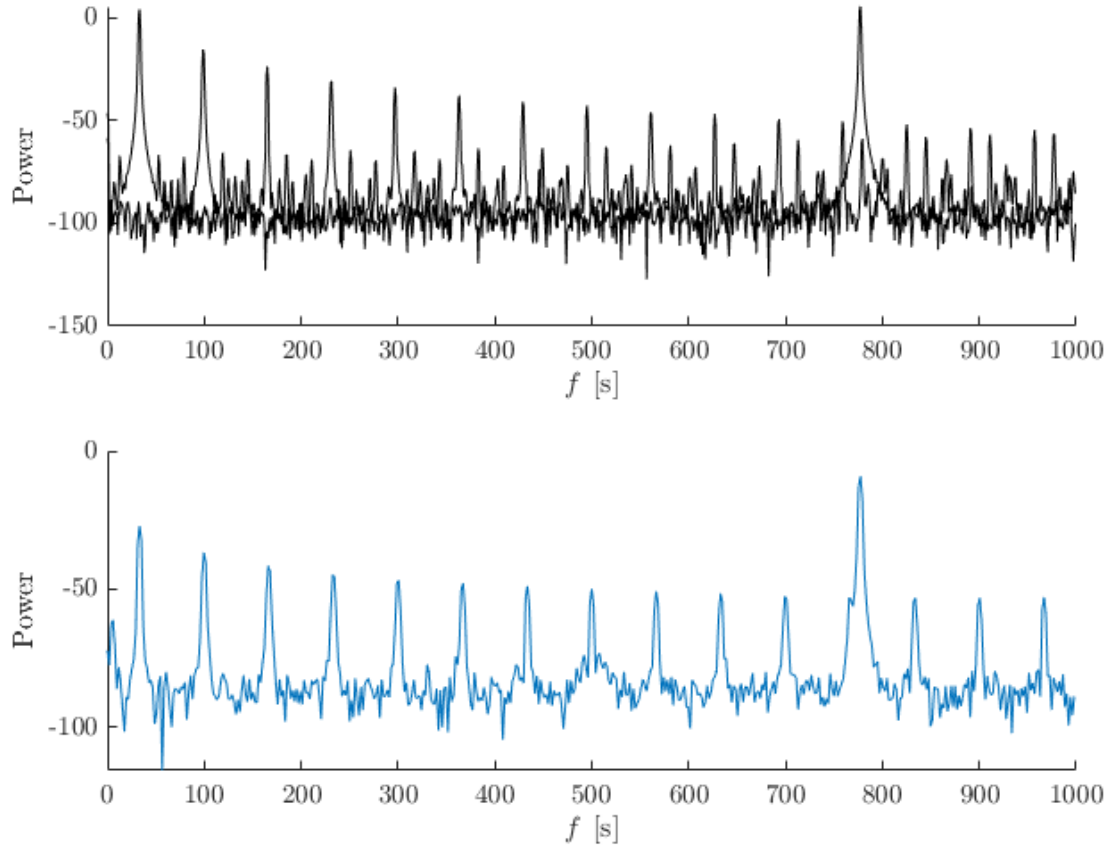


Figure 6: Guess and Actual

5 Conclusion

A MATLAB Script

```
1 clear;clc;close all
2 % ----- Import Data
   -----
3 % data(:,1) = time/freq
4 % data(:,2) = power/voltage
5 part1sin = importdata('Data Lab 7/Part1_sin.txt').data;
6 part1square = importdata('Data Lab 7/Part1_square.txt').data;
7 part2sin = importdata('Data Lab 7/Part2_sin.txt').data;
8 part2sinAliasing = importdata('Data Lab 7/Part2_sinAliasing.txt
   ').data;
9 part2Final = importdata('Data Lab 7/Part2_timeDomainFinal.txt')
   .data;
10 part2Initial = importdata('Data Lab 7/Part2_timeDomainInitial.
   txt').data;
11 part2Freq = importdata('Data Lab 7/Part2_timeDomainFreqChange.
   txt').data;
12 part31000 = importdata('Data Lab 7/Part3_1000Hz.txt').data;
13 part32000 = importdata('Data Lab 7/Part3_2000Hz.txt').data;
14 part3time = importdata('Data Lab 7/Part3_timeDomain.txt').data;
15 sinwave777 = importdata('Data Lab 7/sinwave_777Hz.txt').data;
16 triangle33 = importdata('Data Lab 7/triangle_33Hz.txt').data;
17
18 %% Figures From Part 1
19 % ----- Part 1 Sine Wave -----
20 figure()
21 hold on;
22 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
   , 'latex');
23 plot(part1sin(:,1),part1sin(:,2),'k')
24 xlabel('$f$ [Hz]');
25 ylabel('Power');
26
27 % ----- Part 1 Square Wave -----
28 figure()
29 hold on;
30 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
   , 'latex');
31 plot(part1square(:,1),part1square(:,2),'k')
32 xlabel('$f$ [Hz]');
33 ylabel('Power');
34
35 %% Figures From Part 2
```



```

36 % ----- Sine Wave at 10kHz Sampling Rate -----
37 figure()
38 hold on;
39 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
40 plot(part2sin(:,1),part2sin(:,2),'k')
41 xlabel('$f$ [Hz]');
42 xlim([0 1700])
43 ylabel('Power');
44
45 % ----- Sine Wave at 2.5kHz Sampling Rate -----
46 figure()
47 hold on;
48 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
49 plot(part2sinAliasing(:,1),part2sinAliasing(:,2),'k')
50 xlabel('$f$ [Hz]');
51 xlim([0 1700])
52 ylabel('Power');
53
54 % ----- Sine Wave time domain initial -----
55 figure()
56 hold on;
57 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
58 plot(part2Initial(:,1),part2Initial(:,2),'k')
59 xlabel('t [s]');
60 xlim([0 .02])
61 ylabel('V');
62 ylim([-3 3])
63
64 % ----- Sine Wave time domain final -----
65 figure()
66 hold on;
67 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
68 plot(part2Final(:,1),part2Final(:,2),'k')
69 xlabel('t [s]');
70 ylabel('V');
71 ylim([-3 3])
72 % ----- Sine wave in time domain with increase Freq -----
73 figure()
74 hold on;
75 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');

```

```

76 plot(part2Freq(:,1),part2Freq(:,2),'k')
77 xlabel('t [s]');
78 ylabel('V');
79 ylim([-3 3])
80
81 %% Figures for part 3
82 % ----- Mystery Signal in time domain -----
83 figure()
84 hold on;
85 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
86 plot(part3time(:,1),part3time(:,2),'k')
87 xlim([.02 .06])
88 xlabel('t [s]');
89 ylabel('V');
90
91 % ----- Mystery Signal f_s at 2000 Hz -----
92 figure()
93 hold on;
94 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
95 plot(part32000(:,1),part32000(:,2),'k')
96 xlabel('$f$ [s]');
97 ylabel('Power');
98
99 % ----- Mystery Signal f_s at 1000 Hz -----
100 figure()
101 hold on;
102 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
103 plot(part31000(:,1),part31000(:,2),'k')
104 xlabel('$f$ [s]');
105 ylabel('Power');
106
107 %% The Extra Graphs
108 figure()
109
110 subplot(2,1,1)
111 hold on;
112 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
113 plot(sinwave777(:,1),sinwave777(:,2),'k')
114 plot(triangle33(:,1),triangle33(:,2),'k')
115 xlabel('$f$ [s]');
116 ylabel('Power');

```

```
117
118 subplot(2,1,2)
119 hold on;
120 set(gca,'defaulttextinterpreter','latex','TickLabelInterpreter'
    , 'latex');
121 plot(part32000(:,1),part32000(:,2))
122 xlabel('$f$ [s]');
123 ylabel('Power');
```